Introduction to the Finite Difference Method: Filling and Draining a Cylindrical Tube

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Chapter 1

Filling a Tank

1.1 Water Tank Exercises

1.1.1 Rectangular Prism

Create a model for the filling of a water tank that is a rectangular prism with a width of 10 cm and a length of 5 cm.

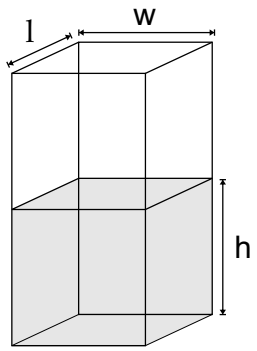

Figure 1.1: Water Tank

Chapter 2

Solving Differential Equations

What we've been doing in the preceding chapters is, basically, solving differential equations. You're given an equation for the rate of change of something (height changes with time), and an initial value, and then have to see how the system evolves over time.

2.1 Constant change

What if the rate of change is constant: our quantity changes at the same rate everywhere. For example:

$$\frac{dy}{dx} = \frac{1}{2} \tag{2.1}$$

time (s)	height measured (cm)	height modeled (cm)
1	0	6.57
7	10	16.00
12	20	23.86
16.8	30	31.72
21.5	40	39.58
26.2	50	45.87

Table 2.1: Combined time, measured data, and modeled data.

Code 2.1: Model of a filling tube without graphing (*water-filling-fd-noGraph.py*)

```
1 import math
2 # Finite Difference Model
3
```

```
4  # PARAMETERS
5  dt = 1.
6  nsteps = 20
7
8  r = 2.25      # radius (cm)
9  Q = 5         # Volume inflow rate: (cubic cm / s)
10 h = 0         # Initial height (cm)
11
12 print(0, h)       # print initial values
13
14 # TIME LOOP
15 for t in range(1, nsteps):
16     modelTime = t * dt
17
18     dh = Q * dt / (math.pi * r**2)     # find the change in height
19     h = h + dh                         # update height
20
21     print(modelTime, h)
```