Higher-Order Programming: The Essence of Functional Programming

○ Higher-Order programming is defined as

- *Programming with functions as arguments to other functions or functions as return values from functions.*

Higher-Order Programming: A Cornerstone of Functional Programming

- It is a natural outgrowth from the lambda calculus where
  a) lambda expressions can be passed to other lambda expressions, and
  b) new lambda expressions can be computed by lambda expressions
- E.g.

a) $(\lambda y. y\ 1)(\lambda x. x + 1) \Rightarrow 2$

b) $(\lambda x. (\lambda y. x + y))\ 1\ 1 \Rightarrow 2$

Modifying Behavior of a Function

- We can use this to write generic functions which we can then make specific by passing in desired behavior via a function.
- Note: this is NOT programming with generics
  - Generics are generic with respect to types
  - Higher-order functions are generic with respect to **behavior**!

Modifying Behavior of a Function

- We have seen this before with 'filter' function in the quicksort,
- The 'filter' function is generic with regards to the ordering predicate

```
function filter
    with ([],_,_) do
        []
    with ([e|rest],pivot,fcmp) do
        [e] + filter (rest,pivot,fcmp)
            if fcmp (e,pivot)  ⬅
            else filter (rest,pivot,fcmp)
end
```

If e is kept or discarded depends on the passed in function – the filter function has a generic filtering capability which is made specific by the passed in predicate.

```
let less = filter (rest,pivot,lambda with (x,y) do x < y).
let more = filter (rest,pivot,lambda with (x,y) do x >= y).
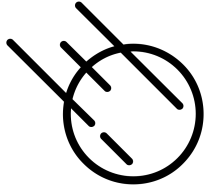```

# Modifying Behavior of a Function

- The Asteroid sort module is another example,

  sort @sort (p:%function, l:%list)

```
1   load system sort.
2
3   let sl = sort @sort(
4   (lambda with (x,y) do true if x<y else false),
5   [10,5,110,50]).
6
7   assert (sl == [5,10,50,110]).
```

```
1   load system sort.
2
3   let sl = sort @sort(
4   (lambda with (x,y) do true if x>y else false),
5   [10,5,110,50]).
6
7   assert (sl == [110,50,10,5]).
```

# Dispatch Tables

- We can also associate behavior with appropriate keys in a dispatch table.

- We can then dispatch (lookup) desired behavior given specific keys.

- Example: A generic 'calculate' function that takes two values and a key symbol and then performs the appropriate computation.
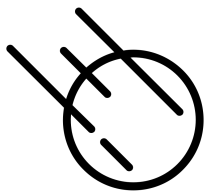
# Dispatch Tables

```
1    load system hash.
2
3    let dispatch_table = hash @hash ().
4
5    dispatch_table @insert [
6        ("+",lambda with (a,b) do a + b),
7        ("-",lambda with (a,b) do a - b),
8        ("*",lambda with (a,b) do a * b),
9        ("/",lambda with (a,b) do a / b)
10   ]
11
12   function calculate with (operator,a,b) do
13       dispatch_table @get operator (a,b)
14   end
15
16   -- Example usage
17   assert (calculate("+", 3, 5) == 8)
18   assert (calculate("-", 7, 2) == 5)
19   assert (calculate("*", 2, 4) == 8)
20   assert (calculate("/", 10, 2) == 5)
```

ln012/dispatch2.ast
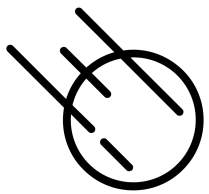
Map & Reduce

- The map and reduce functions are functions that take a function and apply the given function to a lis..
- Both functions are higher-order functions that come straight out of the functional programming tradition.
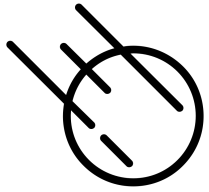
Map

- Below is Asteroid code that explains the behavior of the map function.
- Beware that map is not required to apply the function f in the sequential manner shown here
  - For example, it is free to exploit threads to apply the function f in parallel to the elements of the list.

```
list @map f

-- is equivalent to --

let r = [].
for e in list do
    r @append(f e).
end
let list = r.
```
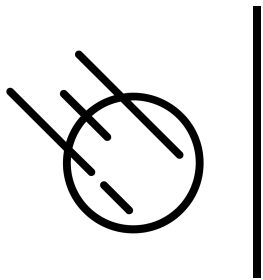
The function argument to f must be of the same type as the list elements
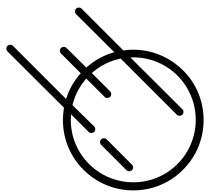
Map

- One interesting application of map is the transformation of a simple list constructor into any kind of list
  - Here we compute a list of alternating 1's and -1's.

```
1    load system math.
2
3    let a = [1 to 10] @map(lambda with x do math @mod (x,2))
4                      @map(lambda with x do 1 if x else -1).
5
6    assert (a == [1,-1,1,-1,1,-1,1,-1,1,-1]).
```

ln012/map.ast

Map

- Most modern languages support some form of 'map' since it is such a powerful programming tool.
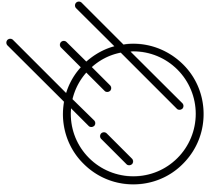
Python

```
1    l = [x for x in range(1,10+1)]
2    it = map(lambda x : x % 2, l)
3    a = list(map(lambda x : 1 if x else -1, it))
4
5    assert(a == [1,-1,1,-1,1,-1,1,-1,1,-1])
```

ln012/map.py

Rust

```
1    use std::vec::Vec;
2
3    fn main() {
4        let a : Vec<i32> = vec![1,2,3,4,5,6,7,8,9,10]
5            .iter()
6            .map(|x| x % 2)
7            .map(|x| if x == 0 { -1 } else { 1 })
8            .collect();
9
10       assert_eq!(a, vec![1, -1, 1, -1, 1, -1, 1, -1, 1, -1]);
11   }
```

ln012/map.rs

Reduce

- Whereas 'map' applies a function to a list producing another list, the 'reduce' function applies a function to a list so that the list gets *reduced* to a single value.
  - In functional languages this is often called 'fold' – folding the list into a single value
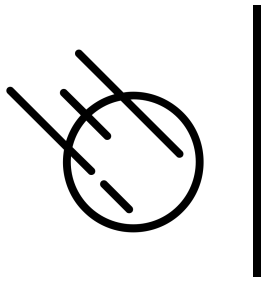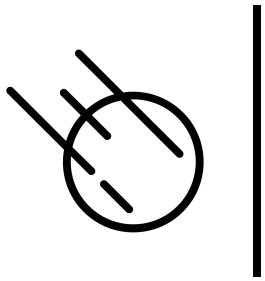
Reduce

○ For example, the reduce function lets us sum the elements of a list without a loop

ln012/reduce.ast

```
1    let value = [1,2,3] @reduce (lambda with (x,y) do x+y).
2
3    assert(value == 6).
```

The argument of the reduce function must be a pair where each component of the pair is of the element type of the list.
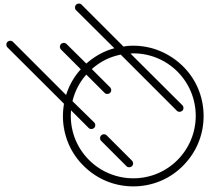
Reduce

- The reduce function gives us an interesting way to implement the factorial of an integer

ln012/fact.ast

```
1    -- factorial with reduce
2    function fact with x do
3        [1 to x] @reduce (lambda with (i,j) do i*j)
4    end
5
6    assert (fact 3 == 6).
```

Reduce

- The Asteroid code below illustrates the behavior of the 'reduce' function
  - Notice the function application to a pair of values!
  - The first value of the pair acts like an accumulator containing the partially reduced value at each function application

```
1    list @ reduce f
2
3    -- is equivalent to --
4
5    let value = list@0.
6    for i in range(len(list)) do
7        let value = f (value,l@i).   <--
8    end
9    -- value has now the reduced value of the list
```
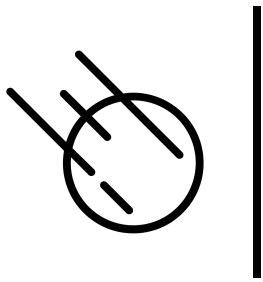
Reduce

Python

```python
1   from functools import reduce
2
3   value = [1, 2, 3]
4   result = reduce(lambda x, y: x + y, value)
5
6   assert result == 6
```

ln012/reduce.py

Rust

ln012/reduce.rs

```rust
1   fn main() {
2       let value: i32 = (1..10).reduce(|acc, e| acc + e).unwrap();
3       assert_eq!(value, 45);
4   }
```