

UPES

MATH2058: Applied Statistics and Probability

Question Bank

Date: September 22, 2025

Instructions

• Questions for practice

Question 0.1. For the two frequency distributions given in the following table, the mean calculated from the first was 25.4 and that from the second was 32.5. Find the values of x and y.

| Class | Distribution I Frequency | Distribution II Frequency |
|---------|--------------------------|---------------------------|
| 10 - 20 | 20 | 4 |
| 20 - 30 | 15 | 8 |
| 30 - 40 | 10 | 4 |
| 40 - 50 | x | 2x |
| 50 - 60 | y | y |

Table 1: Table for Question 0.1

Question 0.2. An incomplete frequency distribution is given in Table 2: Given that the

| Variable | Frequency | | | | |
|----------|-----------|--|--|--|--|
| 10 - 20 | 12 | | | | |
| 20 - 30 | 30 | | | | |
| 30 - 40 | ? | | | | |
| 40 - 50 | 65 | | | | |
| 50 - 60 | ? | | | | |
| 60 - 70 | 25 | | | | |
| 70 - 80 | 18 | | | | |

Table 2: Table for Question 0.2

median value is 46, determine the missing frequencies, using the median formula.

Question 0.3. In a factory employing 3000 persons, in a day 5% work less than 3 hours, 580 work from 3.01 to 4.5 hours, 30% work from 4.51 to 6 hours, 500 work from 6.01 to 7.5 hours, 20% work from 7.51 to 9 hours and the rest work 9.01 or more hours. What is the median hours of work?

Question 0.4. The median and mode of the following wage distribution (refer Table 3) are known to be Rs. 3350 and Rs. 3400 respectively. Find the values of f_3 , f_4 , and f_5 :

| Wages in (Rs.) | No. of Employees |
|----------------|------------------|
| 0 - 1000 | 4 |
| 1000 - 2000 | 16 |
| 2000 - 3000 | f_3 |
| 3000 - 4000 | f_4 |
| 4000 - 5000 | f_5 |
| 5000 - 6000 | 6 |
| 6000 - 7000 | 4 |

Table 3: Table for Question 0.4

Question 0.5. From the Table 4 showing the wage distribution in a certain factory, determine:

- 1. the mean wages,
- 2. the median wages
- 3. the modal wages
- 4. the wage limits for the middle 50% of the wage earners.

| Weekly Wages (Rs.) | No. of employees | Weekly Wages (Rs.) | No. of employees |
|--------------------|------------------|--------------------|------------------|
| 20 - 40 | 8 | 120 - 140 | 35 |
| 40 - 60 | 12 | 140 - 160 | 18 |
| 60 - 80 | 20 | 160 - 180 | 7 |
| 80 - 100 | 30 | 180 - 200 | 5 |
| 100 - 120 | 40 | | |

Table 4: Table for Question 0.5

Question 0.6. Define (i) Arithmetic Mean, (ii) Median, and (iii) Mode of grouped and ungrouped data. Compare and contrast their merits and demerits.

Question 0.7. (i) Explain the main difference between mean deviation and standard deviation.

(ii) Distinguish between absolute and relative measure of dispersion.

Question 0.8. Explain the methods of measuring Skewness and Kurtosis of a frequency distribution.

Question 0.9. Define moments. What is its use? Express first four central moments in terms of moments about origin.

Question 0.10. For a group of 200 candidates, the mean and standard deviation of scores were found to be 40 and 15 respectively. Later on it was discovered that the scores 43 and 35 were misread as 34 and 53 respectively. Find the corrected mean and standard deviation corresponding to the corrected figures.

NOTE: Assume that scores are only non-negative integers, and a score can have frequency > 1.

| X | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
|---|---|---|----|----|----|----|----|---|---|
| f | 1 | 8 | 28 | 56 | 70 | 56 | 28 | 8 | 1 |

Table 5: Table for Question 0.11

Question 0.11. Calculate the first four moments of the following distribution (see Table 5) about the mean and hence find β_1 and β_2 .

Question 0.12. For the frequency distribution (see Table 6) of scores in mathematics of 50 candidates selected at random from among those appearing at a certain examination, compute the first four moments about the mean of the distribution.

Find also the moments coefficients of skewness and Kurtosis and comment on the nature of the distribution.

| Scores: | 50 - | 60 - | 70 – | 80 - | 90 - | 100 - | 110 - | 120 - | 130 - |
|------------|-------|-------|-------|-------|-------|-------|-------|-------|-------|
| | 60 | 70 | 80 | 90 | 100 | 110 | 120 | 130 | 140 |
| Frequency: | 1 | 0 | 0 | 1 | 1 | 2 | 1 | 0 | 4 |
| Scores: | 140 - | 150 - | 160 - | 170 - | 180 - | 190 - | 200 - | 210 - | 220 - |
| | 150 | 160 | 170 | 180 | 190 | 200 | 210 | 220 | 230 |
| Frequency: | 4 | 2 | 5 | 10 | 11 | 4 | 1 | 1 | 2 |

Table 6: Table for Question 0.12