

Recap of Central Results

- Longitudinal modeling of non-Gaussian outcomes is hard!
- Subject specific model \rightarrow Random effects model \rightarrow GLMMs
 - Conditional independence assumption
 - Note: LMM permits additional residual correlation
- GLMM vs. GEE
 - Underlying effects of covariates are the same (biology), but how we model them is different
 - Interpretations are model specific
 - Equal only in special cases
 - Subject specific vs. marginal interpretation
 - Challenging to interpret some parameters

Recap of Central Results (2)

- Inference and estimation
 - MLE from marginal model
 - Theoretical result follow from ML theory: consistency and asymptotic normality of $\hat{\beta}$
 - Main challenge: computation
- Approaches to integration
 - Numerical integration via Adaptive Guassian Quadrature (or others)
 - Approximation: Laplace, Solomon-Cox, PQL and CPQL procedures
 - EM algorithm
 - Note that all of these can be problematic in different situations and slow!

Comments on Integration/Solving in R

- Tools in R:
 - `integrate()` and `cubature` package for integration
 - `nlm()` and `optim()` for optimization
 - `numDeriv()` for getting Hessians
- lme4 bundles a lot of this stuff for you
- SAS is (again) probably a little bit better
- **None of the R packages are perfect and need to look at the output carefully**
- GEE is a bit more stable (numerically)

GLMM Issues

- Assume: Mean model is correct
- Assume: Conditional independence: given b_i , Y_{ij} 's are independent
- Careful: causal statements on what happens if we change X by one unit

Advantages of GLMMs

- If we are interested in conditional inference
- If we want subject specific trajectories
- Major: dealing with missing data

Key References

- Breslow & Day (1989)
- Breslow & Clayton (1993)
- Zeger, Liang, Albert (1988)
- Neuhaus, Kalbfleish, Hauck (1991)
- Zeger & Liang (1992)
- Breslow & Lin (1995)
- Lin & Breslow (1996)
- Lin (1997)

Where we are in 571...

1. Introduction to Correlated Data (HW1)
2. **Linear Mixed Models** (HW2)
3. Review of GLMs and Quasi-likelihood
4. **Generalized Estimating Equations** (HW3)
5. Final project description (HW 5)
6. **Generalized Linear Mixed Models** (HW4)
7. Missing Data
8. Classical and Modern Multivariate Analysis
9. Group Papers Due