

```

In[=]:= (*=====
(*Parameters for 2-meter wormhole*)
(*=====*)

ClearAll["Global`*"];

R0 = 2.0
w = 0.2
A = 0.01
ε = 0.04

hFD = w / 25;

(*=====
(*Conformal factor Φ(r) *)
(*=====*)

ClearAll[ΦSafe];

ΦSafe[x_?NumericQ, y_?NumericQ, z_?NumericQ] :=
Module[{xx = SetPrecision[x, 50], yy = SetPrecision[y, 50],
zz = SetPrecision[z, 50], r, ph}, r = Max[Sqrt[xx^2 + yy^2 + zz^2], ε];
ph = -A (1 - R0 / r) Exp[-((r - R0)^2) / w^2];
SetPrecision[ph, 50]];

(*=====
(*Metric g and inverse*)
(*=====*)

ClearAll[g, gInv];

g[x_?NumericQ, y_?NumericQ, z_?NumericQ] := Module[{f = Exp[2 ΦSafe[x, y, z]]},
{{{-f, 0, 0, 0}, {0, 1/f, 0, 0}, {0, 0, 1/f, 0}, {0, 0, 0, 1/f}}};

gInv[x_?NumericQ, y_?NumericQ, z_?NumericQ] := gInv[x, y, z] = Inverse[g[x, y, z]];

(*=====
(*Finite differences*)
(*=====*)

ClearAll[dΦ];

dΦ[{x_, y_, z_}, dir_] := Module[
{xx = SetPrecision[x, 50], yy = SetPrecision[y, 50], zz = SetPrecision[z, 50], δ = hFD},
Switch[dir, 1, (ΦSafe[xx + δ, yy, zz] - ΦSafe[xx - δ, yy, zz]) / (2 δ),
2, (ΦSafe[xx, yy + δ, zz] - ΦSafe[xx, yy - δ, zz]) / (2 δ), 3,
(ΦSafe[xx, yy, zz + δ] - ΦSafe[xx, yy, zz - δ]) / (2 δ)]];

```

```

(*=====
(*Einstein tensor*)
(*=====*)

ClearAll[Einstein];

Einstein[x_?NumericQ, y_?NumericQ, z_?NumericQ] :=
Module[{grad = Table[dF[{x, y, z}, i], {i, 1, 3}]},
DiagonalMatrix[{-2 Total[grad^2], 2 grad[[1]]^2, 2 grad[[2]]^2, 2 grad[[3]]^2}]];

(*=====
(*Stress-energy tensor*)
(*=====*)

ClearAll[T];
T[x_?NumericQ, y_?NumericQ, z_?NumericQ] := Einstein[x, y, z] / (8 \[Pi]);

(*=====
(*Energy conditions*)
(*=====*)

nullVec = {1, 1, 0, 0};
timeVec = {1, 0, 0, 0};

NEC[x_, y_, z_] := Chop[nullVec.T[x, y, z].nullVec];
WEC[x_, y_, z_] := Chop[timeVec.T[x, y, z].timeVec];

SEC[x_?NumericQ, y_?NumericQ, z_?NumericQ] :=
Module[{Tval = T[x, y, z], \[Rho], px, py, pz}, \[Rho] = -Tval[[1, 1]];
px = Tval[[2, 2]];
py = Tval[[3, 3]];
pz = Tval[[4, 4]];
Chop[\[Rho] + px + py + pz]];

DEC[x_?NumericQ, y_?NumericQ, z_?NumericQ] :=
Module[{Tval = T[x, y, z], \[Rho], px, py, pz}, \[Rho] = -Tval[[1, 1]];
px = Tval[[2, 2]];
py = Tval[[3, 3]];
pz = Tval[[4, 4]];
If[\[Rho] \[GreaterEqual] Abs[px] \&& \[Rho] \[GreaterEqual] Abs[py] \&& \[Rho] \[GreaterEqual] Abs[pz], Chop[\[Rho]], Chop[-\[Rho]]]];

(*=====
(*Exotic energy integral*)
(*=====*)

ClearAll[\[Rho], sqrtMinusDet, integrand];

```

```

ρ[r_?NumericQ] := -T[r, 0, 0][1, 1];
sqrtMinusDet[r_] := Exp[-2 #Safe[r, 0, 0]];
integrand[r_] := 4 π r^2 ρ[r] × sqrtMinusDet[r];

totalExoticEnergy =
NIntegrate[integrand[r], {r, ε, 3 R0}, WorkingPrecision → 50, AccuracyGoal → 8,
PrecisionGoal → 8, Method → {"GlobalAdaptive", "SymbolicProcessing" → 0}];

Print["► Total exotic energy = ", totalExoticEnergy];

(*=====
(*Energy condition table*)
(*=====*)

TableForm[Table[{r, NEC[r, 0, 0], WEC[r, 0, 0], SEC[r, 0, 0], DEC[r, 0, 0]}, {
r, {0.2, 0.5, 1.0, 2.0, 3.0, 4.0}}],
TableHeadings → {None, {"r", "NEC", "WEC", "SEC", "DEC"}}]

Out[=]=
2.

Out[=]=
0.2

Out[=]=
0.01

Out[=]=
0.04

► Total exotic energy = 0.000018749504574268654064883912078406538817004466276537

Out[=]//TableForm=


| r   | NEC | WEC                       | SEC                      | DEC                      |
|-----|-----|---------------------------|--------------------------|--------------------------|
| 0.2 | 0   | 0                         | 0                        | 0                        |
| 0.5 | 0   | 0                         | 0                        | 0                        |
| 1.  | 0   | 0                         | 0                        | 0                        |
| 2.  | 0   | $-1.98314 \times 10^{-6}$ | $3.96629 \times 10^{-6}$ | $1.98314 \times 10^{-6}$ |
| 3.  | 0   | 0                         | 0                        | 0                        |
| 4.  | 0   | 0                         | 0                        | 0                        |


```