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In[*]:= (*=====*)
(*Parameters for 2-meter wormhole*)
(*=====*)
ClearAll["Global`*"];

R0 = 2.0
w = 0.2
A = 0.01
ε = 0.04

hFD = w / 25;

(*=====*)
(*Conformal factor  $\Phi(r)$ *)
(*=====*)

ClearAll[ΦSafe];

ΦSafe[x_?NumericQ, y_?NumericQ, z_?NumericQ] :=
Module[{xx = SetPrecision[x, 50], yy = SetPrecision[y, 50],
  zz = SetPrecision[z, 50], r, ph}, r = Max[Sqrt[xx^2 + yy^2 + zz^2], ε];
ph = -A (1 - R0 / r) Exp[-((r - R0)^2) / w^2];
SetPrecision[ph, 50]];

(*=====*)
(*Metric g and inverse*)
(*=====*)

ClearAll[g, gInv];

g[x_?NumericQ, y_?NumericQ, z_?NumericQ] := Module[{f = Exp[2 ΦSafe[x, y, z]]},
  {{-f, 0, 0, 0}, {0, 1/f, 0, 0}, {0, 0, 1/f, 0}, {0, 0, 0, 1/f}}];

gInv[x_?NumericQ, y_?NumericQ, z_?NumericQ] := gInv[x, y, z] = Inverse[g[x, y, z]];

(*=====*)
(*Finite differences*)
(*=====*)

ClearAll[dΦ];

dΦ[{x_, y_, z_}, dir_] := Module[
  {xx = SetPrecision[x, 50], yy = SetPrecision[y, 50], zz = SetPrecision[z, 50], δ = hFD},
  Switch[dir, 1, (ΦSafe[xx + δ, yy, zz] - ΦSafe[xx - δ, yy, zz]) / (2 δ),
  2, (ΦSafe[xx, yy + δ, zz] - ΦSafe[xx, yy - δ, zz]) / (2 δ), 3,
  (ΦSafe[xx, yy, zz + δ] - ΦSafe[xx, yy, zz - δ]) / (2 δ)]];

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(*=====*)
(*Einstein tensor*)
(*=====*)

ClearAll[Einstein];

Einstein[x_?NumericQ, y_?NumericQ, z_?NumericQ] :=
  Module[{grad = Table[D[{x, y, z}, i], {i, 1, 3}]},
    DiagonalMatrix[{-2 Total[grad^2], 2 grad[[1]]^2, 2 grad[[2]]^2, 2 grad[[3]]^2}]];

(*=====*)
(*Stress-energy tensor*)
(*=====*)

ClearAll[T];
T[x_?NumericQ, y_?NumericQ, z_?NumericQ] := Einstein[x, y, z] / (8  $\pi$ );

(*=====*)
(*Energy conditions*)
(*=====*)

nullVec = {1, 1, 0, 0};
timeVec = {1, 0, 0, 0};

NEC[x_, y_, z_] := Chop[nullVec.T[x, y, z].nullVec];
WEC[x_, y_, z_] := Chop[timeVec.T[x, y, z].timeVec];

SEC[x_?NumericQ, y_?NumericQ, z_?NumericQ] :=
  Module[{Tval = T[x, y, z],  $\rho$ , px, py, pz},  $\rho$  = -Tval[[1, 1]];
    px = Tval[[2, 2]];
    py = Tval[[3, 3]];
    pz = Tval[[4, 4]];
    Chop[ $\rho$  + px + py + pz]];

DEC[x_?NumericQ, y_?NumericQ, z_?NumericQ] :=
  Module[{Tval = T[x, y, z],  $\rho$ , px, py, pz},  $\rho$  = -Tval[[1, 1]];
    px = Tval[[2, 2]];
    py = Tval[[3, 3]];
    pz = Tval[[4, 4]];
    If[ $\rho \geq \text{Abs}[px]$  &&  $\rho \geq \text{Abs}[py]$  &&  $\rho \geq \text{Abs}[pz]$ , Chop[ $\rho$ ], Chop[- $\rho$ ]]];

(*=====*)
(*Exotic energy integral*)
(*=====*)

ClearAll[ $\rho$ , sqrtMinusDet, integrand];

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ρ[r_?NumericQ] := -T[r, 0, 0][[1, 1]];
sqrtMinusDet[r_] := Exp[-2 Sqrt[r, 0, 0]];
integrand[r_] := 4 π r^2 ρ[r] × sqrtMinusDet[r];

totalExoticEnergy =
  NIntegrate[integrand[r], {r, ε, 3 R0}, WorkingPrecision → 50, AccuracyGoal → 8,
    PrecisionGoal → 8, Method → {"GlobalAdaptive", "SymbolicProcessing" → 0}];

Print["> Total exotic energy = ", totalExoticEnergy];

(*=====*)
(*Energy condition table*)
(*=====*)

TableForm[Table[{r, NEC[r, 0, 0], WEC[r, 0, 0], SEC[r, 0, 0], DEC[r, 0, 0]},
  {r, {0.2, 0.5, 1.0, 2.0, 3.0, 4.0}}],
  TableHeadings → {None, {"r", "NEC", "WEC", "SEC", "DEC"}}]

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Out[8]=

2.

Out[9]=

0.2

Out[10]=

0.01

Out[11]=

0.04

► Total exotic energy = 0.000018749504574268654064883912078406538817004466276537

Out[12]//TableForm=

r	NEC	WEC	SEC	DEC
0.2	0	0	0	0
0.5	0	0	0	0
1.	0	0	0	0
2.	0	$-1.98314 \times 10^{-6}$	$3.96629 \times 10^{-6}$	$1.98314 \times 10^{-6}$
3.	0	0	0	0
4.	0	0	0	0