Report for Advance Algorithm Programming Assignment 1

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1 Implementation Details

1.1 algorithm

The algorithm is as follows:

1. Create points in 4D using 3 coordinates : $(\mathbf{x}, \mathbf{y}, \mathbf{z}, \mathbf{x^2 + y^2 + z^2})$

2. Compute convex hull in 4D by calling qhull[1] with 4D points.

3. Looping through all facets in 4D convex hull,

   - Save the vertices of a facets as the vertices of tetrahedron. This vertices are 3 coordinates($\mathbf{x}, \mathbf{y}, \mathbf{z}$).

   - Compute the sign volume of tetrahedron

   - If the normal vector of tetrahedron points downward and the volume is not zero, generate faces of tetrahedron. In other words, if this tetrahedron is lower convex hull and all points are not coplanar, render this tetrahedron.

1.2 software

OS : Window 8.1K
IDE : Visual Studio 2013
*NOTE : I use the dynamic library for freeglut.

2 Example Output

Here are example results. Each image in Fig. 1 Fig. 12 shows that (a) A set of points, (b) a set of edges in Delanauy triangulation, (c)a set of faces in Delanauy triangulation, and (d) a set of total tetrahedra. We can observe that Delanauy triangulation does not have intersections between edges. Otherwise, a simple projection of whole tetrahedra has multiple intersections between edges (Fig. 13).

3 Know bugs/limitations

There are some limitations on this code. First, this code doesn't handle the duplication of faces while add tetrahedron to be draw. Also, I found some visual artifact on the Delanauy triangulation of ellipsoid(Fig. 14). I could not find the reason why.

References

[1] Qhull. http://www.qhull.org/. Accessed: 2015-10-14. 2
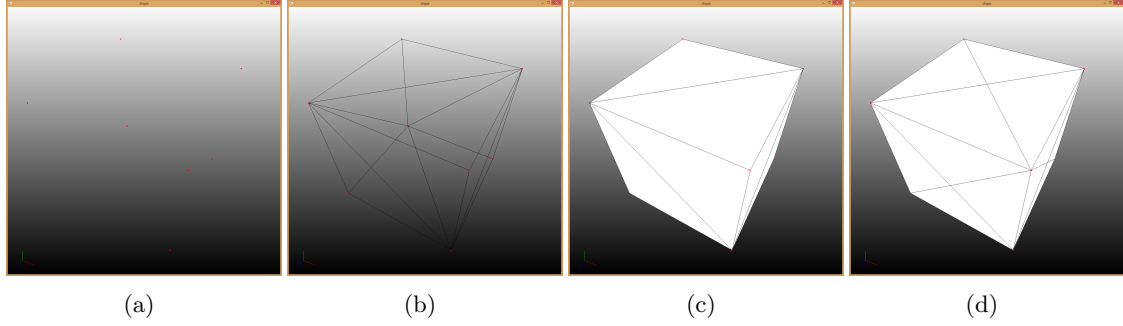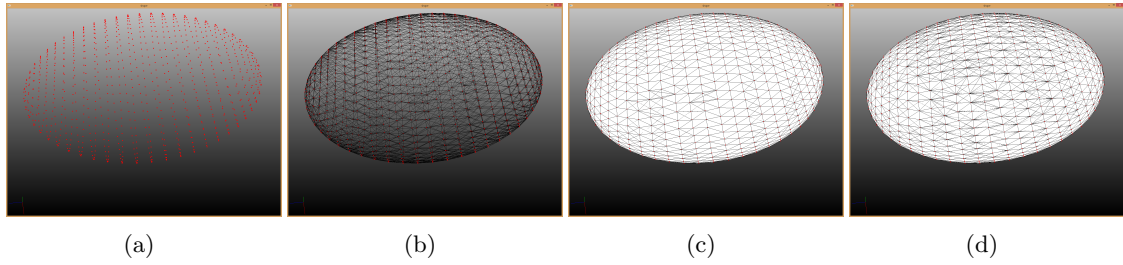
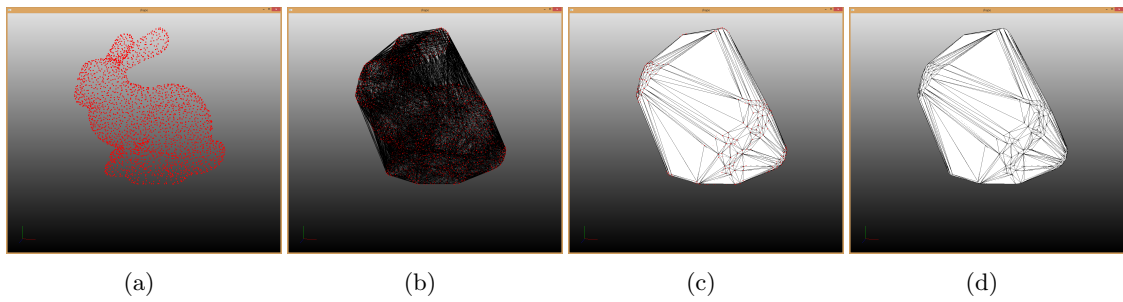Figure 1: A cube example

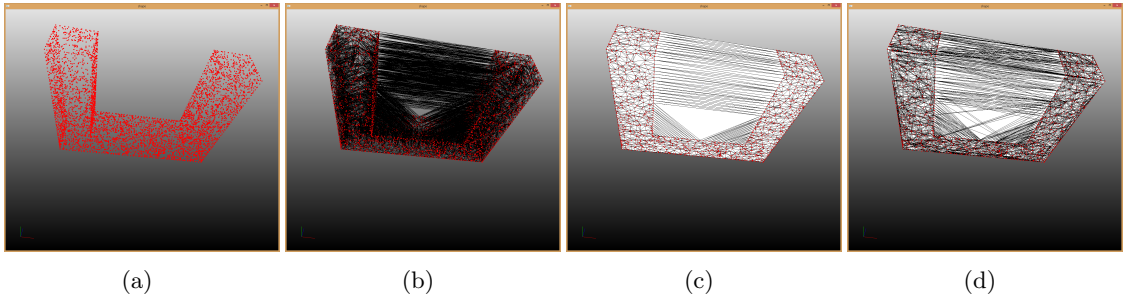Figure 2: An ellipsoid example

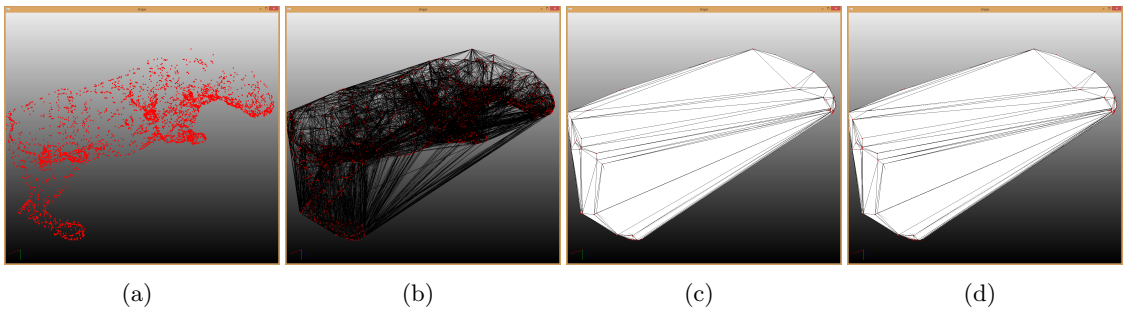Figure 3: A bunny example
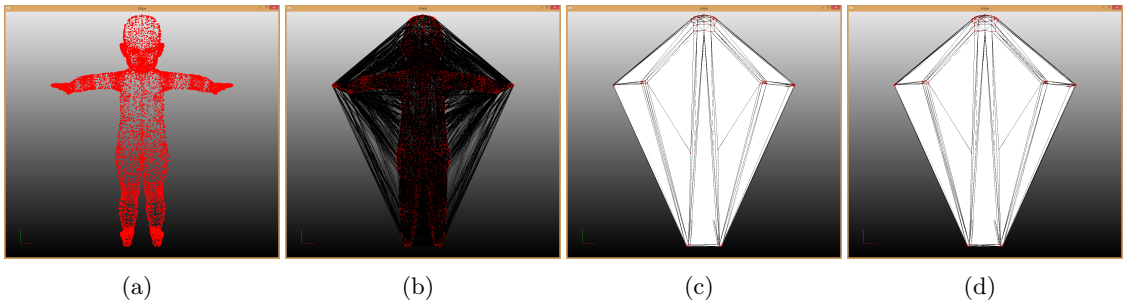
Figure 4: An 'U' example
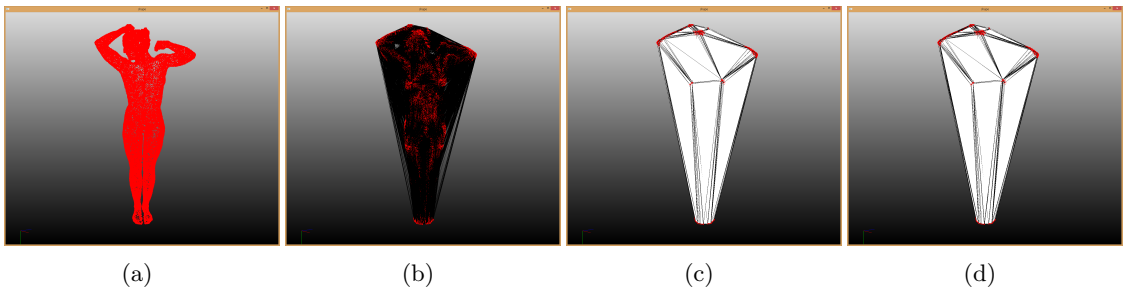

Figure 5: A bull example

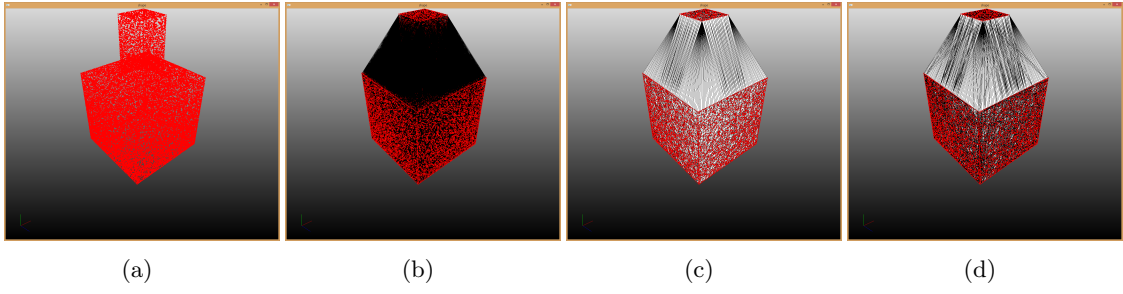Figure 6: An baby example

Figure 7: An woman example

(a)   (b)   (c)   (d)

Figure 8: A 'T' example

(a)   (b)   (c)   (d)
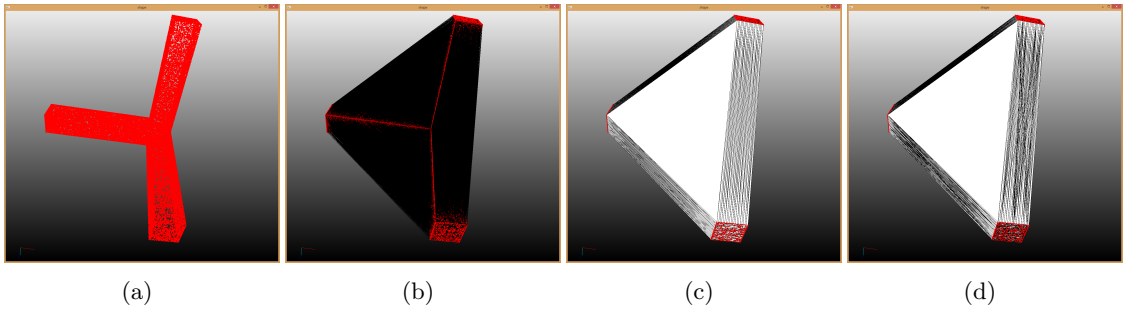
Figure 9: An 'Y' example

(a)   (b)   (c)   (d)
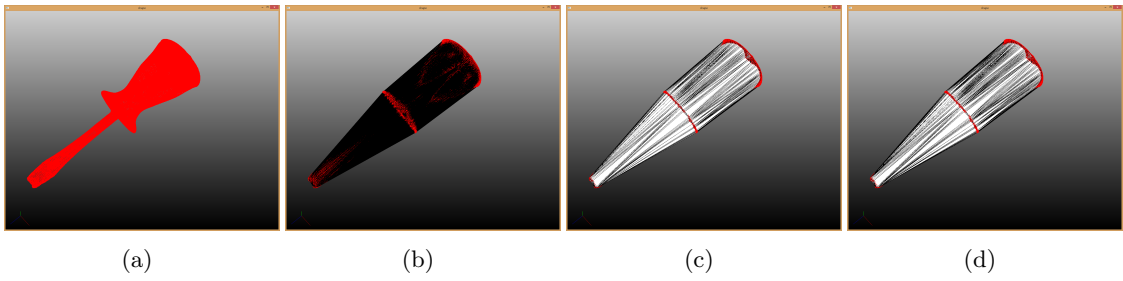
Figure 10: A screwdriver example

(a)   (b)   (c)   (d)

Figure 11: A spoon example

(a)   (b)   (c)   (d)
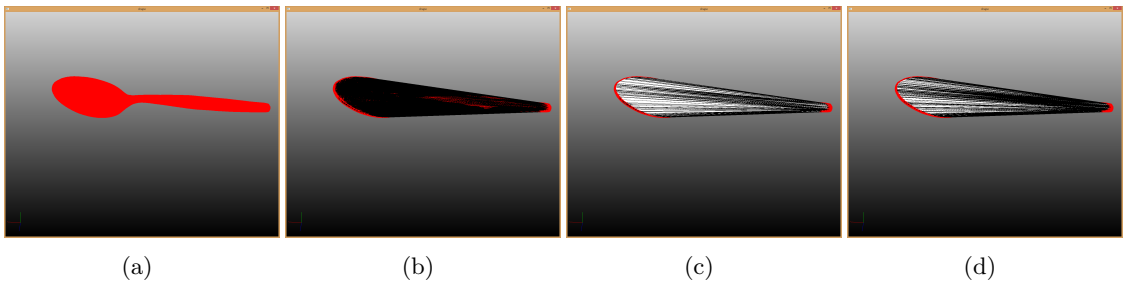
Figure 12: A teeth example

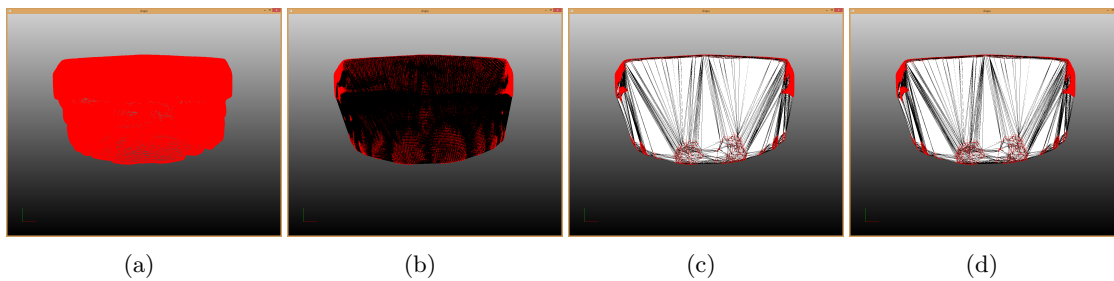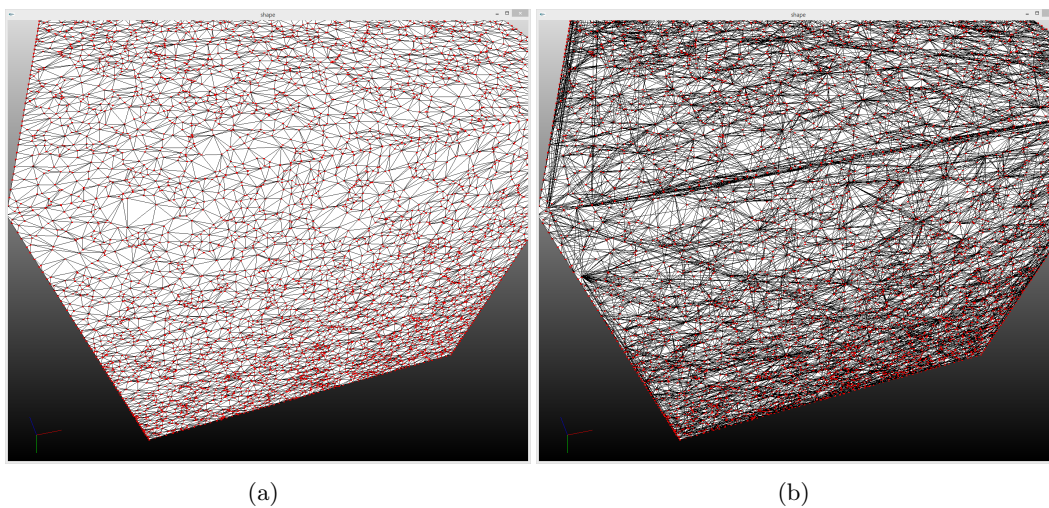(a)   (b)

Figure 13: Difference between projection result of Delanauy triangulation and all tetrahedra.

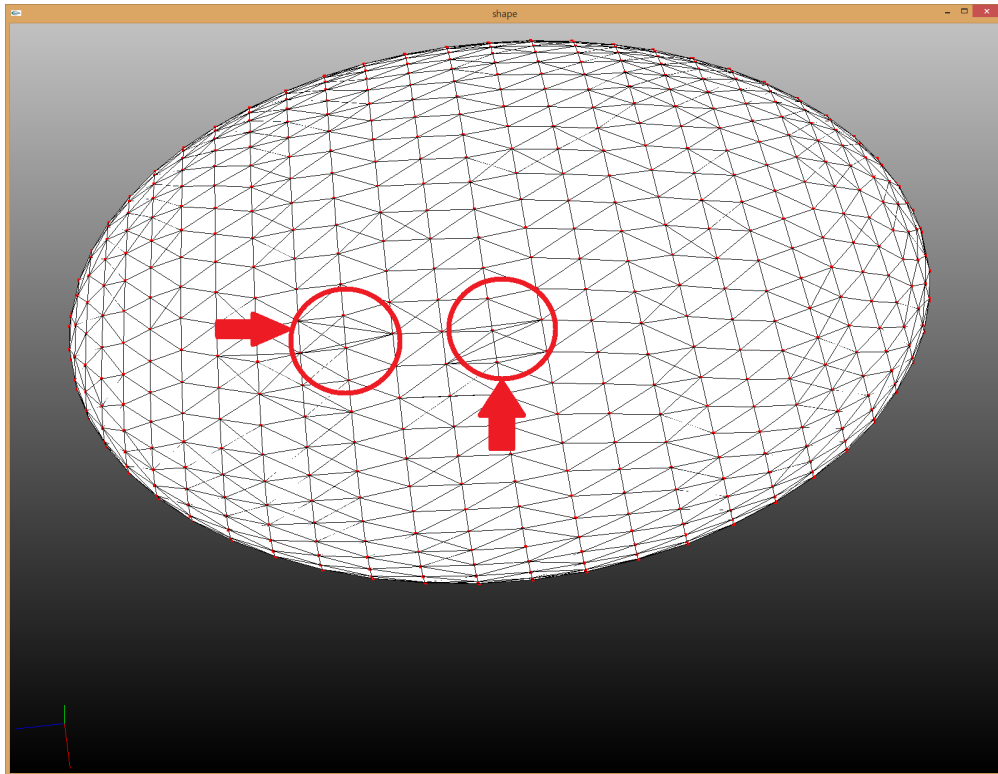Figure 14: Ellipsoid bug