

CSCI 3907/6907

Fall 2019

Lecture 6

Formal Grammars & Syntactic Parsing

Notes

- The due date for 2nd homework is Oct 8
- You should have already formed a group **only** for your **final project**

Syntax and Grammar

- **Syntax:** The way words are arranged in a sentence
- Some syntactic notions we've seen:
 - Regular languages
 - N-gram language models
 - Parts-of-speech tagging

Syntactic Parsing

- Analyzing a sentence to identify certain syntactic features
 - Useful for many applications such as grammar checking
- An important task in NLP to meditate between *surface forms* and *meaning*
 - Relation extraction
 - Semantic role labeling
 - Paraphrase detection

Constituency in English

- A **constituent** is a group of words acting as a single unit or phrase
 - e.g. Noun Phrases (*Harry, Harry the Horse, Three parties from Brooklyn, They, A high-class spot such as Mindy's*)
- Constituents appear in similar syntactic contexts
 - For example, noun phrases can be followed by verbs:
 - Three parties from Brooklyn *arrive* ...
 - They *arrive* ...
 - A high-class spot such as Mindy's *attracts* ...
- The locations the constituents can be placed (preposed or postposed constructions)
 - *On September seventeenth*, I'd like to fly from Atlanta to Denver
 - I'd like to fly *on September seventeenth* from Atlanta to Denver
 - I'd like to fly from Atlanta to Denver *on September seventeenth*

Context-Free Grammars (CFG)

- Constituency in English can be modeled using **Context-Free Grammar** (CFG), also called **Phrase-Structure** Grammar
- Consists of a set of **rules** (productions) and a **lexicon** (words and symbols)
 - Rules express the ways that symbols of the language can be grouped and ordered together

CFG - Example

- Productions for a noun phrase (NP):

$NP \rightarrow Det\ Nominal$

$NP \rightarrow ProperNoun$

$Nominal \rightarrow Noun \mid Nominal\ Noun$

- Symbols in CFG
 - Terminal symbols \rightarrow corresponds to words in the language (e.g. flight)
 - Non terminal symbols \rightarrow clusters or generalizations of these terminals

CFG – Example – Cont.

- Productions for a noun phrase (NP):

$NP \rightarrow Det\ Nominal$

$NP \rightarrow ProperNoun$

$Nominal \rightarrow Noun \mid Nominal\ Noun$

- The left of the arrow is a single **non-terminal** symbol
- The right of the arrow is an ordered set of non-terminals and **terminals** (words from the lexicon)

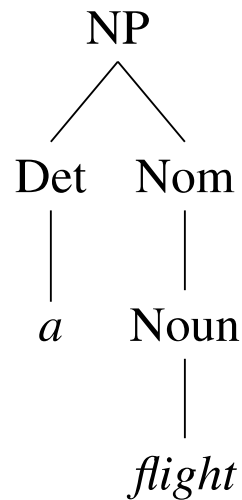
Parts-of-speech { $Det \rightarrow a$
 $Det \rightarrow the$
 $Noun \rightarrow flight$ } terminals

CFG as a Generator - Example

- rewrite the symbol on the left with the string of symbols on the right
- Starting with NP :

Derivation
of “a flight” from NP

$NP \rightarrow Det\ Nominal$
Det Nominal
 $Nominal \rightarrow Noun$
Det Noun
 $Det \rightarrow a$
a Noun
 $Noun \rightarrow flight$
a flight



Parse Tree

Formal Language

- The formal language defined by a CFG is the set of all strings (of terminals) that can be derived from the **start symbol**.
 - A grammar must have a designated start symbol, typically called **S**.
 - Rules must be defined to expand the start symbol.

$$S \rightarrow NP VP$$

Example: CFG Grammar

Grammar Rules	Examples
$S \rightarrow NP VP$	I + want a morning flight
$NP \rightarrow$ <ul style="list-style-type: none">$Pronoun$$Proper-Noun$$Det Nominal$	<ul style="list-style-type: none">ILos Angelesa + flight
$Nominal \rightarrow$ <ul style="list-style-type: none">$Nominal Noun$$Noun$	<ul style="list-style-type: none">morning + flightflights
$VP \rightarrow$ <ul style="list-style-type: none">$Verb$$Verb NP$$Verb NP PP$$Verb PP$	<ul style="list-style-type: none">dowant + a flightleave + Boston + in the morningleaving + on Thursday
$PP \rightarrow Preposition NP$	from + Los Angeles

Example: Lexicon

Noun → *flights* | *breeze* | *trip* | *morning*

Verb → *is* | *prefer* | *like* | *need* | *want* | *fly*

Adjective → *cheapest* | *non-stop* | *first* | *latest*
| *other* | *direct*

Pronoun → *me* | *I* | *you* | *it*

Proper-Noun → *Alaska* | *Baltimore* | *Los Angeles*
| *Chicago* | *United* | *American*

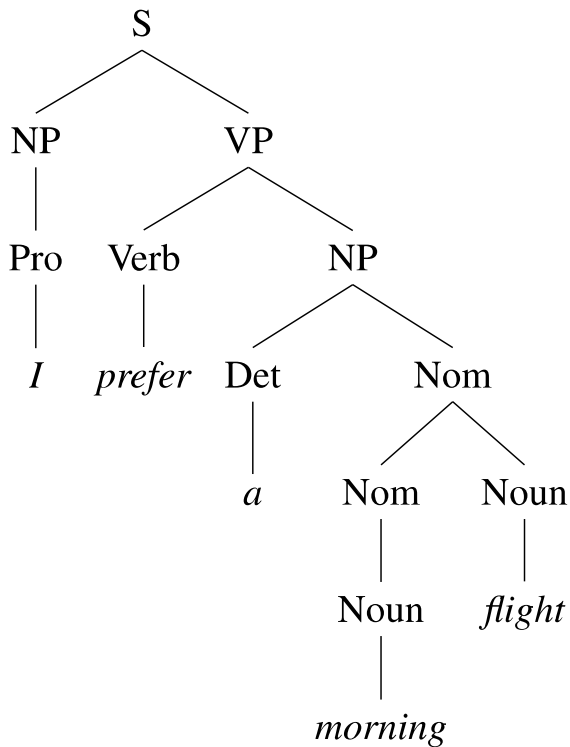
Determiner → *the* | *a* | *an* | *this* | *these* | *that*

Preposition → *from* | *to* | *on* | *near*

Conjunction → *and* | *or* | *but*

Bracketed Notation

- Sometimes it's more convenient to represent a parse tree in a compact form called **bracketed notation**:



[_S [_{NP} [_{Pro} I]] [_{VP} [_V prefer] [_{NP} [_{Det} a] [_{Nom} [_N morning] [_{Nom} [_N flight]]]]]]

Formal Definition of a CFG

- $G = (T, N, S, R)$
 - T is a set of **terminal** symbols
 - N is a set of **nonterminal** symbols
 - S is the **start symbol** ($S \in N$)
 - R is a set of **rules/productions** of the form $X \rightarrow \gamma$
 - $X \in N$ and $\gamma \in (N \cup T)^*$
- A grammar G generates a language L

Grammar Rules for English

Some Grammar Rules for English

- A subset of grammar rules and main constituents for English:
 - (1) Sentence constructions
 - (2) The Noun Phrase (NP)
 - (3) The Verb Phrase (VP)
 - (4) Coordination

(1) Sentence Constructions

- **Declarative** structure: a subject noun phrase followed by a verb phrase.

$$S \rightarrow NP VP$$

- I want a flight from Ontario to Chicago
- The flight should be 11 a.m. tomorrow

- **Imperative** structure: verb phrase, with no subject.

$$S \rightarrow VP$$

- Show the lowest fare
- List all flights from 5 to 7 p.m

(1) Sentence Constructions

- **yes-no question** structure: an auxiliary verb followed by a noun phrase, followed by a verb phrase.

$$S \rightarrow Aux\ NP\ VP$$

- Does any of these flights have stops?
- Can you give me the same information for United?

- **wh-subject-question** structure: similar to declarative structure, but the noun phrase starts with a wh- word.

$$S \rightarrow Wh-NP\ VP$$

- Which airlines fly from Ontario to Chicago?

(1) Sentence Constructions

- **wh-non-subject-question** structure: similar to yes-no structure, but starts with a wh- NP.

$$S \rightarrow Wh-NP Aux NP VP$$

- What flights do you have from Ontario to Chicago?

(2) The Noun Phrase

- NP \longrightarrow Pronoun | ProperNoun | **Det Nominal**

- **Determiners:** Can be

- a simple lexical determiner (a, an, the)

- A stop
- The flights
- Those flights

- or a more complex expression:

- United's flight
- United's pilots' union
- Denver's mayor's mother's canceled flight

Det \rightarrow *NP* 's

(2) The Noun Phrase

- The **nominal** follows the determiner, and can contain pre- and post- head noun modifiers.

Nominal → *Noun*

- Pre-modifiers: before the head noun, we can have : **cardinal** numbers (one ,two, ..), **ordinal** numbers (first, second, ..), **quantifiers** (some, all, ...) , and/or **adjectives**.
 - We can also define Adjective Phrases (AP), which may include adverbs before the adjective
 - A *non-stop* flight
 - The *longest* layover

(2) The Noun Phrase

- Head noun post-modifiers:
 - **Prepositional phrases:**

Nominal \rightarrow *Nominal PP*

- All flights *from Cleveland*
- Arrival *in San Jose before 11 p.m.*

(2) The Noun Phrase

- Head noun post-modifiers:
 - **Non-finite clauses:**
 - Gerundive (-ing): a verb phrase that begins with a gerundive (-ing) form
 - Any flight *leaving on Thursday*
 - Flights *arriving within thirty minutes*
- Nominal* → *Nominal GerundVP*
- Infinitive forms
 - The last flight *to arrive in Boston*
 - *-ed* and :
 - Which is the aircraft *used by this flight?*

(2) The Noun Phrase

- Head noun post-modifiers:
 - **Relative clauses:** a clause that begins with a relative pronoun (that, who, ...)
$$\textit{Nominal} \rightarrow \textit{Nominal RelClause}$$
$$\textit{RelClause} \rightarrow (\textit{who} \mid \textit{that}) \textit{VP}$$
 - Flights *that leave in the morning*
 - Combining multiple modifiers:
 - All flights *from Boston leaving before 5 p.m*

(3) The Verb Phrase

- Some basic VP production rules:

$VP \rightarrow Verb$ disappear

$VP \rightarrow Verb NP$ prefer a morning flight

$VP \rightarrow Verb NP PP$ leave Boston in the morning

$VP \rightarrow Verb PP$ leaving on Thursday

- An entire sentence (**sentential complement**) can follow a verb

$VP \rightarrow Verb S$

- I think *I would like to take the 9:30 a.m flight*
- Tell me *how to get from the airport to downtown.*

(3) The Verb Phrase

- Another VP can follow a verb, such as the infinitive **VP complements** that can follow some verbs
 - I want *to fly from Denver to Chicago*
- Not every verb is compatible with every verb phrase.
 - “want” can take either an NP complement (*want a flight*), or an infinitive VP complement (*want to book a flight*).
 - “find” cannot take a VP complement, only NP complements (*I found a flight*)
 - Some verbs cannot take any complements, like “disappear”
 - Traditionally called **intransitive** verbs

(3) Verb Phrase

- Subcategorization frames \rightarrow the possible set of complements
- Define separate types of verbs:

Verb-with-NP-complement \rightarrow *find* | *leave* | *repeat* | ...

Verb-with-S-complement \rightarrow *think* | *believe* | *say* | ...

Verb-with-Inf-VP-complement \rightarrow *want* | *try* | *need* | ...

- And modify VP productions accordingly:

VP \rightarrow *Verb-with-no-complement* disappear

VP \rightarrow *Verb-with-NP-comp NP* prefer a morning flight

VP \rightarrow *Verb-with-S-comp S* said there were two flights

(4) Coordination

- Join multiple phrases using **conjunctions** (and, or, but, ...) to form larger phrases of the same type.

$$NP \rightarrow NP \text{ and } NP$$
$$VP \rightarrow VP \text{ and } VP$$

- I need to know *the aircraft* and *the flight number*.
 - Which flights do you have *leaving Denver* and *arriving in San Francisco*?
- All non-terminals can be conjoined in this manner, so we can define a general rule:

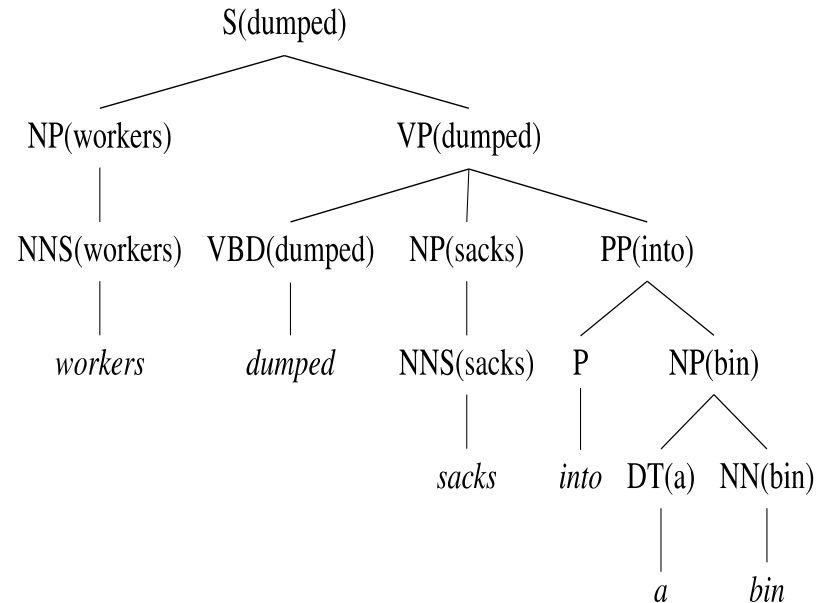
$$X \rightarrow X \text{ and } X$$

Heads and Head Finding

- Syntactic constituents can be associated with a lexical **head**
- A head → a specific word in the phrase that is grammatically the most important:
 - A noun is the head of an NP (e.g. the **dog** walking by)
 - A verb is the head of VP (e.g. **walks** up the street)

Lexicalized Parse Trees

- Each constituent is annotated with a lexical head



Identifying Head Words

- CFG rules can be augmented to identify one right-hand constituent as the head child
 - Choosing a head child node can be complicated in practice
- Alternatively, head words can be identified dynamically in the context of specific sentences

Head Finding

- A set of simple rules can be used to annotate nodes in parse trees with their appropriate head words
- For example, to find the head child of VP:
 - If the VP contains a V, the head child is the leftmost V;
 - Else, if the VP contains a MD, the head child is the leftmost MD;
 - Else, if the VP contains a VP, the head child is the leftmost VP;
 - Else, the head is the leftmost child.
- Apply the rules bottom up to annotate with lexical heads (The headword of a constituent is the headword of its head child).

TreeBanks

Treebanks

- A **treebank** → an annotated corpus of sentences and their corresponding parse trees
- The **Penn Treebank** project has produced treebanks for various corpora including the Brown Corpus and the Wall Street Journal for English
 - As well as some treebanks for few other languages.

Penn TreeBank (PTB) Format

“The flight should arrive at 11 a.m tomorrow”

```
((S
  (NP-SBJ The/DT flight/NN )
  (VP should/MD
    (VP arrive/VB
      (PP-TMP at/IN
        (NP eleven/CD a.m/RB ))
      (NP-TMP tomorrow/NN )))))
```

PTB Format

“The flight should arrive at 11 a.m tomorrow”

```
((S                                PTB POS Tags
  (NP-SBJ The/DT flight/NN )
  (VP should/MD
    (VP arrive/VB
      (PP-TMP at/IN
        (NP eleven/CD a.m/RB ))
      (NP-TMP tomorrow/NN )))))
```

Traces of Syntactic Movement

“We would have [^] to wait until we
have collected on those assets,”
he said [^].

```
( (S (‘ ‘ ‘ ‘)
  (S-TPC-2
    (NP-SBJ-1 (PRP We) )
    (VP (MD would)
      (VP (VB have)
        (S
          (NP-SBJ (-NONE- *-1) )
          (VP (TO to)
            (VP (VB wait)
              (SBAR-TMP (IN until)
                (S
                  (NP-SBJ (PRP we) )
                  (VP (VBP have)
                    (VP (VBN collected)
                      (PP-CLR (IN on)
                        (NP (DT those)(NNS assets))))))))))
          (, ,) (’ ’ ’ ’)
          (NP-SBJ (PRP he) )
          (VP (VBD said)
            (S (-NONE- *T*-2) ))
          (. .) ))
  )
)
```

PTB Grammar

- We can infer the Context-Free Grammar of the language represented by the PTB corpus
- The grammar is relatively flat, resulting in numerous long rules. For example:

$$\text{VP} \rightarrow \text{VBP PP PP PP PP PP ADVP PP}$$

This mostly happens because we go *from* football *in* the fall *to* lifting *in* the winter *to* football *again in* the spring.

PTB Grammar – Cont.

- Examples of NP productions:

$$\text{NP} \rightarrow \text{DT JJ JJ VBG NN NNP NNP FW NNP}$$

[_{DT} The] [_{JJ} state-owned] [_{JJ} industrial] [_{VBG} holding] [_{NN} company] [_{NNP} Instituto]
[_{NNP} Nacional] [_{FW} de] [_{NNP} Industria]

$$\text{NP} \rightarrow \text{NP JJ , JJ ‘ ‘ SBAR ‘ ‘ NNS}$$

[_{NP} Shearson's] [_{JJ} easy-to-film], [_{JJ} black-and-white] “[_{SBAR} Where We Stand]”
[_{NNS} commercials]

Grammar Equivalence

- Two formal grammars are equivalent if they produce the same set of strings
 - **Strong equivalence:** the two grammars generate the same set of strings *and* assign the same parse tree to each sentence (merely renaming of the non-terminal symbols)
 - **Weak equivalence:** the two grammars generate the same set of strings but do not assign the same parse tree to each sentence
 - $A \rightarrow B C D$ can be represented as the following two rules
 - $A \rightarrow B X$
 - $X \rightarrow C D$

Chomsky Normal Form (CNF)

Normal Form

- A grammar is said to be in **Chomsky Normal Form** (CNF) if it is ϵ -free and all productions are of the form $A \rightarrow BC$ or $A \rightarrow a$
 - *The right-hand side is either two non-terminals or one terminal.*
- CNF grammars have binary parse trees
- Any CFG can be converted to a weakly equivalent CNF grammar

Normal Form - Example

- The following PTB rules:

$VP \rightarrow VBD \ NP \ PP$

$VP \rightarrow VBD \ NP \ PP \ PP$

$VP \rightarrow VBD \ NP \ PP \ PP \ PP$

$VP \rightarrow VBD \ NP \ PP \ PP \ PP \ PP$

...

- Can be converted to:

$VP \rightarrow VBD \ NP$

$NP \rightarrow NP \ PP$

Converting a CFG to CNF

- Three situations:
 - Rules that mix terminals and non-terminals in the right-hand side
 - Rules with a single non-terminal in the right-hand side (unit productions)
 - Rules with more than 2 non-terminals in the right-hand side

Converting a CFG to CNF

- Rules that mix terminals and non-terminals in the right-hand side \rightarrow introduce a new dummy non-terminal that only covers that terminal in the rule

$$\begin{array}{ccc} \textit{INF-VP} \rightarrow \textit{to VP} & \xrightarrow{\quad} & \begin{array}{l} \textit{INF-VP} \rightarrow \textit{TO VP} \\ \textit{TO} \rightarrow \textit{to} \end{array} \end{array}$$

Converting a CFG to CNF

- Rules with a single non-terminal in the right-hand side (unit productions) → eliminate unit productions by replacing them with all possible non-unit production rules

$VP \rightarrow INF-VP$

$INF-VP \rightarrow TO VP$



$VP \rightarrow TO VP$

Converting a CFG to CNF

- Rules with more than 2 non-terminals in the right-hand side \rightarrow introduce new non-terminals that spread the longer sequence over several new rules
- The choice of what to replace is random

$$S \rightarrow Aux NP VP \quad \longrightarrow \quad \begin{array}{l} S \rightarrow XI VP \\ XI \rightarrow Aux NP \end{array}$$

Converting a CFG to CNF - Summary

1. Copy all conforming rules to the new grammar unchanged
2. Convert terminals within rules to dummy non-terminals
3. Convert unit-productions
4. Make all rules binary and add them to new grammar

Example

Convert the following Grammar to CNF

Grammar	Lexicon
$S \rightarrow NP VP$	$Det \rightarrow that \mid this \mid the \mid a$
$S \rightarrow Aux NP VP$	$Noun \rightarrow book \mid flight \mid meal \mid money$
$S \rightarrow VP$	$Verb \rightarrow book \mid include \mid prefer$
$NP \rightarrow Pronoun$	$Pronoun \rightarrow I \mid she \mid me$
$NP \rightarrow Proper-Noun$	$Proper-Noun \rightarrow Houston \mid NWA$
$NP \rightarrow Det Nominal$	$Aux \rightarrow does$
$Nominal \rightarrow Noun$	$Preposition \rightarrow from \mid to \mid on \mid near \mid through$
$Nominal \rightarrow Nominal Noun$	
$Nominal \rightarrow Nominal PP$	
$VP \rightarrow Verb$	
$VP \rightarrow Verb NP$	
$VP \rightarrow Verb NP PP$	
$VP \rightarrow Verb PP$	
$VP \rightarrow VP PP$	
$PP \rightarrow Preposition NP$	

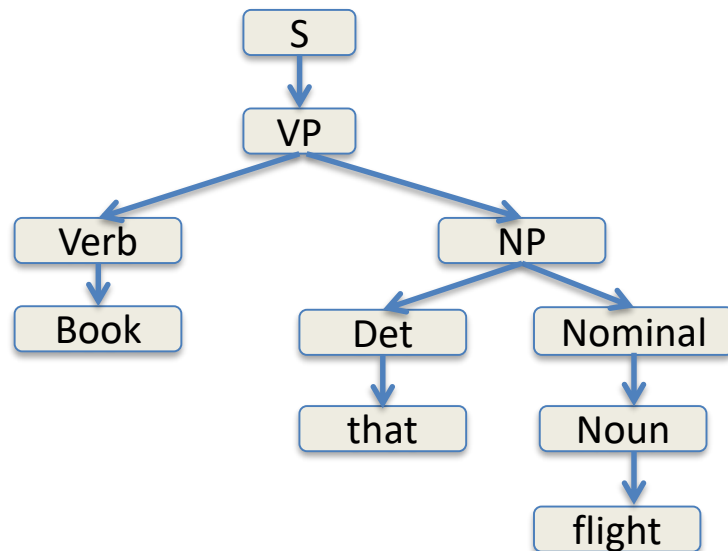
Syntactic Parsing

Syntactic Parsing

- The process of generating (possibly multiple) parse-trees given a sentence and a formal grammar
- Parsing with CFGs : all possible parse trees that span the entire input sentence and have **S** as the root

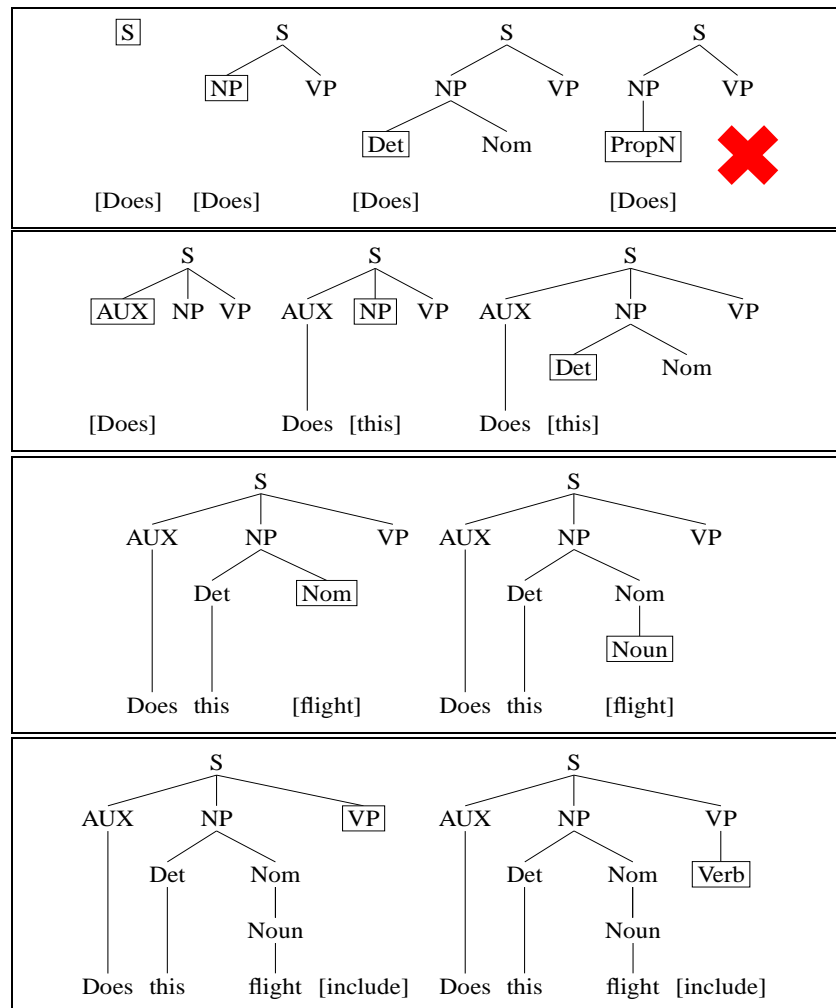
Syntactic Parsing as Search

- Searching through the space of possible parse trees to find the correct parse tree for a given sentence
- Two search strategies:
 - Top-Down Parsing
 - Bottom-Up Parsing
- Example: Book that flight →



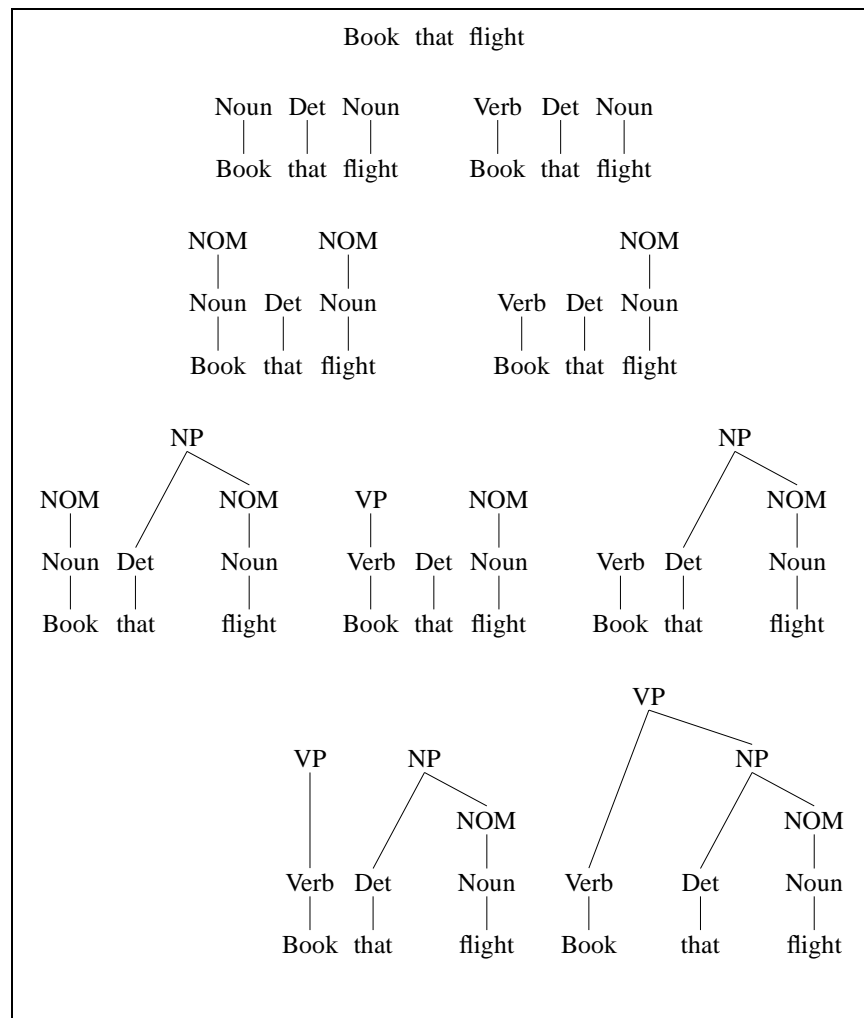
Top-Down Parsing

- *Example: Does this flight include ...*
- Start from S, then expand all production rules
- Eliminate rules that don't lead to words in the observed sentence
- The trees are expanded **depth-first** (expanding the most-recently generated nodes) and left-to-right.



Bottom-up Parsing

- *Example: Book that flight*
- Start from the observed words, and combine them upwards
- A successful parse results in a tree rooted at **S** that spans all words in the sentence



Repeated Parsing of Sub-trees

- Both search approaches have drawbacks
 - **local ambiguity** (ambiguity that results from looking at partial input)
 - the naïve approaches described so far result in repeated parsing of sub-trees
- **Dynamic programming** parsing algorithms use a table of partial-parses to efficiently parse ambiguous sentences.
 - Top-down: The **Earley** algorithm (not covered in this class)
 - Bottom-up: The **CKY** algorithm

CKY Parsing

- The **CKY** algorithm is a dynamic programming approach to bottom-up syntactic parsing
- Requires grammars in Chomsky Normal Form (CNF).
 - Can be used with any Context-Free Grammar, but it has to be converted to CNF first

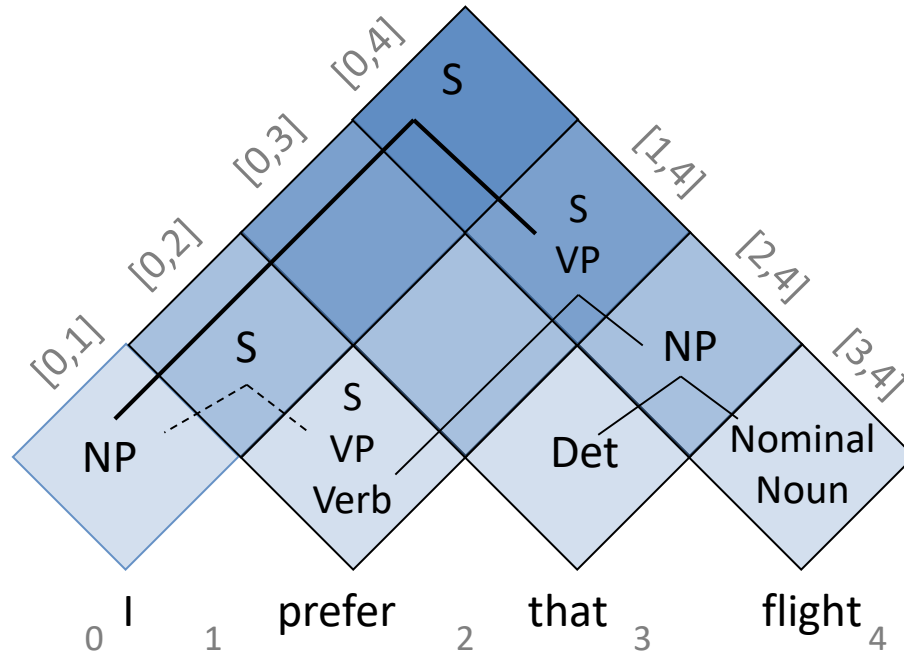
CKY Recognition

- A two-dimensional matrix is used to encode the structure of a binary tree
- For a sentence of length n , we work with the upper right triangle of an $(n+1) \times (n+1)$ matrix
- Each cell $[i,j]$ contains the set of **non-terminals** that span the input from i to j
- The cell that represents the entire parse tree is $[0,n]$ (the upper right corner)

	[0,1]	[0,2]	[0,3]	[0,4]
		[1,2]	[1,3]	[1,4]
			[2,3]	[2,4]
				[3,4]

Example

- “I prefer that flight”



$S \rightarrow NP VP$
$S \rightarrow XI VP$
$XI \rightarrow Aux NP$
$S \rightarrow book \mid include \mid prefer$
$S \rightarrow Verb NP$
$S \rightarrow X2 PP$
$S \rightarrow Verb PP$
$S \rightarrow VP PP$
$NP \rightarrow I \mid she \mid me$
$NP \rightarrow TWA \mid Houston$
$NP \rightarrow Det Nominal$
$Nominal \rightarrow book \mid flight \mid meal \mid money$
$Nominal \rightarrow Nominal Noun$
$Nominal \rightarrow Nominal PP$
$VP \rightarrow book \mid include \mid prefer$
$VP \rightarrow Verb NP$
$VP \rightarrow X2 PP$
$X2 \rightarrow Verb NP$
$VP \rightarrow Verb PP$
$VP \rightarrow VP PP$
$PP \rightarrow Preposition NP$

CKY Recognition Algorithm

function CKY-PARSE(*words*, *grammar*) returns *table*

for *j* from 1 to LENGTH(*words*) do

for all $\{A \mid A \rightarrow \text{words}[j] \in \text{grammar}\}$

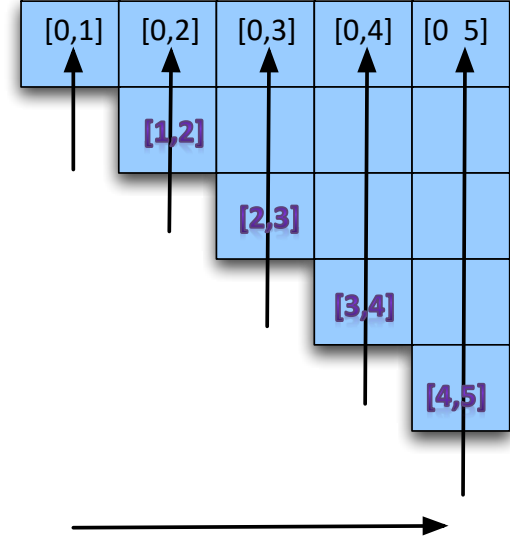
$\text{table}[j-1, j] \leftarrow \text{table}[j-1, j] \cup A$

for *i* from *j* - 2 downto 0 do

for *k* from *i* + 1 to *j* - 1 do

for all $\{A \mid A \rightarrow BC \in \text{grammar} \text{ and } B \in \text{table}[i, k] \text{ and } C \in \text{table}[k, j]\}$

$\text{table}[i, j] \leftarrow \text{table}[i, j] \cup A$



Example

- “Book the flight through **Houston**”

<i>Book</i>	<i>the</i>	<i>flight</i>	<i>through</i>	<i>Houston</i>
S, VP, Verb Nominal, Noun [0,1]		S,VP,X2		S,VP,X2
	[0,2]	[0,3]	[0,4]	[0,5]
	Det	NP		NP
	[1,2]	[1,3]	[1,4]	[1,5]
		Nominal, Noun		Nominal
		[2,3]	[2,4]	[2,5]
			Prep	PP
			[3,4]	[3,5]
				NP, Proper- Noun
				[4,5]

Completed parse tree using CKY

$S \rightarrow NP VP$
$S \rightarrow X1 VP$
$X1 \rightarrow Aux NP$
$S \rightarrow book \mid include \mid prefer$
$S \rightarrow Verb NP$
$S \rightarrow X2 PP$
$S \rightarrow Verb PP$
$S \rightarrow VP PP$
$NP \rightarrow I \mid she \mid me$
$NP \rightarrow TWA \mid Houston$
$NP \rightarrow Det Nominal$
$Nominal \rightarrow book \mid flight \mid meal \mid money$
$Nominal \rightarrow Nominal Noun$
$Nominal \rightarrow Nominal PP$
$VP \rightarrow book \mid include \mid prefer$
$VP \rightarrow Verb NP$
$VP \rightarrow X2 PP$
$X2 \rightarrow Verb NP$
$VP \rightarrow Verb PP$
$VP \rightarrow VP PP$
$PP \rightarrow Preposition NP$

Example

- “Book the flight through **Houston**”
- $j=5$

$table[j-1, j] \quad table[j-1, j] [A$

Table[4,5] = {NP, Proper-Noun}

NP \rightarrow TWA | Houston

ProperNoun \rightarrow TWA | Houston

Book	the	flight	through	Houston
S, VP, Verb, Nominal, Noun [0,1]	[0,2]	S,VP,X2 [0,3]	[0,4]	[0,5]
	Det [1,2]	NP [1,3]	[1,4]	[1,5]
		Nominal, Noun [2,3]	[2,4]	Nominal [2,5]
			Prep [3,4]	[3,5]
				NP, Proper- Noun [4,5]



Example

- “Book the flight through **Houston**”
- $j=5$

$i=3, k=4$

for i from $j-2$ downto 0 do
 for k $i+1$ to $j-1$ do
 for all $\{A \mid A \rightarrow BC \in \text{grammar and } B \in \text{table}[i, k] \text{ and } C \in \text{table}[k, j]\}$
 $\text{table}[i, j] \leftarrow \text{table}[i, j] \cup A$

$\text{Table}[3,5] = \{\text{PP}\}$

$\text{PP} \rightarrow \text{Prep NP}$

Book	the	flight	through	Houston
S, VP, Verb, Nominal, Noun [0,1]	[0,2]	S,VP,X2 [0,3]	[0,4]	[0,5]
	Det [1,2]	NP [1,3]	[1,4]	NP [1,5]
		Nominal, Noun [2,3]	[2,4]	[2,5]
			Prep [3,4]	PP [3,5]
				NP, Proper- Noun [4,5]



Example

- “Book the flight through **Houston**”
- $j=5$

$i=2, k=3$

for i from $j-2$ downto 0 do
 for k $i+1$ to $j-1$ do
 for all $\{A \mid A \in BC \text{ grammar and } B \in \text{table}[i, k] \text{ and } C \in \text{table}[k, j]\}$
 $\text{table}[i, j] \leftarrow \text{table}[i, j] \cup A$

$\text{Table}[2,5] = \{\text{Nominal}\}$

Nominal \rightarrow Nominal PP

Book	the	flight	through	Houston
S, VP, Verb, Nominal, Noun [0,1]	[0,2]	S,VP,X2 [0,3]	[0,4]	[0,5]
	Det [1,2]	NP [1,3]	[1,4]	NP [1,5]
		Nominal, Noun [2,3]	[2,4]	Nominal [2,5]
			Prep [3,4]	PP [3,5]
				NP, Proper- Noun [4,5]



Example

- “Book the flight through **Houston**”
- $j=5$

$i=2, k=4$

for i from $j-2$ downto 0 do
 for k $i+1$ to $j-1$ do
 for all $\{A \mid A \in BC \in \text{grammar and } B \in \text{table}[i, k] \text{ and } C \in \text{table}[k, j]\}$
 $\text{table}[i, j] \leftarrow \text{table}[i, j] \cup A$

$\text{Table}[2,5] = \{\text{Nominal}\}$

Book	the	flight	through	Houston
S, VP, Verb, Nominal, Noun [0,1]	[0,2]	S,VP,X2 [0,3]	[0,4]	[0,5]
	Det [1,2]	NP [1,3]	[1,4]	NP [1,5]
		Nominal, Noun [2,3]	[2,4]	Nominal [2,5]
			Prep [3,4]	PP [3,5]
				NP, Proper- Noun [4,5]



Example

- “Book the flight through **Houston**”
- $j=5$

$i=1, k=2$

for i from $j-2$ downto 0 do
 for k $i+1$ to $j-1$ do
 for all $\{A \mid A \rightarrow BC \in \text{grammar and } B \in \text{table}[i, k] \text{ and } C \in \text{table}[k, j]\}$
 $\text{table}[i, j] \leftarrow \text{table}[i, j] \cup A$

$\text{Table}[1,5] = \{\text{NP}\}$

$\text{NP} \rightarrow \text{Det Nominal}$

Book	the	flight	through	Houston
S, VP, Verb, Nominal, Noun [0,1]	[0,2]	S,VP,X2 [0,3]	[0,4]	[0,5]
	Det ←	NP ←		NP ↓
	[1,2]	[1,3]	[1,4]	[1,5]
		Nominal, Noun [2,3]	[2,4]	Nominal [2,5]
			Prep [3,4]	PP [3,5]
				NP, Proper- Noun [4,5]

Example

- “Book the flight through **Houston**”
- $j=5$

$i=1, k=3$

for i from $j-2$ downto 0 do
 for k $i+1$ to $j-1$ do
 for all $\{A \mid A \rightarrow BC \in \text{grammar and } B \in \text{table}[i, k] \text{ and } C \in \text{table}[k, j]\}$
 $\text{table}[i, j] \leftarrow \text{table}[i, j] \cup A$

$\text{Table}[1,5] = \{\text{NP}\}$

$? \rightarrow \text{NP PP}$

Book	the	flight	through	Houston	
S, VP, Verb, Nominal, Noun [0,1]	[0,2]	S,VP,X2 [0,3]	[0,4]	[0,5]	
	Det ← [1,2]	NP ← [1,3]	[1,4]	NP [1,5]	←
		Nominal, Noun [2,3]	[2,4]	Nominal [2,5]	
			Prep [3,4]	PP [3,5]	
				NP, Proper- Noun [4,5]	

Example

- “Book the flight through **Houston**”
- $j=5$

$i=0, k=1$

for i from $j-2$ downto 0 do
 for k $i+1$ to $j-1$ do
 for all $\{A \mid A \rightarrow BC \in \text{grammar and } B \in \text{table}[i, k] \text{ and } C \in \text{table}[k, j]\}$
 $\text{table}[i, j] \leftarrow \text{table}[i, j] \cup A$

$\text{Table}[0,5] = \{S_1, \text{VP}, \text{X2}\}$

$S \rightarrow \text{VP NP}$
 $\text{VP} \rightarrow \text{Verb NP}$
 $\text{X2} \rightarrow \text{Verb NP}$

Book	the	flight	through	Houston
S, VP, Verb, Nominal, Noun [0,1]	[0,2]	S, VP, X2 [0,3]	[0,4]	S ₁ , VP, X2 S ₂ , VP S ₃
	Det [1,2]	NP [1,3]	[1,4]	NP [1,5]
		Nominal, Noun [2,3]	[2,4]	Nominal [2,5]
			Prep [3,4]	PP [3,5]
				NP, Proper- Noun [4,5]

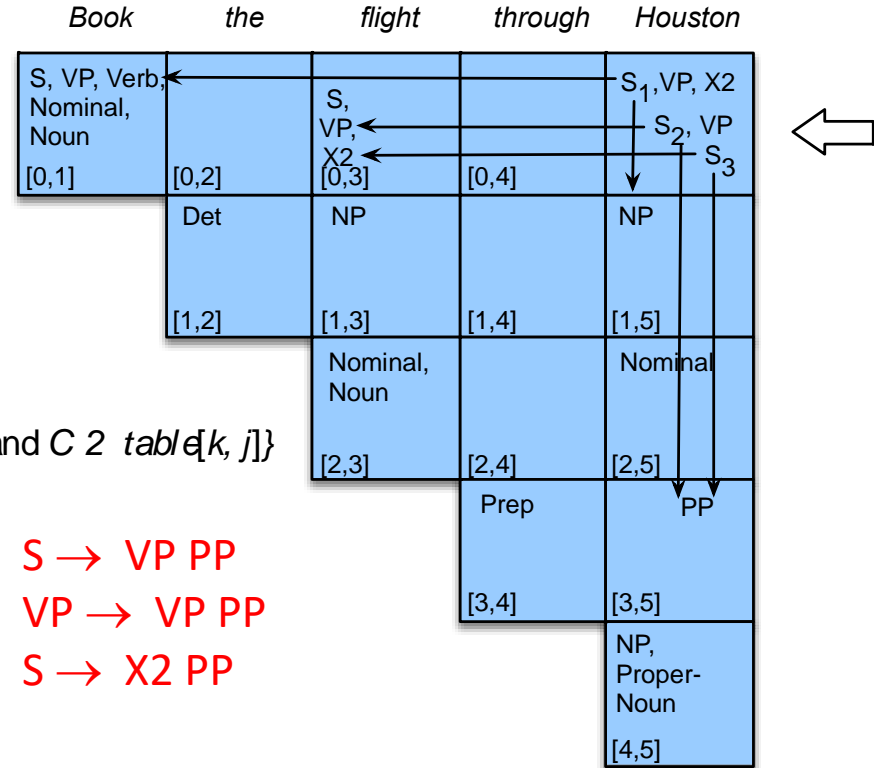
Example

- “Book the flight through **Houston**”
- $j=5$

$i=0, k=3$

for i from $j-2$ downto 0 do
 for k $i+1$ to $j-1$ do
 for all $\{A \mid A \rightarrow BC \in \text{grammar and } B \in \text{table}[i, k] \text{ and } C \in \text{table}[k, j]\}$
 $\text{table}[i, j] \leftarrow \text{table}[i, j] \cup A$

$\text{Table}[0,5] = \{S_1, \text{VP}, X_2, S_2, \text{VP}, S_3\}$

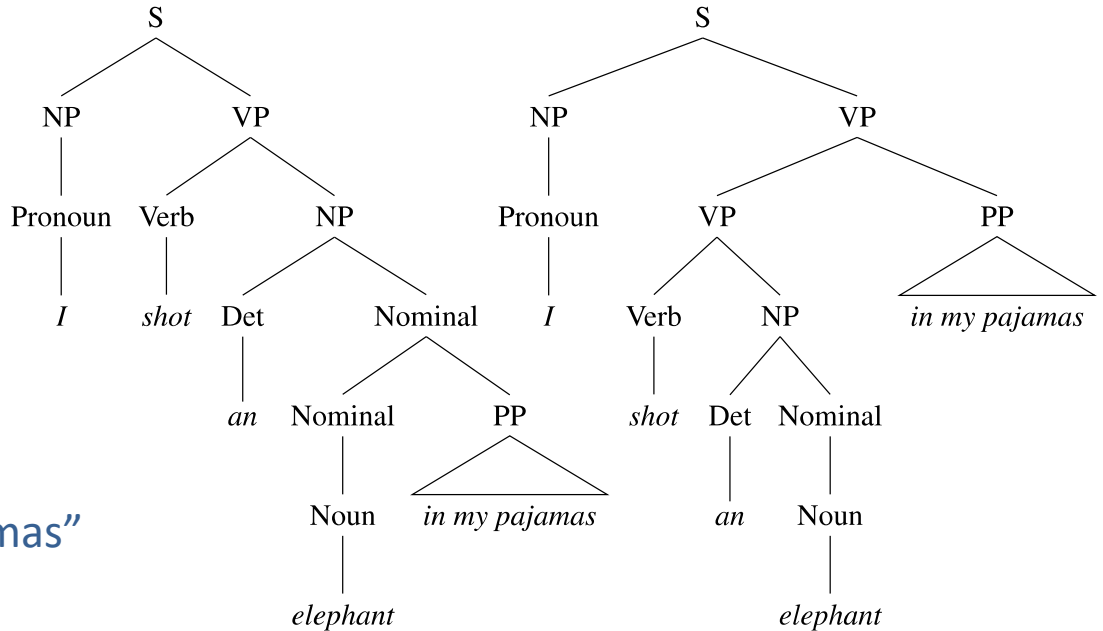


$S \rightarrow \text{VP PP}$
 $\text{VP} \rightarrow \text{VP PP}$
 $S \rightarrow X_2 \text{ PP}$

Structural Ambiguity

Structural Ambiguity

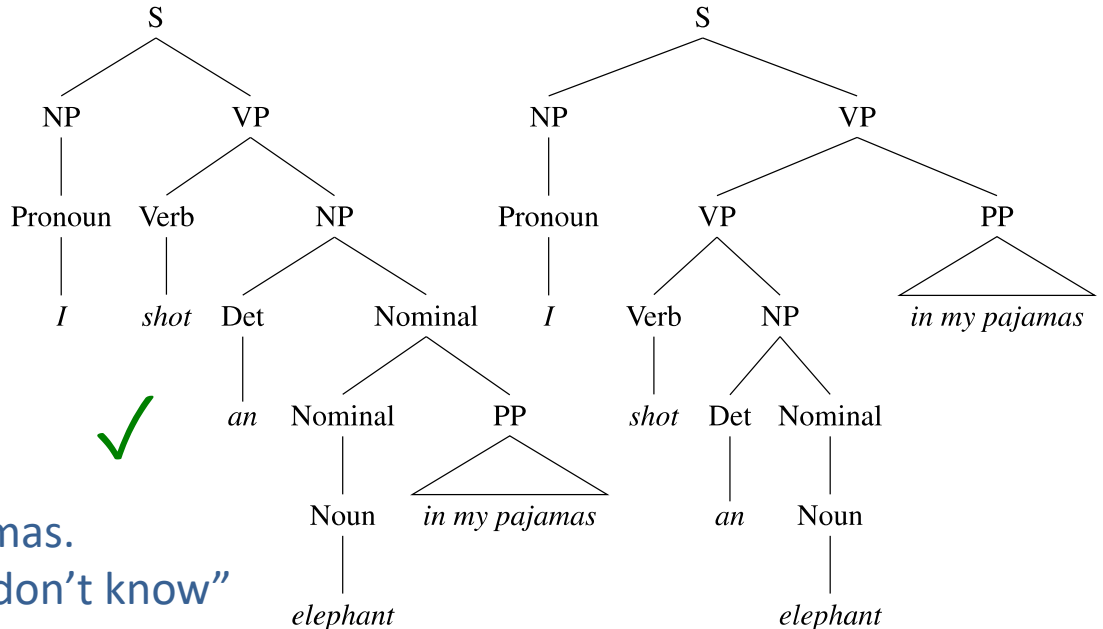
- When a grammar can generate multiple parse trees from a sentence.



"I shot an elephant in my pajamas"

Structural Ambiguity

- When a grammar can generate multiple parse trees from a sentence.



"I shot an elephant in my pajamas.
How he got into my pajamas I don't know"

Structural Ambiguity

- **Attachment ambiguity:** when a constituent can be attached to the tree in more than one place.
 - “We saw the Eiffel Tower flying to Paris”
- **Coordination ambiguity:** ambiguity that arises from conjunctions, such as *and*.
 - “Nation-wide television and radio”

Disambiguation

- Out of all the valid parse trees generated by the Grammar, which is the correct one?
 - Or rather, which one is most **likely** to be the correct one?
 - As usual, we need a probabilistic model ...
 - Probabilistic Formal Grammar
 - A probabilistic parser
 - A Treebank to train the model

Probabilistic CFG (PCFG)

- $G = (T, N, S, R, P)$
 - T is a set of terminal symbols
 - N is a set of nonterminal symbols
 - S is the start symbol ($S \in N$)
 - R is a set of rules/productions of the form $X \rightarrow \gamma$
 - P is a probability function
 - $P: R \rightarrow [0,1]$
 - $\forall X \in N, \sum_{X \rightarrow \gamma \in R} P(X \rightarrow \gamma) = 1$
- A grammar G generates a language model L : $\sum_{g \in T^*} P(g) = 1$

Probabilities of all expansion of each
non-terminal sum to 1

Example

Grammar		Lexicon
$S \rightarrow NP VP$	[.80]	$Det \rightarrow that [.10] \mid a [.30] \mid the [.60]$
$S \rightarrow Aux NP VP$	[.15]	$Noun \rightarrow book [.10] \mid flight [.30]$
$S \rightarrow VP$	[.05]	$\mid meal [.015] \mid money [.05]$
$NP \rightarrow Pronoun$	[.35]	$\mid flight [.40] \mid dinner [.10]$
$NP \rightarrow Proper-Noun$	[.30]	$Verb \rightarrow book [.30] \mid include [.30]$
$NP \rightarrow Det Nominal$	[.20]	$\mid prefer [.40]$
$NP \rightarrow Nominal$	[.15]	$Pronoun \rightarrow I [.40] \mid she [.05]$
$Nominal \rightarrow Noun$	[.75]	$\mid me [.15] \mid you [.40]$
$Nominal \rightarrow Nominal Noun$	[.20]	$Proper-Noun \rightarrow Houston [.60]$
$Nominal \rightarrow Nominal PP$	[.05]	$\mid NWA [.40]$
$VP \rightarrow Verb$	[.35]	$Aux \rightarrow does [.60] \mid can [.40]$
$VP \rightarrow Verb NP$	[.20]	$Preposition \rightarrow from [.30] \mid to [.30]$
$VP \rightarrow Verb NP PP$	[.10]	$\mid on [.20] \mid near [.15]$
$VP \rightarrow Verb PP$	[.15]	$\mid through [.05]$
$VP \rightarrow Verb NP NP$	[.05]	
$VP \rightarrow VP PP$	[.15]	
$PP \rightarrow Preposition NP$	[1.0]	

Using PCFGs

- $P(t)$ – The probability of a tree t is the product of the probabilities of the rules used to generate it

Disambiguation

- $P(s)$ – The probability of the string s is the sum of the probabilities of the trees which have that string as their yield

$$P(s) = \sum_j P(s, t) \text{ , where } t \text{ is a parse of } s$$

Language
Modeling

PCFGs for Disambiguation

- Which parse tree is most likely?

$$P(T, S) = P(T)P(S|T)$$

$T \rightarrow$ a parse tree
 $S \rightarrow$ a sentence

- Since a parse tree include the words as leaves, $P(S|T) = 1$.

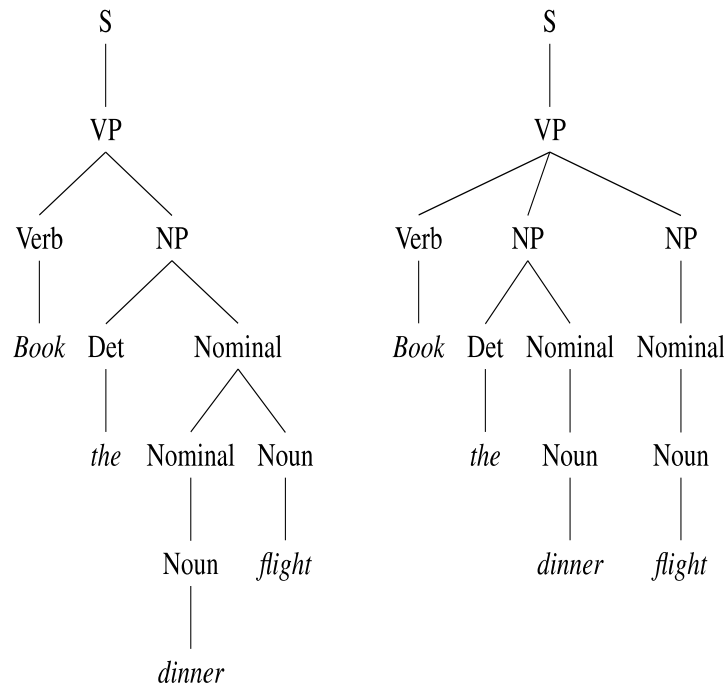
$$P(T, S) = P(T)P(S|T) = P(T)$$

- Find the most likely parse tree:

$$\hat{T}(S) = \underset{T \text{ s.t. } S = \text{yield}(T)}{\operatorname{argmax}} P(T)$$

Which Parse Tree is More Likely

Grammar		Lexicon
$S \rightarrow NP VP$	[.80]	$Det \rightarrow that [.10] \mid a [.30] \mid the [.60]$
$S \rightarrow Aux NP VP$	[.15]	$Noun \rightarrow book [.10] \mid flight [.30]$
$S \rightarrow VP$	[.05]	$\mid meal [.015] \mid money [.05]$
$NP \rightarrow Pronoun$	[.35]	$\mid flight [.40] \mid dinner [.10]$
$NP \rightarrow Proper-Noun$	[.30]	$Verb \rightarrow book [.30] \mid include [.30]$
$NP \rightarrow Det Nominal$	[.20]	$\mid prefer [.40]$
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$VP \rightarrow Verb NP PP$	[.10]	$\mid on [.20] \mid near [.15]$
$VP \rightarrow Verb PP$	[.15]	$\mid through [.05]$
$VP \rightarrow Verb NP NP$	[.05]	
$VP \rightarrow VP PP$	[.15]	
$PP \rightarrow Preposition NP$	[1.0]	



$$P(T_{left}) = .05 * .20 * .20 * .20 * .75 * .30 * .60 * .10 * .40 = 2.2 \times 10^{-6}$$

$$P(T_{right}) = .05 * .10 * .20 * .15 * .75 * .75 * .30 * .60 * .10 * .40 = 6.1 \times 10^{-7}$$

Probabilistic CKY Parsing

- Given a grammar of V non-terminals and a sentence of length n , create a 3-dimensional $(n+1) \times (n+1) \times V$ matrix
 - store probabilities of the various constituents.
 - **Backpointers** to reconstruct the most likely tree.

Example

Find the most likely
parse tree for:

“book the flight through
Houston”

Grammar		Lexicon
$S \rightarrow NP VP$	[.80]	$Det \rightarrow that [.10] \mid a [.30] \mid the [.60]$
$S \rightarrow Aux NP VP$	[.15]	$Noun \rightarrow book [.10] \mid flight [.30]$
$S \rightarrow VP$	[.05]	$\mid meal [.015] \mid money [.05]$
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$NP \rightarrow Det Nominal$	[.20]	$\mid prefer [.40]$
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$VP \rightarrow Verb NP$	[.20]	$Preposition \rightarrow from [.30] \mid to [.30]$
$VP \rightarrow Verb NP PP$	[.10]	$\mid on [.20] \mid near [.15]$
$VP \rightarrow Verb PP$	[.15]	$\mid through [.05]$
$VP \rightarrow Verb NP NP$	[.05]	
$VP \rightarrow VP PP$	[.15]	
$PP \rightarrow Preposition NP$	[1.0]	

Example

<i>Book</i>	<i>the</i>	<i>flight</i>	<i>through</i>	<i>Houston</i>
S, VP, Verb Nominal, Noun [0,1]	[0,2]	S VP,X2 [0,3]	[0,4]	S,VP,X2 [0,5]
	Det [1,2]	NP [1,3]	[1,4]	NP [1,5]
		Nominal, Noun [2,3]	[2,4]	Nominal [2,5]
			Prep [3,4]	PP [3,5]
				NP, Proper- Noun [4,5]

$$\begin{array}{l}
 \max \left\{ \begin{array}{l}
 S \rightarrow VP NP \\
 P(S \rightarrow VP NP) * P(VP \rightarrow Book) * Table[1,3,NP] \\
 S \rightarrow Verb NP \\
 P(S \rightarrow Verb NP) * P(VP \rightarrow Book) * Table[1,3,NP]
 \end{array} \right.
 \end{array}$$

Example

	<i>Book</i>	<i>the</i>	<i>flight</i>	<i>through</i>	<i>Houston</i>
S, VP, Verb Nominal, Noun [0,1]			S,VP,X2 [0,3]		S VP,X2 [0,5]
	Det [1,2]	NP [1,3]			NP [1,5]
		Nominal, Noun [2,3]			Nominal [2,5]
			Prep [3,4]		PP [3,5]
					NP, Proper- Noun [4,5]

$$\begin{array}{l}
 \max \left\{ \begin{array}{l}
 S \rightarrow VP NP \\
 P(S \rightarrow VP NP) * P(VP \rightarrow Book) * Table[1,5, NP] \\
 S \rightarrow VP PP \\
 P(S \rightarrow VP PP) * Table[0,3, VP] * Table[3,5, PP]
 \end{array} \right.
 \end{array}$$

Learning Rule Probabilities

- **Counting from a Treebank**

$$P(a \rightarrow b/a) = \frac{\text{Count}(a \rightarrow b)}{\sum_g \text{Count}(a \rightarrow g)} = \frac{\text{Count}(a \rightarrow b)}{\text{Count}(a)}$$

- **No Treebank?** Expectation Maximization ...
 - Start with equal probabilities for all rules in a CFG
 - Parse corpus
 - Re-estimate probabilities
 - Repeat until convergence

Evaluation

- Evaluating parse trees at the sentence level is rather harsh
 - Parses are often partially correct, especially for longer sentences
 - So we need a fine-grained evaluation metric
- Measure how much the constituents in a generated parse (hypothesis) resemble hand-annotated constituents from a treebank (reference).
 - A hypothesis parse constituent C_h is labeled correct if there is a reference constituent C_r with the same starting point, end point, and non-terminal symbol

$$\text{labeled recall} = \frac{\text{\# of correct constituents in hypothesis parse of } s}{\text{\# of correct constituents in reference parse of } s}$$

$$\text{labeled precision} = \frac{\text{\# of correct constituents in hypothesis parse of } s}{\text{\# of total constituents in hypothesis parse of } s}$$

Problems with PCFG

1. Poor independence assumption (structural dependencies)

1. Lack of lexical conditioning (lexical dependencies)

(1) Problems with PCFG

- **Independence assumption between sub-trees**
 - The probability of a particular rule is independent of the rest of the tree
 - Can result in poor probability estimates
- The choice of how a node expands can depend on the location of the node in the parse tree
 - In English, NPs that are syntactic subjects are more likely to be pronouns than NPs that are syntactic objects

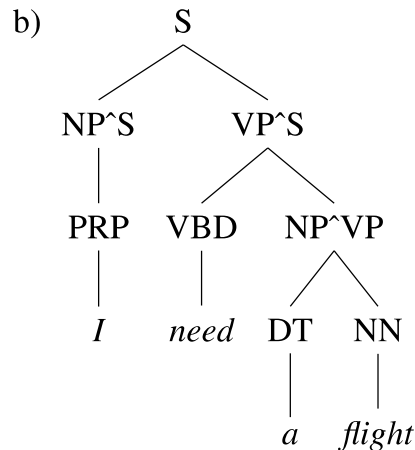
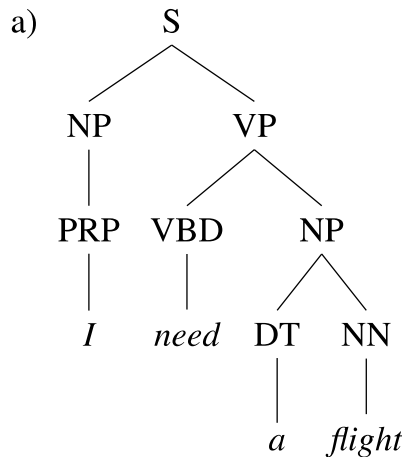
	Pronoun	Non-Pronoun
Subject	91%	9%
Object	34%	66%

(1) Problems with PCFG – Cont.

- **Independence assumption between sub-trees**
 - Yet PCFGs only include overall probabilities of each NP production
$$NP \rightarrow DT\ NN \ .28$$
$$NP \rightarrow PRP \ .25$$
 - This can be resolved to *some extent* by
 - adding **parent annotations**
 - modifying probabilities accordingly.

Parent Annotation

- Example:
 - NPs with S parents (like subjects) are marked **$NP^{\wedge}S$**
 - NPs with VP parents (like objects) are marked **$NP^{\wedge}VP$** .
- Equivalent to **subcategorization**
- Results in larger grammars and may result in overfitting, but relatively simple to implement:
 - only split a rule **if**
 - subcategories are frequent enough
 - **and** the split results in improving performance in a development set

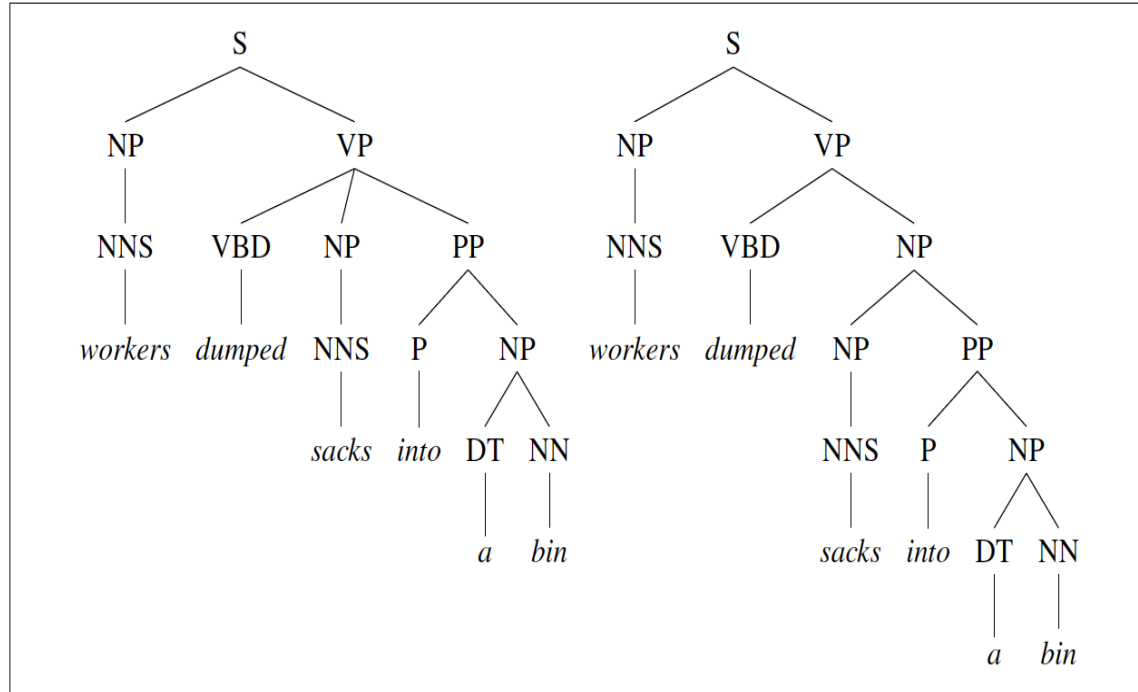


(2) Problems with PCFGs

- **Lack of sensitivity to the words in the parse tree**
 - The parse probabilities include the probability of a word given parts-of-speech
 - Words can be useful for resolving attachment and coordination ambiguities
 - “Dogs in houses and cats” – *cats* is more likely to be conjoined with *dogs* than *houses*.
 - [dogs in houses]and[cats] **vs.** [dogs]in[houses and cats].

(2) Problems with PCFGs – Cont.

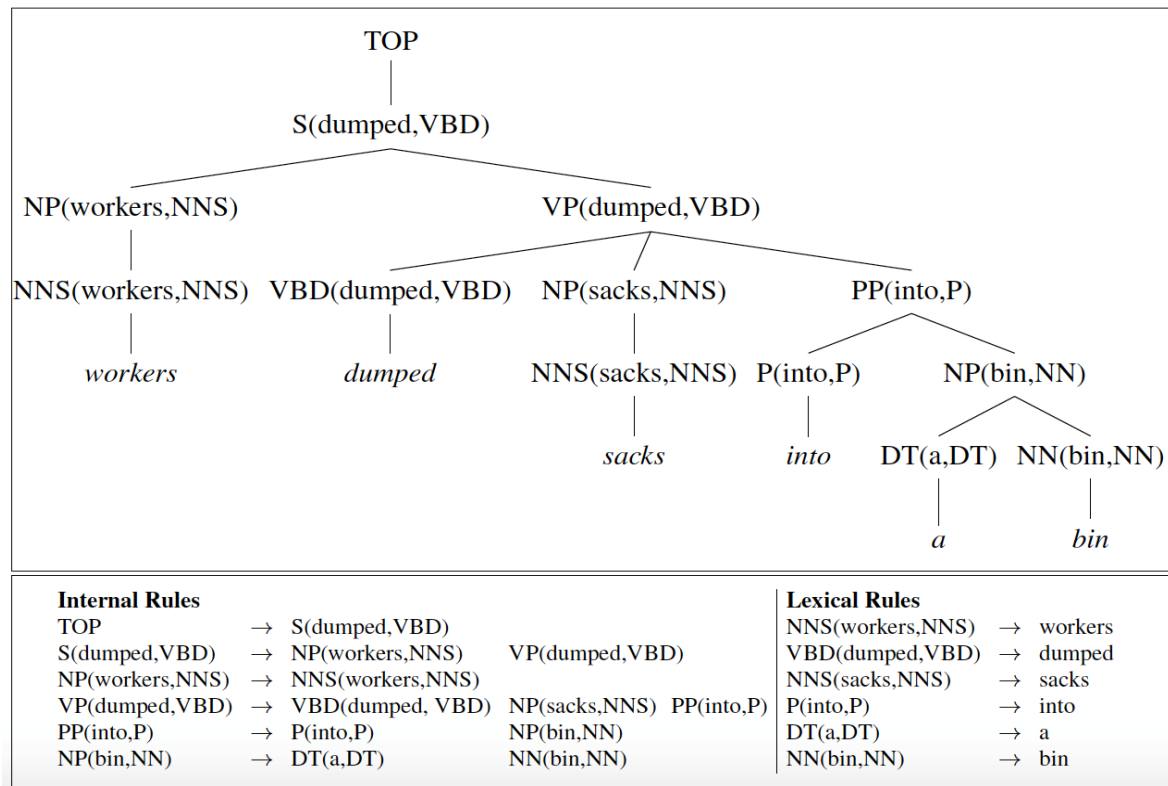
- Workers dumped sacks ***into a bin***



(2) Problems with PCFGs – Cont.

- **Lexicalized PCFGs**

- Annotate non-terminals with lexical heads
- Results in large fine-grained rules whose probabilities cannot be estimated directly with MLE



(2) Problems with PCFGs – Cont.

- **Lexicalized PCFGs**
 - Additional independence assumptions are introduced to work around that (see **Collins** parser as an example)

Partial Parsing

Partial Parsing

- Partial (or shallow) parse may be sufficient for some tasks
 - E.g. information extraction, information retrieval
 - **Chunking** → the process of identifying **non-overlapping** segments of texts that correspond to major constituent types
 - noun phrases, verb phrases, adjective phrases, and prepositional phrases
- [*NP* The morning flight] [*PP* from] [*NP* Denver] [*VP* has arrived.]

Chunking

- Definition of chunks may vary by application
- The following guidelines generally apply:
 - The phrases are non-recursive: they do not include smaller constituents of the same type
 - Only need to identify phrase boundaries and phrase type
 - Post-head modifiers are generally excluded
 - No attachment ambiguities

Chunking as Classification

- Identify phrase boundaries and types in a single classification task using **IOB** tagging
 - Tags for beginning (**B**) and inside (**I**) of each chunk type.
 - Tag **O** for tokens outside any chunk.

The morning flight from Denver has arrived
B_NP I_NP I_NP B_PP B_NP B_VP I_VP

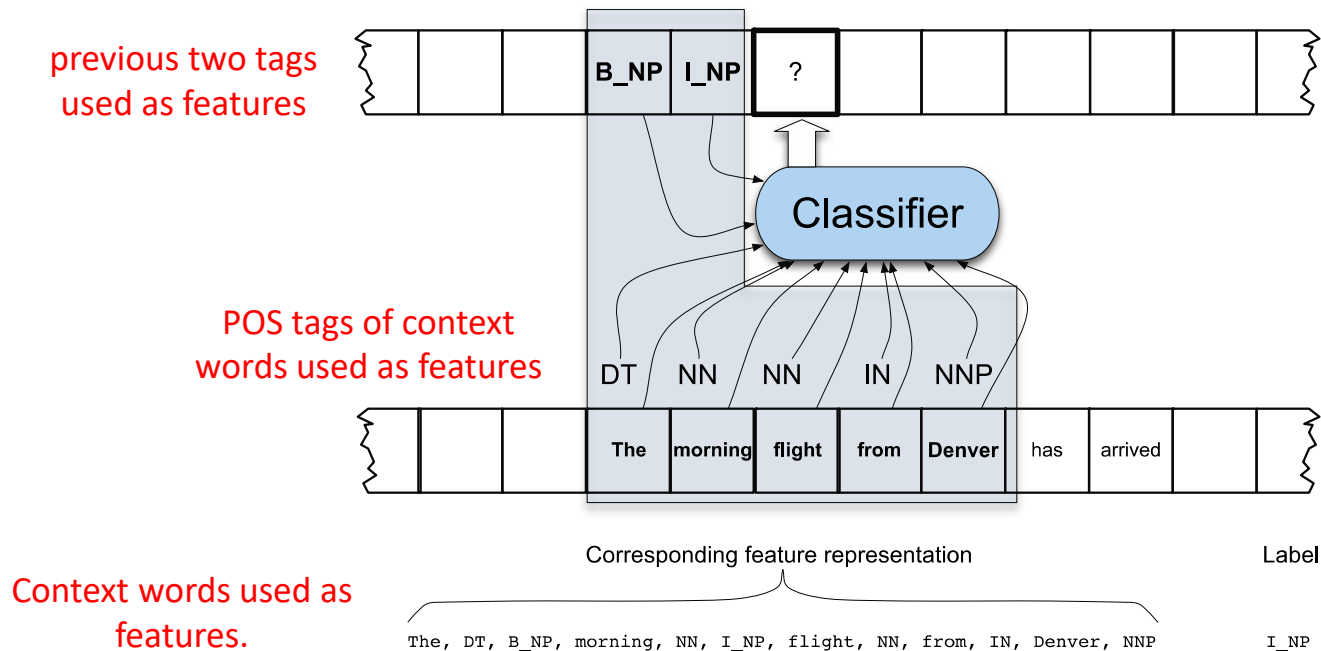
all main phrase
types

The morning flight from Denver has arrived.
B_NP I_NP I_NP O B_NP O O

If we're only
interested in NP's

Supervised Training

- Given a training set with labeled chunks (can be derived from a Treebank), we can use any sequence classification model



Evaluation of Chunking Systems

- Since chunking models identify spans of text with labels, word level accuracy is not a suitable measure.
 - Number of identified chunks may vary ...
- **Precision** and **Recall** are used to evaluate the system

$$\textbf{Precision:} = \frac{\text{Number of correct chunks given by system}}{\text{Total number of chunks given by system}}$$

$$\textbf{Recall:} = \frac{\text{Number of correct chunks given by system}}{\text{Total number of actual chunks in the text}}$$

Supervised Learning – Classical Approach

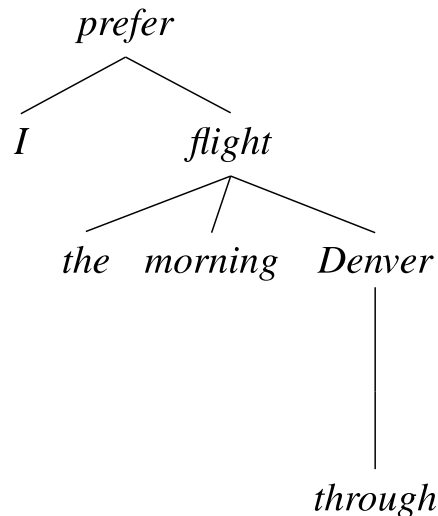
- Identify the problem (e.g. chunking, POS tagging, ... etc)
- Do we have human annotated data?
- Cleaning and Preprocessing (e.g. remove all e-mails or noisy characters, tokenization, lemmatization, etc)
- Input and output representation – feature extraction and output representation
- What type of algorithms work best?
- How do we evaluate? Intrinsic or extrinsic evaluation

Dependency Parsing

Dependency Grammar

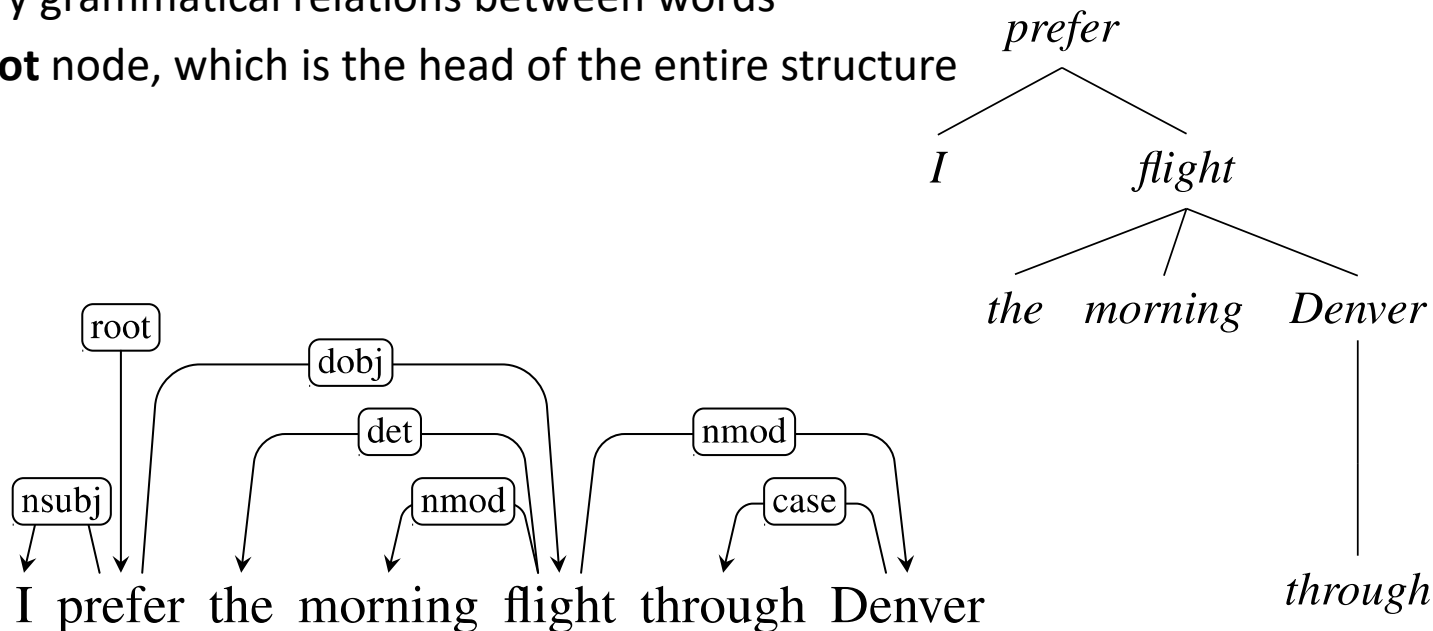
- Important in contemporary speech and language processing systems
- Consists of lexical items linked by binary asymmetric relations (“arrows”) called dependencies

- The arrows are commonly **typed** with the name of grammatical relations (subject, prepositional object, apposition, etc.)

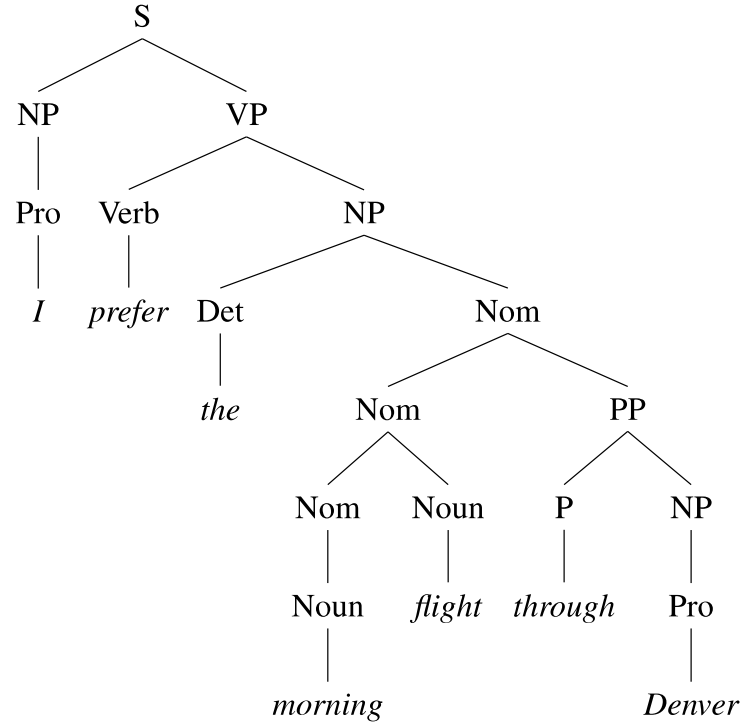
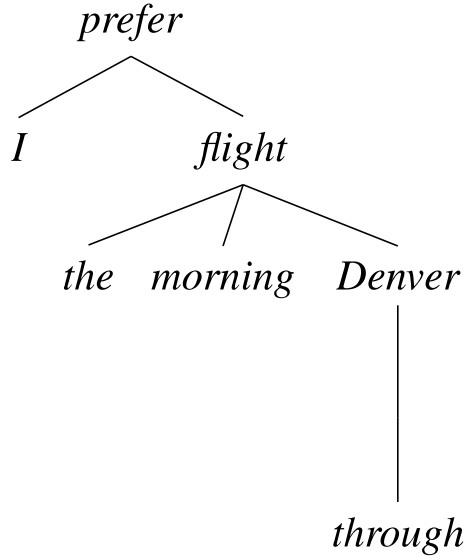


Typed Dependency Structure

- Directed labeled arcs from heads to dependents
- Express binary grammatical relations between words
- Includes a **root** node, which is the head of the entire structure



Dependency vs. Phrase Structure



Advantages of Dependency Structure

- Encode important semantic relationships that are often buried in complex phrase structures
- Particularly useful for languages with rich morphology and relatively free word order.
 - Phrase structure grammars can get very complex for some languages

Dependency Relations

- Dependency structures are comprised of **binary** relations based on traditional grammatical relations
 - Subject, direct object, indirect object, etc.
- The arguments of these relations consist of a **head** and a **dependent**
- The **Universal Dependencies** project includes dependency relations that are applicable across languages

Examples of Universal Dependency Relations

Clausal Argument Relations	Description
NSUBJ	Nominal subject
DOBJ	Direct object
IOBJ	Indirect object
CCOMP	Clausal complement
XCOMP	Open clausal complement
Nominal Modifier Relations	Description
NMOD	Nominal modifier
AMOD	Adjectival modifier
NUMMOD	Numeric modifier
APPOS	Appositional modifier
DET	Determiner
CASE	Prepositions, postpositions and other case markers
Other Notable Relations	Description
CONJ	Conjunct
CC	Coordinating conjunction

Dependency Treebanks

- A dependency grammar has a notion of a **head**
 - Officially, CFGs don't
- But modern linguistic theory and all modern statistical parsers (Charniak, Collins, Stanford, ...) do, via hand-written phrasal “**head rules**”:
 - The head of a Noun Phrase is a noun/number/...
 - The head of a Verb Phrase is a verb/modal/....
- The head rules can be used to automatically extract a dependency parse from a CFG parse
 - At least for English. Morphologically rich languages typically require manually annotated treebanks

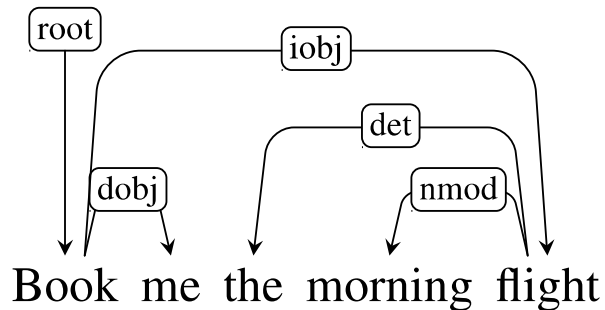
Formalisms

- Dependency structures are directed graphs $G = (V, A)$
 - A set of vertices **V**
 - V is typically the set of words in a sentence, but can also consist of stems and affixes for morphologically rich languages
 - A set of arcs **A**; ordered pairs of vertices from V (captures head dependents and grammatical function relationships between elements in V)
- A dependency Tree is a directed graph with the following constraints:
 1. There is a single **root** node with no incoming arcs
 2. All other vertices have exactly one incoming arc
 3. There is a unique path from the root to each vertex in the graph

Transition-Based Parsing

- A stack-based parsing approach
- **Configurations** consist of:
 - A stack
 - Input buffer of words
 - A set of relations representing a dependency tree
- The goal of parsing is to find a final configuration where all input words have been accounted for and a dependency tree has been created

Example



Step	Stack	Word List	Action	Relation Added
0	[root]	[book, me, the, morning, flight]	SHIFT	(book → me)
1	[root, book]	[me, the, morning, flight]	SHIFT	
2	[root, book, me]	[the, morning, flight]	RIGHTARC	
3	[root, book]	[the, morning, flight]	SHIFT	
4	[root, book, the]	[morning, flight]	SHIFT	
5	[root, book, the, morning]	[flight]	SHIFT	(morning ← flight)
6	[root, book, the, morning, flight]	[]	LEFTARC	
7	[root, book, the, flight]	[]	LEFTARC	
8	[root, book, flight]	[]	RIGHTARC	
9	[root, book]	[]	RIGHTARC	
10	[root]	[]	Done	(root → book)

Transition-Based Parsing

- **Start** with an initial configuration:
 - The stack consists of a ROOT node
 - The word list consists of all words in the input
 - An empty set of relations
- In the **final** configuration,
 - the word list should be empty
 - stack only includes the ROOT
 - The set of relations will represent the parse tree

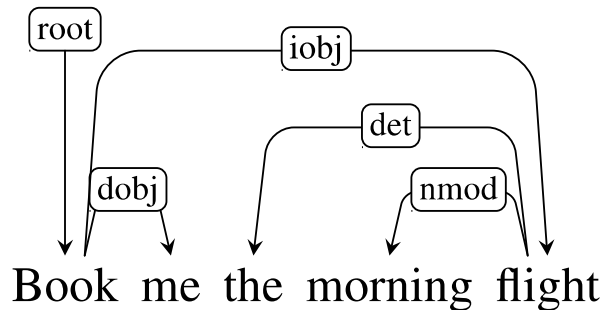
Arc-Standard Approach

- In **arc-standard** dependency parsing, one of three operations may be performed at each step:
 - **LEFTARC**: Assert a head-dependent relation between the word at the top of stack and the word directly beneath it; remove the lower word from the stack
 - **RIGHTARC**: Assert a head-dependent relation between the second word on the stack and the word at the top; remove the word at the top of the stack
 - **SHIFT**: Remove the word from the front of the input buffer and push it onto the stack

Arc-Standard Approach

- A straightforward greedy algorithm. Yet effective and simple to implement:
 - Words are examined in a single pass through the input from left to right
 - Transitions only assert relations between elements at the top of the stack
 - Once an element has been assigned a head, it's removed from the stack and is no longer available for processing

Example

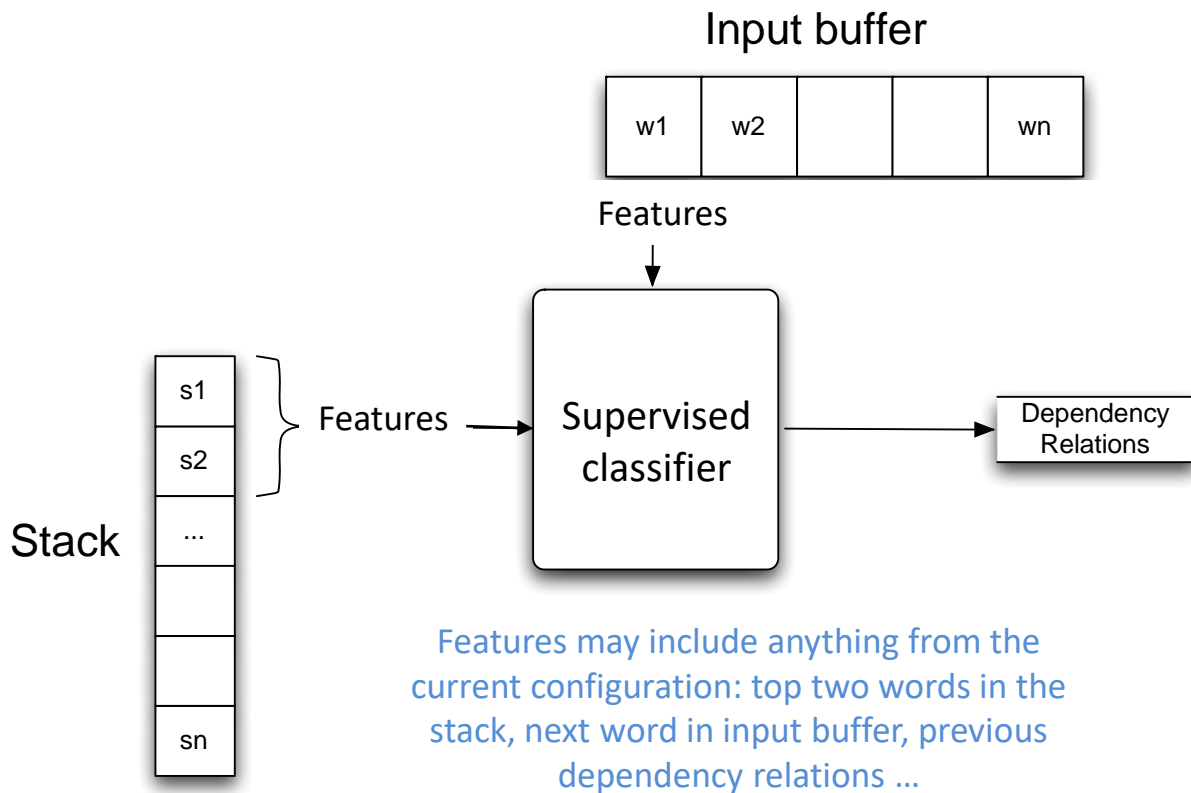


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6	[root, book, the, morning, flight]	[]	LEFTARC	
7	[root, book, the, flight]	[]	LEFTARC	
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10	[root]	[]	Done	(root → book)

Transition-Based Parsing

- To produce labeled arcs, we can expand the set of transition operators to include LEFTARC and RIGHTARC for each type of dependency relation.
 - LEFTARC_NSUBJ, RIGHTARC_NSUBJ, LEFTARC_DOBJ, ...
- Selecting the transition operator is typically done with **supervised machine learning** methods
 - Train a classifier that predicts the correct transition given the current configuration

Transition-Based Parsing



Evaluation

- Unlabeled attachment accuracy → percentage of words that are assigned the correct head
- Labeled attachment accuracy → percentage of words that are assigned the correct head with the correct label
- Label accuracy → percentage of words with correct labels (regardless of head)
- Precision and recall for each relation type

Resources

- The Stanford Parser:
 - Java implementation of lexicalized PCFG Constituency and dependency parsers for : English, German, French, Arabic, Chinese, and Spanish.

<https://nlp.stanford.edu/software/lex-parser.html>