

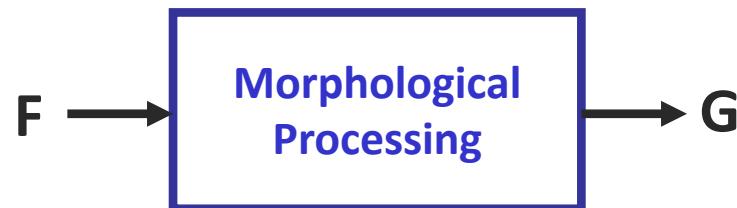
Digital Image Processing

Lecture #4
Ming-Sui (Amy) Lee

Morphological Image Processing

Morphological Processing

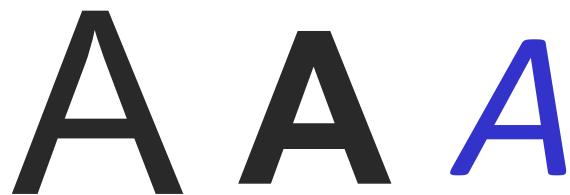
- Morphology
 - Morpho-: shape/form/structure
 - -ology: study
- Morphological image processing
 - Post-processing
 - Binary images → gray-level image



Morphological Processing

■ For some applications

- Structures of objects composed by lines or arcs
- Care about the pattern connectivity
- Independent of width



Hand-written characters



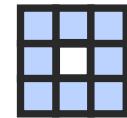
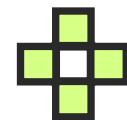
Fingerprint patterns

Morphological Processing

■ Binary image connectivity

○ Pixel bond

- Specify the connectivity of a pixel with its neighbors
- Four-connected neighbor → bond = 2
- Eight-connected neighbor → bond = 1



○ Minimally connected

- Elimination of any black (object) pixel (except boundary pixels) results in disconnection of the remaining black (object) pixels

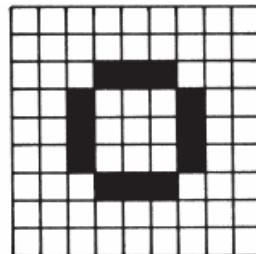
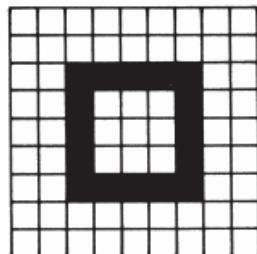
Morphological Processing

■ Binary image connectivity

○ Example

0 0 0	0 0 0	0 0 0	0 0 0	0 1 1
0 1 1	0 1 1	0 1 0	0 1 1	1 1 1
0 1 0	0 0 1	0 0 0	0 1 1	1 1 1
Four-connected	Eight-connected	Isolated	Corner	Interior
$B = 4$	$B = 3$	$B = 0$	$B = 5$	$B = 11$
0 0 0	1 0 0	1 1 1	0 1 1	
0 1 0	1 1 1	0 1 0	0 1 1	
0 0 1	1 0 1	1 1 1	0 1 1	
Spur	Bridge	H-connected	Exterior	
$B = 1$	$B = 7$	$B = 8$	$B = 8$	

○ Another example



Morphological Processing

- Binary hit or miss transformations
 - Select a $n \times n$ hit pattern (odd-sized mask)
 - Compare with a $n \times n$ image window
 - Match \rightarrow hit \rightarrow change the central pixel value
 - Otherwise \rightarrow miss \rightarrow do nothing
 - Example
 - To clean the isolated binary noise

0 0 0

0 1 0 Hit or miss?

0 0 0

Morphological Processing

■ Binary hit or miss transformations

- $0 \rightarrow \text{background}$ 0 0 0
- $1 \rightarrow \text{object (black)}$ 0 1 0 Hit or miss?
- 0 0 0

○ Logical expression

$$\begin{bmatrix} X_3 & X_2 & X_1 \\ X_4 & X & X_0 \\ X_5 & X_6 & X_7 \end{bmatrix}$$

$$G(j,k) = X \cap (X_0 \cup X_1 \cup \dots \cup X_7)$$

■ Example

- If $G(j,k) = X \cap 1 \rightarrow \text{do nothing}$
- If $G(j,k) = X \cap 0$
 - If $X=0 \rightarrow G(j,k)=0 \rightarrow \text{do nothing}$
 - If $X=1 \rightarrow \text{hit} \rightarrow G(j,k)=0$

Morphological Processing

■ Binary hit or miss transformations

$$G(j,k) = X \cap (X_0 \cup X_1 \cup \dots \cup X_7)$$

$\Rightarrow 2^9$ possible mask patterns

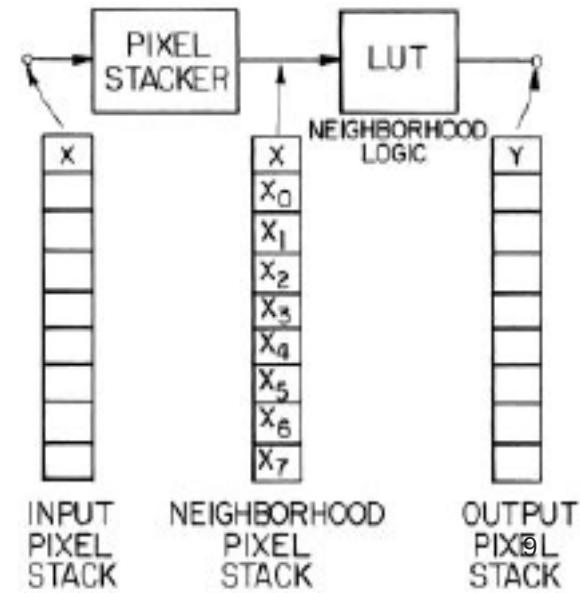
○ Implementation

■ Pixel stack

- Treat the 8 neighboring pixels as a “byte”

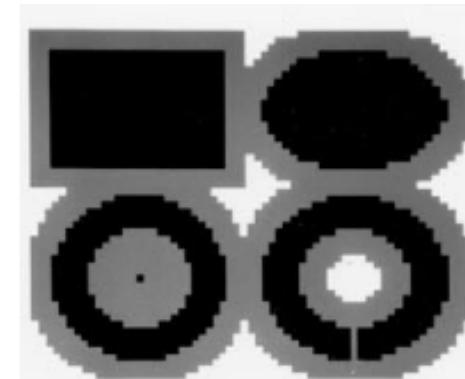
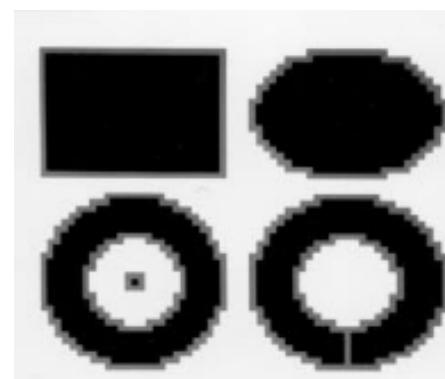
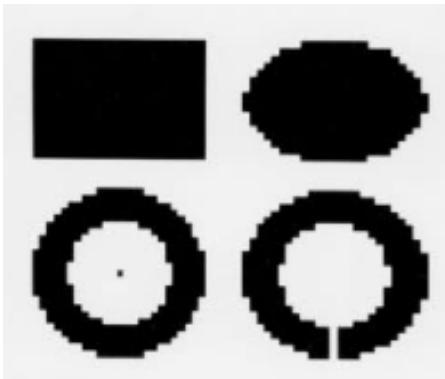
$$\begin{bmatrix} X_3 & X_2 & X_1 \\ X_4 & X & X_0 \\ X_5 & X_6 & X_7 \end{bmatrix} \otimes \begin{bmatrix} 2^{-4} & 2^{-3} & 2^{-2} \\ 2^{-5} & 2^0 & 2^{-1} \\ 2^{-6} & 2^{-7} & 2^{-8} \end{bmatrix}$$

■ Look-Up-Table (LUT)



Morphological Processing

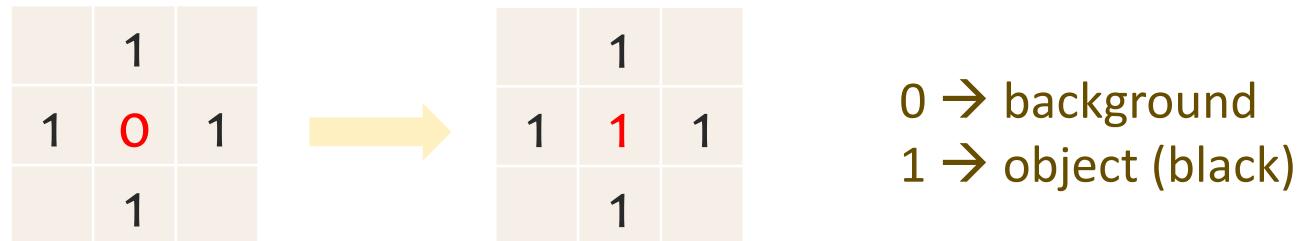
- Simple morphological processing based on binary hit or miss rules
 - Additive operators ($0 \rightarrow 1$)
 - Interior fill
 - Diagonal fill
 - Bridge
 - 8-neighbor dilate



Morphological Processing

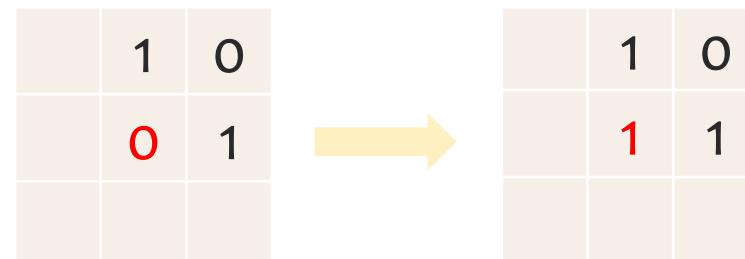
○ Interior fill

- Create a black pixel if all four-connected neighbor pixels are black



○ Diagonal fill

- Create a black pixel if creation eliminates the eight-connectivity of the background



Morphological Processing

Bridge

- Create a black pixel if creation results in connectivity of previously unconnected neighboring black pixels

1	0	0
0	0	1
0	0	0



1	0	0
0	1	1
0	0	0

0 → background
1 → object (black)

8-neighbor dilate

- Create a black pixel if at least one eight-connected neighbor pixel is black

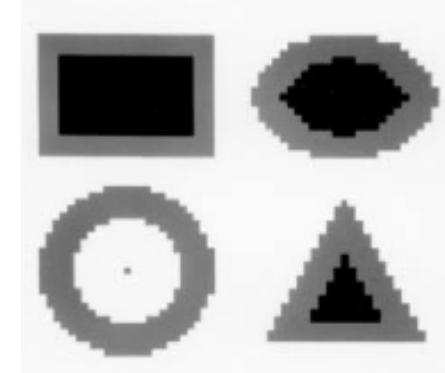
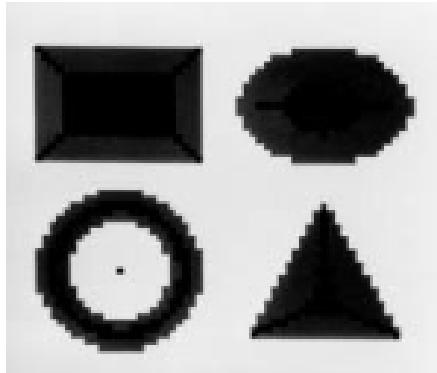
0	0	0
0	0	0
1	0	0



0	0	0
0	1	0
1	0	0

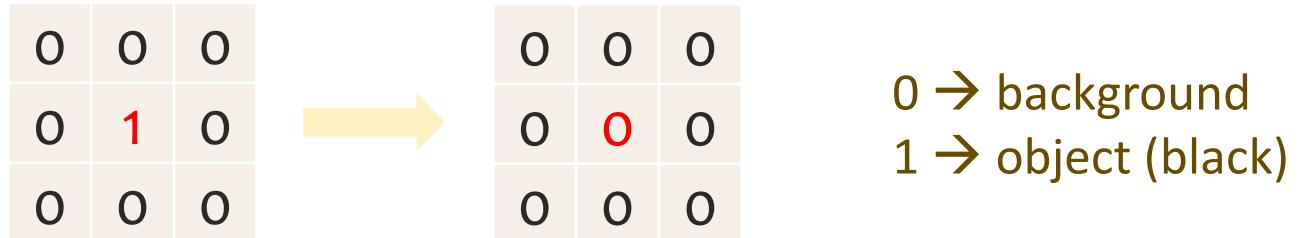
Morphological Processing

- Simple morphological processing based on binary hit or miss rules
 - Subtractive operators ($1 \rightarrow 0$)
 - Isolated pixel removal
 - Spur removal
 - Interior pixel removal
 - H-break / Eight-neighbor erode



Morphological Processing

- Isolated pixel removal
 - Erase a black pixel with eight white neighbors



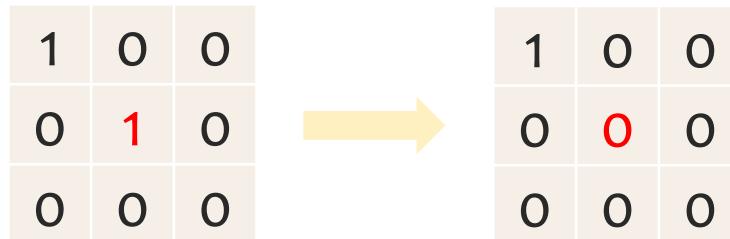
0	0	0
0	1	0
0	0	0

→

0	0	0
0	0	0
0	0	0

0 → background
1 → object (black)

- Spur removal
 - Erase a black pixel with a single eight-connected neighbor



1	0	0
0	1	0
0	0	0

→

1	0	0
0	0	0
0	0	0

Morphological Processing

○ Interior pixel removal

- Erase a black pixel if all four-connected neighbors are black

0 → background
1 → object (black)

	1	
1	1	1
	1	

→

0	1	0
1	0	1
0	1	0

○ H-break

- Erase a black pixel that is H-connected

1	1	1
0	1	0
1	1	1

→

1	1	1
0	0	0
1	1	1

Morphological Processing

- Eight-neighbor erode

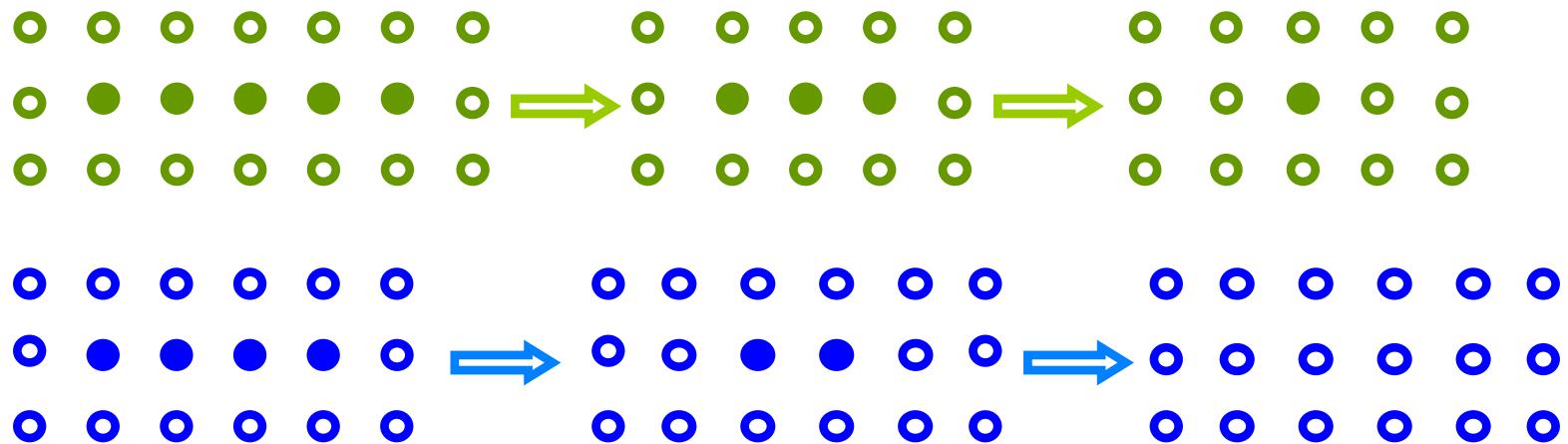
- Erase a black pixel if at least one eight-connected neighbor pixel is white



[Morphological Processing]

■ Example

○ Subtractive operator



- doesn't prevent total erasure and ensure connectivity
- In this case, only a 3x3 window does not sufficient to tell whether the final stage of iteration is reached or not

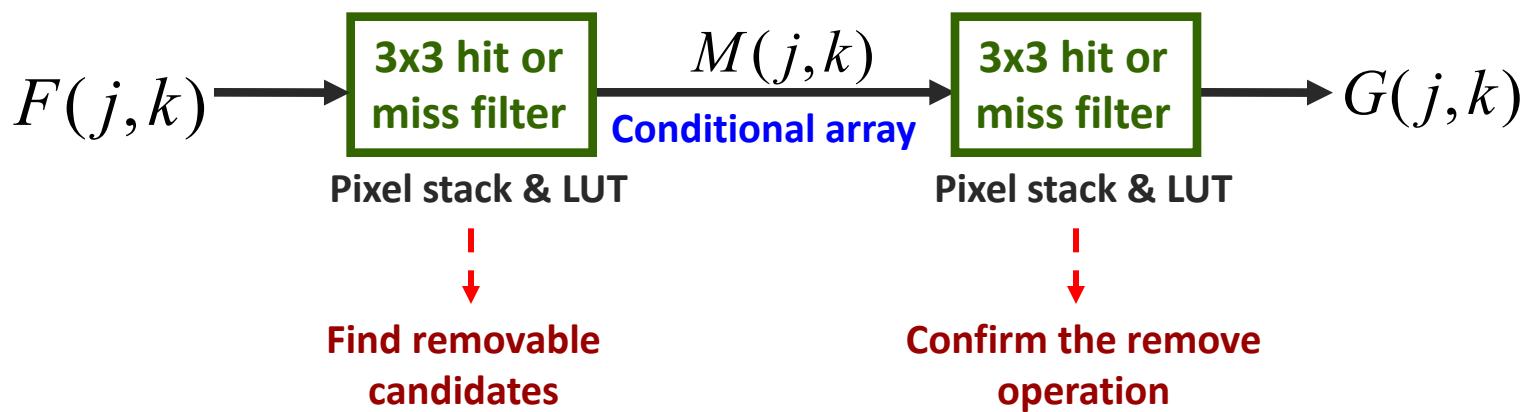
Morphological Processing

■ Solutions

- Approach I
 - Apply a filter with larger size
 - “fairly complicated patterns”, “many combinations”
- Approach II
 - Consider a structural (composite) design with 3x3 filters: two-stage approach
 - Application dependent
 - Thinning, shrinking, skeletonizing
 - Share the same structure but vary in some modular details

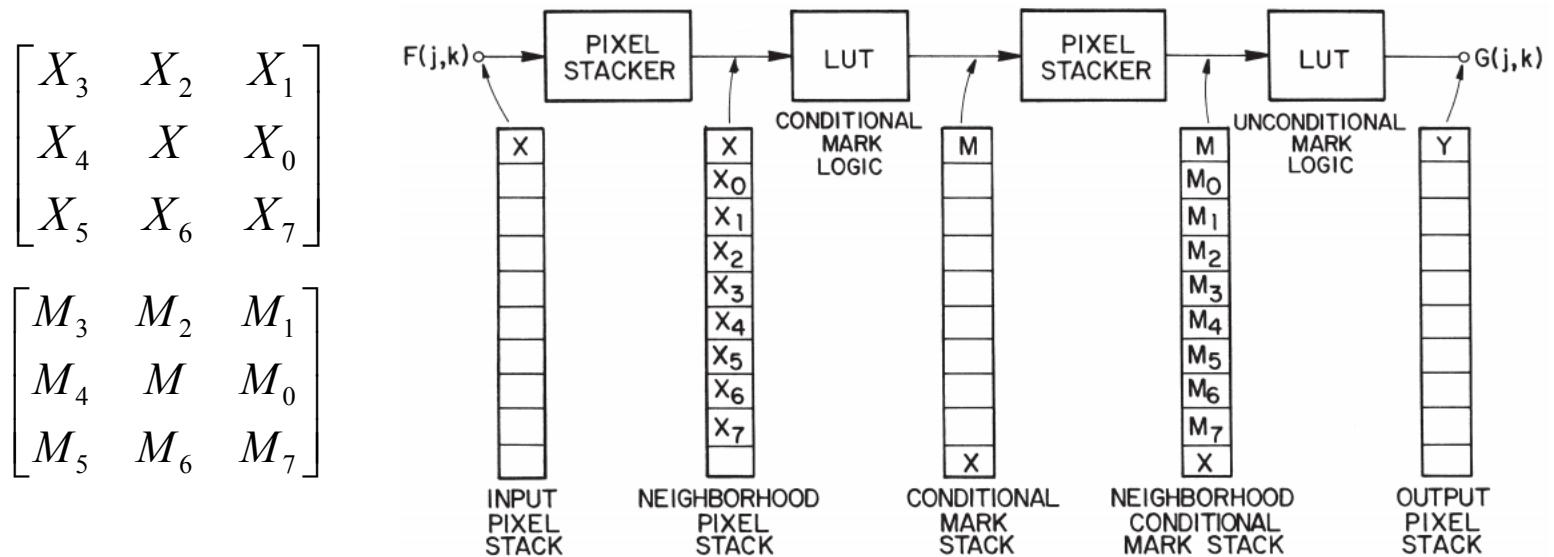
Morphological Processing

- Advanced morphological processing
 - Shrinking/Thinning/Skeletonizing
 - Conditional erosion
 - Prevent total erasure & Ensure connectivity



Morphological Processing

- Advanced morphological processing
 - Shrinking/Thinning/Skeletonizing
 - Conditional erosion
 - Prevent total erasure & Ensure connectivity



Morphological Processing

■ Shrinking/Thinning/Skeletonizing

- Stage I
 - Generate a binary image $M(j,k)$ called the conditional array (or mask)
 - If $M(j,k)=1$, it means (j,k) is a candidate for erasure
 - If $M(j,k)=0$, it means no further operation is needed on (j,k)
- Stage II
 - Based on the center pixel, X , and $M(j,k)$ pattern, we decide whether to erase X or not in the output $G(j,k)$
 - If there's a hit → do nothing
 - If there's a miss → erase the center pixel

Morphological Processing

■ Stage I → Part of Table 14.3-1

TABLE 14.3-1. Shrink, Thin and Skeletonize Conditional Mark Patterns [$M = 1$ if hit]

		Table	Bond					Pattern	
				0	0	1	1	0	0
S	1	1	0	1	0	0	1	0	0
		0	0	0	0	0	0	1	0
S	2	0	0	0	0	1	0	0	0
		0	1	1	0	1	1	0	0
S	3	0	0	0	0	0	0	0	0
		0	1	1	0	1	1	0	0
TK	4	0	0	1	0	1	1	0	1
		0	1	1	1	0	1	1	0
STK	4	0	0	0	0	0	1	0	0
		0	1	1	0	1	1	0	1
				0	0	1	1	1	1
				0	0	0	0	0	1

Table: Shrink (S), Thin (T), Skeletonize (K)

Bond: classification, narrow down the search space

Pattern: coded as an 8-bit symbol for a filter

$$\begin{bmatrix} X_3 & X_2 & X_1 \\ X_4 & X & X_0 \\ X_5 & X_6 & X_7 \end{bmatrix} \otimes \begin{bmatrix} 2^{-4} & 2^{-3} & 2^{-2} \\ 2^{-5} & 2^0 & 2^{-1} \\ 2^{-6} & 2^{-7} & 2^{-8} \end{bmatrix}$$

Morphological Processing

- Stage II → Part of Table 14.3-2

TABLE 14.3-2. Shrink and Thin Unconditional Mark Patterns
 $[P(M, M_0, M_1, M_2, M_3, M_4, M_5, M_6, M_7) = 1 \text{ if hit}]^a$

Pattern									
Spur	Single 4-connection								
0 0 M	M 0 0	0 0 0	0 0 0						
0 M 0	0 M 0	0 M 0	0 M M						
0 0 0	0 0 0	0 M 0	0 0 0						
$G(j, k) = X \cap [\overline{M} \cup P(M, M_1, \dots, M_7)]$ where $P(M, M_1, \dots, M_7)$ is an erasure inhibiting logical variable									
L Cluster									
0 0 M	0 M M	M M 0	M 0 0	0 0 0	0 0 0	0 0 0	0 0 0	0 0 0	
0 M M	0 M 0	0 M 0	M M 0	M M 0	0 M 0	0 M 0	0 M M		
0 0 0	0 0 0	0 0 0	0 0 0	M 0 0	M M 0	0 M M	0 0 M		
$\begin{bmatrix} M_3 & M_2 & M_1 \\ M_4 & M & M_0 \\ M_5 & M_6 & M_7 \end{bmatrix} \otimes \begin{bmatrix} 2^{-4} & 2^{-3} & 2^{-2} \\ 2^{-5} & 2^0 & 2^{-1} \\ 2^{-6} & 2^{-7} & 2^{-8} \end{bmatrix}$									
4-Connected offset									
0 M M	M M 0	0 M 0	0 0 M						
M M 0	0 M M	0 M M	0 M M						
0 0 0	0 0 0	0 0 M	0 M 0						

Morphological Processing

■ Stage II → Part of Table 14.3-2 (cont'd)

Spur corner cluster

0 A M MB 0 0 0 M M0 0
0 MB A M0 A M0 0 MB
M0 0 0 0 M MB 0 0 A M

Corner cluster

MMD
MMD
DDD

Tee branch

D M0 0 MD 0 0 D D 0 0 DMD 0 M0 0 M0 DMD
MMM MMM MMM MMM MM0 MM0 0 MM 0 MM
D 0 0 0 0 D 0 MD DM0 0 M0 DMD DMD 0 M0

$$A \cup B \cup C = 1, \quad D = 0 \cup 1, \quad A \cup B = 1$$

Morphological Processing

- Stage II → Part of Table 14.3-3

TABLE 14.3-3. Skeletonize Unconditional Mark Patterns

$[P(M, M_0, M_1, M_2, M_3, M_4, M_5, M_6, M_7) = 1 \text{ if hit}]^a \quad A \cup B \cup C = 1, \quad D = 0 \cup 1$

Pattern											
Spur											
0	0	0	0	0	0	0	0	<i>M</i>	<i>M</i>	0	0
0	<i>M</i>	0	0	<i>M</i>	0	0	<i>M</i>	0	0	<i>M</i>	0
0	0	<i>M</i>	<i>M</i>	0	0	0	0	0	0	0	0
Single 4-connection											
0	0	0	0	0	0	0	0	0	0	<i>M</i>	0
0	<i>M</i>	0	0	<i>M</i>	<i>M</i>	<i>M</i>	<i>M</i>	0	0	<i>M</i>	0
0	<i>M</i>	0	0	0	0	0	0	0	0	0	0
L corner											
0	<i>M</i>	0	0	<i>M</i>	0	0	0	0	0	0	0
0	<i>M</i>	<i>M</i>	<i>M</i>	<i>M</i>	0	0	<i>M</i>	<i>M</i>	<i>M</i>	<i>M</i>	0
0	0	0	0	0	0	0	<i>M</i>	0	0	<i>M</i>	0

[Morphological Processing]

■ Example - shrinking

$$\begin{matrix} 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \end{matrix}$$

$$F(j,k)$$

$$\begin{matrix} 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & M & M & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \end{matrix}$$

$$M(j,k)$$

$$\begin{matrix} 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & P & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \end{matrix}$$

$$P(j,k)$$

$$\begin{matrix} 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \end{matrix}$$

$$G(j,k)$$

[Morphological Processing]

■ Example - shrinking

$$\begin{matrix} 0 & 0 & 0 & 0 \\ 0 & 1 & 1 & 0 \\ 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 0 \end{matrix}$$

$$F(j,k)$$

$$M(j,k)$$

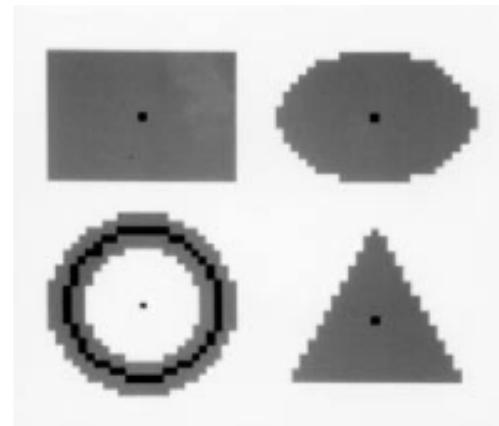
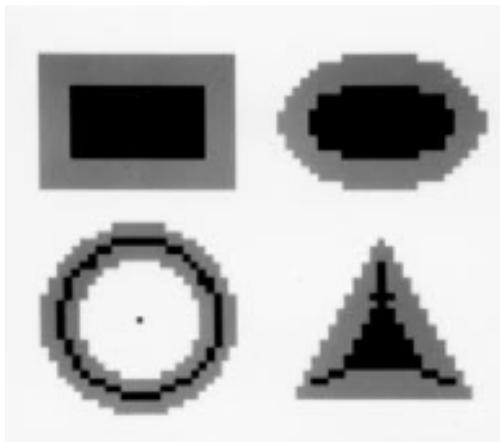
$$P(j,k)$$

$$G(j,k)$$

Morphological Processing

■ Shrinking

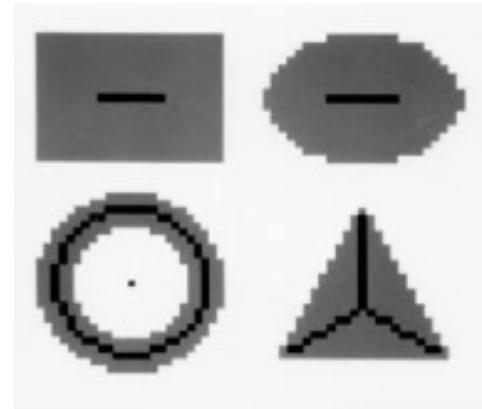
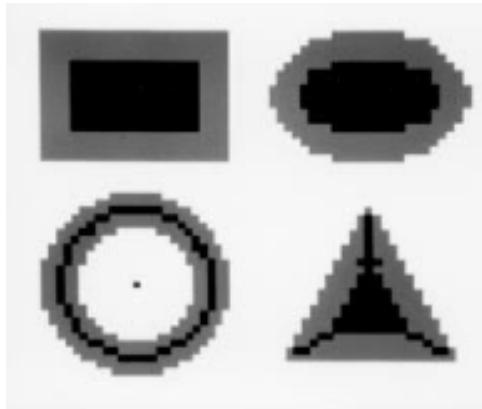
- Erase black pixels such that an object without holes erodes to a single pixel at or near its center of mass, and an object with holes erodes to a connected ring lying midway between each hole and its nearest outer boundary



Morphological Processing

■ Thinning

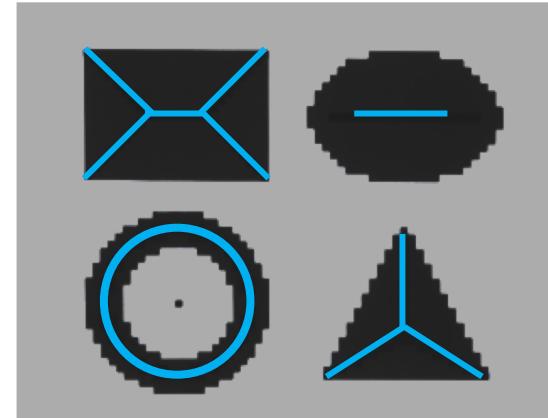
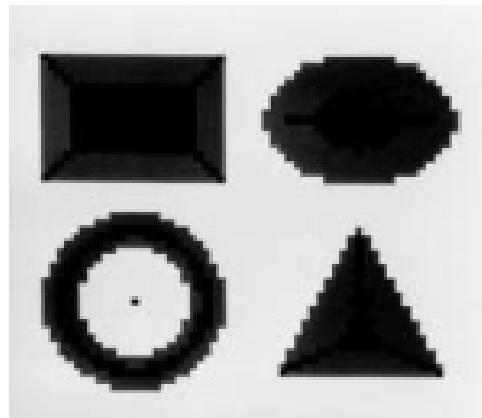
- Erase black pixels such that an object without holes erodes to a **minimally connected stroke** located **equidistant from its nearest outer boundaries**, and an object with holes erodes to a minimally connected ring midway between each hole and its nearest outer boundary



Morphological Processing

Skeletonizing

- The medial axis skeleton consists of the set of points that are **equally distant** from **two closest** points of an object boundary



Morphological Processing

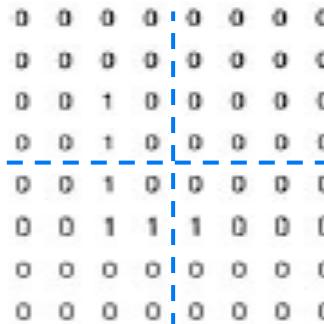
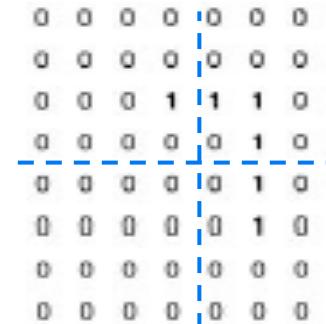
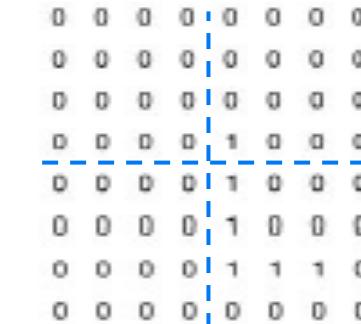
Algebraic operations on binary arrays

0 0 0 0 0 0	0 0 0 0 0 0	1 1 1 1 1 1			
0 0 1 1 0 0	0 0 0 0 0 0	1 1 0 0 1 1			
0 0 1 1 0 0	0 1 1 1 1 0	1 1 0 0 1 1			
0 0 1 1 0 0	0 1 1 1 1 0	1 1 0 0 1 1			
0 0 1 1 0 0	0 0 0 0 0 0	1 1 0 0 1 1			
0 0 0 0 0 0	0 0 0 0 0 0	1 1 1 1 1 1			
A		B		\bar{A}	
complement					
0 0 0 0 0 0	0 0 0 0 0 0	0 0 0 0 0 0			
0 0 1 1 0 0	0 0 0 0 0 0	0 0 1 1 0 0			
0 1 1 1 1 0	0 0 1 1 0 0	0 1 0 0 1 0			
0 1 1 1 1 0	0 0 1 1 0 0	0 1 0 0 1 0			
0 0 1 1 0 0	0 0 0 0 0 0	0 0 1 1 0 0			
0 0 0 0 0 0	0 0 0 0 0 0	0 0 0 0 0 0			
$A \cup B$		$A \cap B$		$A \text{XOR } B$	
union		intersection		exclusive-OR	
OR		AND		XOR	

Morphological Processing

■ Generalized dilation and erosion

- Reflection and translation of a binary image

$F(j,k)$	$\tilde{F}(j,k)$	$T_{1,2}\{F(j,k)\}$
		

- Dilation

$$G(j,k) = F(j,k) \oplus \underline{H(j,k)}$$

Structuring element

- Erosion

$$G(j,k) = F(j,k) \ominus H(j,k)$$

Morphological Processing

Dilation $G(j,k) = F(j,k) \oplus H(j,k)$

- Can be implemented in several ways
- Minkowski addition definition

$$\begin{array}{cccccc}
 0 & 0 & 0 & 0 & 0 & 0 \\
 0 & 0 & 1 & 0 & 0 & 0 \\
 0 & 1 & 1 & 0 & 0 & 0 \\
 0 & 0 & 1 & 1 & 0 & 0 \\
 0 & 0 & 0 & 0 & 0 & 0
 \end{array}
 \quad
 \begin{array}{cccccc}
 1 & 1 & 0 & & & \\
 1 & 1 & 0 & & & \\
 1 & 0 & 0 & & & \\
 & & & & & \\
 & & & & &
 \end{array}$$

$$G(j,k) = \bigcup_{(r,c) \in H} T_{r,c} \{F(j,k)\}$$

$$G(j,k) = T_{0,0} \{F(j,k)\} \cup T_{0,1} \{F(j,k)\} \cup T_{1,0} \{F(j,k)\}$$

$$\cup T_{1,1} \{F(j,k)\} \cup T_{2,0} \{F(j,k)\}$$

0 0 0 0 0	· 0 0 0 0 0	· · · · ·	· · · · ·	· · · · ·	0 0 0 0 0 0 0
0 0 1 0 0	· 0 0 1 0 0	0 0 0 0 0	· 0 0 0 0 0	· · · · ·	0 0 1 1 0 0 0
0 1 1 0 0	· 0 1 1 0 0	0 0 1 0 0	· 0 0 1 0 0	0 0 0 0 0	0 1 1 1 0 0 0
0 0 1 1 0	· 0 0 1 1 0	0 1 1 0 0	· 0 1 1 0 0	0 0 1 0 0	0 1 1 1 1 0 0
0 0 0 0 0	· 0 0 0 0 0	0 0 1 1 0	· 0 0 1 1 0	0 1 1 0 0	0 1 1 1 1 0 0
		0 0 0 0 0	· 0 0 0 0 0	0 0 1 1 0	0 0 1 1 0 0 0
				0 0 0 0 0	0 0 0 0 0 0 0
$T_{0,0}\{F(j,k)\}$	$T_{0,1}\{F(j,k)\}$	$T_{1,0}\{F(j,k)\}$	$T_{1,1}\{F(j,k)\}$	$T_{2,0}\{F(j,k)\}$	$G(j,k)$



Morphological Processing

■ Erosion $G(j,k) = F(j,k) \Theta H(j,k)$

- Can be implemented in several ways
- Dual relationship of Minkowski addition

$$G(j,k) = \bigcap_{(r,c) \in H} \bigcap T_{r,c} \{F(j,k)\}$$

//Sternberg definition//

$$G(j,k) = \bigcap \bigcap_{(r,c) \in H} T_{r,c} \{F(j,k)\}$$

$$\begin{matrix} 1 & 1 & 1 & 1 & 1 \end{matrix}$$

$$\begin{matrix} 1 & 1 & 1 & 1 & 1 & 1 & 1 & 0 & 0 & 0 \end{matrix}$$

$$\begin{matrix} 1 & 1 & 0 & 0 & 0 & 0 \end{matrix} \ominus \begin{matrix} 1 & 0 & 0 \end{matrix} = \begin{matrix} 1 & 1 & 0 \end{matrix}$$

$$\begin{matrix} 1 & 1 & 1 & 1 & 1 & 1 & 1 & 0 & 0 & 0 \end{matrix}$$

$$\begin{matrix} 1 & 1 & 1 & 1 & 1 & 1 \end{matrix}$$

$$F(j,k)$$

$$H(j,k)$$

$$G(j,k)$$

//Serra definition//

$$G(j,k) = \bigcap \bigcap_{(r,c) \in \tilde{H}} T_{r,c} \{F(j,k)\}$$

$$\begin{matrix} 1 & 1 & 1 & 1 & 1 \end{matrix}$$

$$\begin{matrix} 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 0 & 0 & 0 \end{matrix}$$

$$\begin{matrix} 1 & 1 & 0 & 0 & 0 \end{matrix} \ominus \begin{matrix} 1 & 0 & 0 \end{matrix} = \begin{matrix} 0 & 0 & 0 \end{matrix}$$

$$\begin{matrix} 1 & 1 & 1 & 1 & 1 & 1 & 1 & 1 & 0 & 0 & 0 \end{matrix}$$

$$\begin{matrix} 1 & 1 & 1 & 1 & 1 \end{matrix}$$

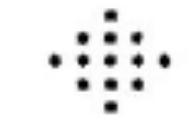
$$F(j,k)$$

$$H(j,k)$$

$$G(j,k)$$

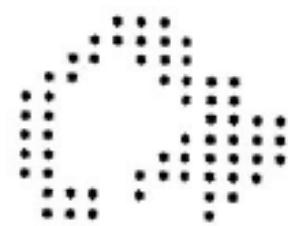
Morphological Processing

■ Example



Structuring
element

original



Dilation



original



Erosion



Morphological Processing

■ Example

Historically, certain computer programs were written using only two digits rather than four to define the applicable year. Accordingly, the company's software may recognize a date using "00" as 1900 rather than the year 2000.



Structuring element

0	1	0
1	1	1
0	1	0

Historically, certain computer programs were written using only two digits rather than four to define the applicable year. Accordingly, the company's software may recognize a date using "00" as 1900 rather than the year 2000.



Morphological Processing

■ Example

Original fingerprint



Skeletonized fingerprint



The original fingerprint contains ridges with width of several pixels.
The skeletonized fingerprint contains ridges only a single pixel wide.

[Morphological Processing]

■ Applications

- **Boundary Extraction**
 - Extract the boundary (or outline) of an object
- **Hole Filling**
 - Given a pixel inside a boundary, hole filling attempts to fill that boundary with object pixels
- **Connected Component Labeling**
 - Scan an image and groups its pixels into components based on pixel connectivity

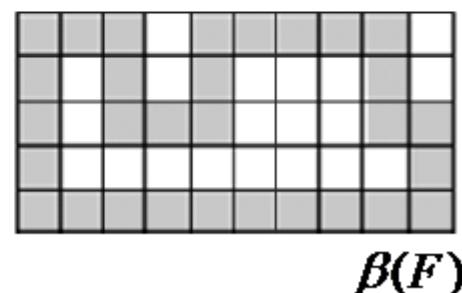
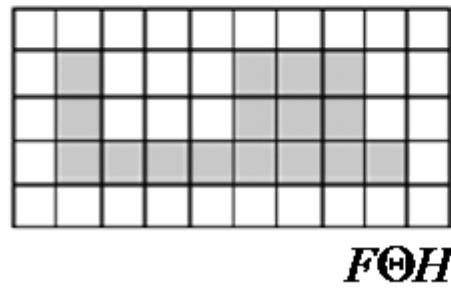
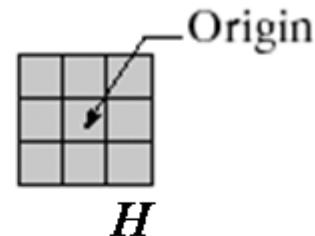
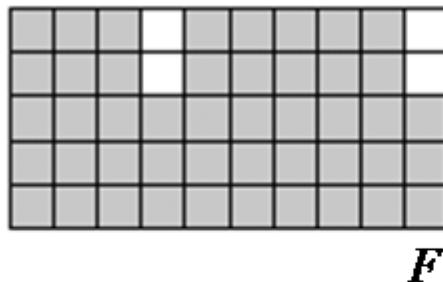
[

Morphological Processing

]

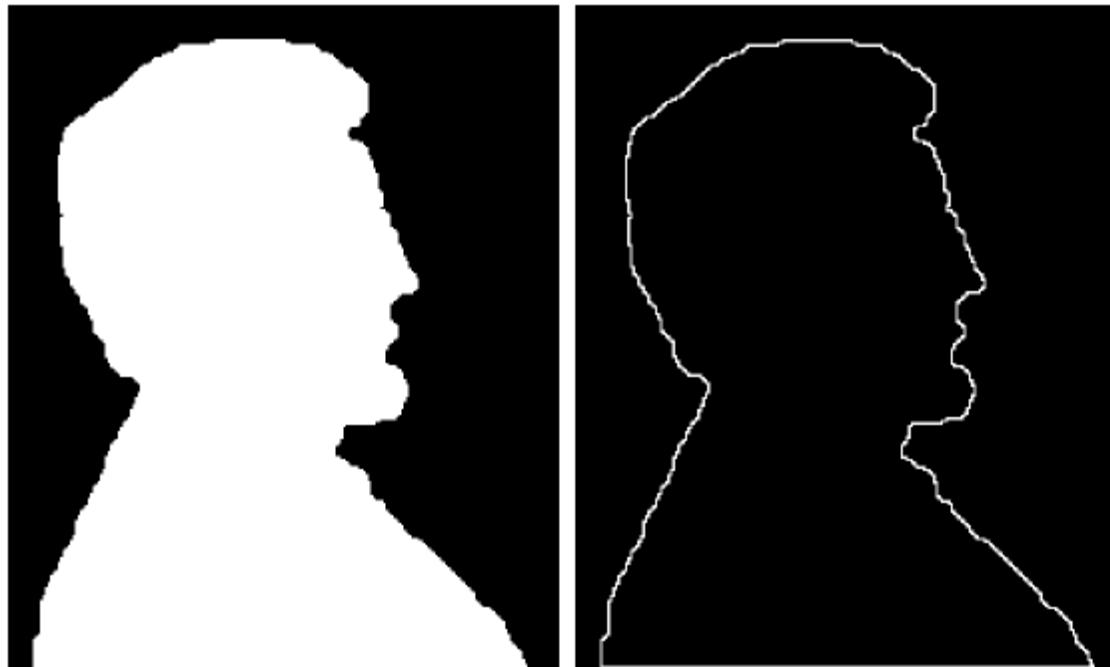
■ Boundary Extraction

$$\beta(F(j,k)) = F(j,k) - (F(j,k) \Theta H(j,k))$$



Morphological Processing

■ Example



Original Image

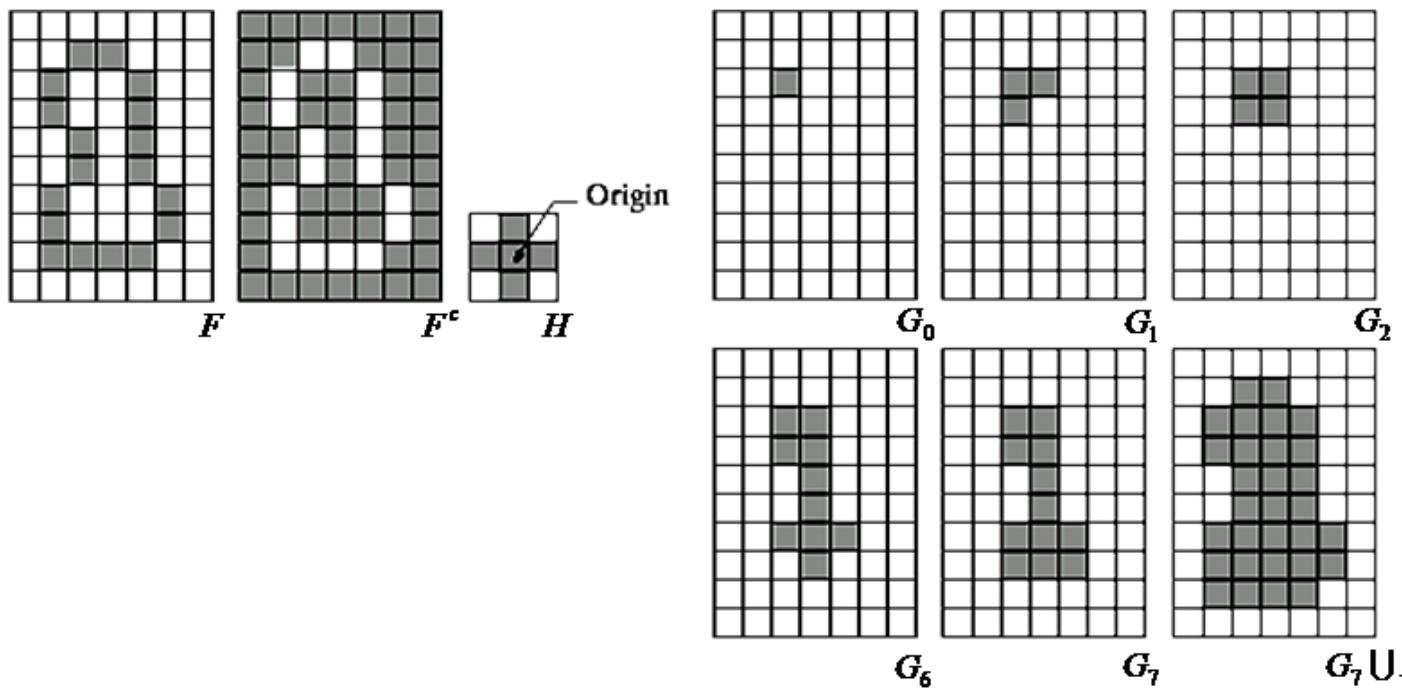
Extracted Boundary

Morphological Processing

Hole Filling

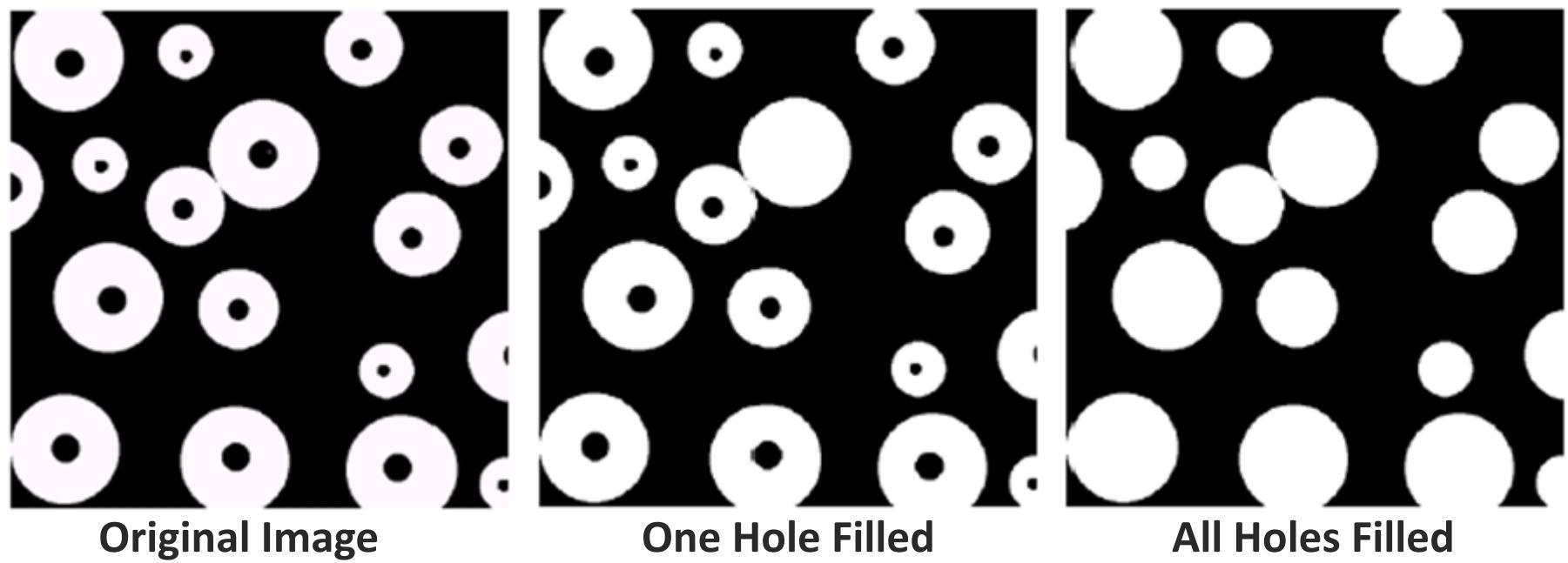
$$G_i(j,k) = (G_{i-1}(j,k) \oplus H(j,k)) \cap F^c(j,k) \quad i=1,2,3\dots$$

$$G(j,k) = G_i(j,k) \cup F(j,k)$$



Morphological Processing

■ Example

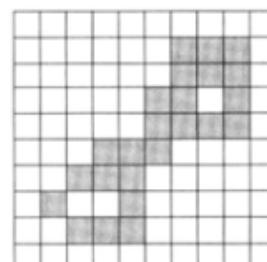


Morphological Processing

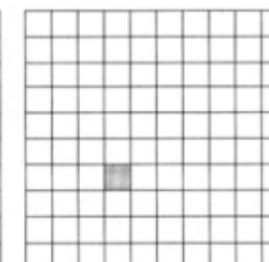
Connected Component Labeling

$$G_i(j,k) = (G_{i-1}(j,k) \oplus H(j,k)) \cap F(j,k) \quad i=1,2,3,\dots$$

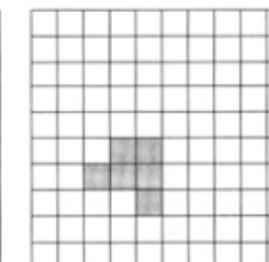
Structuring element based on 8-connectivity 



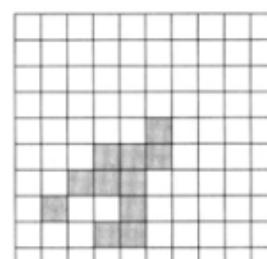
F



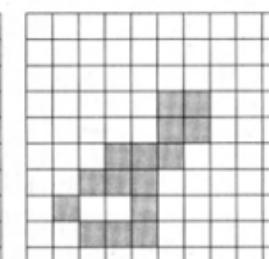
G_0



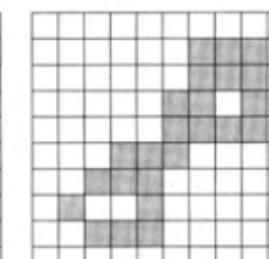
G_1



G_2



G_3



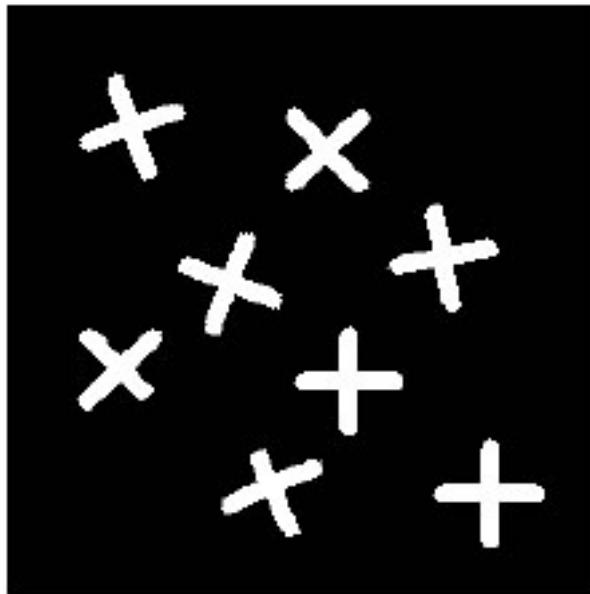
G_6

[

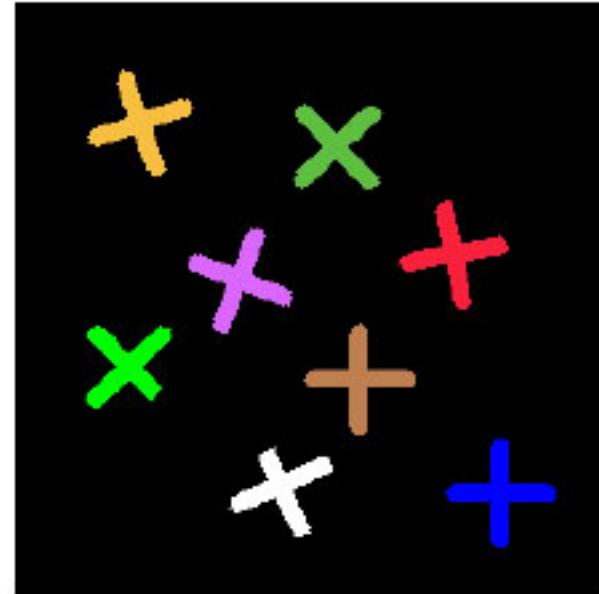
Morphological Processing

]

- Example



Original Image



Labelled Components

Morphological Processing

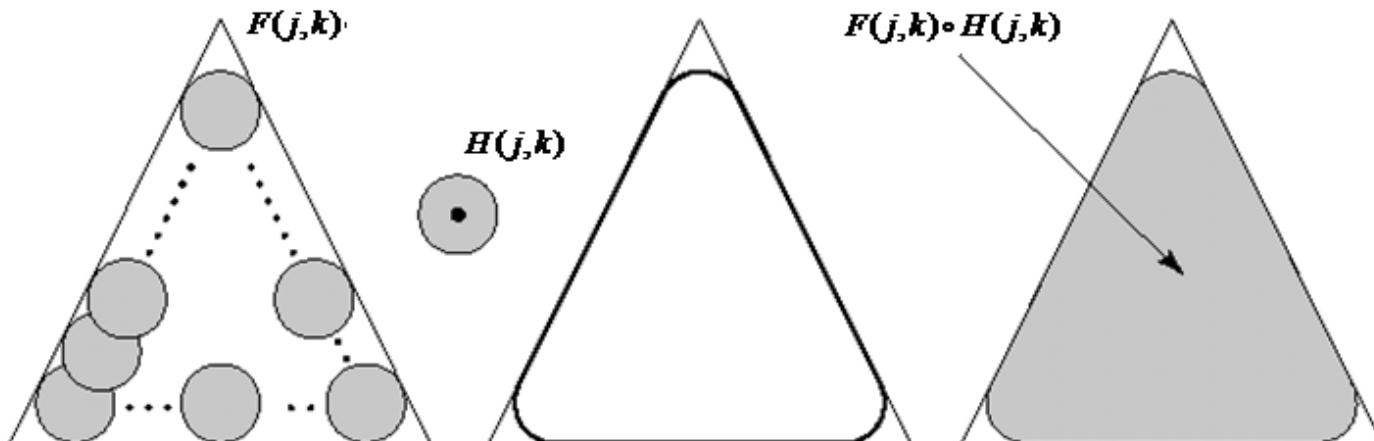
■ Applications

○ Open operator

$$G(j,k) = F(j,k) \circ H(j,k) = [F(j,k) \ominus H(j,k)] \oplus H(j,k)$$

■ With a compact structuring element

- Smoothes contours of objects
- Eliminates small objects
- Breaks narrow strokes



Morphological Processing

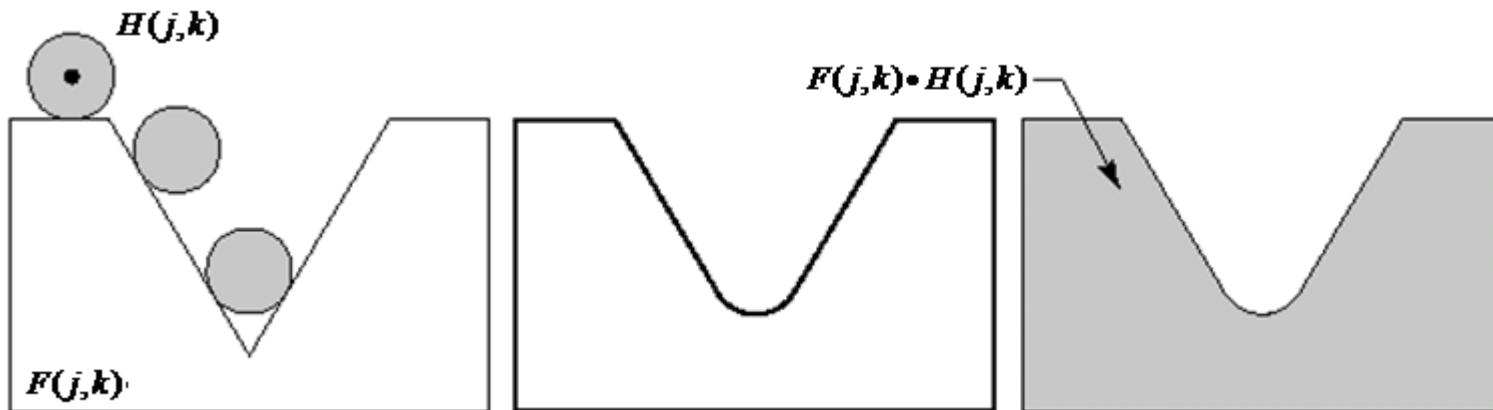
■ Applications

- Close operator

$$G(j,k) = F(j,k) \bullet H(j,k) = [F(j,k) \oplus H(j,k)] \Theta \tilde{H}(j,k)$$

- With a compact structuring element

- Smoothes contours of objects
- Eliminate small holes
- Fuses short gaps between objects



Morphological Processing

Example



original



(a) close



(b) open

Q: repeated openings/closings?



Compare (a) with the
original image



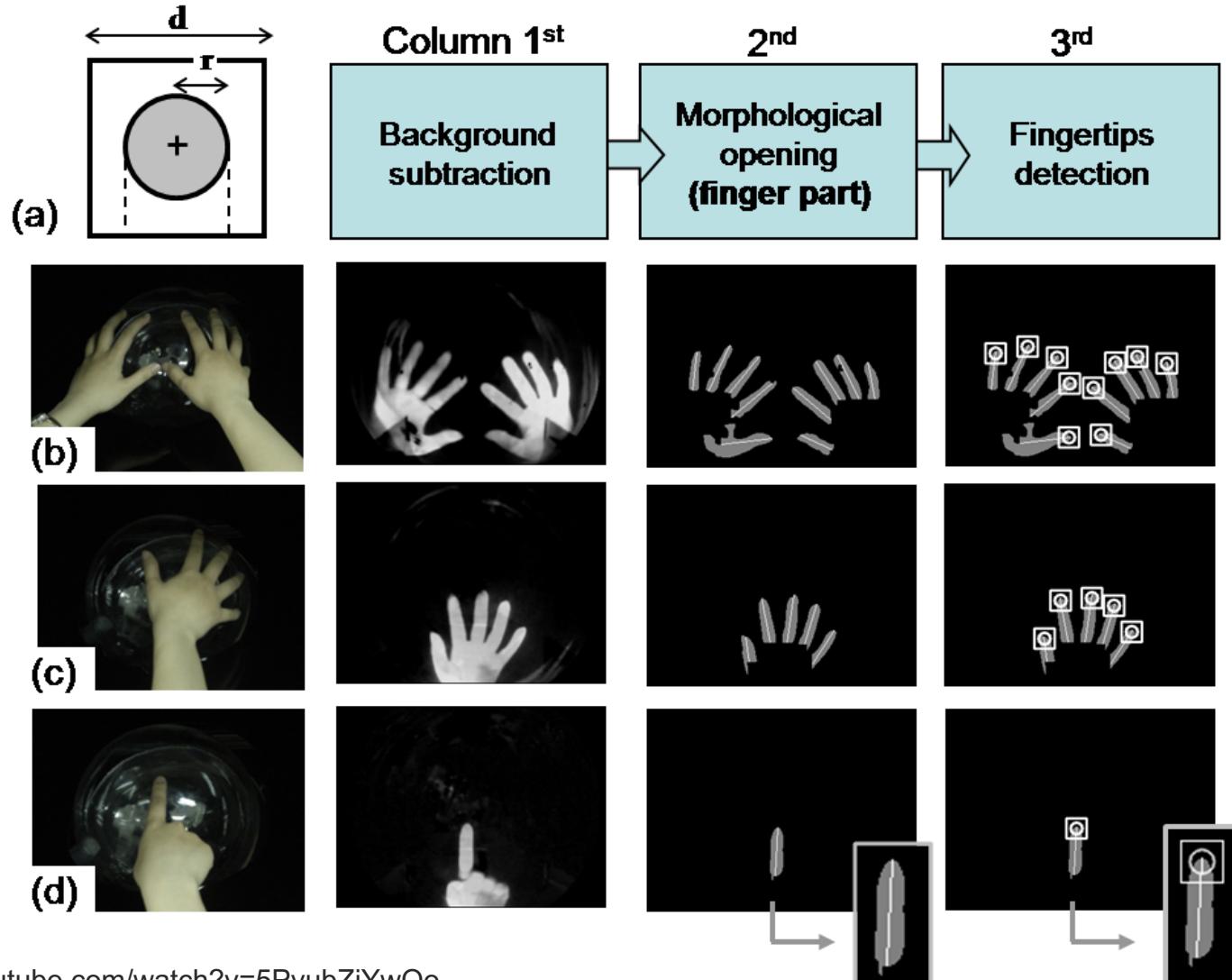
Compare (b) with the
original image

Morphological Processing

■ Example



[MCBall



Some videos

- **Morphing**
 - <https://www.youtube.com/watch?v=-rnVUzA8yMY>
- **SIGGRAPH 2013**
 - <https://www.youtube.com/watch?v=JAFhkdGtHck>
- **SIGGRAPH 2015**
 - <https://www.youtube.com/watch?v=XrYkEhs2FdA>
- **SIGGRAPH 2017**
 - <https://www.youtube.com/watch?v=5YvIHREdVX4>
- **SIGGRAPH 2018**
 - <https://www.youtube.com/watch?v=t952yS8tcg8>
- **SIGGRAPH 2019**
 - <https://www.youtube.com/watch?v=EhDr3Rs5fTU>
- **SIGGRAPH 2020**
 - https://www.youtube.com/watch?v=jYdMKdRUq_8