Synthetic Volatility Forecasting and Other Aggregation Techniques for Time Series Forecasting Preliminary Exam

David Lundquist¹

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A seemingly unprecedented event might make one ask

- What does it resemble from the past?
- What past events are most relevant?
- Oan we incorporate past events in a systematic, principled manner?



When would we ever have to do this?

- Event-driven investing strategies (unscheduled news shock)
- Pairs trading strategies
- Structural shock to macroeconomic conditions (scheduled news possibly pre-empted by news shock)
- Biomedical panel data subject to exogenous shock or interference

Example

Oil nose-dives as Saudi Arabia and Russia set off 'scorched earth' price war

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Example

Oil crashes by most since 1991 as Saudi Arabia launches price war



By Matt Egan, CNN Business

② 3 minute read · Updated 3:21 PM FDT Mon March 9, 2020

Punchline of the paper

Forecasting is possible under structural shocks, so long as we incorporate external information to account for the nonzero errors.



Background and related methods

Volatility Modeling

- GARCH is slow to react (Andersen et al. 2003)
- Asymmetric GARCH models catch up faster but need post-shock data
- Realized GARCH (Hansen, Huang, and Shek 2012), in our setting, would require post-shock information and/or high-frequency data in order to outperform, and Realized GARCH is highly parameterized

Background and related methods

Forecast Augmentation

- Clements and Hendry 1998; Clements and Hendry 1996 laid the groundwork for modeling nonzero errors in time series forecasting
- Guerrón-Quintana and Zhong 2017 use a series' own errors to correct the forecast for that series
- Dendramis, Kapetanios, and Marcellino 2020 use a similarity-based procedure to correct linear parameters in time series forecasts
- Foroni, Marcellino, and Stevanovic 2022 adjust pandemic-era forecasts using intercept correction techniques and data from Great Financial Crisis
- Lin and Eck 2021 use distanced-based weighting (a similarity approach) to aggregate and weight fixed effects from a donor pool



Outline

- Introduction
- Setting
 - Model Setup
 - Volatility Profile of a Time Series
- Post-shock Synthetic Volatility Forecasting Methodology
- Properties of Volatility Shock and Shock Estimators
- Real Data Example
- Mumerical Examples
- Discussion
- Future directions for Synthetic Volatility Forecasting
 - Signal Recovery
 - Stochastic Volatility
 - Synthetic Impulse Response Functions
- Supplement



The news has broken but markets are closed

- After-hours trading provides a poor forum in which to digest news
- The news constitues public, material information relevant to one or more traded assets
- The qualitative aspects of the news provide basis upon which to match to past events



A Primer on GARCH

Let $\{a_t\}$ denote an observable, real-valued discrete-time stochastic process. We say $\{a_t\}$ is a strong GARCH process with respect to $\{\epsilon_t\}$ iff

$$\sigma_t^2 = \omega + \sum_{k=1}^m \alpha_k a_{t-k}^2 + \sum_{j=1}^s \beta_j \sigma_{t-j}^2$$

$$a_t = \sigma_t \epsilon_t$$

$$\epsilon_t \stackrel{iid}{\sim} E[\epsilon_t] = 0, Var[\epsilon_t] = 1$$

$$\forall k, j, \alpha_k, \beta_j \ge 0$$

$$\forall t, \omega, \sigma_t > 0$$

Our Model is Nested Within GARCH-X



Volatility Profile

```
AbsoluteReturn_* * .1
                            AbsoluteRetum_+* ,2
                          AbsoluteReturn + -1.2
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Synthetic Volatility Forecasting and Other Ag

What's the method here?





Some things to think about with papers like this

Simplest Simulation Setup



A more benign example

Example (Coverging at the slowest rate possible)

Fix
$$\alpha = 1, \beta > 1$$
. Let $\lambda_i = \frac{1}{i \log^{\beta}(i+1)}$.



How noise is hidden just right



After all of this waiting, we formalize the notion under discussion.

Definition (Asymptotically Benign)



We analyze the real-world example with Brexit included.

Bibliography

- Andersen, Torben G et al. (2003). "Modeling and forecasting realized volatility". In: *Econometrica* 71.2, pp. 579–625.
- Clements, Michael and David F Hendry (1998). Forecasting economic time series. Cambridge University Press.
 - Clements, Michael P and David F Hendry (1996). "Intercept corrections and structural change". In: *Journal of Applied Econometrics* 11.5, pp. 475–494.
- Dendramis, Yiannis, George Kapetanios, and Massimiliano Marcellino (2020). "A similarity-based approach for macroeconomic forecasting". In: Journal of the Royal Statistical Society Series A: Statistics in Society 183.3, pp. 801–827.
- Foroni, Claudia, Massimiliano Marcellino, and Dalibor Stevanovic (2022). "Forecasting the Covid-19 recession and recovery: Lessons from the financial crisis". In: *International Journal of Forecasting* 38.2, pp. 596–612.