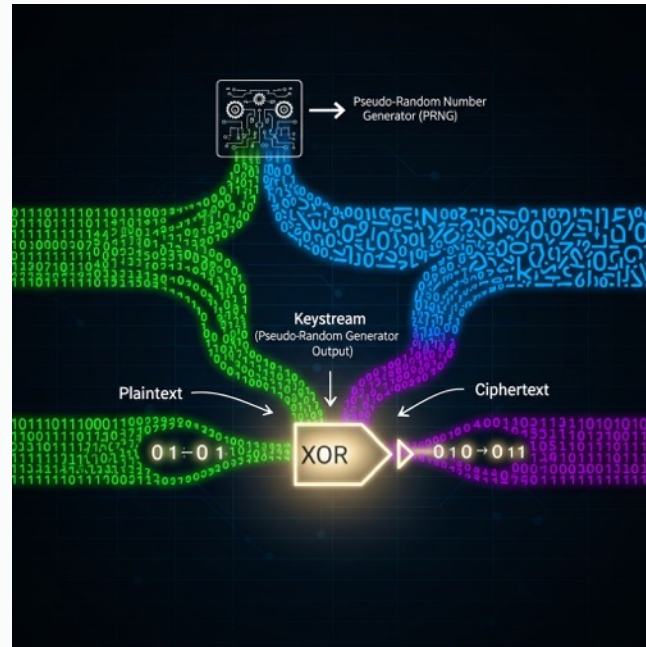


Stream ciphers

old, but now back in
the spotlight



Secret key cryptography

Alice and Bob share

- A crypto protocol E
- A secret (symmetric) key K
- They communicate using E with key K
- Adversary knows E , knows some exchanged messages but ignores K

Two approaches:

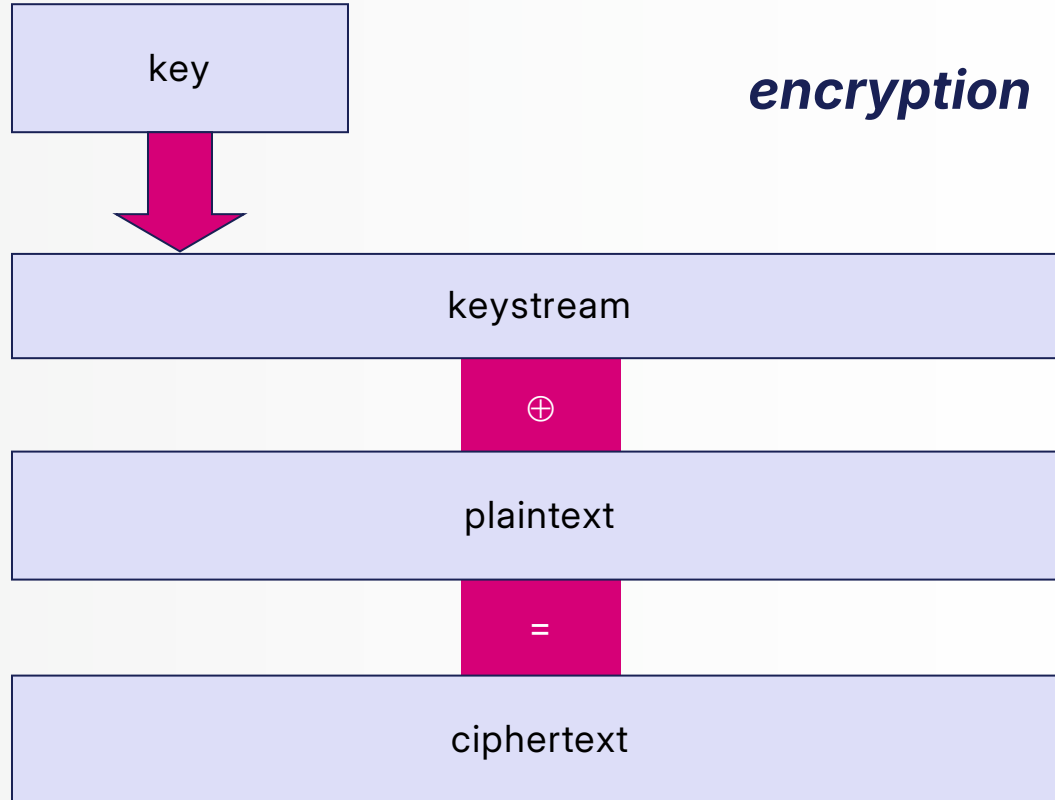
- Stream Ciphers
- Block ciphers

Stream ciphers

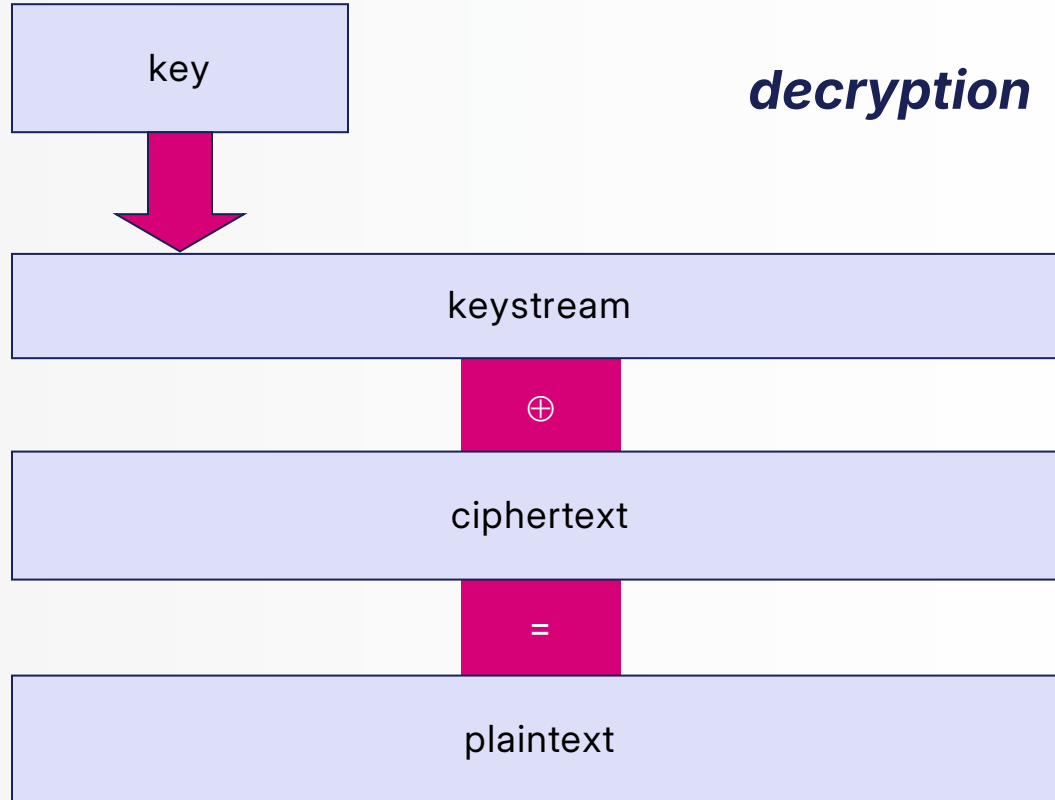
- define a secret key (*seed*)
- using the seed generate a byte stream (*keystream*):
 i -th byte is function of
 - only key (*synchronous* stream cipher), or
 - both key and first $i-1$ bytes of ciphertext
asynchronous stream cipher)
- obtain ciphertext by bitwise XORing plaintext and keystream

x	y	$x \oplus y$
0	0	0
0	1	1
1	0	1
1	1	0

Synchronous stream cipher



Synchronous stream cipher



Synchronous stream ciphers in practice

- Many ciphers before 1940
- Enigma - II world war (Germany)
- A5 – GSM (encryption cell phone-base station)
- WEP – used in Ethernet 802.11 (wireless)
- RC-4 (Ron's Code, used by WEP)

A5/1 stream cipher

- Developed in 1987, used to ensure over-the-air communication privacy in the GSM cellular telephone standard
- A major dispute arose in the mid-1980s between NATO signal intelligence agencies about whether GSM encryption should be strong or intentionally weakened
- Used in both Europe and the United States. A related variant, A5/2, was a deliberately weakened version intended for export to certain regions
- The design was initially kept secret, but leaked in 1994 and fully reverse-engineered in 1999 by Marc Briceno
- Multiple serious vulnerabilities in the cipher were subsequently identified



RC-4

- RC: Ron's Code
 - (Ron = Ronald Rivest, MIT, born in 1947 in NY state)
- Considered safe: 1987 - 1994 kept secret, after '94 extensively studied
 - insecure from 2004
- Good for exporting (complying with US restrictions)
- Easy to program, fast
- Very popular: Lotus Notes, SSL, Wep etc.
- RC4's weak key schedule can give rise to a variety of serious problems

RC-4 weaknesses

- Biased output in early keystream bytes
- Vulnerable if keys are reused
- Broken in protocols like WEP and TLS (early versions)
- Today deprecated

RC-4 properties

- variable key length (byte)
- synchronous
- starting from the key, it generates an apparently random permutation
- eventually the sequence will repeat
- however, long period $> 10^{100}$
- very fast: 1 byte of output requires 8-16 instructions

RC-4 initialization

Goal: generate a (pseudo)random permutation of the first 256 natural numbers

1. $j=0$
2. $S_0=0, S_1=1, \dots, S_{255}=255$
3. Assume a key of 256 bytes k_0, \dots, k_{255} (if the key is shorter, repeat)
4. for $i=0$ to 255 do
 1. $j = (j + S_i + k_i) \bmod 256$
 2. exchange S_i and S_j

In this way we obtain a permutation of $0, 1, \dots, 255$, the resulting permutation is a function of the key

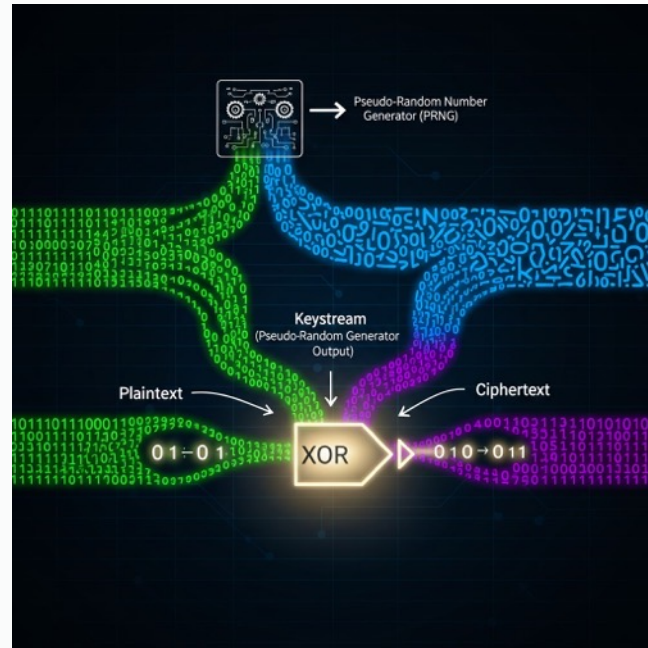
RC-4 keystream generation

Input: permutation S of $0, 1, \dots, 255$

1. $i = 0, j = 0$
2. while (true)
 1. $i = (i + 1) \bmod 256$
 2. $j = (j + S_i) \bmod 256$
 3. exchange S_i and S_j
 4. $t = (S_i + S_j) \bmod 256$
 5. $k = S_t$ // compute XOR

at every iteration compute the XOR between k and next byte of plaintext (or ciphertext)

Perfect ciphers and One-Time Pad



Perfect ciphers

Plaintext space = $\{0, 1\}^n$, D known

Given a ciphertext C the probability that exists k_2 such that $D_{k_2}(C) = P$ for any plaintext P is equal to the apriori probability that P is the plaintext

In other words: *the ciphertext does not reveal any information on the plaintext*

$$\Pr[\text{plaintext} = P \mid \text{ciphertext} = C] = \Pr[\text{plaintext} = P]$$

in short:

$$\Pr[P|C] = \Pr[P]$$

Probabilities are over the key space and the plaintext space

Conditional probabilities

$$\Pr[P|C] = \Pr[P \wedge C] / \Pr[C]$$

(def. of cond. pr.)

$$\Pr[P|C] * \Pr[C] = \Pr[C|P] * \Pr[P]$$

(Th. Bayes)

In a perfect cipher

$$\Pr[P|C] = \Pr[P]$$

by replacing into Bayes

$$\Pr[P] * \Pr[C] = \Pr[C|P] * \Pr[P]$$

$$\Pr[C] = \Pr[C | P]$$

One-time pad (OTP)

AKA Vernam Cipher,
invented in 1917 and
patented in 1919
while *Gilbert Vernam*
was working at AT&T

Plaintext space:
 $\{0,1\}^n$

Keystream space:
 $\{0,1\}^n$

The scheme is
symmetric;
*keystream K is
chosen at random*

$$E_K(P) = C = P \oplus K$$

$$D_K(C) = C \oplus K = \\ P \oplus K \oplus K = P$$

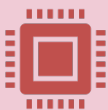
Features of OTP



Claim: one-time pad is a perfect cipher. [given a k bit cipher text every k -bit plain text has got same probability if key is random]



Problem: size of keystream space, as show by the following



Theorem (Shannon): A cipher cannot be perfect if the size of its key space is less than the size of its message space

Proof of Shannon's theorem

By contradiction

Assume $\#keys(l) < \#messages(n)$ and consider ciphertext C_0 s.t. $\Pr[C_0] > 0$ (C_0 must exist!)

For some key K , consider $P = D_K(C_0)$. There exist at most l ($\#keys$) such messages (one per each key)

Choose message P_0 s.t. it is not of the form $D_K(C_0)$ (there exist $n-l$ such messages)

Hence $\Pr[C_0|P_0] = 0$

But in a perfect cipher $\Pr[C_0|P_0] = \Pr[C_0] > 0$.
Contradiction

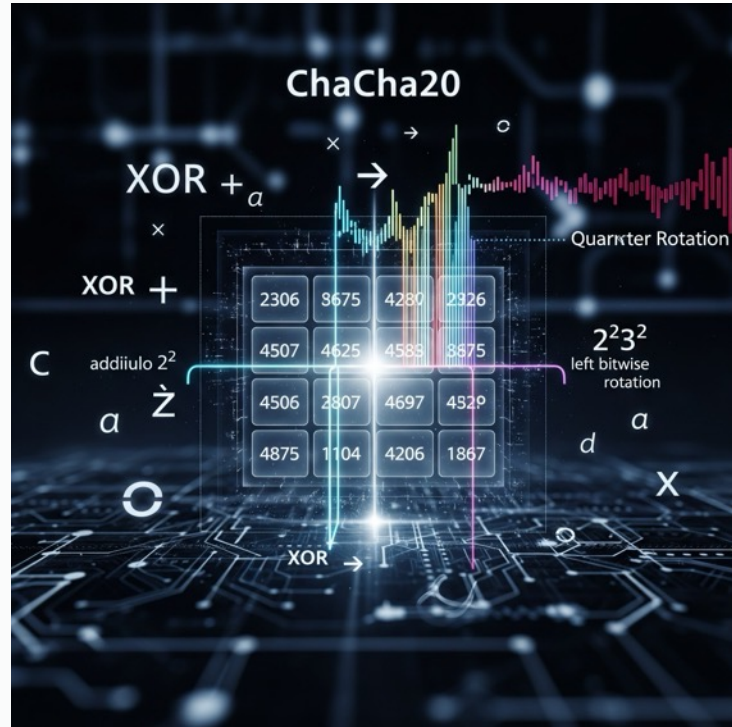
Consequences

- OTP is perfect if
 - keystream truly random
 - keystream space not less message space
- if seed (key) is reused we get same keystream K for two different encryptions. Heavy consequences
 - $C1 = P1 \oplus K, C2 = P2 \oplus K$
 - Assume pair plaintext, ciphertext $(P1, C1)$ known (KPA)
 - Attacker computes $C1 \oplus C2 = P1 \oplus K \oplus P2 \oplus K$
 - \oplus commutative and associative, so: $C1 \oplus C2 = P1 \oplus P2 \oplus K \oplus K = P1 \oplus P2$ (by properties of \oplus)
 - $P1 \oplus P2 \oplus P1$ (known) = $P2$ (Success!)

Conclusion

- OTP is not obsolete
- it needs a truly random long keystream
 - PRNG not enough
- not to be reused
- This makes OTP unpractical
- Otherwise... OTP is theoretically unbreakable (the only with proved perfect security)

ChaCha20



ChaCha20, a synchronous stream cipher

Objectives

- Understand the design and purpose of ChaCha20
- Compare it to older stream cipher models
- Learn how ChaCha20 builds on the one-time pad concept

Background & history

- Designed in 2008 by Daniel J. Bernstein as an improvement of Salsa20
- Standardized in RFC 8439 by the IETF
- Focus: high speed, simplicity, and resistance to timing attacks
- Adopted in security-critical applications like TLS 1.3, OpenSSH, WireGuard, Signal, etc.

Stream ciphers recap

- Stream ciphers generate a keystream and encrypt data by XORing it with plaintext
- Fast, low-latency encryption ideal for real-time applications
- Example: the One-Time Pad — perfectly secure but impractical

From OTP to ChaCha20

- ChaCha20 mimics the One-Time Pad by generating a pseudo-random keystream
- Key idea: instead of a long random keystream, we use a small key + counter + nonce (random number to be used once) to generate keystream blocks
- XOR remains the central operation, just like OTP

Inputs to ChaCha20

- **256-bit key**: shared secret
- **96-bit nonce**: unique per message/session
- **32-bit block counter**: changes per block to ensure keystream uniqueness
 - a block is a chunk of 512 bits of plaintext
- These inputs determine the internal state that drives the keystream

Block structure

- 512-bit state divided into 16 32-bit words
 - 384 bits are variable and 128 are coming from constants
- Layout
 - 4 constant words
 - 8 key words
 - 1 counter word
 - 3 nonce words
- This state is transformed to produce 64-byte keystream blocks

Quarter-round function

- Core operation: processes 4 words (from state) with **Add, Rotate, XOR (ARX)**
- Lightweight and fast on all CPUs
- Provides diffusion and non-linearity
- Designed for simplicity and timing safety

10 Double-rounds and output

- ChaCha20 performs 20 operations, organized as 10 double-rounds
- Each double-round consists of
 - 1 column-wise operation: applies 4 Quarter-Round functions to the columns of the 4×4 word matrix
 - 1 diagonal-wise operation: applies 4 Quarter-Round functions to the diagonals of the matrix
- 1 double-round = 8 Quarter-Round functions
- These transformations ensure that all 16 words of the state are thoroughly mixed in a defined pattern
- After all 10 double-rounds: add the final state to the original state (mod 2^{32}) to get 64 bytes of keystream

Encryption with XOR

- **ciphertext = plaintext \oplus keystream**
- Same operation used for decryption: **plaintext = ciphertext \oplus keystream**
- Stateless per block: no chaining between blocks required

Security goals of ChaCha20

- Designed to resist
 - Key recovery
 - Keystream prediction
 - Timing attacks
- No known practical attacks on full 10 double-round version
- High performance across platforms, even without hardware support

Real-world usage

- TLS 1.3: used as an option (in addition to others) for secure web traffic
- Signal, WhatsApp: encrypt messages using ChaCha20 (or other, depending on context)
- WireGuard VPN: lightweight and fast encryption
- OpenSSH: option for encrypted shell sessions, now less used