Universal Threshold Signatures: Multi-Chain Cryptographic Infrastructure with Post-Quantum Security

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Abstract

We present a comprehensive universal threshold signature framework supporting 20+ blockchains through unified cryptographic protocols with post-quantum security. Our system integrates four core protocols—CMP (ECDSA), FROST (Schnorr/EdDSA), LSS (dynamic resharing), and Doerner (2-party optimization) with chain-specific adapters providing native support for XRPL, Ethereum, Bitcoin, Solana, Cardano, TON, and 14 additional networks. The framework achieves sub-25ms signing latency, 100% test coverage, and Byzantine fault tolerance up to t-1 malicious parties. We introduce the LSS protocol for live membership changes without downtime, enabling practical deployment in production custody systems. quantum security via Ringtail lattice-based signatures provides 128/192/256-bit security levels as quantum-resistant alternatives. Performance benchmarks demonstrate 12-82ms key generation and 8-40ms signing across threshold configurations from 3-of-5 to 10-of-15. The system is production-deployed securing billions in digital assets across enterprise custody solutions, DeFi protocols, and cross-chain bridges. This work represents over four years of continuous development (February 2021 - August 2025) with 800+

commits.

1 Introduction

Threshold signatures enable distributed signing authority where t out of n parties must collaborate to produce valid signatures, providing security against key compromise and single-point failures. While theoretical foundations exist, practical deployment across heterogeneous blockchain ecosystems presents significant engineering challenges:

- 1. **Protocol Diversity**: Different signature schemes (ECDSA, EdDSA, Schnorr) require distinct threshold protocols
- 2. Chain Compatibility: Each blockchain has unique signing requirements (message formats, encodings, hash functions)
- 3. **Dynamic Membership**: Real-world systems need to add/remove parties without reconstructing keys
- 4. **Performance**: Enterprise applications require sub-second signing latency
- 5. Quantum Resistance: Long-term security demands post-quantum alternatives

This paper presents a unified framework addressing all challenges simultaneously through:

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Universal Protocol Integration Four complementary threshold protocols (CMP, FROST, LSS, Doerner) cover the complete spectrum from 2-party to large-scale threshold signing with ECDSA, EdDSA, and Schnorr support.

Multi-Chain Adapters Native implementations for 20+ blockchains translate protocol outputs to chain-specific formats (BIP-340 Taproot, EIP-155/1559/4844 Ethereum, XRPL STX/SMT prefixes, Solana PDAs).

Dynamic Resharing LSS protocol enables live membership changes and threshold updates without master key reconstruction or system downtime.

Post-Quantum Security Ringtail lattice-based signatures provide quantum-resistant alternatives with Module-LWE hardness assumptions.

Production Validation Comprehensive testing (100% coverage, zero skipped tests), security audits, and real-world deployment securing billions in digital assets.

1.1 Contributions

- 1. **Unified Framework**: First production system integrating multiple threshold protocols with universal chain support
- 2. LSS Dynamic Resharing: Novel protocol for live membership changes with automatic fault tolerance
- 3. Chain Adapter Architecture: Extensible pattern for blockchain-agnostic threshold signatures
- 4. **Post-Quantum Integration**: Practical quantum-resistant threshold signatures for existing blockchains
- 5. **Performance Optimization**: Sub-25ms signing through constant-time arithmetic and parallel processing

6. **Production Deployment**: Battle-tested implementation securing enterprise custody and DeFi protocols

1.2 Version History

- v2021.02 (February 2021): Initial implementation with CMP and FROST protocols
- v2021.08 (August 2021): Added chain key derivation (BIP-32 compatible)
- v2023.05 (May 2023): Doerner 2-party protocol integration
- v2024.12 (December 2024): LSS dynamic resharing protocol
- v2025.08 (August 2025): Multi-chain adapters and Ringtail post-quantum signatures

2 Background

2.1 Threshold Cryptography

A (t,n)-threshold signature scheme distributes signing authority among n parties such that any subset of size t+1 can collaboratively generate valid signatures, while no coalition of t or fewer parties can forge signatures or reconstruct the private key.

Definition 1 (Threshold Signature Scheme). A(t,n)-threshold signature scheme consists of:

- $KeyGen(1^{\lambda}, t, n) \rightarrow (pk, \{sk_i\}_{i=1}^n)$: Distributed key generation producing public key pk and private shares sk_i
- $Sign(m, S, \{sk_i\}_{i \in S}) \rightarrow \sigma$: Collaborative signing where $|S| \ge t + 1$
- $Verify(m, \sigma, pk) \rightarrow \{0, 1\}$: Standard signature verification

2.2 Digital Signature Schemes

ECDSA The Elliptic Curve Digital Signature Algorithm is used by Bitcoin, Ethereum, and

XRPL. Signatures are (r, s) pairs where:

$$r = (k \cdot G)_x \mod q$$

 $s = k^{-1}(H(m) + r \cdot x) \mod q$

EdDSA Edwards-curve Digital Signature Algorithm (Ed25519) is used by Solana, Cardano, TON, and NEAR. Signatures are (R, s) where:

$$R = r \cdot B$$
$$s = r + H(R, A, m) \cdot a$$

Schnorr Bitcoin Taproot (BIP-340) uses Schnorr signatures (R, s) with:

$$s = k + H(R, P, m) \cdot x$$

2.3 Post-Quantum Cryptography

Quantum computers threaten all elliptic curve and factoring-based schemes via Shor's algorithm [7]. NIST's post-quantum standardization selected lattice-based schemes (Dilithium, Kyber) for quantum resistance. Module-LWE hardness provides security assumptions for lattice cryptography.

2.4 Related Work

GG18/GG20 Gennaro-Goldfeder protocols [5, 6] introduced MPC-based ECDSA threshold signatures but lacked identifiable abort.

CGGMP21 Canetti et al. [1] (CMP protocol) added identifiable aborts, 4-round online signing, and proactive refresh.

FROST Komlo-Goldberg [2] developed efficient 2-round threshold Schnorr signatures with pre-processing.

Two-Party ECDSA Doerner et al. [4] optimized 2-of-2 ECDSA for constant-time performance.

3 Core Protocols

Our framework integrates four complementary threshold protocols, each optimized for specific use cases.

3.1 CMP Protocol

The CMP protocol [1] provides (t, n)-threshold ECDSA signatures with identifiable abort. We implement the enhanced version with:

Key Generation 4-round protocol using Shamir secret sharing and Paillier homomorphic encryption:

- 1: Sample $x^{(i)} \in \mathbb{F}_q$, compute $X^{(i)} = x^{(i)} \cdot G$
- 2: Sample safe primes $p^{(i)}, q^{(i)}$, compute $N^{(i)} = p^{(i)}q^{(i)}$
- 3: Define VSS polynomial $f^{(i)}(Z) = x^{(i)} + \sum_{l=1}^{t} f_l^{(i)} Z^l$
- 4: Broadcast commitments, exchange encrypted shares
- 5: Verify ZK proofs: Π_{mod} , Π_{prm} , Π_{sch}
- 6: Compute share $\mathsf{sk}^{(i)} = \sum_{j=1}^{n} f^{(j)}(i) \bmod q$

Pre-signing 7-round protocol generating presignature triples (k_i, γ_i, ρ_i) using multiplicative-to-additive (MtA) conversion:

$$k = \sum_{i \in S} k_i \cdot \lambda_i \mod q$$
$$\gamma = k \cdot x = \sum_{i \in S} \gamma_i \cdot \lambda_i \mod q$$

Online Signing 4-round signing given message m and presignature:

$$R = \gamma^{-1} \cdot G, \quad r = R_x \bmod q$$

$$s_i = k_i (H(m) + r \cdot x_i \cdot \lambda_i)$$

$$s = \sum_{i \in S} s_i \bmod q$$

Identifiable Abort ZK proofs at each round enable identification of malicious parties failing to follow protocol.

3.2 FROST Protocol

FROST [2] provides efficient threshold Schnorr/EdDSA signatures with 2-round signing.

Key Generation Similar to CMP but simplified for Schnorr:

- 1: Each party i samples polynomial $f_i(z)$ with $f_i(0) = s_i$
- 2: Broadcast commitments $F_{il} = f_{il} \cdot G$ for $l = 0, \ldots, t$
- 3: Send shares $f_i(j)$ to party j via secure channel
- 4: Each party computes $s_j = \sum_i f_i(j)$ and verifies commitments
- 5: Public key: $Y = \sum_{i} F_{i0}$

Signing 2-round protocol with nonce commitments:

- 1: **Round 1:** Each signer i samples (d_i, e_i) , computes (D_i, E_i) , broadcasts commitment
- 2: **Round 2:** Reveal (D_i, E_i) , compute binding factor $\rho_i = H(\text{context})$
- 3: Compute group commitment $R = \sum_{i} (D_i + \rho_i E_i)$
- 4: Challenge: c = H(R, Y, m)
- 5: Each party computes $z_i = d_i + \rho_i e_i + \lambda_i s_i c$
- 6: Aggregate: $z = \sum_{i} z_{i}$
- 7: Output signature (R, z)

Taproot Compatibility We implement BIP-340 [8] compatibility by:

- ullet Normalizing public key Y to even y-coordinate during keygen
- Negating nonces if R has odd y-coordinate
- Using BIP-340 challenge hash $c = H(\text{tag}||R_x||Y_x||m)$

Hedged Nonces We enhance security using deterministic nonces with optional randomness:

$$k \leftarrow \text{KDF}(s_i)$$

$$a \xleftarrow{R} \{0, 1\}^{256}$$

$$(d_i, e_i) \leftarrow H_k(\text{SSID}||m||a)$$

3.3 LSS Dynamic Resharing

The LSS protocol [3] solves critical operational challenges: live membership changes without downtime or master key reconstruction.

Motivation Traditional threshold schemes require complete key regeneration to change n or t. For systems with 24/7 uptime requirements, coordinating simultaneous key migration is operationally infeasible. LSS enables seamless transition from (t,n) to $(t',n\pm k)$ while maintaining liveness.

Architecture

- Bootstrap Dealer: Orchestrates resharing protocol, never handles unencrypted secrets
- Signature Coordinator: Public API for signing requests, triggers automatic rollback on failures
- Participant Nodes: Hold private key shares, maintain generation history

Resharing Protocol Transition from shares $\{a_i^{\text{old}}\}$ to $\{a_i^{\text{new}}\}$:

- 1: Auxiliary Secret Generation: Parties generate shares of temporary secrets w, q via JVSS
- 2: Blinded Secret: Original parties compute $a \cdot w$ using interpolation
- 3: **Inverse Blinding:** Compute $z = (q \cdot w)^{-1}$ and distribute shares
- 4: **Final Shares:** Each party j computes $a_i^{\text{new}} = (a \cdot w) \cdot q_j \cdot z_j$

Key property: $\sum_{j \in S'} \lambda_j^{S'} a_j^{\text{new}} = a$ for any authorized subset S' of size $\geq t' + 1$.

Shard Generations Each resharing increments generation counter. Historical generations maintained for rollback:

- Generation 0: Initial key generation
- **Generation** g: After g resharing operations
- Rollback: Revert to generation g-1 on signing failures

Automated Fault Tolerance

- Signature coordinator detects signing failures
- Automatically triggers rollback to previous generation
- Evicts Byzantine parties from current generation
- Maintains liveness even with t-1 malicious parties

FROST Integration LSS seamlessly extends FROST signing:

- 1: function DynamicReshare-FROST($\{\text{config}_i^{\text{old}}\}$, newParties, t')
- 2: Run LSS resharing protocol on FROST shares
- 3: Update verification shares Y_j via Lagrange interpolation
- 4: Maintain public key Y unchanged
- 5: **return** {config_i^{new}}
- 6: end function

3.4 Doerner 2-Party Protocol

The Doerner protocol [4] optimizes 2-of-2 ECDSA for minimal latency using oblivious transfer and garbled circuits.

Key Generation

- 1: Party 1 samples x_1 , Party 2 samples x_2
- 2: Public key: $Y = x_1 \cdot G + x_2 \cdot G$
- 3: Exchange Paillier public keys for MtA

Signing Constant-time 2-party computation:

- 1: Generate additive shares of k via OT
- 2: Compute k^{-1} using garbled circuit
- 3: MtA to compute shares of $k^{-1} \cdot x$
- 4: Each party computes s_i , aggregate to s

Performance: \sim 5ms for 2-party signing vs. \sim 15ms for CMP.

4 Multi-Chain Adapter Architecture

4.1 Unified Interface

We define a chain-agnostic interface abstracting signature operations:

- 1: **function** SignerAdapter
- 2: $\mathbf{Digest}(tx) \to \text{hash}$: Compute chainspecific message digest
- 3: **SignEC**(hash, share) \rightarrow partial: Generate partial signature
- 4: **AggregateEC**(partials) \rightarrow signature: Combine partial signatures
- 5: **Encode**(signature) \rightarrow bytes: Format for blockchain submission
- 6: **FormatPublicKey**(point) \rightarrow address: Derive chain address
- 7: end function

4.2 Chain-Specific Adapters

4.2.1 XRPL Adapter

XRP Ledger requires specific hash prefixes and signature normalization:

Hash Prefixes

- Single-signing: STX prefix (0x53545800)
- Multi-signing: SMT prefix (0x534D5400)

Hash Function SHA-512Half (first 256 bits of SHA-512):

 $digest = SHA-512Half(prefix||tx_blob)$

Signature Normalization XRPL requires low-S values:

- 1: **if** s > q/2 **then**
- $2: \qquad s \leftarrow q s$
- 3: end if

Public Key Format

- ECDSA: 33-byte compressed (0x02/0x03 prefix)
- EdDSA: ED prefix (0xED) + 32-byte public key

4.2.2 Ethereum Adapter

Support for legacy and modern transaction types:

Transaction Types

- **Legacy**: RLP encoding, EIP-155 chain ID in signature
- EIP-1559: Base fee + priority fee, type 0x02
- EIP-4844: Blob transactions, type 0x03

Signature Encoding

$$v = \begin{cases} 27 + \text{recovery_id} & \text{(pre-EIP-Polynomial of the presentations)} \\ 35 + 2 \cdot \text{chainID} + \text{recovery_id} & \text{(EIP-155)} \end{cases}$$

Contract Wallet Support EIP-1271 signature verification for smart contract wallets via isValidSignature interface.

4.2.3 Bitcoin Adapter

Support for legacy, SegWit, and Taproot:

Signature Hash Types

- SIGHASH_ALL (0x01): Sign all inputs and outputs
- SIGHASH_SINGLE (0x03): Sign corresponding output
- SIGHASH_ANYONECANPAY (0x80): Sign only one input

Taproot (BIP-340) Schnorr signatures with:

- x-only public keys (32 bytes, even y)
- Tagged hashes: H(tag||tag||m)
- Signature: (R_x, s) where R_x is x-coordinate

PSBT Support Partially Signed Bitcoin Transactions enable collaborative signing workflow.

4.2.4 Solana Adapter

EdDSA signatures with Program Derived Addresses (PDAs):

Message Format

- 1: Header: numSignatures, numReadonly, numReadonlyUnsigned
- 2: Account keys: [pubkey₁,..., pubkey_n]
- 3: Recent blockhash (32 bytes)
- 4: Instructions: program ID, accounts, data

PDA Derivation

 $PDA = H(seeds||program_id||"ProgramDerivedAddress")$

(pre-EIP-155) where ${\cal H}$ outputs a point off the Ed25519 curve.

Versioned Transactions Support for address lookup tables (v0 transactions).

4.2.5 TON Adapter

Bag of Cells (BOC) serialization with EdDSA:

Cell Structure

- Hash: SHA-256 of cell representation
- Depth: Maximum reference depth
- References: Up to 4 child cells
- Data: Up to 1023 bits

Workchain Support TON uses multiple workchains (basechain = 0, masterchain = -1).

4.2.6 Cardano Adapter

Multi-era support (Byron, Shelley, Allegra, Mary, Alonzo, Babbage):

Signature Schemes

- EdDSA: Standard signing
- ECDSA: secp256k1 for interoperability
- Schnorr: Taproot-style signatures

Plutus Scripts Smart contracts require witness sets with redeemers and datums.

Multi-Signature Native multi-sig scripts with AND/OR logic.

4.3 Performance Comparison

Chain	Sig Type	Hash	Encode	Total
XRPL	ECDSA	$1.2 \mathrm{ms}$	$0.3 \mathrm{ms}$	$1.5 \mathrm{ms}$
Ethereum	ECDSA	$0.8 \mathrm{ms}$	$0.4 \mathrm{ms}$	$1.2 \mathrm{ms}$
Bitcoin	Schnorr	$0.9 \mathrm{ms}$	$0.2 \mathrm{ms}$	$1.1 \mathrm{ms}$
Solana	EdDSA	$1.1 \mathrm{ms}$	$0.5 \mathrm{ms}$	$1.6 \mathrm{ms}$
TON	EdDSA	$1.4 \mathrm{ms}$	$0.6 \mathrm{ms}$	$2.0 \mathrm{ms}$
Cardano	EdDSA	$1.0 \mathrm{ms}$	$0.4 \mathrm{ms}$	1.4ms

Table 1: Chain adapter overhead (mean, single-threaded)

5 Post-Quantum Security

5.1 Ringtail Lattice-Based Signatures

Ringtail provides quantum-resistant threshold signatures using Module-LWE hardness assumptions.

Security Levels

- Level 1: 128-bit quantum security (NIST Category 1)
- Level 3: 192-bit quantum security (NIST Category 3)
- Level 5: 256-bit quantum security (NIST Category 5)

Key Generation Distributed sampling of lattice shares:

- 1: Sample $\mathbf{A} \xleftarrow{R} R_q^{k \times l}$ (public randomness)
- 2: Each party i samples $\mathbf{s}_i \leftarrow \chi_{\eta}$ (secret share)
- 3: Compute $\mathbf{t}_i = \mathbf{A}\mathbf{s}_i + \mathbf{e}_i$ where $\mathbf{e}_i \leftarrow \chi_{\eta}$
- 4: Public key: $\mathbf{t} = \sum_i \mathbf{t}_i$

Signing Fiat-Shamir with aborts:

- 1: Each party samples $\mathbf{y}_i \leftarrow \chi_{\gamma}$
- 2: Compute commitment $\mathbf{w}_i = \mathbf{A}\mathbf{y}_i$
- 3: Aggregate: $\mathbf{w} = \sum_{i} \mathbf{w}_{i}$
- 4: Challenge: $c = H(\mathbf{w}, m) \in \mathcal{C}$
- 5: Response: $\mathbf{z}_i = \mathbf{y}_i + c\mathbf{s}_i$
- 6: if $||\mathbf{z}_i|| > B$ then abort and restart
- 7: end if
- 8: Aggregate: $\mathbf{z} = \sum_{i} \mathbf{z}_{i}$
- 9: Signature: (w, z)

Share Refresh Proactive security via share randomization:

- 1: Each party samples $\Delta \mathbf{s}_i \leftarrow \chi_{\eta}$
- 2: Update share: $\mathbf{s}'_i = \mathbf{s}_i + \Delta \mathbf{s}_i$
- 3: Broadcast $\Delta \mathbf{t}_i = \mathbf{A} \Delta \mathbf{s}_i + \mathbf{e}_i$
- 4: Verify $\sum_{i} \Delta \mathbf{t}_{i} = \mathbf{0}$ (public key unchanged)
- 5:

Chain Integration Ringtail signatures can be verified on-chain via:

- Smart contract verification (Ethereum, Cardano)
- Native verification opcodes (future Bitcoin soft fork)
- Off-chain verification with on-chain anchoring

5.2 Performance Comparison

Scheme	Keygen	Sign	Verify
ECDSA (CMP)	12ms	$15 \mathrm{ms}$	$2 \mathrm{ms}$
EdDSA (FROST)	$10 \mathrm{ms}$	$8 \mathrm{ms}$	2 ms
Schnorr (FROST)	$10 \mathrm{ms}$	$8 \mathrm{ms}$	2 ms
Ringtail-128	$45 \mathrm{ms}$	$120 \mathrm{ms}$	$35 \mathrm{ms}$
Ringtail-192	$68 \mathrm{ms}$	$180 \mathrm{ms}$	$52 \mathrm{ms}$
Ringtail-256	$95 \mathrm{ms}$	$240 \mathrm{ms}$	$70 \mathrm{ms}$

Table 2: Performance comparison: classical vs. post-quantum (3-of-5 threshold)

6 Performance Evaluation

6.1 Experimental Setup

Hardware

- CPU: Apple M1 Pro / Intel i7-12700K
- RAM: 32GB DDR4
- Network: Localhost (0.1ms latency) / LAN (5ms latency)

Implementation Go 1.24.5, constant-time arithmetic via saferith library, parallel processing for heavy computations.

6.2 Benchmark Results

6.3 Scalability Analysis

Key Generation Complexity $O(n^2)$ due to pairwise share distribution. Optimizations:

- Parallel proof generation (4x speedup on 4 cores)
- Batched commitment verification
- Efficient broadcast using Merkle trees

Signing Complexity O(n) for online phase. CMP presigning amortizes costs across multiple signatures.

Network Latency Impact

- Localhost (0.1ms): Minimal impact, CPU-bound
- LAN (5ms): 15-25% overhead for multiround protocols
- WAN (50ms): 2-3x slowdown, dominated by network rounds

6.4 Throughput

Concurrent Signing Independent signatures can be parallelized:

• CMP: 200 signatures/sec (with presignature pool)

- FROST: 350 signatures/sec
- Doerner: 800 signatures/sec (2-party)

Presignature Generation CMP presignatures can be precomputed:

- 3-of-5: 22 presignatures/sec
- 5-of-9: 10 presignatures/sec
- 10-of-15: 4 presignatures/sec

7 Security Analysis

7.1 Threat Model

Adversary Capabilities

- Byzantine Faults: Up to t-1 parties may deviate arbitrarily
- Network Control: Adversary controls message scheduling (but not content)
- Static Corruption: Party corruption before protocol execution
- Adaptive Corruption: Party corruption during execution (restricted)

Security Goals

- Unforgeability: No coalition of size $\leq t$ can forge signatures
- Robustness: Honest parties output valid signatures despite Byzantine faults
- Identifiable Abort: Malicious parties detected and excluded

7.2 Protocol Security

Theorem 1 (CMP Security). The CMP protocol achieves (t, n)-threshold unforgeability under the ECDSA security assumption, DDH assumption in the Paillier group, and security of zero-knowledge proofs in the random oracle model.

Operation	3-of-5	5-of-9	7-of-11	10-of-15	Complexity
CMP Keygen	$12 \mathrm{ms}$	$28 \mathrm{ms}$	$45 \mathrm{ms}$	82ms	$O(n^2)$
CMP Presign	$45 \mathrm{ms}$	$98 \mathrm{ms}$	$152 \mathrm{ms}$	$230 \mathrm{ms}$	$O(n^2)$
CMP Sign	$15 \mathrm{ms}$	$32 \mathrm{ms}$	$48 \mathrm{ms}$	$75 \mathrm{ms}$	O(n)
FROST Keygen	$10 \mathrm{ms}$	$25 \mathrm{ms}$	42ms	78ms	$O(n^2)$
FROST Sign	$8 \mathrm{ms}$	$18 \mathrm{ms}$	$28 \mathrm{ms}$	$45 \mathrm{ms}$	O(n)
LSS Keygen	$12 \mathrm{ms}$	$28 \mathrm{ms}$	$45 \mathrm{ms}$	$82 \mathrm{ms}$	$O(n^2)$
LSS Reshare	$20 \mathrm{ms}$	$35 \mathrm{ms}$	$52 \mathrm{ms}$	$75 \mathrm{ms}$	$O(n \cdot n')$
LSS Sign	$18 \mathrm{ms}$	$35 \mathrm{ms}$	$55 \mathrm{ms}$	$88 \mathrm{ms}$	O(n)
Doerner Keygen	8ms	_	_	_	O(1) (2-party)
Doerner Sign	$5 \mathrm{ms}$	_	_	_	O(1) (2-party)
Verification	$2 \mathrm{ms}$	$2 \mathrm{ms}$	$2 \mathrm{ms}$	$2 \mathrm{ms}$	O(1)

Table 3: Performance benchmarks across threshold configurations (mean of 100 runs, localhost network). Complexity indicates scaling with party count.

Theorem 2 (FROST Security). FROST achieves existential unforgeability under chosenmessage attack under the discrete logarithm assumption in the random oracle model, with robustness against up to t-1 malicious parties.

Theorem 3 (LSS Security). The LSS dynamic resharing protocol maintains (t, n)-threshold security across generations, with share forward security: compromised old shares cannot forge signatures after resharing.

Theorem 4 (Ringtail Security). Ringtail achieves existential unforgeability under the Module-LWE hardness assumption with parameters providing quantum security levels 1, 3, or 5 per NIST standards.

7.3 Implementation Security

Constant-Time Arithmetic All cryptographic operations use constant-time implementations (saferith library) to prevent timing attacks.

Side-Channel Resistance

- No secret-dependent branches
- No secret-dependent memory access patterns

• Blinding of intermediate values

Zero-Knowledge Proofs All protocols use ZK proofs at critical steps:

- Π_{mod} : Paillier modulus is product of two primes
- Π_{prm}: Correct Paillier parameter generation
- Π_{sch}: Schnorr proof of knowledge
- Π_{affg}: Affine operation with group commitment
- Π_{log} : Discrete logarithm equality

7.4 Security Audit Findings

Third-party security audit (2024) identified and resolved:

- 1. **Nonce Generation**: Enhanced to hedged deterministic nonces
- 2. Range Proofs: Tightened bounds in ZK proofs
- 3. **Session Binding**: Strengthened session ID to prevent replay attacks
- 4. **Abort Handling**: Improved abort identification in CMP

Low severity recommendations implemented.

8 Deployment Applicaand tions

Production Deployment 8.1

The framework is production-deployed securing:

- Enterprise Custody: Multi-billion dollar institutional custody with geographic distribution of signing parties
- DeFi Protocols: Decentralized autonomous organizations (DAOs) with on-chain governance
- Cross-Chain **Bridges**: Thresholdcontrolled bridge contracts securing cross-chain asset transfers
- Wallet Abstraction: Consumer-facing MPC wallets with mobile/web interfaces

8.2 Use Cases

Multi-Jurisdictional Custody 5-of-7 threshold with parties in different jurisdictions:

- Compliance: No single jurisdiction controls kevs
- Disaster recovery: 2 party failures tolerable
- Geographic distribution: US, EU, Asia locations

DAO Treasury threshold for large protocol treasuries:

- Security council members hold shares
- On-chain governance triggers signing
- LSS resharing for council elections

All high and medium severity issues resolved. **Institutional Trading** 3-of-5 threshold for high-frequency trading:

• Compliance team: 2 shares

• Trading desk: 2 shares

• Risk management: 1 share

• CMP presignatures for low latency

Personal Custody 2-of-3 threshold for individual users:

• Mobile device: 1 share

• Hardware wallet: 1 share

• Cloud backup (encrypted): 1 share

 Doerner protocol for mobile-hardware signing

Integration Examples 8.3

XRPL Bridge

```
// 5-of-9 threshold controlling bridge account
config := cmp.Keygen(curve.Secp256k1{},
    selfID, parties, 4, pool)
```

```
// XRPL multi-sign transaction
xrpl := adapters.NewXRPLAdapter(
    adapters.SignatureECDSA, true)
digest, _ := xrpl.Digest(txBlob)
// Threshold signing with 5 parties
signature := cmp.Sign(config, signers,
    digest, pool)
```

encoded, _ := xrpl.Encode(signature)

Ethereum DAO Treasury

```
Management 7-of-11 // 7-of-11 FROST threshold for gas efficiency
                     config := frost.Keygen(curve.Secp256k1{},
                         selfID, parties, 6, pool)
```

```
// EIP-1559 transaction
eth := adapters.NewEthereumAdapter()
tx := &adapters.EIP1559Transaction{
    ChainID: big.NewInt(1),
```

```
Nonce: 42,
    // ... other fields
}
digest, _ := eth.Digest(tx)
// 2-round FROST signing
signature := frost.Sign(config, signers,
    digest, pool)
encoded, _ := eth.Encode(signature)
```

Dynamic Validator Set

```
// Initial 5-of-9 validator set
// Add 3 new validators → 7-of-12
newParties := append(oldParties,
   newValidators...)
newConfigs := lss.Reshare(oldConfigs,
   newParties, 6, pool)
// Signing continues with new set
signature := lss.Sign(newConfigs[selfID],
   signers, message, pool)
```

Operational Metrics

Uptime 99.95% availability over 12-month period with:

- Automatic failover to backup parties
- LSS rollback for Byzantine fault recovery
- Zero downtime during membership changes

Signing Volume

- 2M+ signatures generated in production
- 500-2000 signatures/day across all deployments
- Peak load: 50 concurrent signing sessions

Error Rates

• Protocol failures: < 0.01% (mostly network timeouts)

- Identifiable aborts: 3 incidents (Byzantine parties excluded)
- LSS rollbacks: 12 automated recoveries

Comparison with Alterna-9 tives

Advantages

- 1. Universal Chain Support: Native adapters for 20+ blockchains vs. generic signature output requiring manual integration
- ing vs. static key distribution
- 3. Post-Quantum Ready: Ringtail lattice signatures vs. elliptic-curve only
- 4. **Protocol Diversity**: Four complementary protocols vs. single implementation
- 5. Production Validation: 100% test coverage, security audit, real-world deployment

Trade-offs

- 1. Complexity: More features require larger codebase (vs. minimal research implementations)
- 2. **Performance**: ECDSA protocols slower than BLS (15ms vs. 5ms), but BLS lacks chain support
- 3. Trust Assumptions: LSS coordinator trusted for liveness (not secrecy)

10 Future Work

10.1 Short-Term Enhancements

Additional Protocols

- CGGMP21 updates (enhanced abort identification)
- SpeedyMuSig2 for fast 2-round Schnorr
- GG18-based EdDSA threshold signatures

System	Protocols	Chains	Dynamic	Post-Quantum	Signing	\mathbf{Pr}
tss-lib [9]	GG18, GG20	Generic	No	No	$60 \mathrm{ms}$	-
ZenGo X [10]	GG20, EdDSA	5+	No	No	$40 \mathrm{ms}$	
Multi-Party-ECDSA [11]	Lindell 2P	Generic	No	No	$30 \mathrm{ms}$	R
Threshold-BLS [12]	BLS	Ethereum 2.0	No	No	$5 \mathrm{ms}$	
Lux Threshold	CMP, FROST, LSS, Doerner	20+	Yes (LSS)	Yes (Ringtail)	8-40ms	

Table 4: Comparison with existing threshold signature systems. Our framework uniquely combines multiple protocols, extensive chain support, dynamic membership, and post-quantum security in a production-ready package.

Chain Support Expansion

- Tier 2 chains: Cosmos, Polkadot, Avalanche, Aptos, Sui
- Privacy chains: Zcash, Monero (threshold view keys)
- Emerging chains: Movement, Monad, Berachain

Performance Optimization

- GPU acceleration for ZK proof generation
- WebAssembly compilation for browser deployment
- Presignature pool management with predictive allocation

10.2 Medium-Term Research

Asynchronous Protocols Remove need for synchronization:

- Asynchronous DKG (distributed key generation)
- Threshold signing with guaranteed termination
- Network partition tolerance

Proactive Security Enhancements

- Automated share refresh scheduling
- Mobile adversary resistance (adaptive corruption)
- Key escrow and recovery mechanisms

Advanced LSS Features

- Concurrent resharing without coordinator
- Threshold changes without full resharing
- Hierarchical threshold structures

10.3 Long-Term Vision

Fully Homomorphic Threshold Signatures Enable threshold signing over encrypted data without revealing intermediate values.

Quantum-Safe Interoperability Hybrid classical/post-quantum schemes for gradual transition:

- Dual signatures (ECDSA + Ringtail)
- Merkle aggregation for efficiency
- Backward compatibility with existing chains

Decentralized Threshold Networks Public infrastructure for threshold signing-as-a-service:

- Economic incentives for liveness
- Slashing for Byzantine behavior
- Automated party discovery and reputation

AI Agent Integration Threshold signatures for AI economies:

- AI agents provisioned with single shares
- Multi-agent consent workflows
- "Know Your Agent" cryptographic identity

11 Conclusion

We presented a comprehensive universal threshold signature framework addressing practical deployment challenges across 20+ blockchains. Our system integrates four core protocols (CMP, FROST, LSS, Doerner) with chain-specific adapters providing native support for diverse signature schemes (ECDSA, EdDSA, Schnorr, post-quantum Ringtail).

The LSS dynamic resharing protocol enables live membership changes without downtime or master key reconstruction, solving critical operational challenges for production systems. Performance benchmarks demonstrate sub-25ms signing latency with 100% test coverage and Byzantine fault tolerance.

Production deployment secures billions in digital assets across enterprise custody, DeFi protocols, and cross-chain bridges, validating the framework's practical viability. Post-quantum Ringtail signatures provide quantum-resistant alternatives for long-term security.

Over four years of continuous development (February 2021 - August 2025, 800+ commits), we evolved from initial CMP/FROST implementation to a production-ready universal infrastructure. The framework's extensible architecture and comprehensive testing establish a foundation for next-generation threshold cryptography.

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