Is real-time transit information helpful? Analyzing the impacts of public transit real-time information on users waiting time

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**Abstract:**

Real-time information (RTI) and Transit real-time information apps (RTI apps) have claimed to have significant impact on passengers’ waiting time and user experience. Although previous research thoroughly surveyed and simulated the overall impact on certain stops, few studies investigate the impact’s mechanism and its spatiotemporal pattern. In this paper, we first introduce several trip planning strategies (TPSs) for both RTI and non-RTI users’ incidence behavior and corresponding quantitative descriptions. We also theorize and later validate the concept of reclaimed delay and discontinuity delay during the synchronization process. Then, with the support of GTFS real-time data, we optimize the RTI-based *prudent tactic* TPS and calculate the waiting time for each TPSs. Moreover, we compare different TPSs to measure RTI’s waiting time reduction. The results prove that RTI apps using the optimized *prudent tactic* can decrease waiting time for some users, however, it shows great variation geographically and temporally and cannot achieve global optimality for all stops. It also shows that RTI apps using the *greedy tactic* TPS will make users wait significantly longer than the bus delay, even longer than those who leave home randomly.

**Keywords:** Transit real-time information; GTFS; waiting time; mobile apps.

1. **Introduction**

Capabilities for collecting data and sharing real-time information about transportation systems is changing how people navigate and travel through cities. For example, apps and services such as Google Traffic, INRIX and Waze provide departure time and route suggestions for automobile-based travel based on current and predicted traffic and travel times, allowing users to avoid traffic congestion, minimize travel time and arrive on-time more frequently (Cabannes et al., 2018). Correspondingly, many public transit agencies are sharing schedule and real-time vehicle location data to enable navigation apps that make public transit more convivial and useful to users.

Public transit navigation apps allow users to discover and navigate public transit systems with complex routes and schedules (Dutzik, Madsen, & Baxandall, 2013). Public transit apps often provide real-time information (RTI) on vehicle locations and delays to help users to deal with this inevitable feature of public transit (Brakewood et al., 2014). In particular, RTI can allow users to reduce the amount of time they must wait for public transit at stops; this is crucial since wait time is perceived as onerous by users and cited as a major reason why people do not like using public transit (Algers, Hansen, & Tegner, 1975; Fan, Guthrie, & Levinson, 2016; Gkioulou, 2013; Larsen & Sunde, 2008; Reed, 1995). The rationale behind the saved waiting time is that RTI allows users to determine the best time to leave their home, workplace or similar location to travel (typically, walk) to a public stop so as to minimize wait time. When delay happens, RTI app users can access to the real-time status of buses and adjust their departure time accordingly (Brakewood, Barbeau, & Watkins, 2014; Brakewood, Rojas, Zegras, Watkins, & Robin, 2015; Cats & Gkioulou, 2017; Ferris, Watkins, & Borning, 2010; Papangelis, Nelson, Sripada, & Beecroft, 2016; Watkins, Ferris, Borning, Rutherford, & Layton, 2011). Figure 1 illustrates a typical public transit navigation app with RTI.



Figure 1 a typical interface of a real-time transit mobile app (Transit).

Ideally, RTI apps can diminish waiting time to 0, which means as soon as users arrive at the stop, the bus arrives and leaves. However, this attempted minimization of wait time by users can be risky. During the time interval between when a person leaves their home and arrives at the stop, the actual arrival time of the bus may change. For example, if the bus is behind schedule, the driver may take opportunities to catch up the delay by speeding up. This means that a user may end up missing the bus since the RTI can become inaccurate during their travel from home to the bus stop, resulting in a much longer wait time. Paradoxically, the use of RTI may increase waiting times based on the actual performance of the public transit system and the time required to travel to the designated stop. In the sense of utility, RTI could be a double-edge sword.

Nevertheless, in the sense of social equity, RTI could be also a double-edge sword. RTI is especially more important for systems with sparser timetable and longer headways. For example, in a system with average headway of 30 minutes, people is highly likely to care more about getting the performance of a specific vehicle via real-time information, since the possible waiting time is significantly longer; while in a system with average headway of 2 minutes, people may not care about how a specific vehicle works, since there will be another one shortly after the bus. Surely, “Frequency is Freedom” (Walker, 2012); however, in a less frequent transport system which cannot sustain high frequency with limited funds and manpower, RTI’s role is of more importance as a cheap and effective complement. In this paper, we would like to quantitatively investigate the authenticity of this statement.

Yet, even with more and more technology breakthroughs in this area, there are still economic and intellectual barriers for certain population to get access to the public transit real-time information. People who do not use smart phone application or do not own a smart phone cannot know the real-time status. These ordinary users have to plan their trips according to the schedule, their daily experience, or even random. Based on these facts, we would like to assess the average waiting time difference between non-RTI and RTI users and social justice issue behind the difference.

In this paper, we examine the impacts of RTI on public transit users’ waiting time based on empirical performance of a public transit system. We compare several trip planning strategies for deciding when to leave home to travel to the designated stop, including strategies that either ignore or exploit RTI. We assess and optimize different strategies’ waiting time and missed risk by consulting historical real-time bus feed. Based on the results, we compare non-RTI and RTI-based trip planning strategies. We also show how the performance of these strategies vary in different geographic and temporal level.

1. **Literature review**

Analyzing the impacts of timely public transit information predates the development of contemporary real-time data provided via webpages and smart phone apps. For example, Reed (1995) investigates signage and telephone’s real-time information’s impact on passengers’ waiting time. After the widespread application of smart personal devices, real-time information is becoming more accessible due to less expensive automated vehicle location system and the open data policy. Correspondingly, the body of literature is steadily growing and there are numerous studies investigating real-time information’s impact on public transit users (Brakewood et al., 2014; Brakewood, Macfarlane, & Watkins, 2015; Cats & Gkioulou, 2017; Ferris et al., 2010; Fries, Dunning, & Chowdhury, 2011; Liu, Shi, & Jian, 2017; Papangelis et al., 2016; Watkins et al., 2011). We are going to review the literature based on two dimensions: information media and methodology.

**By information media.** We first categorize research according to their information media, including static signage, telephone and text services, and smart phone application. Signage and at-stop displays can provide transit users useful information and reduce actual and perceived wait time (Dziekan & Vermeulen, 2006; Reed, 1995). Moreover, at-stop displays’ psychological effect is even more important: systems showing the next train or bus’s departure time can greatly release anxiety (Dziekan & Vermeulen, 2006). However, users can only get arrival information at the stop; this limits its effectiveness beyond reassuring the user since the decision to leave the origin has already occurred.

Telephone service and text services are more useful than signage since people can get access to the real-time information before deciding to travel to the stop or station (Reed, 1995). However, the provision of real-time transit information via the World Wide Web and smartphone apps has made this information more accessible and useful. RTI apps provide users ability to comprehend the sophisticated timetable in a transit system, for both scheduled and real-time timetable. They provide both scheduled and real-time support for transit users with portable smart phone through user-friendly interface.

Many studies investigated the waiting time reduction by mobile real-time information, and the results are diverse: some concluded that RTI reduces the waiting time; for example, 91% percent of RTI users self-reported spending less waiting time in Seattle, 2010 (Ferris et al., 2010). Moreover, RTI users can save 2.4 minutes in Seattle, 2011 (Watkins et al., 2011) and 1.79 minutes in Tampa, 2014 (Brakewood et al., 2014) according to a self-reported survey. Especially, in rural Scotland. RTI user can even save 7 minutes in average (Papangelis et al., 2016). Meanwhile, the others concluded that RTI’s impact on different users is not significant. Fries et al. (2011) reported that pre-trip travel time savings by RTI is small while the major beneficial effect is the reduction in anxiety. Brakewood, Rojas, et al. (2015) found that there were no statistically significant differences between RTI and non-RTI users’ waiting time according to the survey in Boston.

**By research methods.** Moreover, we can categorize research according to the research methods. These methods can be categorized into two main groups; survey-based methods and simulation models.

Survey-based method is definitely the majority among all RTI impact studies. Survey-based methods include on-board surveys (Fan et al., 2016), before-after surveys (Chow, Block-Schachter, & Hickey, 2014), web-based surveys (Ferris et al., 2010), in-person surveys (Watkins et al., 2011), interviews and observations (Papangelis et al., 2016), and stated preference surveys (Liu et al., 2017). Surveys sample respondents with the same questions; they measure many variables, test hypotheses, and conclude temporal sequence from questions about past behavior, experiences, or characteristics (Neuman & Robson, 2014). Without the support of automatic real-time data, passenger surveys are the most direct methods to assess transit system use, especially for user experience and perceptions. Meanwhile, survey data can quantitatively assess different attributes using self-reported data (Neuman & Robson, 2014), which partially guarantees generalizability and authenticity. Besides, in contrast to the automatic generated data, the surveys’ data also point to users, instead of vehicles. The human-centered nature of survey data also guarantees its direct and close connection with human per se.

However, survey methods may not be suitable to solve other problems: survey-based studies investigate perceived or self-reported waiting time instead of actual waiting time. The perceived waiting time is different from the actual waiting time. For example, in Seattle, RTI users’ self-reported average perceived waiting time were 7.54 minutes compared to non-RTI users’ 9.86 minutes, while the average actual waiting time obtained by observers for RTI users is 9.23 minutes compared to non-RTI users’ 11.21 minutes (Watkins et al., 2011). Consequently, compared with value obtained by physical sensors or observers, the self-reported information may be biased by the users themselves.

Moreover, the survey’s size, especially for traditional data collection methods, is relatively small due to high cost of data collection (Goyder, 1986). On the other hand, some affordable methods are biased, especially IT (Information technology)-based methods. Mail survey (Rossi, Wright, & Anderson, 2013), text/phone call survey, and internet-based survey (Wright, 2005) can significantly reduce the time and economic cost of the survey. However, these methods face a same challenge: it is hard to access a representative sample (Rossi et al., 2013; Wright, 2005). For public transport system, not all users can get access to these IT-based services while the survey will only sample certain specific people.

Mathematical simulation is also often used to investigate and solve problems that are too difficult or costly to measure directly. For example, Cats & Gkioulou (2017) adopted an agent-based model to simulate the influence of transit reliability and real-time information on waiting time uncertainty. Agent-based model simulation usually adopts several assumptions and represents the simultaneous actions and interactions of various agents. The simulation tries to imitate and predict the performance of a complex system such as a transit system (Gkioulou, 2013).

Although the overall impact of the real-time data on waiting time was well explored, few studies investigated the variance of the impact (Brakewood & Watkins, 2018). Most studies investigated the overall average waiting time or perceived waiting time in certain areas; however, no one has investigated the variance of this impact relative to transit system’s on-time performance. The gaps include the waiting time’s distribution, spatial patterns, temporal patterns, and the mechanism of the impact.

Moreover, ironically, there are no studies using actual real-time transit data source due to the lack of easily accessible transit schedule and real-time vehicle location data, allowing the measurement and assessment of public transit delays at high spatial and temporal resolution. It is crucial to understand the real-time data by the real-time data per se.

The emergence of big data creates a precious chance to understand the real-time data and the manipulation process of it for the public transit authorities, RTI apps providers, and the passengers themselves. Transit real-time big data’s large size (volume), high update frequency (velocity), and impartial measuring perspective (veracity) make it a good source to understand both the performance of the transit system and the behavior of transit users. We would like to address the gaps of waiting time problem in the real-time transit context and implement it using the very same real-time transit data that the RTI apps are using.

1. **Methodology**

In this section, we first introduce the data source and corresponding manipulation processes. Moreover, we describe the synchronization process during the procedure of transit and the concept of *delay reclamation*. Based on the synchronization theory, we propose and model several trip planning strategies (TPSs) during the process of decision making and optimize the RTI apps user’s strategy based on deterministic real-time data. We also calculate the waiting time difference between RTI apps users’ deterministic process and non-RTI users’ probabilistic process.

* 1. **Data**

In response to the two major actors, the user and the system, we used two separate data sources.

**User behavior - General Transit Feed Specification (GTFS)**. Introduced by Google in 2006, the General Transit Feed Specification (GTFS) consists of two data standards: GTFS static and GTFS real-time expansion. GTFS static indicates the schedule data of a transit system in several separate tables (Google Developers, 2016). GTFS static is the current *de facto* standard for transit system schedules and transit geographic information (Google Developers, 2016). As a standard for open data, it is easy to share and access for the public, transit apps providers, and researchers.

Besides schedule data, GTFS provides an expansion of real-time data, which includes vehicles’ geographic data with high temporal resolution. GTFS real-time data includes two parts: buses’ location real-time data and the trip updates, which specifies the fluctuations in the real-time timetable (Google Developers, 2018). Unlike many traditional transit data, GTFS real-time data have large volume, relatively high resolution, and full system coverage; and also, unlike many big data, GTFS provides a homogeneous protocol to effectively transmit transit real-time information with normalized standard. As a result, most RTI apps will use the estimated arrival time provided by GTFS trip update for the buses’ real-time information (Google Developers, 2018; Transit app, 2019). Therefore, we can simulate RTI users’ behavior from the GTFS trip update data.

**System performance – Automatic Passenger Counting (APC).** Although GTFS data’s resolution is relatively high, its *temporal accuracy* is not satisfying. GTFS data is updated based on a fixed interval; it could be 15 seconds to 2 minutes depending on different systems. Consequently, the final updated time could be different from the actual arrival time and the updated time could be inaccurate.

To solve the low temporal accuracy issue, we used another administrative data source: Automatic Passenger Counting (APC) data. The APC data is collected by the passenger counters installed on each bus, which is primarily intended to summary the ridership. Moreover, the data also contains the accurate arrival/departure time recorded promptly at each stop. Compared with GTFS, it is more appropriate to use APC to calculate the system performance and RTI-based users’ actual performance.

However, because the APC devices are not available for every bus, its system coverage is not 100% unlike GTFS. Correspondingly, to make the APC data possible to sustain the calculation, we will merge the APC data and GTFS to achieve both higher temporal accuracy and 100% system coverage: for every GTFS real-time record, query the corresponding trip and stop in the APC database and overwrite if exists.

For the development and implementation of our methods, we selected Columbus, Ohio and Central Ohio Transit Authority (COTA) as the site for the case study. First, COTA bus system’s average headways are considerably large, which makes the waiting time a significant factor when actually using the system; second, as a typical car-oriented city, the case study can be easily expanded to other cities and larger scales with same data support and methodologies. We collected and organized all history GTFS schedule data in MongoDB and Python environment from Application Programming Interface (API) provided by COTA from May 2018 to May 2019; for GTFS real-time, we archived the streamed data with frequency of 1 minute for the same time period. We also received the APC data from COTA from May 2018 to May 2019. The databases’ volume is in terabyte level; correspondingly, to improve the computational performance, we also parallelized the outmost loops (buffers × dates) on a workstation with 40 virtual CPU cores.

Even so, the computational overhead is considerably large. Therefore, we selected bus route No. 2 as our research target for several reasons:

* Bus route No. 2 is the one of the busiest routes in the COTA bus system.
* Its spatiotemporal coverage in the COTA bus system;
* It has two schedules with different headways. We can study the impact of headways on the performance.
  1. **Synchronization**

Taking a bus could be conceptualized as a synchronization process between the walking trip to the target stop and the target bus’s *trip sequence array*. Trip sequence array is defined as the collection of trips running on the same route as the target bus in the direction of target bus.

Depending on user’s arrival time at the stop *t*, the actual bus that user will take can be different from the scheduled one. We use the same concept in the transfer synchronization process: *desynchronization degree* (DD), to measure the desynchronization between the bus and user at the stop. DD is an integer indicator that represent how many buses the user loses in the trip sequence array:

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| --- | --- | --- |
|  |  | (1) |

It also means that if the user arrives at the stop between bus DD = n – 1 and bus DD = n, then the user will take bus DD = n.

When synchronizing, the process of walking is linear: the users can control the walking time by selecting their home departure time (HDT). Except for very crowded conditions in dense cities, we can assume walking time is linear with respect to distance.

In contrast, the actual real-time performance of the bus is non-linear: the bus will not run at a fixed velocity and the expected time of arrival of bus at the stop is constantly changing. The vehicle operator can change the vehicle’s speed based on conditions in real-time. Most relevant to our question, a vehicle operator can make up for an initial delay by increasing speed. Indeed, public transit agencies value on-time performance and may incentivize drivers to compensate for delays when possible, considering speed limits and safety considerations.

We therefore introduce the concept of *reclaimed delay (RD).* Similar to delay propagation (Park, Mount, Liu, Xiao, & Miller, 2019), it is the time difference between the actual time of departure (ATD) and the expected time of departure (ETD) at the stop. It also represents the delay that the bus catches up between two stops.

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|  |  | (2) |

Where: S is the collection of stops on the route, i is the target stop, t is the current time.

Figure 2 shows corresponding space-time diagram of the expected synchronization, the actual desynchronization, and delay reclamation process. After the user leaves home, the actual bus trip (blue line) will diverge from the expected bus trip (red line) and converge with the scheduled bus trip (yellow line): since the bus has an initial delay near the user’s home, the bus accelerates and catches up the delay with the schedule. However, the user’s walking trip is still aiming for the expected bus trip. Consequently, the bus arrives earlier than the user’s expected time and the user will miss the bus.

The reclaimed delay could be small but critical for RTI apps users: consequently, the RTI apps user will lose the bus and suffer waiting time penalty for a relatively long time. Thus, the synchronization of these two processes is highly unstable. Besides the delay reclamation mechanism, inaccurate geographic locations and delays in updates due to internet congestion and failures may also contribute to the desynchronization.



Figure 2 space-time diagram of the expected synchronization and the actual desynchronization

Besides reclaimed delay, due to the discrete nature of the GTFS real-time data, there are a *discontinuity delay* for all RTI-based trip planning strategies as shown in Figure 3: if RTI apps do not interpolate the void between the data feeds and their corresponding timestamp, the RTI-based users will wait until the data is updated. However, when the data is updated, the RTI-based user is already late for the bus. Similarly, if the user decides to leave between two updates, although the RTI apps will show a good result based on the last update, in reality the user will miss the bus. Either scenario is the consequence of discontinuity of the real-time data. Exactly like reclaimed delay, although the discontinuity delay could be very small in value, it still can result in desynchronization and significantly long waiting time. Both reclaimed delay and discontinuity delay produce potential missed risk for RTI-based users.



Figure 3 the discontinuity delay of real-time data

* 1. **Trip planning strategies**

A trip planning strategy (TPS) can be interpreted as a tactic for a user to plan and execute a transit trip. Assuming no disturbance on user’s walking and boarding process, different TPSs have only one controllable factor to determine the actual waiting time: the time to leave home for the transit (home departure time, HDT). RTI apps relaxes the fixed timetable in a frequently delayed transit system, thus saving waiting time for RTI apps users. In the sense of saving waiting time, a trip planning strategy can also be interpreted as a rule of optimization. Depending on how to determine the home departure time, there are different trip planning strategies for both RTI apps and non-RTI users and their different purposes.

**[Non-RTI trip planning strategy]**

In traditional incidence behavior studies, users are divided into two groups: timetable-independent passengers, who are not aware of the system schedule and performance, and timetable-dependent passengers, who are aware of the system schedule or empirical performance (Frumin & Zhao, 2012). These two user groups are introduced in the context of non-RTI experience. Here, we moreover divide non-RTI users into three groups.

**Arbitrary tactic (AT)**. Before the time of smart phone, text, and public real-time information, under many circumstances, transit users were not necessarily planning their trips. A simple strategy is to walk to the stop and catch the subsequent bus arbitrarily. The major assumption is that the user’s arrival time is independent from the vehicle system (Frumin & Zhao, 2012). For the same reason, these users are also considered timetable-independent.

Because the user’s decision-making process is random, it is reasonable to assume user’s HDT or user’s arrival time is evenly distributed among the headway between two buses. Traditionally, the average waiting time is the expectation of the random variable headway (Frumin & Zhao, 2012):

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|  |  | (3) |

where: is the average waiting time, is the average headway, is the standard variance of headway.

However, since we have access to the real-time vehicle departure time data, we can calculate the empirical average waiting time as the mean of the departure time of target bus and its subsequent bus:

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|  |  | (4) |

where: is the median of the target bus and its subsequent bus and is the walking time. is the bus’s actual real-time departure and is the very first prior bus’s actual real-time departure time.

Theoretically, this strategy is not very efficient since it is always the half of the buses’ actual headway. Therefore, we can make it a good benchmark for other TPSs: if another TPS’s performance is even worse than AT, we can say that it is not effective.

**Scheduled tactic (ST)**. Without knowing any information about the running status, users can still follow the schedule published to the public in advance. Traditionally known as timetable-dependent users, ST users prefer earlier final arrival time than convenience. Under this circumstance, the user will follow the scheduled timetable of the transit system regardless of possible delay and the consequent waiting time:

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|  |  | (5) |

Where: is the user’s home departure time (HDT), is the walking time from user’s home to the stop, is the scheduled bus departure time.

Consequently, the RTI apps user will not benefit from waiting time reduction. However, since theoretically no bus/train will leave earlier than the scheduled time, ST minimizes the missing risk. ST is another benchmark for all TPSs, which theoretically has the lowest missing risk.

**Empirical tactic (ET**). If a user can get access to the historical information on system performance, either from daily experience or a database, the user can relax the HDT based on the empirical average time/maximum time without any RTI.

For the derivation of , different users may adopt different ET strategy. In general, there are two parameters to determine an empirical HDT: learning function and learning memory. Learning function means the rules to generate the historical information, such as averaging and minimizing. Learning memory is the available time period for the learning process. Ordinary users will not memorize all the historical information due to limited memory and limited access to the historical data. For example:

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|  |  | (6) |

where: is the user’s empirical arrival time for the bus trip is the bus trip’s actual departure time on day *i*, and n is the learning memory (days). This specific ET strategy’s learning function is minimizing and its learning memory is n days.

ET is a common non-RTI strategy. In this paper, we also investigate waiting time’s relationship with ET strategy’s learning function (averaging and minimizing) and learning memory (1 days – 10 days). Based on the results, we will find an ET strategy with the smallest average waiting time.

**[RTI-based trip planning strategy]**

To investigate the RTI-user’s behaviors, we need to first conceptualize the RTI apps’ trip planning process. The process of RTI apps’ decision making consists of several steps: First, RTI apps will provide different path choices for users and their HDT or users will find the desired bus trips/routes from the list in the RTI app. Then, the trip update data will provide estimated time of departure (ETD) at the target stops for RTI apps or users. Finally, RTI apps or users will subtract estimate walking time and obtain estimated HDT. The estimated HDT is not constant; instead, RTI apps will update it according to the real-time trip update data.

Previous research has proven that RTI users will adapt their behavior to shorten their waiting times (Cats & Gkioulou, 2017). Depending on the relationship between given estimated HDTs and the current time, the user will decide the actual HDT. Just like non-RTI strategies, the essential part is the criteria to derive the actual HDT.

**Greedy tactic (GT)**. Most transit users do not want to wait. Moreover, if a user encounters extreme weather events, especially cold weather and heavy precipitation, she/he may want to reduce the waiting time as much as possible. In practice, a greedy tactic (GT) user will check the relationship between suggested HDT and current time by consulting RTI apps. She/he will only leave if the RTI app tells her/him so according to the real-time data, when the bus’s ETD at the stop is equal to or greater than walking time plus current time:

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| --- | --- | --- |
|  |  | (7) |

Where: is the scheduled bus’s ETD at the stop given by RTI app and real-time data, and is the current time when .

This strategy can achieve temporary optima as shown in Figure 2 as the green line. However, due to the instability of transit system, the missing risk of GT is also the highest. Due to the possible reclaimed delay and discontinuity delay, the bus will likely leave earlier than ETD. Even a smallest disturbance during the walking process or the bus running status during user’s walking can result in a missing bus using this strategy. Consequently, the user may suffer from a long waiting time penalty, which is almost equal to a headway, the largest possible waiting time.

**Prudent tactic (PT)**. Figure 2 and Figure 3 together show the high risk of GT trip planning strategy. If a user would like to save waiting time and keep some degree of missing risk simultaneously, she/he may leave a short buffer of several minutes earlier than GT. Similar strategies were adopted in the context of scheduled time: some passengers would leave 2-3 minutes before scheduled service arrival in case of some unexpected “risky” events, such as delay by the elevators (Fonzone, Schmöcker, & Liu, 2015). These risk-averse reactions are usually defined as costs of unreliability (Frumin & Zhao, 2012).

Similarly, a prudent RTI passenger will leave a short buffer for the risk of missing bus and unexpected reclaimed delay and discontinuity delay. This short time buffer, which is defined as *insurance buffer* (IB), trades some time to reduce missing risk, thus decreasing instability of the buses’ real-time performance. PT users’ HDT is:

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|  |  | (8) |

where: IB is the insurance buffer.

The buffer strategy is a combination of empirical and real-time result: the calculation of buffer is empirical, and the calculation of actual home departure time is based on the empirical buffer and real-time information. Figure 4 also suggests the relationship between IB and reclaimed delay. RTI-based strategy is risky due to the existence of reclaimed delay, thus, the ultimate purpose of IB is to compensate for the reclaimed delay. Therefore, in the theoretical optimal PT scenario, an optimal insurance buffer should be exactly equal to the reclaimed delay to achieve 0 waiting time. Practically, IB can also relax the instability caused by the discontinuity nature of RTI feeds and some measurement errors.

Insurance buffer’s value is also a good indicator of the transit users’ risk attitude: It represents how much time the user is willing to gamble to gain the waiting time reduction. We define two extreme values of risk attitude: *risk-seeking* and *risk-averse*. *Risk-seeking* means the user would rather seek for the waiting time reduction regardless of the potential missed risk, which will possibly incur an additional large waiting time caused by desynchronization; *risk-averse* means the user would rather wait more time to avoid desynchronization. The less IB’s value is, the more risk-seeking and less risk-averse the user is.

Prudent tactic and greedy tactic can be categorized as a *prudent tactic family*, for GT is a special case of PT with IB = 0. With different IBs, each prudent tactic can vary in actual waiting time. We would like to optimize IBs and find the best prudent tactic with maximal waiting time reduction.

**Prudent tactic with optimal insurance buffer (PT optimal)**. Previous research concentrated on PT system’s optimization in the stage of planning and operation. Due to the lack of authority and information access, ordinary users were rarely considered as a part of optimization process. However, with RTI, although users still cannot directly improve the real-time systematic performance (delay, ridership) of the system per se, optimization can be conducted in the individual level to reduce waiting time.

Correspondingly, we introduce the concept of volunteered optimization: despite transit systems’ instability and uncertainty, users with appropriate RTI advice can adapt and optimize each trip according to the delay and real-time information. Volunteered optimization is independent from the scheduled timetable; instead, it is based on the real-time status and decentralized. The RTI apps or the public transit service providers will pre-calculate all the optimal parameters; users will consult the suggested home departure time and leave home accordingly. In this way, with the maximization of waiting time reduction in the individual level, the overall waiting time penalty will also be diminished. To achieve volunteered optimization, it is necessary to optimize each individual trip, which is from prudent tactic family. Correspondingly, we need to find the prudent tactic with optimal insurance buffer: *PT optimal*.

Figure 4 shows the how PT optimal resynchronizes with the actual bus trip. Instead of the expected walking trip (shown as green solid line), the PT optimal user will follow the RTI apps’ pre-calculated optimal plan with insurance buffer (shown as green dash line). Due to the existence of insurance buffer, the reclaimed delay is therefore offset and the user will successfully take the expected bus.



Figure Space-time diagram of the PT optimal's trip

For PT or GT, the users will plan their HDT according to the bus’s ETD instead of the real departure time. Here we define expected waiting time:

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| --- | --- | --- |
|  |  | (9) |

where: is the ETD, t is the user’s arrival time at the stop, is PT strategy’s HDT, and is the walking time. Combining Equation (4) and Equation (9), we have: . For PT family, insurance buffer should be at least equal to the expected waiting time.

To find the , empirically, we simulated the users’ real-time waiting time using different IB. Figure 5 is the flow chart of PT optimization. There are four major steps in the learning process:

* Calculation: Calculate the performance for all designated buffers for optimization (0 – 300 seconds). The results contain user’s arrival time at the stop and the actual taken bus’s departure time for users with different walking time (0– 9 minutes).
* Optimization: Find the smallest waiting time and the corresponding buffer each day. If there are multiple smallest waiting time, designate the one with smaller buffer.
* Finalization: For each day, reduce all past days’ buffers into one by finding the maximum of the optimal buffers. Meanwhile, to accommodate the seasonal major changes in the schedule, we will restart the learning process whenever the major change is facilitated.
* Revalidation: Based on the finalized buffers, calculate the performance of each day.

All of the steps can be conducted by RTI apps or transit providers in the operational stage on the fly. In this way, we guarantee the optimality of obtained buffers: first, *calculation step* and *optimization step* guarantees that obtained buffers in each day have the least waiting time; second, *optimization step* guarantees that obtained buffers are the smallest one among the buffers with the least waiting time; third, *finalization step* guarantees that trips with finalized buffers are most synchronized for each day when revalidating the performance. In the sense of risk attitude, we adopted a *risk-neutral* strategy: we want to find the smallest buffers while trying to keep synchronized for most trips.



Figure 5 Flow chart of PT optimization algorithm

For the first dominating step of the optimization process, the total computation complexity for our study case is polynomial but of high power. The optimization process of produces massive number of parameters . We minimized waiting time over , which will have a different IB for each day, each trip, each stop, and each walking distance from the stop (0 – 10 min).

* 1. **Measures**

We would like to measure the difference of waiting time and risk of missing a bus/train between the RTI users and non-RTI users. Therefore, we define two measures: the missing risk and average waiting time.

**Missed bus risk.** The missed bus risk measures the probability of missing a bus based on the TPS relative to the actual performance of the transit system:

|  |  |  |
| --- | --- | --- |
|  |  | (10) |

Where: n is total number of trips;

Here we define missing a bus/train as: the actual bus’s desynchronization degree is larger than 0. This also means the user takes a different bus after the scheduled bus.

**Actual waiting time**. Average waiting time measures the expected wait time across all trips based on the TPS. We start by defining the actual waiting time:

|  |  |  |
| --- | --- | --- |
|  |  | (11) |

Where: is the actual waiting time, is the bus’s actual real-time departure time, and is user’s arrival time at the stop. is user’s HDT, and is user’s walking time from home to the stop. Equation (11) also proves that the only factor that user can control and can affect waiting time is , based on a static walking time.

Based on the actual waiting time, we define average waiting time as the mathematical expectation of waiting time’s distribution across all trips.

|  |  |  |
| --- | --- | --- |
|  |  | (12) |

where: n is total number of trips and is the waiting time of each trip .

1. **Analysis**

In this section, we focus on the geographic and temporal analysis of buffer, waiting time, and waiting time difference between different TPSs. For the study area and target, we choose COTA bus No. 2 from Southeast to Northwest from May 2018 to May 2019. The bus route has two schedules: the frequent one originates from red circled stop (frequent originating stop) in Figure 6 with headway of 10 – 15 minutes, while the standard on originate from blue circled stop (standard originating stop) in Figure 13 with headway of 20 – 30 minutes (COTA, 2019).



Figure Bus route 2's standard and frequent service map (COTA, 2019).

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
| Trip planning strategy | Waiting time mean | Waiting time deviation | Risk mean | Risk deviation |
| Scheduled tactic | 252 seconds | 345 seconds | 6.28% | 16.55% |
| Optimal prudent tactic | 282 seconds | 381 seconds | 10.18% | 17.70% |
| Empirical tactic with memory | 334 seconds | 494 seconds | 18.39% | 38.74% |
| Arbitrary tactic | 510 seconds | - | - | - |
| Greedy tactic | 751 seconds | 707 seconds | 74.63% | 74.50% |

Table Each TPS's waiting time and missed risk's mean and deviation

Table 1 shows themean and deviation of each TPS’s waiting time and missed risk. In general, PT optimal’s average waiting time is larger than scheduled tactic’s. However, due to larger variation, in some area and time PT optimal can be especially more effective.

ET family and ET with memory = 6 are less effective: in average, an ET user has to wait almost 1 minutes longer than a PT optimal user. Meanwhile, despite as a member of PT family, GT’s performance is very poor. Its average waiting time is even longer than the arbitrary static. The terrible performance is due to its high missed risk.

Moreover, in the sense of risk attitude, scheduled tactic is the most risk-averse TPS, since the user is willing to avoid desynchronization with longer expected waiting time. As opposed to ST, greedy tactic is the most risk-seeking TPS, since the user leaves no insurance to seek for the maximal expected waiting time reduction. PT optimal, otherwise, can be regarded as a balance point between the two polar, which can be called *risk-neutral* TPS.

* 1. Geographic pattern

**Arbitrary tactic**

Arbitrary tactic has an average waiting time of half of the headway. Therefore, we can observe a drastic change between standard schedule and frequent schedule due to the increase of headway in Figure 8 (top left). Intuitively, the performance of AT should have been the worst among the TPSs. However, it can outperforms the RTI-based greedy tactic for almost 4 minutes. This also proves that RTI users without proper advice could wait significantly longer than even arbitrary tactic.

**Scheduled tactic**

As shown in Figure 8 (top right), the average waiting time starts from 0 while it accumulates and propagates along the route with fluctuations just like the actual delay. Theoretically, ST waiting time is exactly the delay of the bus they take, since no bus should be leaving before the scheduled time and the buses’ actual departure should be always later than the scheduled time. In other terms, the theoretical missed risk is always 0. However, ST’s actual missed risk is 6.28%.

**Empirical tactic**

In this section, we validate each empirical tactic with settings selected from 2 learning functions and 9 learning memories. Figure 7 visualizes the waiting time of 18 TPSs in the ET family. Two curves start at a same point, since averaging and minimizing are the same with the memory of 1. For minimizing learning function, the waiting time increases with negative acceleration along with increasing learning memory; for averaging learning function, the waiting time will decrease with increasing acceleration along with increasing learning memory. Minimizing also have a U-shape curve that waiting time is the smallest when memory period is 6. It proves that minimizing’s performance is much better than averaging’s and we conclude that the empirical tactic with minimizing and memory = 6 is the best ET among the others. Figure 8 (bottom left) and Figure 9 (top right) show the average waiting time and missed risk of ET with memory =6.

Figure the waiting time of ET family with minimizing and averaging learning function and 1 – 9 learning memories

Meanwhile, as a non-RTI trip planning strategy, ET with memory does not outperform the RTI-based prudent tactic optimal. It also strengthens a simple intuitive assumption: real-time information helps, somewhat.

**Greedy tactic**

Figure 8 (bottom right) shows the graphic pattern of GT’s waiting time and Figure 9 (bottom) missed risk. Ironically, as a RTI-based trip planning strategy, GT’s performance is the worst: it cannot even outperform arbitrary tactic. The primary reason is the high missed risk. Despite the shortest expected waiting time, due to delay reclamation and discrete real-time data feed, GT users have the largest missed risk thus the longest waiting time.

As a member of PT family, GT’s waiting time’s pattern is influenced by the walking time. Figure 11 and Figure 12 show GT’s waiting time and missed risk’s relationship with walking time. For GT, due to its high missed risk, longer walking distance will generally improve its performance. The fact that missed risk is initially at a high level makes longer walking time a similar role as insurance buffer: longer walking time will destabilize the synchronization process and make more desynchronized trips synchronized again.

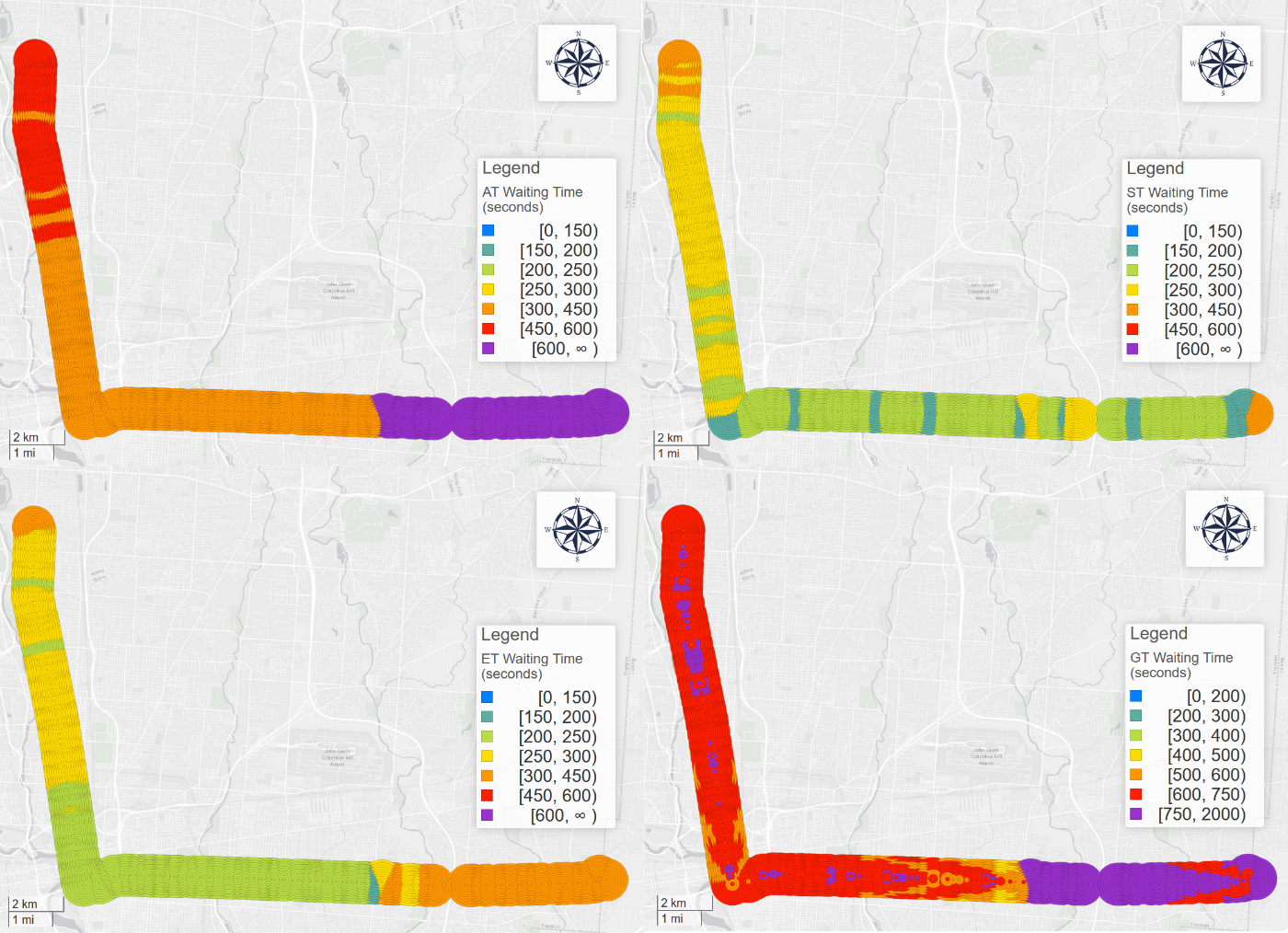


Figure 8 AT (top left), ST (top right), ET (bottom left), GT (bottom right)'s waiting time pattern

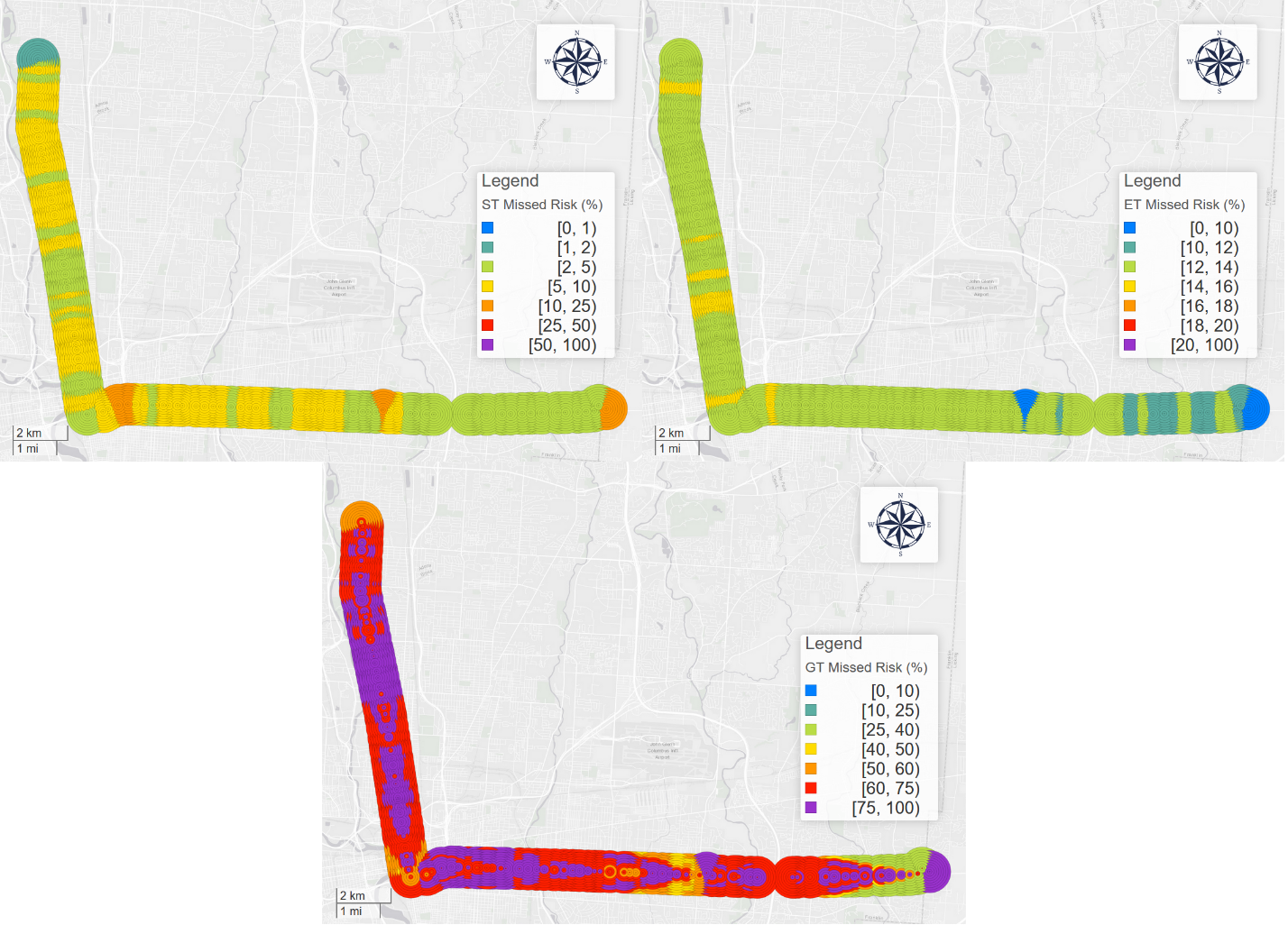


Figure 9 ST (top left), ET with memory (top right), GT (bottom)'s missed risk pattern

Moreover, because GT is the “expected walking trip” shown as the green solid line in Figure 2 and Figure 3, we validated the correctness of reclaimed and discontinuity delay proposed in the method section.

[Proof of reclaimed and discontinuity delay]

The inefficiency of GT also proves the correctness of synchronization and delay reclamation process in Figure 2 and the discontinuity delay in Figure 3. To moreover show the relationship between reclaimed delay, discontinuity delay and miss risk, we also calculate the delay reclamation and miss risk for each specific trip. We summarized that during the whole year, when a delay reclamation occurred, there were 88.87% chance that the GT user would miss the bus empirically.

Besides reclaimed delay, to validate the existence of discontinuity delay, we calculated 31 trip planning strategies in the PT family, each with a uniform insurance buffer for all trips and all stops from 0 (greedy tactic) to 300 seconds. We moreover plot the line charts of each index and its changing rate, which represents IB/ home departure time’s impact on them. Figure 10 shows how the average waiting time and the miss risk change with the uniform insurance buffer. Each graph of changing rate shows clear discrete pattern: there were several sudden changes for each indicator’s changing rate at 60, 120, 180, and 240 seconds, which are all multiples of the interval of the real-time data (60 seconds). The points between these sudden changes are relatively close, forming a stepped curve. Moreover, Figure 11 demonstrates that the miss risk changed fastest when buffer = 60 seconds, which is exactly the interval of the real-time data. All these discontinuous change prove the existence of the discontinuity delay. The buffer will ease both reclaimed delay and discontinuity delay simultaneously, however, due to the discrete nature of discontinuity delay, only multiples of 60 seconds will we observe the sudden change of discontinuity.

Figure 10 average waiting time/missed risk and their changing rates' relationship with the uniform buffer.

**Prudent tactic optimal**

We validate the PT optimal and investigate its geographic patterns from three directions.

[Perpendicular direction – Walking time]

Figure 11 illustrates the relationship between waiting time and walking time and Figure 12 shows the relationship between missed risk and walking time. For PT optimal, the longer walking time is, the longer will the user wait and the riskier the user will be to miss the bus. This supports the claim that the longer distance the user lives from the stop, the more unstable their trip becomes. During the longer walking time to the stop, the bus could be more likely to accelerate to catch up the delay, making RTI users miss the target bus.

Figure 11 PT optimal, GT, AT, ET, and ST’s waiting time's relationship with the walking time

Figure 12 PT optimal, GT, ET, and ST’s missed risk's relationship with the walking time

[Forward direction – Marginalized stops]

Figure 13 (left) shows PT optimal’s average waiting time on COTA bus route No.2 from Southeast to Northwest. Noticeably, there are two significant high clusters near the two originating stops (red circled and blue circled) in the standard and frequent No.2 bus schedule. Figure 9 (top left) demonstrates the missed risk for the PT optimal, and it also shows two unnatural high missed risk clusters near the two originating stops.

This is because the lack of real-time data in the very beginning of bus trips. The real-time information will not be available until the bus leaves the originating stop. For certain trips, by the time the real-time information is updated, the user already loses the bus. Under this circumstance, buffer will not help improve the missed risk of such trips since IB’s effectiveness depends on accessible real-time information, and these users are not given the correct real-time data correctly. Meanwhile, users who live far from the stop will have higher missed risk and will consequently suffer from even more waiting time.

Out of the two high clusters, the standard originating stop (blue circled) has higher waiting time. The headway near the standard originating stop (red circled) are larger in the bus schedule. Both the high missed risk and large headways contribute to the unnatural long waiting time at the standard originating stop (blue circled) compared to the frequent originating stop (red circled).

Based on these facts, we can call these stops *marginalized stops*. It suggests that RTI strategies may be less effective at these stops. In these areas, public transit users are vulnerable and may be unable to get real-time information or right information.

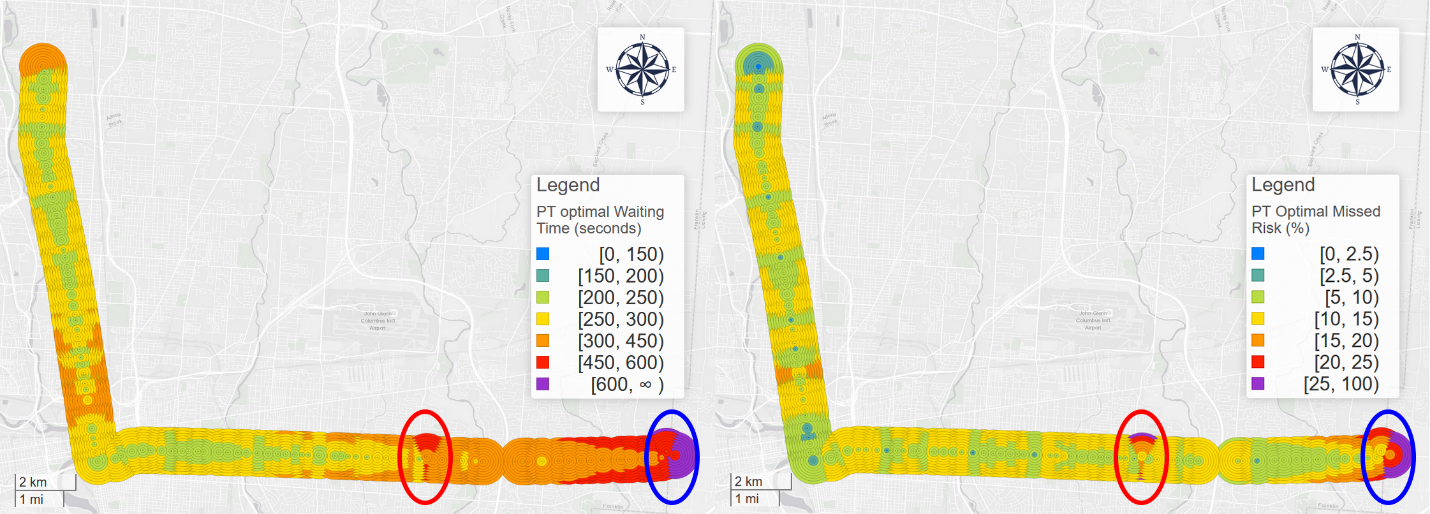


Figure PT optimal’s insurance buffer for each stop and average waiting time in COTA bus route No. 2 from Southeast to Northwest.

[Diagonal direction – Contour lines]

An obvious pattern that can be observed in the map is the parallel diagonal contour lines. In the map, for each point on the contour line, their values are almost the same. Most maps above prove the presence of the contour lines. We can conceptualize the contour lines in a smaller scale: two neighboring circles at two subsequent stops with the same value. It is the smallest unit of the contour line. These two circles’ walking time difference is nearly equal to the bus’s running time between the two stops. With more neighboring circles with the same value, the contour lines are formed.

There are two reasons for this phenomenon. First, for the two neighboring circles, essentially these users in the two areas are aiming for the same bus but at different bus stops; second and most importantly, users in the two areas will get a same real-time data simultaneously and plan their trips according to the same data feed, thus arrive at the target stop at the same time. Therefore, if no disturbance or acceleration between the two stops, the two trips are the same, only with different walking distance. This also suggests that the gaps on the maps are the point where delay oscillates, and the bus is running in the constant speed in the areas with smooth contour lines. The contour lines’ formation can also be understood in another temporal sense: after the bus receives a disturbance at a stop, the disturbance will persist and spread outwards when the bus is moving to following stops.

[Geographic difference between ST and PT optimal]

Figure 14 (right) shows the average waiting time difference between ST and PT optimal on COTA bus route No. 2 from Southeast to Northwest. The differences represent the distinction between performance of best non-RTI users (ST) and best RTI users (PT optimal), respectively. We can observe that PT optimal does not outperform ST for all stops. In fact, for most stops, especially for those stops in the upstream near the originating stops, ST’s performance is much better than PT optimal.

We can observe the originating stops have exceptional high waiting time due to larger headway. For most stops, waiting time keeps a relatively low level, but we can hardly observe a stop with an even lower waiting time. This is because IB reduces desynchronization risk when the user catches the bus, but it also makes people wait more time for these synchronized trips. In conclusion, too large (risk-averse) or too small (risk-seeking) buffers all impair the effectiveness of PT optimal, but too small buffers will especially result in desynchronization and suffer more waiting time.

The comparison moreover shows the difference’s highly polarized geographic and temporal patterns. Although PT optimal’s average waiting time is larger than ST’s, the variation of PT optimal is also larger. To moreover prove the variation, geographically, we divide the stops into two groups at stop “North High Street & Euclid Avenue” shown as a grey line in Figure 14; temporally, we divide the whole year by September 1st 2018. The results are shown in Table 2. Upstream stops and time after September had higher waiting time penalty, while downstream stops and before September had lower.

|  |  |  |  |
| --- | --- | --- | --- |
| PT optimal - ST waiting time difference (seconds) | Before Sep 1st 2018 | After Sep 1st 2018 | All year |
| Upstream stops | 1 | 117 | 68 |
| Downstream stops | -91 | 24 | -21 |
| All stops | -32 | 84 | 27 |

Table PT optimal – ST waiting time difference according to different spatiotemporal division

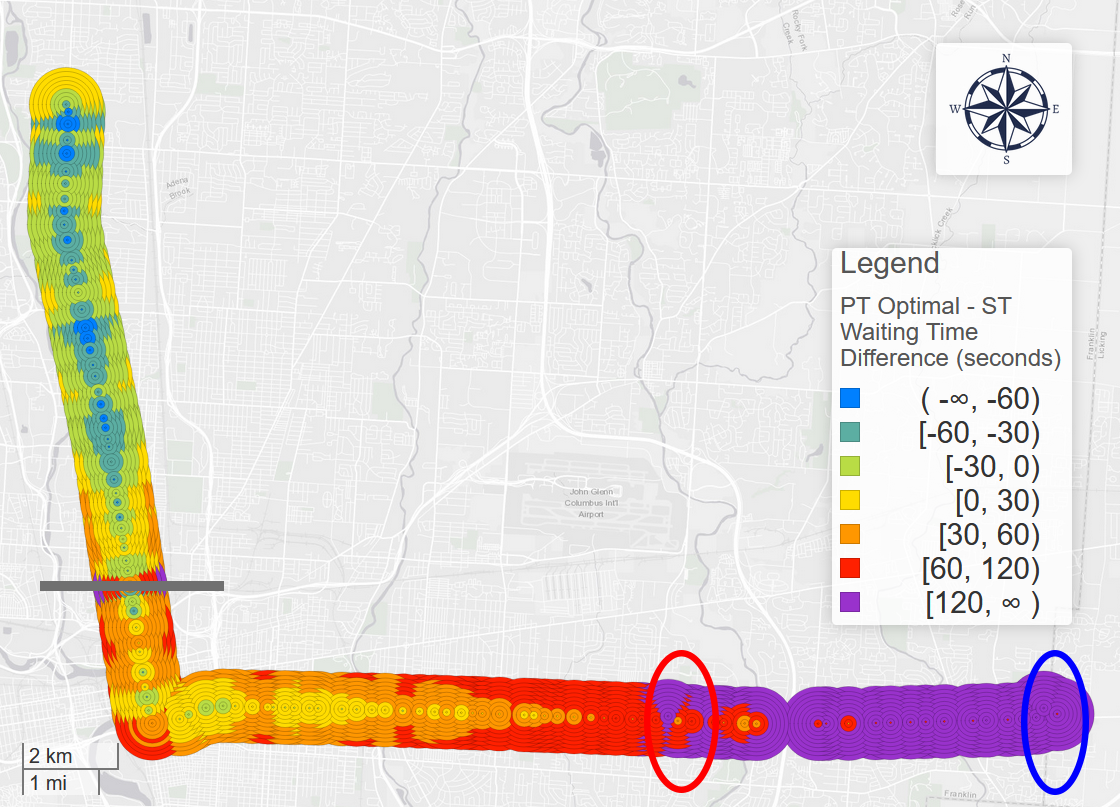


Figure PT optimal – ST waiting time difference for each stop and walking time in COTA bus route No. 2 from Southeast to Northwest in 2018.

* 1. Temporal patterns

In this section, we conducted several temporal analyses based on two resolution levels: day of week and hour.

**Day of week.** Figure 15 visualizes each TPS’s waiting time on each day of week. For non-ST TPSs, they share similar changing patterns: Weekends have the highest average waiting time and Wednesday and Thursday have lowest waiting time; the reason is that the headways of the weekends are much higher and schedules in the weekends are independent from weekdays. An extreme example is ET. Since Saturday’s schedule is totally different from weekdays and Sunday, it makes the learning process impossible thus leaving ET’s Saturday blank. However, for ST, Monday is the lowest and Sunday is the highest day.

Figure 15 each TPS's waiting time on each day of week.

Figure each TPS's missed risk on each day of week.

**Hour.** We also analyzed the hourly patterns for each TPS. Figure 17 visualized the hourly average waiting time for arbitrary tactic, scheduled tactic, empirical tactic, greedy tactic, and prudent tactic optimal. For high headway hours like 6:00 to 8:00 and 21:00 to 24:00, AT, ET, GT, and PT optimal all have higher waiting time, since the price of missing a bus will dramatically increase. Although the overall performance of the system during these hours is better than normal hours, on the contrary, users using these TPSs will not benefit but will suffer from buses’ large headway. This also suggests that delay is not the only and absolute standard to assess a system’s performance, instead, actual waiting time matters more since it is directly linked to the user’s experience. This is especially true in the context of real-time transit apps.

Like the global average waiting time, for most hours, the sequence is GT > AT > ET > PT optimal ≥ ST. However, there are several exceptions, especially for PT optimal and ST: for high headway hours in the morning and midnight, PT optimal’s performance is worse than ST’s; while for most hours during 8:00 to 21:00, PT optimal’s performance is almost the same as ST; especially, for afternoon hours from 17:00 to 20:00 with higher delay, ST user’s waiting time will increase thus PT optimal’s performance becomes better than ST. In this sense, it is generally better for transit users to follow scheduled tactic in the morning commuting and follow PT optimal in the afternoon commuting. This also suggests that PT optimal is more sensitive to the headway.

Figure 17 each TPS’s hourly average waiting time (range focuses on 0 – 1200 seconds).

Figure 18 each TPS's hourly missed risk.

**Headway.** As previous analyses suggest, headway is a crucial implicit factor for the performance of TPSs. The two temporal analyses also suggest two empirical rules:

* The larger the headways are, the *more* effective PT optimal is, compared to *arbitrary tactic*. This is obvious since AT’s waiting time is exactly the half of the headway. To moreover prove this, we investigated the correlation between the average waiting time difference in each hour and the average headway. The Pearson correlation coefficient is 0.9798 and the p-value is smaller than 0.0001. Figure 19 (left) shows the strong positive correlation between headway of each hour and the waiting time difference. Some former studies also suggested the same conclusion: in rural Scotland, RTI users can save 7 minutes in average (Papangelis et al., 2016), while in other studies in urban areas, the saved time is much less (Brakewood et al., 2014; Chow et al., 2014). RTI will flatten the radical waiting time difference between different systems caused by different scheduled frequencies.
* The larger the headways are, the *less* effective PT optimal is, compared to *scheduled tactic*. Likewise, we tested the correlation between the each hour’s average headway and corresponding performance difference. The Pearson correlation coefficient is -0.6201 and the p-value is 0.0012. Figure 19 (right) is the scatter plot of the two variables. The results show strong negative correlation between headway and the ST - PT waiting time difference.

Figure Scatter plots between Headway and AT/ST - PT optimal waiting time difference

1. Conclusion

Many papers have given empirical evidences that real-time information (RTI) and transit RTI apps can decrease transit users’ waiting time (Brakewood & Watkins, 2018). However, few studies systematically investigated the variance of this impact, including spatiotemporal patterns, mechanism of the impact, and optimized the system performance from users’ perspective. In this study, using GTFS real-time data, we first introduce the concept of trip planning strategy (TPS) and five types of TPSs for both RTI and non-RTI users. We also theorize and later validate the concept of reclaimed delay and discontinuity delay during the synchronization process between users and buses. Then, we optimize RTA users’ *prudent tactic* TPS with optimal insurance buffer. Based on different TPSs’ performance, we calculate the waiting time difference between different TPSs and conduct geographic and temporal analysis in different directions and resolutions. The analyses results show that PT optimal users in upstream stops will wait much more time than the ST users, and PT optimal users in this area may suffer from larger missed risk than ST users; also, temporally speaking, PT optimal users are more advantageous during 13:00 – 20:00 than ST users. All the results show that although RTI apps using PT optimal can indeed save time for certain users in certain stops and during certain hours, they cannot achieve global optimality. Moreover, greedy tactic’s performance is the worst among all TPSs despite it is RTI-based. GT’s performance is even worse than the arbitrary tactic. This moreover suggests that RTI apps could make users’ waiting time significantly longer if apps are not using the appropriate trip planning strategy.

The empirical results and the volunteered optimization system can provide vital information for transit users, planners, and real-time transit app providers. With more access to real-time data, transit system planning should not only engage with the schedule but also real-time performance; RTI apps development should not only engage with real-time performance but also empirical performance; passengers’ trip planning should not only engage with empirical performance but also all the information above. To achieve these three goals, future RTI apps should be able to combine schedule, real-time, and empirical information into one holistic information, with corresponding computation and networking support.

There are still numerous potentials in both academic and industry area. For example, to improve accuracy and reliability of the public systems and the RTI apps, transit authority or RTI apps providers can add pre-calculated insurance buffers to GTFS data so that RTI apps’ trip planning results inflect transit system’s empirical performance. Meanwhile, the optimization of prudent tactic is not fully explored, as there are unlimited numbers of methods to find the best insurance buffer. Unlike simple non-RTI strategies that can be conceptualized and calculated by human intuition from experience, RTI-based TPSs’ optimization processes should and can only be finished by the backend of the RTI apps, in which more complicated and effective algorithms can be applied. For example, with all the abundant auto-generated data, machine learning and neural network should be able to outperform traditional predicting algorithms.

Moreover, although individual passenger’s performance is systematically discussed in this paper, we do not investigate or simulate the proportions of each user group as Jolliffe & Hutchinson (1975) and Bowman & Turnquist (1981) contributed to the classification and simulation of three classes of passengers with different incidence behaviors. Future research may survey the different user group or the apps provides may disclose statistics of their users, so that RTI apps’ collective impact on the whole population could be calculated.

**Appendix A**

**Optimization problem of prudent strategy’s waiting time.**

We constitute the optimization problem in the following formula.

|  |  |  |
| --- | --- | --- |
|  |  | (13) |

Subject to:

|  |  |  |
| --- | --- | --- |
|  |  | (14) |
|  |  | (15) |
|  |  | (16) |
|  |  |  |

Where: is the actual waiting time for the user who lives walking time from the stop and intends to catch trip . is the collection of all trips, and is the stops on trip , is the designated walking time range. is the actual departure time of target bus, and is the actual arrival time at the stop for the user. is the expected waiting time as well as the insurance buffer. is the expected departure time of the scheduled bus.

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High-headway;

High-delay: works better.

Add utility.