

### 4.3

(I'll use  $\vdash$  to indicate reduction steps)

**S1**

$$\begin{aligned}\neg(p \vee q) &\vdash \neg(\mathbf{T} \vee \mathbf{F}) \vdash \neg\mathbf{T} \vdash \mathbf{F} \\ \neg p \vee q &\vdash \neg\mathbf{T} \vee \mathbf{F} \vdash \mathbf{F} \vee \mathbf{F} \vdash \mathbf{F}\end{aligned}$$

**S2**

$$\begin{aligned}\neg(p \vee q) &\vdash \neg(\mathbf{T} \vee \mathbf{T}) \vdash \neg\mathbf{T} \vdash \mathbf{F} \\ \neg p \vee q &\vdash \neg\mathbf{T} \vee \mathbf{T} \vdash \mathbf{F} \vee \mathbf{T} \vdash \mathbf{T}\end{aligned}$$

**S3**

$$\begin{aligned}\neg(p \vee q) &\vdash \neg(\mathbf{F} \vee \mathbf{T}) \vdash \neg\mathbf{T} \vdash \mathbf{F} \\ \neg p \vee q &\vdash \neg\mathbf{F} \vee \mathbf{T} \vdash \mathbf{T} \vee \mathbf{T} \vdash \mathbf{T}\end{aligned}$$

### 4.5

- a. "The train will either arrive or it won't arrive." This is not analytically true; it is a logical tautology (of the form  $p \vee \neg p$ ).
- b. "If it rains, we'll get wet." I think this has to be synthetic, because the speaker could be holding an umbrella, which would make the statement false.
- c. "Every doctor is a doctor." Though Saeed's discussion classified "my father is my father" as analytic, I tend to disagree. I'd say this is a tautology. Denote " $x$  is a doctor" by  $p(x)$ . Then this statement is of the form  $\forall x.p(x) \Rightarrow p(x)$ , which is a logical tautology; i.e. it holds no matter what  $p$  means. If I understood the discussion correctly, analytic truths are tautological only once you incorporate the meanings of the words.
- d. "If albert killed a deer, then Albert killed an animal." Finally, this is analytic, because in our language, a deer is an animal, so this statement must be true (but only after knowing the relationship between deer and animal).

- e. “Madrid is the captial of Spain.” This is synthetic, as it is concievable that Madrid could, one day, not be the capital of Spain anymore.
- f. “Every city has pollution problems.” This is synthetic, as it may not even be true right now.

## 4.6

- 1.  $a$  entails  $b$ , because “passed” and “failed” are simple antonyms (i.e. “passed” is the same as “didn’t fail”).
- 2.  $a$  entails  $b$ , because, well, of the relationship between the words “inherit” and “own”.
- 3.  $a$  does not entail  $b$ , since Cassidy could have sold the farm.
- 4.  $a$  entails  $b$  (under the assumption that the word “poison” implies “kill”, rather than just “make sick” or something).
- 5.  $a$  entails  $b$ , since  $b$  is just the passive construction of  $a$  (thus  $b$  entails  $a$  also).
- 6.  $a$  does not entail  $b$ , because if nobody liked the show, then it is still true that “not everyone” liked the show.

Um, how were we supposed to use the composite truth table for those?

## 4.7

**announce** Factive: “he announced that #4 took the lead” and “he didn’t announce that #4 took the lead” both presuppose that “#4 took the lead” (this is arguable, because just because something is announced does not make it true).

**assume** Not factive: “she assumed that armageddon was not coming” does not presuppose that “armageddon was not coming”.

**be** Not factive.

**aware** Factive: “he was aware that she had been crying” and “he was not aware that she had been crying” both presuppose that “she had been crying”.

**believe** Not factive. Neither “John believes that aliens exist” nor “John doesn’t believe that aliens exist” presuppose that “aliens exist”.

**be fearful** Hmmm, not factive, I think. “Sue was fearful of aliens coming” does not presuppose that aliens were coming.

**be glad** Factive. “Jamie was glad that it was christmas” and “Jamie was not glad that it was christmas” both presuppose that it was christmas.

**be sorry** Factive. Use the same sentence as above.<sup>1</sup>

**be worried** Not factive. “Paul was worried that the red coats were coming” does not presuppose that they were coming.

**know** Factive. “Daniel knew that there was a blue horse” and “Daniel didn’t know that there was a blue horse” both presuppose that “there was a blue horse”.

**reason** Factive. That is arguable, because “Willard Quine reasoned that ‘this statement is false’ must be false” doesn’t presuppose that what he reasoned was true, only that he reasoned it.

**reported** Factive. “Jimmy reported that the ant colony had grown” and “Jimmy did not report that the ant colony had grown” both presuppose that “the ant colony had grown”.

## 4.8

The following will be the reasoning, so I don’t have to monotonously repeat it. If I say “presuppose”, then I negated the sentence and *b* was still true. If I say “entail”, then I negated the sentence and *b* did not necessarily follow anymore.

### 1. Presuppose.

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<sup>1</sup>Yeah, I’m lazy, I know.

**2.** Entail.

**3.** Presuppose.

**4.** Entail.

**5.** Presuppose.