

# Synthetic Impulse Response Functions

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## Abstract

We adopt techniques from an inferential procedure known as synthetic control to construct a new impulse response function (IRF) estimator. Distinct from estimates generated from Wold decomposition or local projections (LP), synthetic IRFs leverage information from the context surrounding a shock with the goals of both reducing risk while also limiting bias. The method relies upon Wold and/or LP IRF estimates on multivariate time series from a "donor pool". These estimates in turn are aggregated using distanced-based weighting, a procedure in which the donor multivariate series are judged based on similarity to the target multivariate series. We also develop a procedure to discount the donor series based on signal-to-noise ratio. This adjustment supports the "unit-shock" convention used in impulse response function analysis. Simulations and empirical examples are provided.

## 1 Introduction

The technique of distanced-based weighting and synthetic, aggregation methods is naturally suited to IRF and vector autoregressions more generally due to the multivariate setting that comes for free. There is no need to search for predictive or otherwise informative covariates.

Challenge: suppose a researcher knew that a countable set of donors  $\mathcal{D}$  could be used to maximize fit (loosely defined) in the context of impulse response function estimation. However, for a particular donor  $d_m, m \in \mathcal{D}$ , the shock at time  $t^*$  is not observed and hence its magnitude must be inferred.

1. Estimate the shock  $\epsilon_i, t^*$  for each donor.
2. If estimate requires parametric assumption, then scale estimates appropriately to satisfy the unit-shock assumption.
3. Confidence intervals? Strong assumptions needed?
4. Need to be very clear about whether this is an inferential or predictive tool.

Ideas

1. Can we use the Wold decomposition as ground truth?
2. Can we use synthetic vol forecasting for Value-at-Risk (VaR)?

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