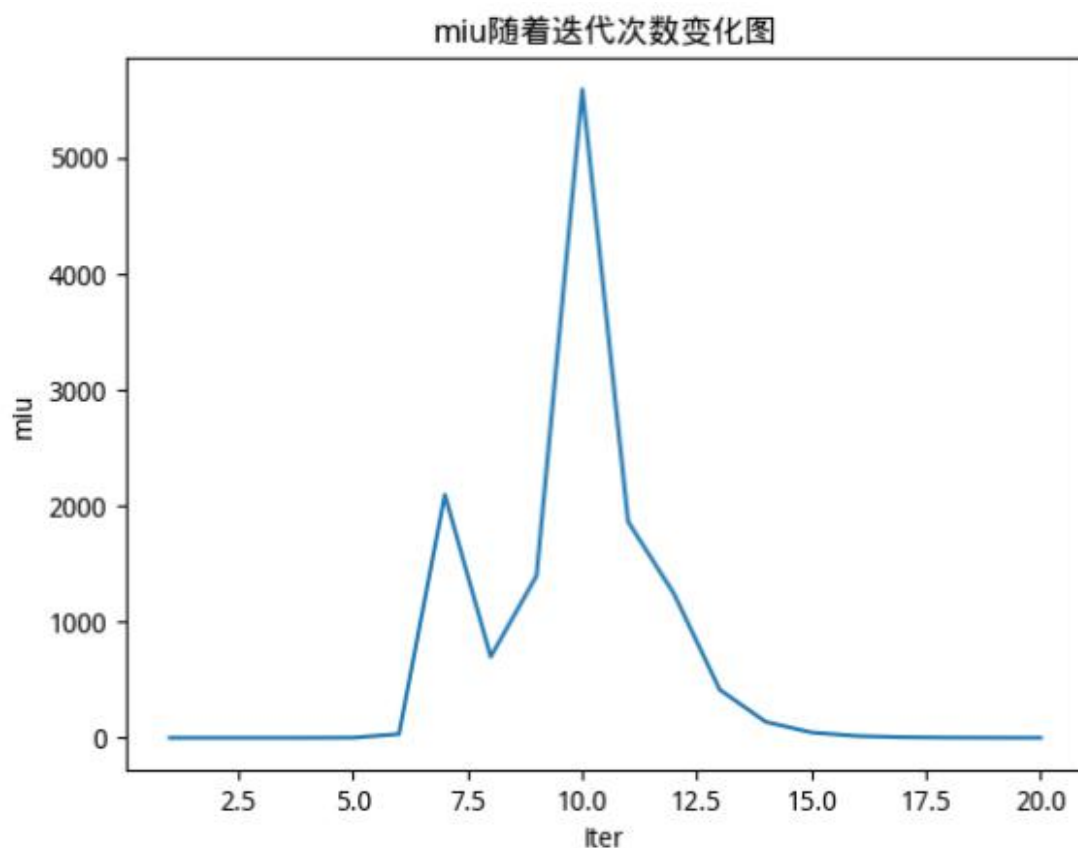


2.

```
import numpy as np
import matplotlib.pyplot as plt
plt.rcParams['font.sans-serif'] = ['Droid Sans Fallback'] #设置中文字体
plt.rcParams['axes.unicode_minus']=False #正确显示负号
tmp = range(1, 21)
x = np.array(tmp)
print(x)
y = np.loadtxt('lambda.txt', unpack=True, dtype=float, usecols=0)
##plt.scatter(x, y, s=0.5, c='r', alpha=1)
plt.plot(x,y)
plt.title('miu 随着迭代次数变化图')
plt.xlabel('iter')
plt.ylabel('miu')
plt.show()
```



3. 公式推导：

受阻尼因子的更新：

若半比例因子分母始终大于 0，如果：增大阻尼减小步长。

$$f_{15} = \frac{\partial \alpha_{b_i b_{k+1}}}{\partial s b_k^3} = \frac{\partial (\alpha_{b_i b_k} + \frac{1}{2} \alpha_{b_k} s t^2)}{\partial s b_k^3} = \frac{1}{2} \frac{\partial \alpha}{\partial s b_k^3} s t^2$$

$$\therefore \frac{\partial \alpha s t}{\partial s b_k^3} = \frac{1}{2} \frac{\partial [\alpha_{b_i b_{k+1}} \otimes \frac{1}{2} s b_k^3 s t^2]}{\partial s b_k^3} (\alpha_{b_{k+1}} - b_k^a)$$

$$= \frac{1}{2} \cdot \left[\frac{\partial R_{b_i b_{k+1}} \exp[-s b_k^3 s t]}{\partial s b_k^3} (\alpha_{b_{k+1}} - b_k^a) \right]$$

$$= \frac{1}{2} \left[\frac{\partial R_{b_i b_{k+1}} [-s b_k^3 s t] (\alpha_{b_{k+1}} - b_k^a)}{\partial s b_k^3} \right]$$

$$= -\frac{1}{2} \frac{\partial R_{b_i b_{k+1}} (\alpha_{b_{k+1}} - b_k^a) \times [-s b_k^3 s t]}{\partial s b_k^3} = -\frac{1}{2} R_{b_i b_{k+1}} (\alpha_{b_{k+1}} - b_k^a) \times (-s t)$$

从而得 $\frac{\partial \alpha_{b_i b_{k+1}}}{\partial s b_k^3} = -\frac{1}{4} R_{b_i b_{k+1}} (\alpha_{b_{k+1}} - b_k^a) s t^2 (-s t)$

若 $s t$ 是 $\alpha_{b_i b_{k+1}}$ 的 $\frac{1}{2}$ 阶导数，而 $\alpha_{b_i b_{k+1}}$ 是 $\frac{1}{4}$ 阶导数，已解决

$$g_{12} = \frac{\partial \alpha_{b_i b_{k+1}}}{\partial s n_k^3} = \frac{1}{2} \frac{\partial \alpha}{\partial s n_k^3} s t^2$$

$$\therefore \frac{\partial \alpha}{\partial s n_k^3} = \frac{1}{2} \frac{\partial [\alpha_{b_i b_{k+1}} \otimes \frac{1}{4} s n_k^3 s t^2]}{\partial s n_k^3} (\alpha_{b_{k+1}} - b_k^a)$$

从而得 $s t$ 式同

$$\Rightarrow \frac{\partial \alpha_{b_i b_{k+1}}}{\partial s b_k^3} = -\frac{1}{4} R_{b_i b_{k+1}} (\alpha_{b_{k+1}} - b_k^a) s t^2 (-\frac{1}{2} s t)$$

4. 证明：

$$\Delta X_{lm} = - \sum_{j=1}^n \frac{v_j^T F'^T}{\lambda_j + \mu} v_j$$

$$\therefore (J^T J + \mu I) \Delta X_{lm} = - J^T F' \quad \mu \geq 0$$

$$\Rightarrow \Delta X_{lm} = (J^T J + \mu I)^{-1} (-F'^T)$$

$$\text{对 } J^T J \text{ 进行特征值分解有: } J^T J = \sum_{j=1}^n \lambda_j v_j v_j^T$$

$$\text{从而 } (J^T J + \mu I)^{-1} = \sum_{j=1}^n \frac{1}{\lambda_j + \mu} v_j v_j^T$$

$$\begin{aligned} \text{从而 } \Delta X_{lm} &= - \sum_{j=1}^n \frac{v_j v_j^T F'^T}{\lambda_j + \mu} \\ &= - \sum_{j=1}^n \frac{v_j^T F'^T v_j}{\lambda_j + \mu} \end{aligned}$$

$$v_j^T F'^T = - J^T F' \text{ 转置交换} \\ = F'^T v_j$$