

# A method for underwater sampling accounting for dilution

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## Abstract

Underwater measurements are important in field biology. Measurements are made from sites of interest that usually have a higher density of specific variables. This requires control over density, because of dilution rates

## Introduction

### Hypothesis and background

### Knowledge gap

### How to fill the knowledge gap

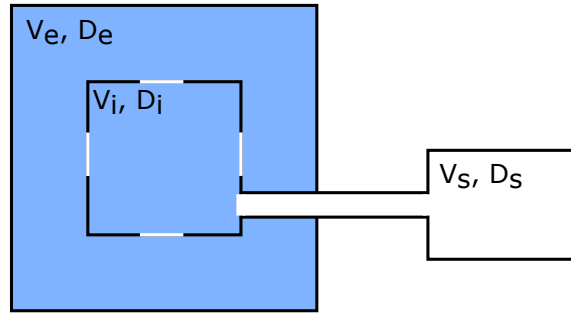


Figure 1: **The subaquatic sampling system consists of an environment ( $E$ ), a system of interest ( $I$ ), and a sample ( $S$ )** The system of interest ( $I$ ) is a subset of the environment ( $E$ ). The hypothesis is that the concentration of certain biogeochemical properties is larger in  $I$  than  $E$  ( $D_I > D_E$ ). As  $I$  is sampled,  $D_I$  will decrease by water dilution

## Methods

Input	Volume	Density
Environment	$V_E = \text{inf}$	$D_E = 10^6 \text{VLP/ml}$
System of Interest	$V_I = 1.4L$	$D_I = 10^7 \text{VLP/ml}$
Sample	$V_S = 0.5L$	$D_S = ?$
Sample rate	$v = 10 \text{ml/s}$	

Let  $I$  be a subaquatic system of interest in an environment  $E$  with a constant volume  $V_I$  (Figure 1). Suppose that our hypothesis is that the concentration of a certain biogeochemical property is higher in  $I$  than in  $D$ ,  $D_I(t=0) > D_E$ . To test this hypothesis, we take a sample  $S$  from  $I$ . Let that sample have a volume  $V_S$ . As water flows out from  $I$  at a rate  $v$ , water flows in from  $E$  at the same rate, thus diluting

the concentration  $D_I$  over time.

Given the sample  $S$ , with volume  $V_S$ , and concentration  $D_S$ , we want to be able to infer the initial concentration of interest  $D_I$ .

First, we want to get the concentration  $D_I$  as a function of time as we extract water at a rate of  $v$ . Because  $V_I$  is constant, only the mass  $M_I$  changes over time:

$$\frac{dM_I}{dt} = (-D_I(t) + D_E)v \quad (1)$$

Integrating, and dividing by  $V_I$  we get the density:

$$D_I(t) = D_E - (D_E - D_I(0)) \exp^{-\frac{v}{V_I}t} \quad (2)$$

In the case of the sample both the mass and density change over time:

$$\frac{dM_S}{dt} = D_I v \quad (3)$$

$$\frac{dV_S}{dt} = v \quad (4)$$

Integrating, we get:

$$M_S(t) = M_s(0) + vD_E t - (M_I(0) - D_E V_I) \exp^{-\frac{v}{V_I}t}. \quad (5)$$

For the volume:

$$V_S(t) = vT \quad (6)$$

## Results

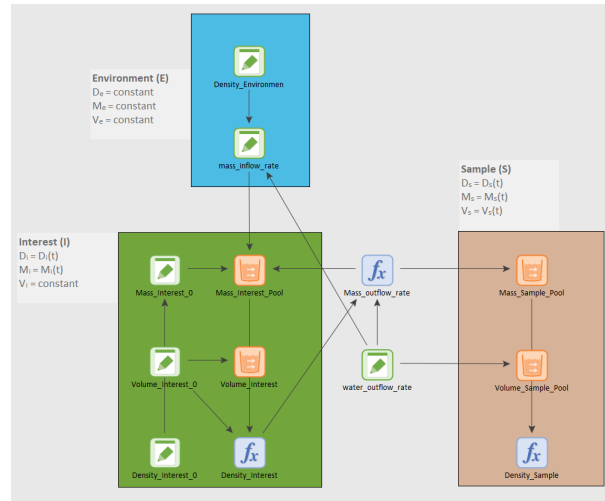


Figure 2: **GoldSim model of the sampling** The model integrates the mass, volume, and density of  $I$  and  $S$  over time

## Discussion

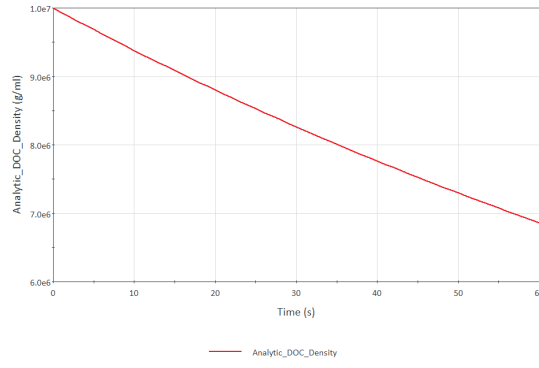


Figure 3: **Density of system of Interest ( $D_I$ ) over time**  $D_I$  decreases exponentially to  $D_E$ , the density of the environment

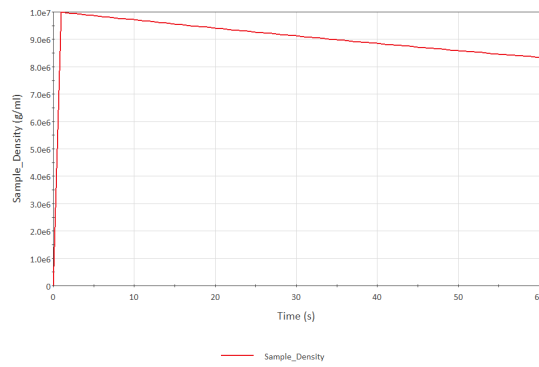


Figure 4: **Density of Sample ( $D_S$ ) over time**