First, generating two samples, say  $u_1$  and  $u_2$ , with size n, where  $u_1, u_2 \sim N(0, 1)$ . Second, calculate the empirical distribution function of y, which is as follow:

$$ku_2 = kF(y) = \begin{cases} \frac{y^{\alpha}}{\alpha} & y \le 1\\ k - e^{-y} & y > 1 \end{cases}$$

where  $k = \frac{1}{\alpha} + \frac{1}{e}$ 

And via inverse transformation, we get

$$y = \begin{cases} (\alpha k u_2)^{1/\alpha} & u_2 \le \frac{1}{\alpha k} \\ -\ln(k - k u_2) & u_2 > \frac{1}{\alpha k} \end{cases}$$

Then, we get x from y if and only if one of the following conditions is established:

- When  $y \le 1$ ,  $u_1 \le e^{-y}$
- When y > 1,  $u < y^{\alpha 1}$