

$$\begin{aligned} \mathcal{S}'_{\text{ds}}[\text{begin } D_V \text{ S end}]env_V \text{ sto} &= \mathcal{S}'_{\text{ds}}[S]env'_V \text{ sto}' \\ \text{where } \mathcal{D}^V_{\text{ds}}[D_V](env_V, \text{sto}) &= (env'_V, \text{sto}') \end{aligned}$$

$$\mathcal{S}'_{\text{ds}}[x:=a]env_V \text{ sto} = \text{sto}[l \mapsto \mathcal{A}[a](\text{lookup } env_V \text{ sto})]$$

$$\text{where } l = env_V x$$

$$\mathcal{S}'_{\text{ds}}[\text{skip}]env_V = \text{id}$$

$$\mathcal{S}'_{\text{ds}}[S_1 ; S_2]env_V = (\mathcal{S}'_{\text{ds}}[S_2]env_V) \circ (\mathcal{S}'_{\text{ds}}[S_1]env_V)$$

$$\mathcal{S}'_{\text{ds}}[\text{if } b \text{ then } S_1 \text{ else } S_2]env_V =$$

$$\text{cond}(\mathcal{B}[b] \circ (\text{lookup } env_V), \mathcal{S}'_{\text{ds}}[S_1]env_V, \mathcal{S}'_{\text{ds}}[S_2]env_V)$$

$$\mathcal{S}'_{\text{ds}}[\text{while } b \text{ do } S]env_V = \text{FIX } F$$

$$\text{where } F \ g = \text{cond}(\mathcal{B}[b] \circ (\text{lookup } env_V), g \circ (\mathcal{S}'_{\text{ds}}[S]env_V), \text{id})$$

$$\mathcal{D}^V_{\text{ds}}[\text{var } x := a; D_V](env_V, \text{sto}) =$$

$$\mathcal{D}^V_{\text{ds}}[D_V](env_V[x \mapsto l], \text{sto}[l \mapsto v][\text{next} \mapsto \text{new } l])$$

$$\text{where } l = \text{sto next and } v = \mathcal{A}[a](\text{lookup } env_V \text{ sto})$$

$$\mathcal{D}^V_{\text{ds}}[\varepsilon] = \text{id}$$

$$\mathcal{D}_{\text{ds}}^{\text{P}}[\text{proc } p \text{ is } S; D_P] \text{env}_V \text{env}_P = \mathcal{D}_{\text{ds}}^{\text{P}}[D_P] \text{env}_V (\text{env}_P[p \mapsto g])$$

$$\text{where } g = \mathcal{S}_{\text{ds}}[S] \text{env}_V \text{env}_P$$

$$\mathcal{D}_{\text{ds}}^{\text{P}}[\varepsilon] \text{env}_V = \text{id}$$

$$\mathcal{S}_{\text{ds}}[x := a] \text{env}_V \text{env}_P \text{sto} = \text{sto}[l \mapsto \mathcal{A}[a](\text{lookup } \text{env}_V \text{sto})]$$

$$\text{where } l = \text{env}_V x$$

$$\mathcal{S}_{\text{ds}}[\text{skip}] \text{env}_V \text{env}_P = \text{id}$$

$$\mathcal{S}_{\text{ds}}[S_1 ; S_2] \text{env}_V \text{env}_P = (\mathcal{S}_{\text{ds}}[S_2] \text{env}_V \text{env}_P) \circ (\mathcal{S}_{\text{ds}}[S_1] \text{env}_V \text{env}_P)$$

$$\mathcal{S}_{\text{ds}}[\text{if } b \text{ then } S_1 \text{ else } S_2] \text{env}_V \text{env}_P =$$

$$\text{cond}(\mathcal{B}[b] \circ (\text{lookup } \text{env}_V), \mathcal{S}_{\text{ds}}[S_1] \text{env}_V \text{env}_P,$$

$$\mathcal{S}_{\text{ds}}[S_2] \text{env}_V \text{env}_P)$$

$$\mathcal{S}_{\text{ds}}[\text{while } b \text{ do } S] \text{env}_V \text{env}_P = \text{FIX } F$$

$$\text{where } F \ g = \text{cond}(\mathcal{B}[b] \circ (\text{lookup } \text{env}_V),$$

$$g \circ (\mathcal{S}_{\text{ds}}[S] \text{env}_V \text{env}_P), \text{id})$$

$$\mathcal{S}_{\text{ds}}[\text{begin } D_V \ D_P \ S \ \text{end}] \text{env}_V \text{env}_P \text{sto} = \mathcal{S}_{\text{ds}}[S] \text{env}'_V \text{env}'_P \text{sto}'$$

$$\text{where } \mathcal{D}_{\text{ds}}^{\text{V}}[D_V](\text{env}_V, \text{sto}) = (\text{env}'_V, \text{sto}')$$

$$\text{and } \mathcal{D}_{\text{ds}}^{\text{P}}[D_P] \text{env}'_V \text{env}_P = \text{env}'_P$$

$$\mathcal{S}_{\text{ds}}[\text{call } p] \text{env}_V \text{env}_P = \text{env}_P p$$