

$$\text{top} = 116 \oplus 111 \oplus 112 = \underline{107} \bmod 11 = 8$$

$$\text{tree} = 116 \oplus 114 \oplus 101 \oplus 101 = \underline{6}$$

$$\text{root} = 114 \oplus 111 \oplus 111 \oplus 116 = \underline{6}$$

$$\text{AVL} = 65 \oplus 86 \oplus 76 = \underline{91} \bmod 11 = 3$$

$$\text{exam} = 101 \oplus 120 \oplus 97 \oplus 109 = \underline{17} \bmod 11 = 6$$

$$\text{pass} = 112 \oplus 97 \oplus 115 \oplus 115 = \underline{14} \bmod 11 = 6$$

$$\text{fail} = 102 \oplus 97 \oplus 105 \oplus 108 = \underline{2}$$

$$\text{DS} = 68 \oplus 83 = \underline{23} \bmod 11 = 1$$

$$\text{PQ} = 80 \oplus 81 = \underline{1}$$

$$\text{stack} = 115 \oplus 116 \oplus 97 \oplus 99 \oplus 107 = \underline{110} \bmod 11 = 0$$

$$\text{pot} = 112 \oplus 111 \oplus 116 = \underline{107} \bmod 11 = 8$$

~~stop~~

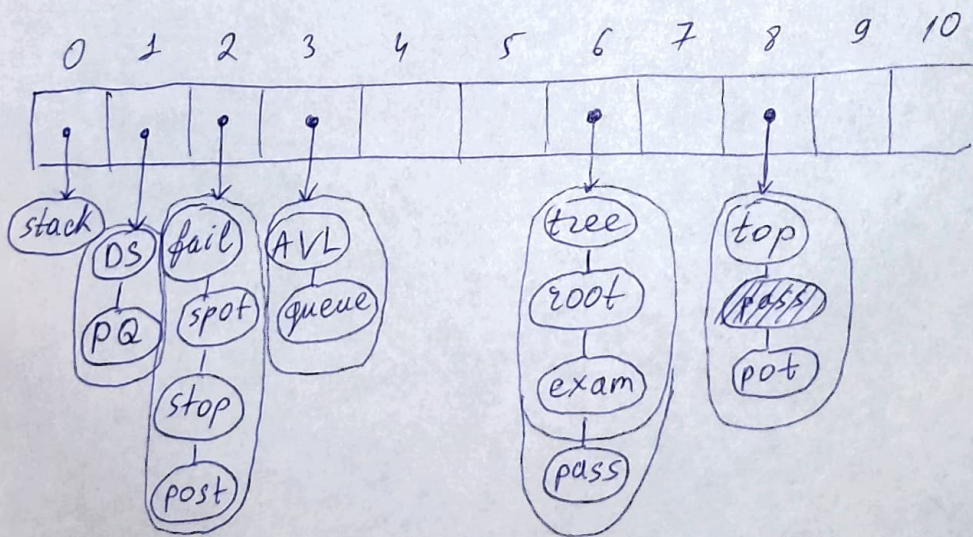
$$\text{spot} = 115 \oplus 112 \oplus 111 \oplus 116 = \underline{24} \bmod 11 = 2$$

$$\text{stop} = 115 \oplus 116 \oplus 111 \oplus 112 = \underline{24} \bmod 11 = 2$$

$$\text{post} = 112 \oplus 111 \oplus 115 \oplus 116 = \underline{24} \bmod 11 = 2$$

$$\text{queue} = 113 \oplus 117 \oplus 101 \oplus 117 \oplus 101 = \underline{113} \bmod 11 = 3$$

a)





$$\begin{aligned}
 6) 71) \text{top} &= 116 \cdot 31^2 + 111 \cdot 31 + 112 = 115029 \\
 \text{tree} &= 116 \cdot 31^3 + 114 \cdot 31^2 + 101 \cdot 31 + 101 = 3568542 \\
 \text{root} &= 114 \cdot 31^3 + 111 \cdot 31^2 + 111 \cdot 31 + 116 = 3506402 \\
 \text{AVL} &= 65 \cdot 31^2 + 86 \cdot 31 + 76 = 65207 \\
 \text{exam} &= 101 \cdot 31^3 + 120 \cdot 31^2 + 97 \cdot 31 + 109 = 3127327 \\
 \text{pass} &= 112 \cdot 31^3 + 97 \cdot 31^2 + 115 \cdot 31 + 115 = 3433489 \\
 \text{fail} &= 102 \cdot 31^3 + 97 \cdot 31^2 + 105 \cdot 31 + 108 = 3135262 \\
 \text{DS} &= 68 \cdot 31 + 83 = 2191 \\
 \text{PQ} &= 80 \cdot 31 + 81 = 2561 \\
 \text{stack} &= 115 \cdot 31^4 + 116 \cdot 31^3 + 97 \cdot 31^2 + 99 \cdot 31 + 107 = 109757069 \\
 \text{pot} &= 112 \cdot 31^2 + 111 \cdot 31 + 116 = 111189 \\
 \text{spot} &= 115 \cdot 31^3 + 112 \cdot 31^2 + 111 \cdot 31 + 116 = 3537154 \\
 \text{stop} &= 115 \cdot 31^3 + 116 \cdot 31^2 + 111 \cdot 31 + 112 = 3540994 \\
 \text{post} &= 112 \cdot 31^3 + 111 \cdot 31^2 + 115 \cdot 31 + 116 = 3446944 \\
 \text{queue} &= 113 \cdot 31^4 + 117 \cdot 31^3 + 101 \cdot 31^2 + 117 \cdot 31 + 101 = 107944209
 \end{aligned}$$

$$\text{MAD} - p=91, a=19, b=23$$

$$\begin{aligned}
 115029 &\rightarrow \underline{11} \\
 3568542 &\rightarrow \underline{6} \\
 3506402 &\rightarrow \underline{6} \\
 65207 &\rightarrow \underline{1} \\
 3127327 &\rightarrow \underline{10} \\
 3433489 &\rightarrow \underline{8} \\
 3135262 &\rightarrow \underline{1} \\
 2191 &\rightarrow \underline{3} \\
 2561 &\rightarrow \underline{15} \\
 109757069 &\rightarrow \underline{9} \\
 111189 &\rightarrow \underline{7} \\
 3537154 &\rightarrow \underline{3} \\
 3540994 &\rightarrow \underline{0} \\
 3446944 &\rightarrow \underline{1} \\
 107944209 &\rightarrow \underline{11}
 \end{aligned}$$



$$b) i) \text{ top} = 116 \cdot 33^2 + 111 \cdot 33^1 + 112 \cdot 33^0 = \cancel{180098} \quad 130098$$

$$\text{tree} = 116 \cdot 33^3 + 114 \cdot 33^2 + 101 \cdot 33 + 101 \cdot 1 = 4296272$$

$$\text{root} = 114 \cdot 33^3 + 111 \cdot 33^2 + 111 \cdot 33 + 116 = 4221476$$

$$\text{AVL} = 65 \cdot 33^2 + 86 \cdot 33 + 76 = 73699$$

$$\text{exam} = 101 \cdot 33^3 + 120 \cdot 33^2 + 97 \cdot 33 + 109 = 3763627$$

$$\text{pass} = 112 \cdot 33^3 + 97 \cdot 33^2 + 115 \cdot 33 + 115 \cdot 1 = 4134487$$

$$\text{fail} = 102 \cdot 33^3 + 97 \cdot 33^2 + 105 \cdot 33 + 108 \cdot 1 = 3774780$$

$$\text{DS} = 68 \cdot 33 + 83 = 2327$$

$$\text{PQ} = 80 \cdot 33 + 81 = 2723$$

$$\text{stack} = 115 \cdot 33^4 + 116 \cdot 33^3 + 97 \cdot 33^2 + 99 \cdot 33 + 107 = 140658614$$

$$\text{root} = 112 \cdot 33^2 + 111 \cdot 33 + 116 = 125747$$

$$\text{spot} = 115 \cdot 33^3 + 112 \cdot 33^2 + 111 \cdot 33 + 116 = 4258502$$

$$\text{stop} = 115 \cdot 33^3 + 116 \cdot 33^2 + 111 \cdot 33 + 112 = 4262854$$

$$\text{post} = 112 \cdot 33^3 + 111 \cdot 33^2 + 115 \cdot 33 + 116 = 4149734$$

$$\text{queue} = 113 \cdot 33^4 + 117 \cdot 33^3 + 101 \cdot 33^2 + 117 \cdot 33 + 101 = 138327323$$

MAD - let's take  $p = 41$ ,  $a = 19$ ,  $b = 23$ .  
 $(130098 \cdot 19 + 23) \bmod 41$

$$[(130098 \cdot 19 + 23) \bmod 41] \bmod 17 = \underline{14}$$

$$[(4296272 \cdot 19 + 23) \bmod 41] \bmod 17 = \underline{2}$$

$$[(4221476 \cdot 19 + 23) \bmod 41] \bmod 17 = \underline{13}$$

$$73699 \rightarrow \underline{14}$$

$$3763627 \rightarrow \underline{16}$$

$$4134487 \rightarrow \underline{19}$$

$$3774780 \rightarrow \underline{1}$$

$$2327 \rightarrow \underline{4}$$

$$2723 \rightarrow \underline{1}$$

$$140658614 \rightarrow \underline{12}$$

$$125747 \rightarrow \underline{6}$$

$$4258502 \rightarrow \underline{12}$$

$$4262854 \rightarrow \underline{3}$$

$$4149734 \rightarrow \underline{1}$$

$$138327323 \rightarrow \underline{14}$$

b) i)

0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16

pass	fail	tree	PQ	DS	spot	pot	stop	post	queue			stack	root	top	AVL	exam
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b) ii)

0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16

stop	AVL	fail	DS	spot	post	tree	root	pass	stack	exam	top	pot	queue		PQ	
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8) iii)  $J = 74$

$$[(74 \cdot 19 + 23) \bmod 41] \bmod 17 = \textcircled{1} - \text{first step}$$

2. Check at index 1, fail  $\neq J$

3. index 2, fail  $\neq J$

4. index 3, fail  $\neq J$

⋮

14. index 10, table[10] == null, fail.

Total number of steps -  $\textcircled{11}$

iv) 2. Check at index 1, fail  $\neq J$

⋮

15. check at index 14, table[14] == null, fail.

Total number of steps -  $\textcircled{15}$