

Assume that samples  $\mathcal{X} = \{x_1, \dots, x_N\}$  follow the Bernoulli distribution with parameter  $\theta$ , i.e.,  $p(x) = \theta^x(1 - \theta)^{1-x}$ . Show that the maximum likelihood estimate of  $\theta$  is  $\theta^{MLE} = \frac{1}{N} \sum_{n=1}^N x_n$ .