

#### Functional Programming

- Functional programming is a declarative programming paradigm where programs are constructed by applying and composing functions.
- Function definitions are expressions that map values to other values, rather than a sequence of imperative statements which update the running state of a program.



#### Functional Programming

Everything is a Value!

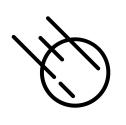
- …including functions!
- This sets functional programming apart from imperative programming where statements like loops and conditionals do not represent values but change of an explicit machine state



## Lambda Calculus

- Let's explore this using the lambda calculus before we commit to any particular language.
- Recall that in the lambda calculus we construct functions as lambda expressions and these functions can be applied to values, e.g.

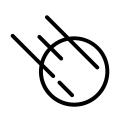
Function application
Substitution
$$(\lambda x. x + 1) \ 1 \Rightarrow x + 1[x \leftarrow 1] \Rightarrow 1 + 1 \Rightarrow 2$$



# Lambda Calculus

• Functions can be input values to other functions!

Function as value 
$$(\lambda y. y. 1)(\lambda x. x + 1) \Rightarrow y. 1[y \leftarrow (\lambda x. x + 1)]$$
$$\Rightarrow (\lambda x. x + 1). 1 \Rightarrow 2$$



### Lambda Calculus

- Functions as return values from functions
  - That is, functions computing new functions!

Function as return value 
$$(\lambda x. (\lambda y. x + y)) 1 1 \Rightarrow (\lambda y. x + y) 1[x \leftarrow 1]$$
 
$$\Rightarrow (\lambda y. 1 + y) 1 \Rightarrow 1 + y[y \leftarrow 1] \Rightarrow 1 + 1 \Rightarrow 2$$



#### **Functional Programming**

- Functional programming is declarative in that the programs deal more with the what rather than the how.
- One way to think about this is: in declarative programming we "declare" what to do for each input configuration.
- This is in stark contrast to imperative programming where we describe how to solve the whole problem in one go without subdivision.

```
-- imperative solution

function len with list do

let remaining_list = list.
let cnt = 0.
repeat

let [_|remaining_list] = remaining_list.
let cnt = cnt + 1.
until remaining_list is [].

end

let q = [ 1 to 10].
assert (len q == 10).
```

```
-- declarative solution

function len

with [] do

with [_|remaining_list] do

1 + len remaining_list

end

let q = [ 1 to 10].

assert (len q == 10).
```

"The How"

"The What"

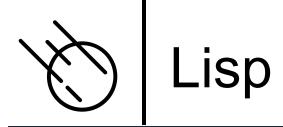




Dr John McCarthy, computer scientist, 1927 – 2011.



- Lisp was developed by John McCarthy in the late 1950's early 60's to solve problems in Al.
- It is the oldest functional programming language.
- Its syntax has been inspired by the lambda calculus.
- It introduced novel features such as recursion and garbage collection.
- It is still in use today as Common Lisp (ANSI compliant).
- Modern descendants: Scheme, Racket, Clojure



 $(\lambda x. x + 1) 1 \Rightarrow 2$ 

```
Welcome to GNU CLISP 2.49 (2010-07-07) <a href="http://clisp.cons.org/">http://clisp.cons.org/</a>
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Type :h and hit Enter for context help.

[1]> ((lambda (x) (+ x 1)) 1)
2
[2]> (defun inc (x) (+ x 1))
INC
[3]> (inc 1)
2
[4]>
```

```
(\lambda y. y. 1)(\lambda x. x + 1) \Rightarrow 2
```

```
[1]> ((lambda (y) (apply y '(1))) (lambda (x) (+ x 1)))
2
[2]> ■
```

$$(\lambda x.(\lambda y.x + y)) 1 1 \Rightarrow 2$$

```
[1]> (apply (apply (lambda (x) (lambda (y) (+ x y))) '(1)) '(1))
2
[2]> ■
```





Robin Milner, computer scientist 1934 – 2010.



- o Robin Milner designed ML as the implementation language for his proof assistant LCF (Logic for Computable Functions) in the 1970's.
- It can be considered the first modern functional programming language,
  - Statically type checked
  - A syntax that is easily recognized by today's developers
  - Very influential, virtually every modern functional programming language can trace its ancestry back to ML
- It is also one of the few high-level programming languages with a full mathematical specification.
- Dialects of ML in wide use today: SMLNJ, Ocaml, F#



 $(\lambda x. x + 1) 1 \Rightarrow 2$ 



 Please read Chapter I in the following paper,

<u>lutzhamel.github.io/CSC493/docs/intro-fp-barendregt.pdf</u>