Introduction to the Finite Difference Method: Filling and Draining a Cylindrical Tube

Lensyl Urbano

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Chapter 1

Filling a Tank

1.1 Water Tank Exercises

1.1.1 Rectangular Prism

Create a model for the filling of a water tank that is a rectangular prism with a width of 10 cm and a length of 5 cm (Figure 1.1.1). There is some data in Table 2.1.

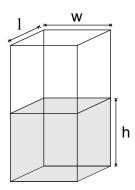


Figure 1.1: Water Tank

Chapter 2

Solving Differential Equations

What we've been doing in the preceding chapters is, basically, solving differential equations. You're given an equation for the rate of change of something (height changes with time), and an initial value, and then have to see how the system evolves over time.

2.1 Constant change

What if the rate of change is constant: our quantity changes at the same rate everywhere. For example:

$$\frac{dy}{dx} = \frac{1}{2} \tag{2.1}$$

time (s)	height measured (cm)	height modeled (cm)
1	0	6.57
7	10	16.00
12	20	23.86
16.8	30	31.72
21.5	40	39.58
26.2	50	45.87

Table 2.1: Combined time, measured data, and modeled data.

Code 2.1: Model of a filling tube without graphing (water-filling-fd-noGraph.py)

```
1 | import math | # Finite Difference Model | 3
```

```
# PARAMETERS
    dt \ = \ 1 \, .
5
    nsteps = 20
6
7
              \# radius (cm)
    r = 2.25
8
                \# \ Volume \ inflow \ rate: (cubic \ cm \ / \ s)
   Q = 5
9
    h = 0
              \# Initial \ height \ (cm)
10
11
    print(0, h) # print initial values
12
13
    # TIME LOOP
14
    for t in range(1, nsteps):
15
        modelTime = t * dt
16
17
        dh = Q * dt / (math.pi * r**2) # find the change in height
18
        h = h + dh
                                           # update height
19
20
        print(modelTime, h)
21
```