

## Comments from the editors and reviewers:

### 1. Reviewer 1

This paper addresses a relevant topic and offers some insightful results. It does need however in my view to undergo substantial revisions before becoming suitable for publication. In the following, I note 9 comments which I consider major and thereafter list minor comments.

Major comments:

1.1. The paper is currently unnecessarily lengthy. I think the essence of the paper and its substance are such that do not require 16 figures and 29 pages. The paper requires some considerable trimming.

Will summarize later

1.2. The authors overstate their results. In essence, the obviously naive approach of planning to arrive the same second as the bus is expected to arrive can be expected to often (and even a majority of cases if there is even a slight systematic bias towards over-predicting the remaining time for arrival) result with missing the bus. I find the so-called the insurance buffer to be the more innovative element in this study. Note its affinity with the notion of 'hidden waiting time' which refers to a high (e.g. 95th) percentile of the expected distribution.

This is a fair comment. We cut down the size of the analysis part and only keep the essence of the results. We answer the questions raised by this comment in following aspects:

- Is it trivial to study the “naive greedy tactic”?

We also make some clarifications in our responses to the comment 2.1 and 2.7. We also add the corresponding explanations in the main text in [section](#).

Greedy tactic is the default tactic that many transit planning apps (for example, Google Map and Transit) suppose their users to use. The default scenario of using a transit planning apps is: the app will provide a home departure time / leaving time calculated from real-time data; many apps will not consider the risk of missing a bus during talking and use a greedy tactic to suggest leaving time. This means that many apps are expecting users to arrive the same second as the bus is expected to arrive. Meanwhile, if users do not realize the risk and choose to believe the results of the transit apps, this user will automatically use a greedy tactic. We think this is one of the contributions of the paper: transit apps which use greedy tactic to calculate their recommended home departure time are not trustworthy, and we provided a systematic way to prove this claim based on the actual real-time data the transit apps are using. We also added more justification in [section 3.4.4](#).

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1.3. Section 2.1 is redundant. I suggest the authors instead review the methods of quantifying the impacts of RTI on waiting times and thereafter report their findings. Also the relevance of the paragraph on surveys and their costs in 2.2 can be removed without any loss of information, unless the authors intend to specifically comment on those conducted in the context of RTI and waiting times.

This is a good suggestion and we removed the former section 2.1 and organize the literature review exactly as the reviewer suggested: we first review the methods of quantifying; we delete most discussions about the survey and move their costs to the corresponding studies in section 2.2 to make the discussion more relevant. We thank the reviewer again for the great suggestion.

We also added a new “Findings” section in section 2.2 to report relevant studies’ findings. We first discuss prior studies’ conclusions about the RTI’s positive impact on the perceived waiting time and actual waiting time. Then we discuss other conclusions that concluded RTI has limited impact on the perceived waiting time and actual waiting time. Finally, we continue the discussion by demonstrating the academic gap in this area and the motivation of the paper. We believe the literature review is now more complete and relevant to the topic of this paper with the useful supplements proposed by the reviewers.

1.4. The literature review I miss analytical approaches such as the studies performed by a study published in this journal ("Evaluating the added-value of online bus arrival prediction schemes") and a related study published in the Journal of ITS ("Real-time bus arrival information system: An empirical evaluation") by the same authors. These studies also considered the impact of RTI on waiting times along the line, as well as function of the prediction horizon which is equivalent to the analysis in relation to walking time performed in this paper. Moreover, the comparison with a waiting time resulting from following the schedule has also been performed. The authors should better acknowledge how their work relates to previous work.

Thank you for pointing this out. We added these very useful references to the corresponding part of our analyses:

1. We add “prediction horizon” to sections of the risk of missing bus and walking distance influence;
2. We also add the citation of the two papers in the real-time when comparing prudent tactic optimal and schedule tactic.

Meanwhile, it is also noteworthy that the contexts of this paper’s and the mentioned two papers’ analyses are - although relevant – but very different. A major difference is the headway. As mentioned in the second paper, the four studied routes have average headway of 4 -7 minutes, which are much more frequent than COTA bus (10 – 30 minutes, average 15 minutes). We also add this conclusion to our conclusion about the relationship between RTI’s effectiveness versus headway.

1.5. The presentation of the method can be dramatically shortened. GTFS and APC are by now very standard data sources in transit research. The notion of "reclaimed delay" is also not new. The impact of initial delays on running times further downstream has been extensively studied with conflicting evidence, see for example:

El-Geneidy, A. M., J. G. Strathman, T. J. Kimpel, and D. T. Crout. 2006. "Effects of bus stop consolidation on passenger activity and transit operations." *Transportation Research Record*

El-Geneidy, A. M., J. Horning, and K. Krizek. 2011. "Analyzing transit service reliability using detailed data from automatic vehicular locator systems." *Journal of Advanced Transportation*.

Cats, O. 2018. "Determinants of bus riding time deviations: Relations between driving patterns and transit performance". *Journal of Transportation Engineering*.

Similarly, departure strategies that have been reported elsewhere like AT can be described briefly.

Thank you very much for pointing this out and we found these literature very useful. The notion of "reclaimed delay" and arbitrary tactic are definitely not new.

1.6. The authors refer to measurement error and schedule recovery efforts as an explanation for an over-estimation of bus arrival time. Even in the absence of those, an over-estimation could simply result from traffic conditions including short signals and skipping stops (no boarding and alighting passengers).

This is a very useful complement and we changed the definition of reclaimed delay in section 3. We also considered these factors in our analyses and calculation. Therefore, we extended the concept of "reclaimed delay": we made it inclusive for driver accelerating and add the scenarios the reviewer mentioned.

The over-estimation scenario can be a major source but not the only source for desynchronization. We can categorize and decompose all sources into two classes: the first one is the measurement error, which does not come from the vehicle's performance change. The second one includes all the vehicles' performance change, including all the mentioned incidents and delays above. These errors can be detected by GTFS records during our calculation by calculating the arrival/departure time at each stop. In other words, we actually could not detect the exact reason from the buses' performance why the desynchronization happened; for example, we cannot distinguish whether it is because of the bus driver's accelerating or a short signal. But this won't affect the actual results shown in this paper.

The comment is very useful and important, so

1.7. A critical point is that IB is introduced only in PT but none of the other TPSs includes an element that is conscious of risk-taking. ST can also include an IB term, i.e. avoiding just missing the bus. This applies also to ET.

This is a good question. We also had this same question at the very beginning of this project. However, we decided to not put this part in the main text and not conduct the same analysis for

the scheduled tactic and empirical tactic. We are going to justify our decisions and discuss whether these analyses add value to this paper in following several aspects:

- What is the purpose of simulating non-RTI strategies and should we concentrate on these strategies?

We need to compare RTI-based trip planning strategies with non-RTI ones to measure their relative performance: whether the naïve greedy tactic can actually save people time compared to traditional ones and if the improved version can outperform them. We can draw two conclusions from this: first, the focus of this paper is still about RTI-based strategies, but non-RTI strategies are more like “benchmarks” as we mentioned in the paper. Second, because we want to compare the traditional strategies with the advanced version, we try to simulate what people will actually do in the real life, instead of an advanced version of these strategies. We will moreover argue why ST/ET with optimized buffers cannot be used by a “traditional user” in next section.

- Is the optimization process practical or meaningful in real life for ET and ST?

In real life, most people cannot perform very difficult optimization operations without any help from a computer. The two learning functions – maximum and average – and especially the maximum learning function are simple and practical for a normal passenger to perform independently. However, finding the optimal insurance buffer will take a lot of computational power and history data, which cannot be performed by a user who want to infer when the bus arrives based on her/his empirical impression or the schedule. Meanwhile, if considering investing computational power to conduct the same optimization of non-RTI strategies with a buffer time, it would be less meaningful since we can conduct the same optimization based on real-time information, which would exploit more information. The information media is also an issue: if this optimization result will be shown on a smartphone via Internet, why not just use real-time information?

- What is the purpose of the insurance buffer?

As we mentioned in the conclusion part, we add insurance buffer to take advantage of the benefit of empirical information to real-time trip planning process to improve its reliability. The insurance buffer will conclude the history performance of the buses; it represents the empirical performance of the bus system. However, empirical tactic also exploits the empirical information, which makes the insurance buffer less meaningful and duplicate.

Meanwhile, if applying the insurance buffer to both ST and ET, the optimal buffer found may be different but the performance will be the same. For example, for a certain stop and a certain trip, if the bus will arrive at 5:05pm and ST user (also the schedule) will arrive at 5:00pm and ET user at 5:06pm. The optimization process will find the optimal buffer based on empirical bus data, which are the same for ST and ET users. For example, the bus arrived at 5:03pm for the subsequent last 6 days, therefore the optimal buffer for ST users will be  $5:00 - 5:03 = -3$  minutes, while the ET users' is 3 minutes. However, they will both arrive at the stop at 5:03pm. Essentially, they are the same strategy with same performance and home departure time.

In conclusion, we think 1) it would be better to use ST and ET without further optimization to represent traditional users' behavior; 2) it would be better to concentrate on the RTI-based prudent tactic due to the theme of the paper. This is also consistent with the reviewers' suggestion that the last draft of this paper is unnecessarily lengthy, as more suggested contents by the reviewers are also added to the paper. We thank the reviewer again for raising the good question we also wondered and hope this answer will help solving this question.

1.8. Notations throughout the manuscript are sloppy. For example, introducing if definitions without indicating the value taken otherwise. There are also other matters, needs to be revisited carefully.

We reworked all of our notations and equations with simpler and more intuitive expressions.

1.9. Some of the conclusions may not be transferable, can the authors please reflect on that? For example, the performance of ST obviously depends on the on-time performance of the service under consideration (in particular, the share of early arrivals). The spatial pattern discussed in 4.3.3. is also clearly caused by the deterioration of the on-time performance further downstream.

This is a reasonable comment and we add the corresponding explanation in the paper. The representativeness and transferability issue is always a concern for any studies which use

- Performance of ST and on-time performance of the service.

This is true, scheduled tactic's performance does depend on the on-time performance of the service according to its definition. However, it is noteworthy that scheduled tactic usually has a very low share of early arrivals. We also made similar clarification in our response to the comment of 2.9. The risk of missing bus for scheduled tactic is the lowest among other strategies; and 6% is a rather low absolute value. Moreover, in COTA's official on-time performance policy, buses are not permitted to run ahead of schedule for normal buses (COTA 2019). Even if a bus leave 1 second earlier than the schedule, the bus is not considered "on-time". This is also followed by many other transit authorities (Bradley 2005; GCRTA 2018).

Meanwhile, the delay propagation from upstream to downstream is very common for different transit systems (Chen et al. 2009; Huo et al. 2014; Liu, Shi, and Qiu 2016). Therefore, although we cannot argue that the conclusions are universally applicable for any other transit systems, the conclusions are transferable for many. However, whether the conclusions introduced in this paper are actually applicable for other transit systems still requires the validation by further research based on actual real-time data in the system. We also add it to the possible future research directions.

- Spatial pattern of ST-PT optimal waiting time difference and its relevance with delay propagation.

The comment is a good suggestion and we add this to the section 4.3.3 to clarify the cause of the phenomenon. Besides delay propagation from upstream to downstream, the prudent tactic's bad performance in the low frequency section and relatively stable pattern in the high frequency section is also another reason. We thank the reviewer for the useful suggestion.

Minor comments:

1.10. Suggest to shorten the title. After the question mark can simply have only "An empirical analysis"

We change the title according to the suggestion.

1.11. TPS is mentioned in the last paragraph of Section 1 but has not been introduced yet

We remove all unnecessary acronyms, such as TPS, according to the reviewer 2's comment.

1.12. Add axes titles in figures 1 and 2

We add axes titles for Figure 1, 2, and 4.

1.13. Broken references in section 3.3

We fix the broken references. We thank the reviewer again for the effort.

1.14. Frumin and Zhao (2012) is not the original source for Eq. 3. Please refer to the original contributor.

We remove the equation to avoid confusions according to this comment and reviewer 2's comment 2.8.

1.15. The description accompanying Figure 3 is not sufficiently clear, please revisit.

This is a reasonable comment. We also see other questions from reviewer 2 about this graph. We add more clarification about this graph.

1.16. Please revisit also the last paragraph in the conclusions, it is not clear to me what is meant by this.

We reorganize the last paragraph.

## 2. Reviewer 2

This paper presents an analysis of a single bus route in Columbus, Ohio to explore the impacts of different passenger trip planning strategies, including those using real-time information, on passenger wait times. Overall, I found the manuscript to contain numerous noteworthy flaws. Specifically, the analysis relies on some unusual assumptions that may be driving the results; furthermore, the scope of the analysis is limited to a single bus route in a single city, limiting the generalizability of the findings. Moreover, the authors have not validated their theory and findings with real world behavioral data, such as from surveys or focus groups. In light of these weaknesses, I recommend significant revisions to the paper. My specific comments are detailed below corresponding to the page number (since there were no line numbers in the manuscript).

## 2.1. Page 2, Paragraph 3

How did the authors come up with the idea that RTI apps can diminish waiting times to zero? Have the authors conducted a survey/focus groups/interviews of riders to demonstrate that this “greedy” strategy is something riders actually do? Numerous prior studies of waiting times have been cited in the literature review section of this paper, and they all included reality high average wait times (e.g., Watkins et al. found 9.23 minutes for RTI users compared to 11.21 minutes for non-users). It seems unrealistic to expect riders to minimize their wait times to zero.

*This is a very good question and one of the very reasons we choose to investigate the RTI’s impact. We also mentioned the same issue in our response to the comment 1.2. We will respond the comment by following several sub-questions.*

- How did the authors come up with the idea that RTI apps can diminish waiting times to zero? Numerous prior studies of waiting times have been cited in the literature review section of this paper, and they all included reality high average wait times (e.g., Watkins et al. found 9.23 minutes for RTI users compared to 11.21 minutes for non-users). It seems unrealistic to expect riders to minimize their wait times to zero.*

It is all true and we made corresponding changes **in the text** to avoid confusion. As the reviewer mentioned in this comment and according to our results in the paper, RTI apps can never *always* diminish actual waiting times to zero and we did not suggest that they can. The “zero wait time” refers to its expected waiting time, instead of actual wait time in Watkins et al. “Zero expected waiting time” means: if everything does not change during the user’s walking and the arrival time keeps the same as the ETA when the user was scheduling the trip, the greedy tactic user’s waiting time will be zero. As the reviewer pointed out, this is clearly a very ideal scenario.

However, this greedy tactic is already adopted by many transit apps to calculate their suggested leaving time before this paper. We summarized the implied principles of greedy tactic and recreated the algorithm in this paper, but essentially the main purpose is to simulate how transit planning apps generally plan the trips for users, instead of creating a new algorithm or a new rule. It is very common for many apps (Google Map, Transit app) and open source trip planning projects (OpenTripPlanner) to assume and expect the user arrives at the exact second/minute when the bus arrives. There is no “waiting time” or “buffer time” in a trip suggestion in the interface of these apps; they will always show a suggested leave time, which is

the expected arrival time subtract the walking time. Therefore, there trip planning apps are essentially following the greedy tactic. Some of the reasons are:

- The naïve and simplistic nature of greedy tactic: it requires no optimization like empirical tactic or prudent tactic, which will reduce the calculation burden for the calculation in the fly. GTFS data is also naturally design for the calculation: all the ETAs are already pre-calculated by the GTFS provider.
- No optimization also means no warranty. Therefore, when people miss the bus, people will not blame the optimization algorithm.
- The temporary optimal solution: as we explained in the former “zero expected waiting time” part, in the moment of trip scheduling, greedy tactic can ideally achieve the 0 waiting time. If assuming the bus performance being stationary, this is the temporary optimal solution.

However, as we shown in the paper, because the future is unpredictable (reclaimed delay, including bus accelerating and short signals) and the updated data’s high interval (discontinuity delay), greedy tactic has a high risk of missing a bus, and missing a bus is highly penalized by longer waiting time. The empirical analyses also show that in fact the greedy tactic’s actual performance is very terrible.

- Have the authors conducted a survey/focus groups/interviews of riders to demonstrate that this “greedy” strategy is something riders actually do?

As we discussed in the last section of the response, greedy tactic is adopted by many transit apps to calculate their suggested leaving time. Many apps (for example, Google Map and Transit) assume and expect the user arrives at the exact second/minute when the bus arrives. If the user follows the suggestion of these apps, even if she/he does not realize the risk of missing the bus, the user is following the greedy tactic.

In this paper, what we did is to summarize the implied principles of greedy tactic and recreate the algorithm adopted by the apps. The main purpose is to simulate how transit planning apps generally plan the trips for users, instead of creating a new rule. In fact, this is one of the contributions of our paper as we define the greedy tactic in a strict mathematical manner, which is not explicitly discussed before.

As for the issue of whether people will actually follow the suggested greedy tactic:

- First, it is certain that some transit app users will follow the suggestion, because this is the default and primary trip planning strategy provided by the apps. This is especially true for some new app users who are not aware of the high risk of greedy tactic.
- Second, greedy tactic can be a very good benchmark to measure an upper bound of the performance, regardless of people’s actual usage rate. Greedy tactic is a special case of prudent tactic when the insurance buffer equals 0. As the most risk-seeking prudent tactic, it is important to investigate its performance.



Therefore, since many transit apps tend to use greedy tactic to calculate the suggested time, it is necessary and meaningful to investigate the greedy tactic's actual waiting time. We acknowledge the value of behavioral validation, however, as we indicated in the end of the paper, the behavioral validation by survey is a limit of this paper and a future direction of the research due to its length and exceeding contents.

For more clarification, please refer to our response to the comment 2.later.

## 2.2. Page 3, Section 2.1

The authors do not differentiate between perceived versus actual wait time differences in the literature review, which is an important distinction in prior research on the impacts of real-time information. Please add a brief discussion.

This is very good point and we distinguish the two measures in the literature review. We discuss the

## 2.3. Page 6, Paragraph 1

The authors claim that APC data is more accurate in terms of arrival/departure time at each stop compared to GTFS-realtime. I found this surprising. How did the authors come to this finding? What analysis did you conduct to demonstrate the accuracy? Additionally, did you verify a sample of the data with real world observations (e.g., ride the bus and manually record the stop times, then compare them to APC and GTFS)? Please justify.

This is another great question. Our foundation of using APC instead of GTFS is: GTFS real-time data is a regularly updated data, which means there is always an interval between the measured time and the actual event time. However, APC data is produced in an on-demand manner, which means the measured time is always the same as the actual event time. In conclusion, the recorded time of GTFS data may not be exactly the time when bus arrives at a stop, but recorded time of APC data is exactly the time of the bus arrival.

and we made several adjustments in the paper to avoid confusions.

Here, we are not discussing about the precision or accuracy in the spatial sense, such as the accuracy of GPS points. Here, we are referring to their *temporal accuracy*. Similar to Firmani et al. (2016)'s definition, we define it as: how accurate is the measure's recorded time compared to the actual time of event occurrence. It represents the systematic error caused by the temporal delay of measurement.

## 2.4. Page 6, Paragraph 2

COTA's data is updated once per minute, which seems quite long compared to many other agencies. For example, the MBTA in Boston updates their bus location data every 5 seconds (see <https://medium.com/@sjbarbeau/introducing-the-gtfs-realtime-validator-e1aae3185439>). This is likely an important data limitation from COTA that is driving some of your results (discussed more later). Please add discussion of typical update/refresh times from other transit agencies.

Page 17, Figure 7 (we merged the two comments due to their relevance)

- Figure 7 shows high sensitivity to the 60 second update of real-time data, which, as previously noted, seems to be a reality high value (e.g., the MBTA updates every 5 seconds). Is there a way you can test the sensitivity of this in your model? At a minimum, it should be discussed as a drawback of the case study of COTA, as it appears to be driving the results shown in Figure 7 and may not apply to other agencies with better real-time data.

This is a very good point. We address this issue in following aspects:

- An overview of some transit systems' GTFS real-time trip-update data updating frequency

Here we show the update frequency of all publicly available transit systems in the US that provide GTFS real-time feed from OpenMobilityData.org (OpenMobilityData 2020). We used the GTFS real-time validator (Center for Urban Transportation Research @ USF 2020) to measure the update frequency of each GTFS real-time feed.

Transit system	Update interval (secs)	Transit system	Update interval (secs)
MBTA	~5	Go Metro, Cincinnati	~30
Community transit	~10	DCTA, Denton, Texas	~30
CATA, Lansing, MI	10 – 20	VIA, San Antonio	~30
MST, Monterey, CA	10 – 20	HART, Tampa, FL	~30
RTC, Southern Nevada	10 – 20	LTD, Eugene, OR	~30
Votran, Daytona Beach, FL	10 – 20	Metro Transit, Madison, WI	~30
ART, Arlington, VA	20 – 30	MTA Maryland	~30
Big Blue Bus	20 – 30	RTA, riverside, CA	~30
Calgary Transit	~30	Capital metro	~60
BART	~30	CT Transit, Hartford	>60

Among 20 transit systems we could successfully test the update frequency, 12 of them have update interval larger than 30 seconds as of May 2020; in fact, MBTA is the only known transit authority that releases such high-frequency GTFS real-time trip-update data feeds in the United States. Moreover, in Google's official GTFS playbook webpage, the GTFS real-time data is

expected to have update frequency around 1 minute (Google Developers n.d.). These statistics shows that the majority of the transit systems in the United States still face non-trivial continuity delay in 2020 large than 30 seconds; the discussion of impact of long update interval larger than 30 seconds is still important for most transit systems.

Moreover, these statistics were calculated in May 2020. Each transit system will gradually increase the update frequency with better equipment and more experience. For example, we know from COTA that they has upgraded the update frequency for the recent two years. Therefore, it is very likely that many transit systems had a larger update interval back in 2018.

- The actual data update frequency of the transit planning apps

What users see on their smartphones are not the trip-update data, but results generated by the transit planning apps. The update frequency of the GTFS real-time data is different from transit planning apps update frequency. Several examples can be given by using the Transit app, which is a popular transit planning app with millions of users. We used a regular Android phone and an iOS tablet to randomly select several routes and different time in a day for testing purposes. We observed the information update frequency on the interface is lower than the data per se. For example, MBTA, the transit systems with the highest update frequency, can still have update intervals from 15 seconds to 1 minute for most routes shown on the actual smartphone app interface, despite theoretically the data are served every 5 seconds. We also witnessed similar phenomena in Capital Area Transportation Authority (CATA) in Lansing MI and Monterey–Salinas Transit (MST) in Monterey, California. This suggests that the actual information update can be lower than the ideal data update frequency.

Meanwhile, some transit planning apps, such as Google Map, will not update the information automatically; instead, the visualized RTI will only update when the user actively refreshes the interface. This moreover suggests that the actual information update frequency can be even longer if the user does not actively update.

- Further implication of higher update interval

Despite the large interval is still common for most transit authorities, the question raised by the comment is still important, because we will witness more transit systems with GTFS trip-update data of higher update frequency in the near future. Meanwhile, as the reviewer mentioned, Figure 7 (Figure XXX in current version) surely depends on the frequency of the RTI. For the mainstream update frequency of 30 seconds, the interval in the figure between each valley will become 30 seconds. However, as for COTA system, we could not get data of different resolution for the same time period, therefore the potential impact of higher frequency still remain largely unknown. It could be a limitation for this paper and could be a very good topic for future studies. We also clarify this in the conclusion part of the paper.

The authors make the assumption that the walking process “is linear with respect to distance.” They later explain that the only way to change the walking time is to depart the home at a different time. However, the assumption of constant walking speed seems highly unrealistic. If a rider sees a bus approaching and they think they might miss it, they are very likely to speed up and potentially even run to meet the bus. Indeed, a study by Dziekan and Kottenhoff (2007) of the subway in Stockholm, Sweden observed passengers entering subway stations and counted the number of passengers running and walking when RTI signage outside the subway station was on, and the results reveal that significantly more people run when the RTI signage was on rather than when the signage was off. In light of this real world evidence, the assumption of constant walking speed seems very unrealistic, and the authors should test the sensitivity of their results to altering this assumption.

Thanks for pointing this out. There are several reasons that we chose to use linear walking process and insurance buffer ahead as the primary assumption:

- Running is not a viable and desirable option for everyone.

Running after seeing the bus approaching can be possible for some younger people, but it is not viable for other passengers such as senior people, disabled people, people with luggage, and parents with children. And the obstruction of buildings and trees, the condition of pavements, and the weather all make running a less likely option for most people. Even if a passenger can run to the stop, compared with planning an insurance buffer ahead, passengers may find it exhausting, stressful, and thus undesirable.

- Running should not be and is not the default assumption for transit planning apps.

Because running is not a viable option for many people, the transit planning apps’ planning logic should not naturally assume everyone should do that. In fact, most transit planning apps will not suggest a “running” phase or suggest people when to run during the walking phase when planning the trip. Therefore, since we are simulating the results provided by the actual transit planning apps and the behavior of people using these apps, we will not primarily assume people and apps will do this.

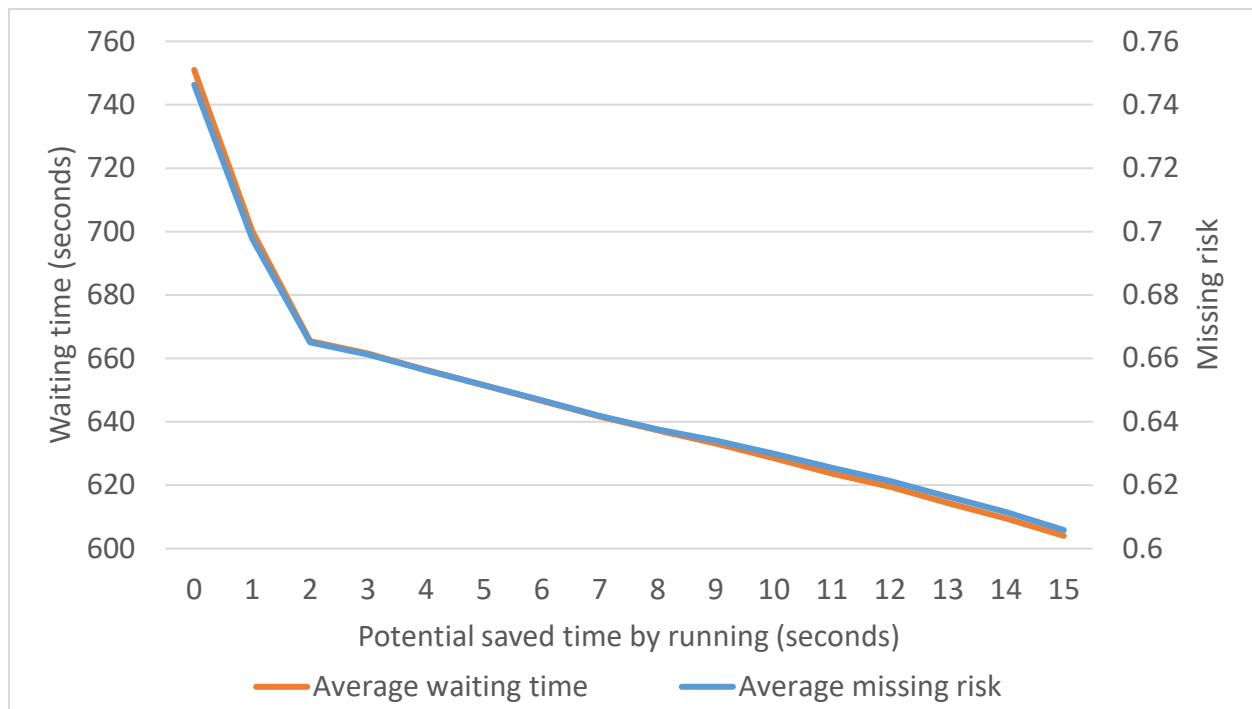
- Sensitivity analysis shows that running is not the primary solution to the bad performance.

However, we know some people will accelerate after they see the target bus approaching and some buses will wait for the passengers when the driver sees the passenger. Therefore, per the reviewer’s suggestion, we added an analysis to test the sensitivity of greedy tactic’s waiting time and missing risk.

We first need to determine a good range of sensitivity buffer to relax the walking time, i.e. how many times the user can save the walking time by running. However, this saved time cannot be too long for two reasons: first, humans cannot run significantly faster than the usual walking speed; and second, the average sprint distance cannot be very long, since the obstruction of buildings and trees usually won’t allow the passenger to see a bus in a very long distance and the route number on the bus usually is undistinguishable. We use the average speed of 3 m/s as the

running speed (Chertoff 2018). We consult the letter height visibility table (James 2017); for a route number on a regular US bus of 20 cm (7.8 inches), the ideal readable distance is about 21 (70 feet) – 24 (80 feet) meters. We will use 24 meters as the sprint distance. In our study, we use 1.4 m/s the standard walking speed for all the calculation. Therefore, the maximum saved time is  $24/(3-1.4) = 15$  seconds. We conducted the sensitivity test based on the extra 0 - 15 seconds during the walking phase. For example, if the saved time by running is 5 seconds, this means that the user will arrive 5 seconds earlier than a normal greedy tactic user at the same stop.

Picture 1 shows the waiting time and missing risk with different potential saved time by running from 0 – 15 seconds. For the maximum potential saved time by running of 15 seconds, the average waiting time is 604 seconds and the missing risk is 60.58%. It shows that even considering the maximum possible saved time by running, the greedy tactic’s performance is still bad; in fact, it still has the highest average waiting time and highest average missing risk among all other trip planning strategies in the Table 2 (currently Table 1) in the paper.



Picture 1: waiting time and missing risk with respect to different potential saved time by running from 0 – 15 seconds.

Therefore, we can conclude that: 1) running is not a viable and desirable option for everyone; 2) running should not be a default option for trip planning apps; 3) even if considering maximum possible running time, the greedy tactic’s performance is still the worst among the all trip planning strategies. Not running is not the cause of the bad performance of the greedy tactic. Instead, its bad performance results from: 1) the optimal scenario (waiting time = 0) is a fragile balance that even a small time shift can make the user miss the bus and wait a very long time; 2) the reclaimed delay and discontinuity delay, as we extensively discussed in our responses and the paper.

2.6. Similar to the previous comment, another recent study by Ferris et al. (2010) found that RTI provided on mobile devices may impact a passenger's decision of where to board the transit vehicle, which would impact the passenger's walking distance to access transit. On a survey of RTI users conducted in Seattle, Washington, 78% of respondents reported they were more likely to walk to a different stop based on RTI (Ferris et al., 2010). Can the authors test this (e.g., changing where to board) in their modelling framework?

The impact of RTI on passenger's path choice is a very important. In this answer, we are going to conceptualize and simulate the decision-making process and investigate if this strategy is rational.

- Conceptualization

First, we will discuss about the motivation of walking to another stop. A major reason of changing stop is that by walking to another “downstream” stop, the passenger can arrive earlier by taking advantage of the bus running time between the two stops as shown in Picture 1. For example, a bus will arrive at stop A at 5:00 pm and stop B at 5:05pm, and passenger will leave the home at 4:55am but it will take the user 6 minutes to walk to stop A. Therefore, if the passenger sticks to stop A, she/he will arrive at 5:06pm thus miss the bus. However, the passenger knows that it takes she/he 8 minutes to walk to stop B and when the passenger arrives at B the time will be 5:03pm, thus the bus won't be missed. Therefore, if the user can outperform the bus by going to an alternative stop, then it is possible to save time by catching the bus which should have been missed at the original stop.

However, we need to compare the walking time difference and bus running time difference to validate if this strategy can indeed save time. We first give the definition of the walking time difference:

$$\Delta t = \frac{x_a - x_o}{v} \quad (1)$$

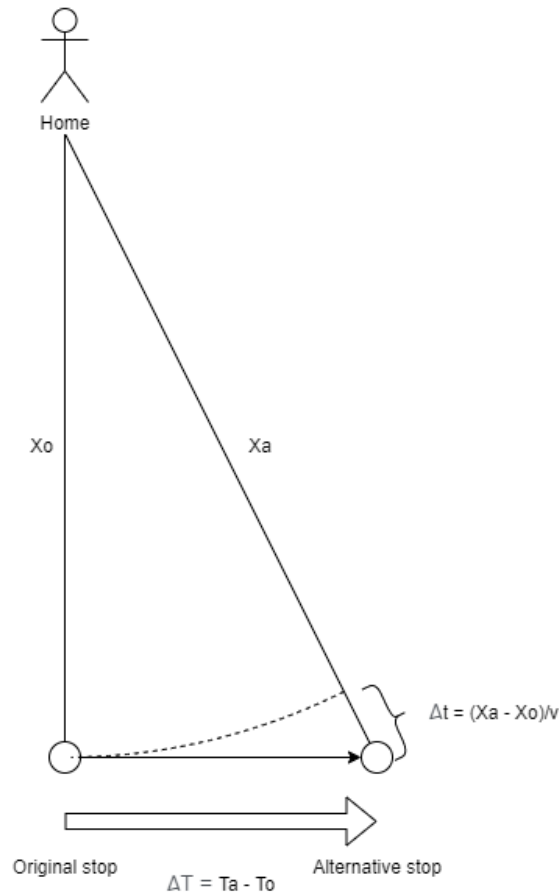
Where  $x_a$  is the distance between home and alternative stop,  $x_o$  is the distance between home and original stop,  $v$  is the walking speed (1.4 m/s).  $\Delta t$  represents the time cost caused by the route changing. Meanwhile, the saved bus running time  $\Delta T$  is:

$$\Delta T = T_a - T_o \quad (2)$$

Where  $T_a$  is the arrival time at the alternative stop and  $T_o$  is the arrival time at the original stop. This will be derived from the history arrival time in the GTFS-APC data. Then we derive the potential saved time:

$$\delta t = \Delta T - \Delta t = T_a - T_o - \frac{x_a - x_o}{v} \quad (3)$$

If the potential saved time is positive, then this says this strategy will save time for the passenger. For the same example above, the saved bus running time  $\Delta T$  is 5 minutes and walking time difference  $\Delta t$  is 2 minutes, therefore the potential saved time  $\delta t$  is 3 minutes and the user will save time.



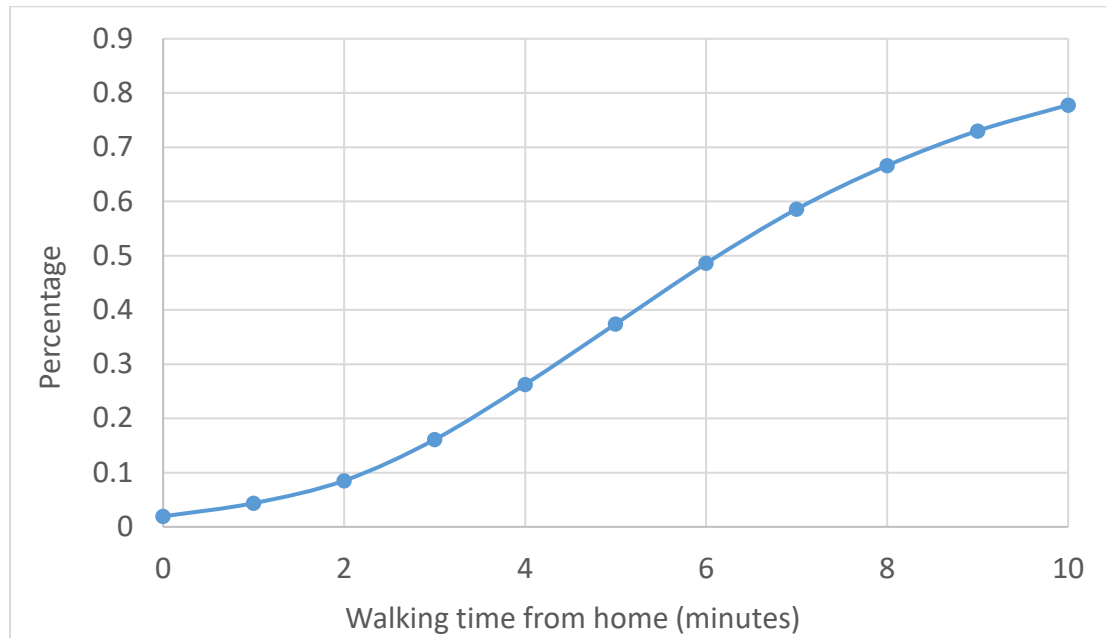
Picture 2: presentation of “walking to another stop” strategy.

Therefore, an important topic about the question raised by the comment is: how often can this strategy save user time in the COTA system? If the empirical data can prove that this strategy can instead save time for passengers, it can justify and validate the behavioral changes reported by prior research. Therefore, we calculate the potential saved time for each stop and its subsequent downstream stop and summarize the ratio of positive potential saved time. We will test the start locations on the perpendicular line from the original stop with different walking time, from 0 to 10 minutes.

For two subsequent arbitrary stops on a route, we will only consider the positions between the stops. For example, in Picture 1, we will not consider the points to the left of original stop or the points to the right of alternative stop, since passengers who live at these points will have an even closer stop in the upstream or downstream and current two stops will not be the closest two stops.

- Results

Picture 3 shows the ratio of positive potential saved time for different walking time from home. It shows the effectiveness of this strategy highly depends on the distance from the home. If the passenger lives very close to the stop, she/he does not want to go to another stop because people's walking speed is much slower than the bus. Meanwhile, if the user lives further from the stop, the changing stop strategy is more effective therefore more people will be prone to do that. This can be a very good supportive proof for the conclusion mentioned by the reviewer based on empirical data.



Picture 3: ratio of positive potential saved time for different walking time from home.

However, this paper concentrates on waiting time instead of path choice. Although the conclusion will definitely add value to the paper, we will present these results in the appendix, considering the already lengthy main text. We thank the reviewer again for the useful comment.

## 2.7. Page 9, Table 1

How did the authors arrive at these 5 trip planning strategies? Similar to my previous comment, have the authors conducted a survey/focus groups/interviews of riders to demonstrate that these are strategies riders actually use?

Thanks for pointing this out. We will revisit each trip planning strategy (TPS) one by one to argue that each of them is actually used by people without conducting a dedicated inductive



survey for justification of using these trip planning strategies. We will prove our point by deductive reasoning.

- Non-real-time trip planning strategy (Schedule, arbitrary, and empirical tactic)

Schedule tactic are the default trip planning strategy that how people will use public transit. Transit system has schedule and people are expected to follow it. It is most certain that people will use this. Arbitrarily leaving home for buses is also another very common TPS, if not the most common. It is most certain that people will use arbitrary tactic. People will memory the historical arrival time and find the earliest one or the average to decide when they will leave for the bus. It is also most certain that people will use the empirical tactic. Non-real-time trip planning strategies' usage is well proven by the common sense and daily experience.

- Greedy tactic

We justify the investigation of greedy tactic in this paper in several aspects:

First, as our responses to the comment 2.1 point out, greedy tactic is adopted by different trip planning apps and algorithms and we are not the first one to come up with it. It is common for the suggested trip plans generated by the apps to follow greedy tactic. Therefore, we can confirm that some people will follow the suggestions thus use the greedy tactic by deductive reasoning. We believe these facts and deduction can be a good evidence to answer the question raised by the reviewer about whether people will use greedy tactic: some people will surely follow the suggestion, although it is largely unknown about the exact ratio of these people.

Second, the necessity of investigating the performance of greedy tactic does not lay on whether or how many people use it. The fact that many apps, especially the most popular ones, adopted this strategy is our primary motivation to measure its performance. Just like what we asked in the title: does real-time information (and real-time information apps) reduce waiting time? If apps and current popular trip planning algorithms are systematically suggesting a trip plan with very poor performance based on real-time information, it is extremely necessary and important to measure its performance, including how bad it is and how bad it can be compared to other traditionally used non-real-time trip planning strategies. Moreover, it would be valuable to find a good way to improve the algorithm. All of these will be based on the investigation of the greedy tactic.

- Prudent tactic

Similar to greedy tactic, there are some facts supporting the actual usage of prudent tactic. We will justify our endeavor to investigate prudent tactic in following aspects:

First, users can actively use prudent tactic. As we mentioned in the section 3.4.5, it is a common strategy to avoid risk of missing a bus by leaving earlier than the suggested time. This is especially true for two kinds of people: the experienced users and users who are less familiar

with the transit system, such as tourists and new residents. Experienced users will notice the unreliability of the suggested time thus leave earlier. New users will feel more insecure thus leave earlier than the expected time to avoid risk.

Second, users can passively use prudent tactic. We mentioned in the paper that greedy tactic is a special case for prudent tactic with insurance buffer = 0. We already demonstrate most apps' default trip planning strategy is greedy tactic; therefore, any trip plan that the user chooses to use is a special form of prudent tactic. For example, if the suggested leaving time by the app using greedy tactic is 5:00pm and the user chooses to leave at 4:58pm, even if the person has no specific intention to plan an exact insurance buffer, the plan that user uses is in fact prudent tactic with buffer = 2 minutes. In this sense, people will certainly use prudent tactic, as long as they consult the real-time data and have an offset before the suggested time. This process can be perceived as a very primitive and coarse prudent tactic; and it is also why we should systematically discuss a more advanced version with well-optimized insurance buffers for specific time and space.

Last, just like greedy static, the necessity of investigating the performance of greedy tactic does not lay on whether or how many people use it. As we discussed in first two reason, for transit systems and app providers, it is extremely important to consider the performance retrospectively and provide an alternative and improved solution to the current greedy tactic. In this paper, we introduce prudent tactic and the prudent tactic optimal. It is certain that the prudent tactic optimal won't be used by anyone right now, but it would be better than the greedy tactic. And if current apps can adopt our solution or develop better solution to solve the insurance buffer and use them as the algorithm to generate suggested route, more people will benefit from this.

In conclusion, from the facts, common sense, and published results that we know, all tactics are indeed used by at least some people. For certain variety of prudent tactic and the prudent tactic optimal, we are sure that no one are using it right now and this is the very reason we are proposing a new algorithm: people will benefit from using it as it is adopted by more apps thus more passengers. On the other hand, it can be a very good potential for future studies to expand the topic to the inductive perspective, because the quantitative composition of users' trip planning strategies is still largely unknown, even if we can infer that people are using them. We thank the reviewer again for providing a useful insight.

## 2.8. Page 10, Equation 3

- It should be noted that the average waiting time formula for random arrivals is generally only applied to high frequency transit routes (e.g., headways less than 10-15 minutes).

This is very true for formula 6 and [we added relevant clarification](#). However, we only give formula 6 to introduce the traditional calculation method. We did not use headway and its

standard variance in our calculation. This is one of motivation to use the high-resolution data without major stochastic assumptions. The actual formula we were using is formula 7: we will find the bus before the targeted bus and produce the average of the two buses' time.

## 2.9. Page 3, Equation 5

- The authors state that the “bus will rarely if ever leave a stop earlier than the scheduled time.” Did the authors verify this statement empirically, such as comparing the GTFS schedule to GTFS-realtime? Drivers occasionally do run “hot.” Please justify the assumption that they don't.

Thanks for pointing this out. We did not assume that buses never run “not” in our calculation. The best answer to this question must be that we present a risk of missing bus for the schedule tactic. The missing risk of schedule tactic represents the chance for buses to leave earlier than the schedule, which is exactly the scenario of “running hot”. From table 2 in the main text, we can see that the mean of schedule tactic's risk of missing bus is 6.28%. If we assume no buses will run “hot”, the number will be 0.

As for the authenticity of this claim, the risk of missing bus is the lowest among other strategies; and 6% is a rather low absolute value. Moreover, in COTA's official on-time performance policy, buses are not permitted to run ahead of schedule for normal buses (COTA 2019). Even if a bus leave 1 second earlier than the schedule, the bus is not considered “on-time”.

## 2.10. Page 11, Figure 3

- What data was used to create the visualization shown in Figure 3?

We implemented the empirical tactic of different memory and calculate the performance based on the same GTFS-APC data we collected. We did not use an external data source or reference. [We added relevant clarification in the main text.](#)

## 2.11. Page 13, Equation 9

- The authors state that “for PT family, insurance buffer should be at least equal to the expected waiting time.” Please explain why this is the case. It wasn't clear to me.

## 2.12. Page 14, Last 2 Paragraphs

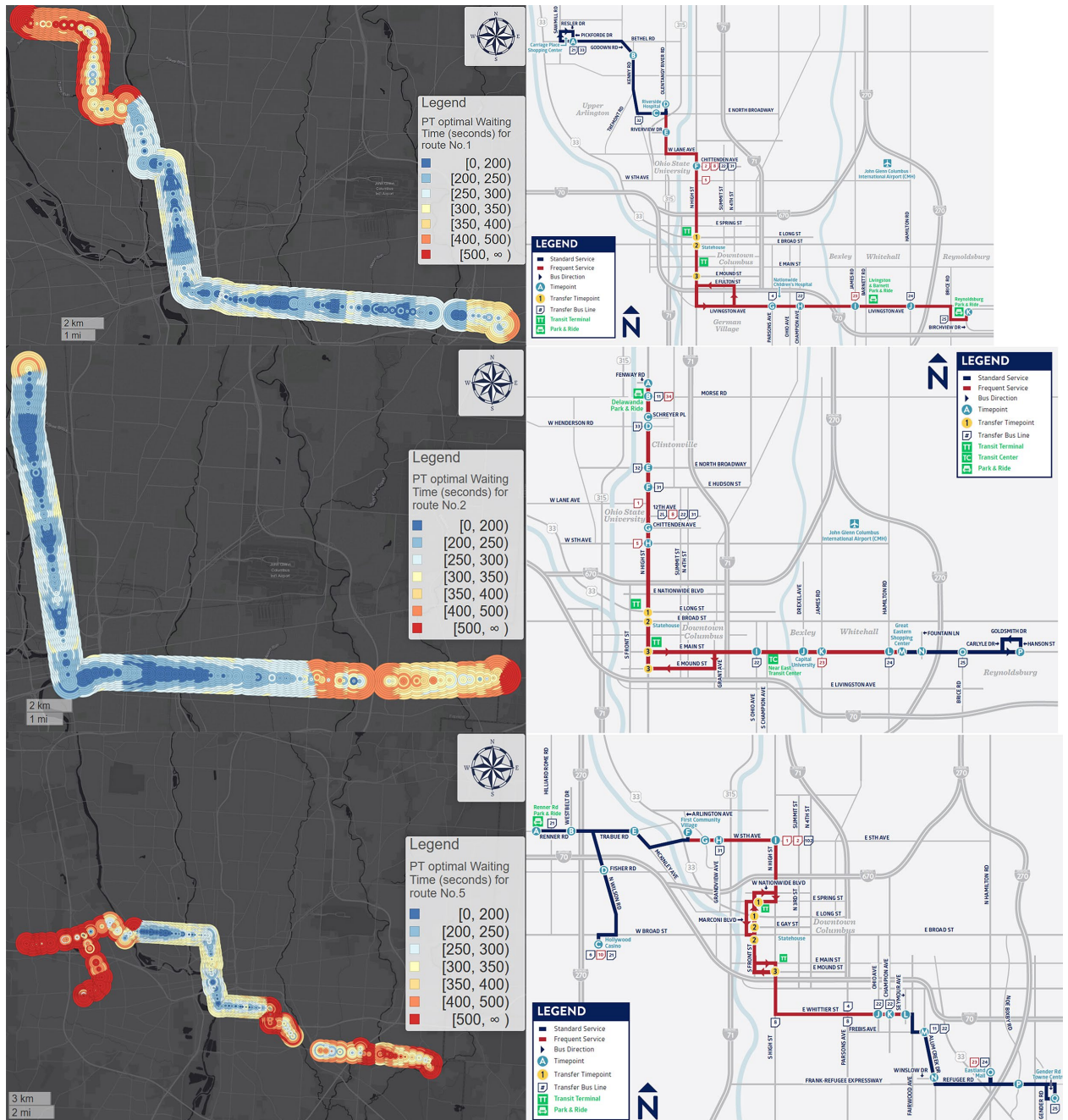
- The authors state that there is a large computational burden to conduct the analysis, so they only selected one bus route for the analysis. This greatly limits the generalizability of the research. Instead of using 1 year of data, why not use 1 week of data and run the analysis for multiple bus routes? I strongly encourage the authors to consider a larger geographic sample.

Thanks for mentioning this. This is a very important question about the representative of route No.2. The core question is: will the selected bus route 2 limit the generalizability of the research?

In this response, we select 6 representative major routes: COTA route 1, 2, 5, 7, 8, and 10. All of these routes have different directions and different and wide spatial and temporal coverage in the City of Columbus. Just as the reviewer suggested, we select the time period from a typical week from 7/15/2018 – 7/21/2018, when there was no major event like football games and extreme weather.

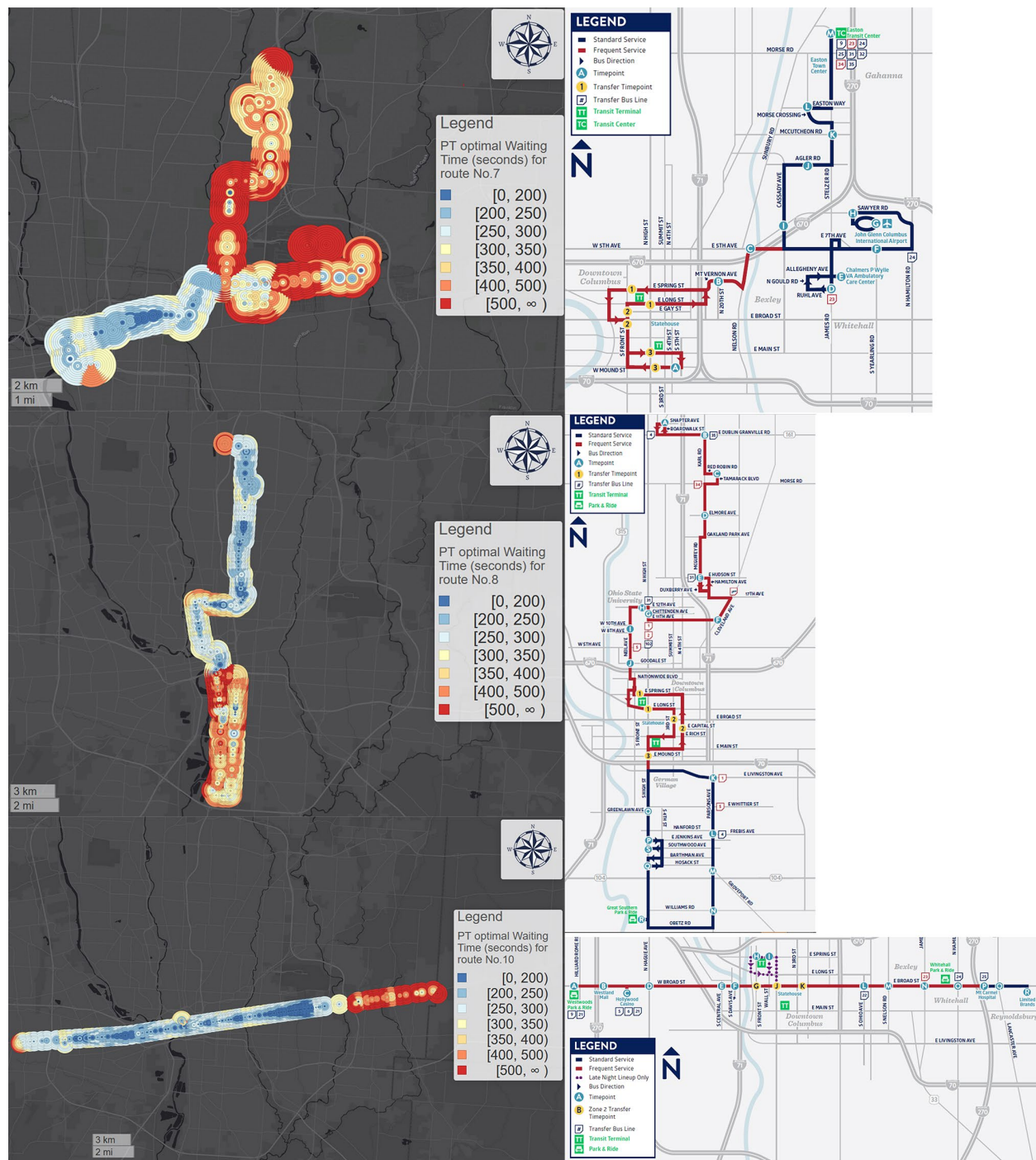
We reproduce the optimization of prudent tactic for each route, which is the core contribution of the paper as reviewer 1 pointed out and have the most heterogeneous spatial pattern. Picture 4 and Picture 5 show the six routes' prudent tactic optimal's waiting time. We can see the spatial distribution of the waiting time is highly similar for different routes: the standard service sections (blue part in the service maps to the right) have higher waiting time while the sections with frequent services (red part in the service maps) have lower waiting time. All the maps have same increasing pattern as the walking time (radius of the concentric circles) increases, as we extensively discussed this in the section of walking time impact. This similarity is not limited to the distribution, but also the specific values of the waiting time. Note the maps have same color schemes.

Therefore, we can conclude that bus route No.2 is a good sample of the whole COTA bus system and selecting it as the research target will not compromise the generalizability of the research. Moreover, analyses based on longer time period is more generalizable and provide more robust conclusions. **However, the question is still worth investigating and we add corresponding clarification in the section of XXX. We also add the** Picture 4 and Picture 5 to the appendix for readers' reference, since the representativeness of the selected route is an important and common question.



Picture 4: Route 1, 2, and 5's PT optimal's waiting time and route map.





Picture 5: Route 7, 8, and 10's PT optimal's waiting time and route map.

- I found the GT results counterintuitive, and I would have expected them to be similar to the PT results. I suspect this is likely due to the assumptions built into your models (e.g., constant walking speed so riders won't run for an approaching bus and the long 60-sec threshold of real time updates).

Yes, it is counterintuitive, however, we show that this counterintuitive phenomenon is justifiable. We explain that 60% of US transit system still have non-trivial update interval larger than 30 seconds, and MTBA is actually the only transit system that provides such as high frequency in US in our responses to the comment 2.4. We also explain why running is not possible for many people and should not be a default assumption for trip planning apps in our responses to comment 2.5. *The sensitivity test also say a lot of things.* This is the main contribution of the paper: we prove that the current algorithm has a very bad performance.

On the other hand, the poor performance of greedy tactic does not mean that real-time information is 100% useless. The majority of the problems are due to the naïve trip planning strategy and, just like the reviewer pointed out, the low update frequency. This is the second main contribution of this paper: we summarize the definition of prudent tactic and insurance buffer and introduce a systematic and sustainable method to optimize the insurance buffer. By using a better and adaptive trip planning strategy which combined the advantages of real-time data and empirical analyses, we can make real-time information more useful for passengers in future.

2.14. Page 22, Figure 13

- For the route shown in Figure 13, how many timepoints are there along the route? Where are the timepoints located? How do the timepoints relate to your findings (in this figure and the subsequent maps of the route)? Please add a discussion of timepoints.

*Will do*

2.15.

- For Figure 13, please make sure the colors in the legends correspond to the same numerical values. It is difficult to compare GT with ST, AT and ET since the ranges for the colors are different. This comment also applies to subsequent figures.

*Will do*

Minor Comments

2.16. On page 9, please fix the reference errors to the figures/tables.

Will do

2.17. The authors introduce many new acronyms throughout the paper, which can be confusing for readers. Please try to limit the use of acronyms that are not commonly found in the prior literature (e.g., consider removing IB, TPS, HDT, etc.).

Will do