Heuristic Analysis

tournament.py modification

The file `tournament2.py` is copy of `tournament.py`, and is changed in following ways:

- Increase NUM_MATCHES from 5 to 25, so more matches will be done to improve banchmark accuracy.
- Remove `ID_Improved` from test_agents, since `ID_Improved` is only needed to run once to get it's performance value.

Heuristic functions

ID_Improved (given)

`ID_Improved` calculate the number of available move of 2 players, and minus them to get the score.

The `tournament2.py` result is as follow:

```
***********************
 Evaluating: ID_Improved
***********************

Playing Matches:
----------
  Match 1: ID_Improved vs   Random      Result: 89 to 11
  Match 2: ID_Improved vs   MM_Null     Result: 73 to 27
  Match 3: ID_Improved vs   MM_Open     Result: 57 to 43
  Match 4: ID_Improved vs MM_Improved   Result: 54 to 46
  Match 5: ID_Improved vs   AB_Null     Result: 64 to 36
  Match 6: ID_Improved vs   AB_Open     Result: 64 to 36
  Match 7: ID_Improved vs AB_Improved   Result: 57 to 43


Results:
----------
ID_Improved          65.43%
```
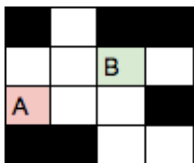
	Random	MM_Null	MM_Open	MM_Improved	AB_Null	AB_Open	AB_Improved	Result
ID_Improved	89	73	57	54	64	64	57	65.43%

custom_score_0 (Improved ID_Improved)

The `custom_score_0` put n moves forward into consideration.

For example, in a 4x4 game:

We first do breadth first search to find the number of move required to go to each cell, in empty board.

Since the calculation is based on empty board, the result can be cached to save CPU.

Then, for each cell which require n moves, we score it r_0^n.

For $r_0 = 1/8$:

Finally, we sum up all cell which is not blocked, and subtract each other.

- Player A: value = 0.316
- Player B: value = 0.193
- score = 0.316 - 0.193 = 0.123

The `tournament2.py` result is as follow:

r_0	Random	MM_Null	MM_Open	MM_Improved	AB_Null	AB_Open	AB_Improved	Result
1/2	88	79	63	60	71	65	66	70.29%
1/3	91	82	68	60	77	67	63	72.57%
1/4	90	83	67	67	82	69	59	73.86%
1/5	86	79	70	63	75	67	68	72.57%
1/6	90	84	76	64	83	77	74	78.29%
1/7	87	79	74	74	77	75	72	76.86%
1/8	90	80	71	61	83	68	68	74.43%
1/9	88	86	64	67	86	75	69	76.43%
1/10	90	87	74	68	85	75	68	78.14%
ID_Imp	89	73	57	54	64	64	57	65.43%

It is better than `ID_Improved`.

custom_score_1 (Neural network)

The `custom_score_1` is based on neural network and minimax Q learning.

First, we convert the 7x7 game data into 7x7x3 = 147 boolean value. The first 7x7 boolean value represent which cell is not blocked. The second 7x7 boolean value represent the location of active player. The third 7x7 boolean value represent the location of inactive player.
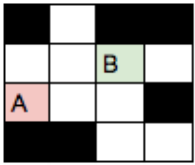
becomes

Then we put the values into 3 hidden layers neural network, which represent the score of 8 move. We apply boolean mask to filter out impossible move.

Score of move a_0 in state s_0:

```
Q(s0,a0)
```

The score of state s_0 would be:

```
max( Q(s0,a0) for all a0 )
```

The neural network is trained by following equation:

```
Q(s0,a0) = -1                                   if loss
         = +1                                   if win
         = - gamma * max( Q(s1,a1) for all a1 ) otherwise
```

Since the Q function return the score of the active player, and the second move is made by opponent, the right hand side of the equation should be negative.

Step of training:

1. Make 100000 moves
2. Train upon 1-100000th move
3. Make 100001st move
4. Train upon 2-100001th move
5. Make 100002st move
6. Train upon 3-100002th move
7. continue...

The `tournament2.py` result is as follow:

moves	Random	MM_Null	MM_Open	MM_Improved	AB_Null	AB_Open	AB_Improved	Result
200000	88	72	52	44	75	53	47	61.57%
300000	88	80	58	53	75	63	51	66.86%
400000	88	78	61	47	70	57	54	65.00%
500000	90	81	61	55	75	54	56	67.43%
600000	88	80	60	55	79	60	51	67.57%
700000	82	77	53	56	80	63	50	65.86%
3760000	90	75	51	54	74	55	45	63.43%

The result is disappointing. The result does not grow in training.

In order to improve performance, complexity of the neural network should be increase. For example, apply convolution layer, and add more feature to input data set. More CPU / GPU time should be required.

Moreover, the trained neural network can be used only in game same as training game. For games which have difference size, it is necessary to train another neural network.

The `custom_score_1` require TensorFlow to run.

custom_score_2 (Distance from center)

The output is the distance between player location to the center. Since we are not sure it is better to stay at center or edge, so we make 2 opposite functions to verify.

- version 2a: Self distance - Opponent distance. Stay on edge will get higher score.
- version 2b: Opponent distance - Self distance. Stay in center will get higher score.

	Random	MM_Null	MM_Open	MM_Improved	AB_Null	AB_Open	AB_Improved	Result
2a	82	73	60	48	64	60	49	62.29%
2b	87	65	62	49	72	56	59	64.29%

The agent is weaker than `ID_Improved`.

The difference is so small that we cannot tell which strategy is better. So we reduce the search_depth to 1 to verify.

	Random	MM_Null	MM_Open	MM_Improved	AB_Null	AB_Open	AB_Improved	Result
2a	37	11	6	7	12	8	8	12.71%
2b	78	54	21	22	43	24	27	38.43%

Now we can see in depth 1 search, stay in center is better than stay in edge. The discovery can be used in building better agent.

custom_score_3 (custom_score_0 + custom_score_2)

custom_score_3 combine custom_score_0 and custom_score_2b by adding them up.

custom_score_3b = custom_score_0(r=1/6) + r3 * custom_score_2b

r_3	Random	MM_Null	MM_Open	MM_Improved	AB_Null	AB_Open	AB_Improved	Result
cs2a	82	73	60	48	64	60	49	62.29%
r=-0.8	83	82	60	58	75	61	56	67.86%
r=-0.6	89	80	65	57	77	57	54	68.43%
r=-0.4	90	80	70	59	78	69	60	72.29%
r=-0.2	88	89	71	58	82	63	65	73.71%
cs0	89	87	75	72	79	71	74	78.14%
r=0.2	92	89	70	66	77	71	67	76.00%
r=0.4	86	80	65	67	77	77	69	74.43%
r=0.6	89	77	72	61	76	70	65	72.86%
r=0.8	90	89	74	64	77	72	72	76.86%
cs2b	87	65	62	49	72	56	59	64.29%

It show both custom_score_2a and custom_score_2b does not improve custom_score_0.

custom_score_4 (Simulation)

custom_score_4 run simulation play to end game, and output the win/loss of the result.

In simulation, the game will choose the move closest to the board center. We choose this feature since it is less CPU consumption and effective.

For the game which win in n step, the function would output r_4^n ($0 < r_4 < 1$). For the game which loss in n step, the function would output $-r_4^n$. So the AI would prefer early win than later win, and prefer later loss than early loss.

The runtime and performance of this function depends on number of blank cell in the board. With more blank cell, simulation require more time, and the result is less accurate. As step count increase, $+/-r_4^n$ would be close to zero. So we may put a cutdown to save CPU. But now we just simulate to endgame.

It is meaningless to tune r_4. We just need to ensure $0 < r_4 < 1$.

type	Random	MM_Null	MM_Open	MM_Improved	AB_Null	AB_Open	AB_Improved	Result
cs4	93	77	67	63	68	68	59	70.71%

It's strength is close to ID_Improved, and weaker than custom_score_0, even though it consume high CPU.

custom_score_5 (custom_score_0 + custom_score_4)

custom_score_5 combine custom_score_0 and custom_score_4 by adding them together.

custom_score_5 = (1-r5) * custom_score_0 + r5 * custom_score_4

To get the best performance of the function, we need to tune r_0, r_4 and r_5 together. For simplicity we take r_0 = 1/6, r_4 = 0.99, and tune r_5.

Result: (r_0 = 1/6, r_4 = 0.99, NUM_MATCHES = 250)

r_5	Random	MM_Null	MM_Open	MM_Improved	AB_Null	AB_Open	AB_Improved	Result
cs0	90	84	76	64	83	77	74	78.29%
0.1	93	88	78	75	83	76	73	80.86%
0.2	95	90	74	77	87	77	72	81.71%
0.3	90	87	75	76	86	78	73	80.71%
0.4	93	89	73	69	90	73	77	80.57%
0.5	94	85	78	77	91	80	71	82.29%
0.6	98	90	78	73	82	84	68	81.86%
0.7	90	91	72	70	89	79	72	80.43%
0.8	91	94	73	71	87	77	66	79.86%
0.9	94	90	75	71	87	71	74	80.29%
cs4	93	77	67	63	68	68	59	70.71%

The performance of custom_score_5 is better than custom_score_0 and custom_score_4. r_0, r_4, and r_5 can be further tuned to achieve better performance.

Conclusion

Here is the summary of the heuristic functions:

type	Random	MM_Null	MM_Open	MM_Imp	AB_Null	AB_Open	AB_Imp	Result
ID_Improved	89	73	57	54	64	64	57	65.43%
cs0	90	84	76	64	83	77	74	78.29%
cs1	90	75	51	54	74	55	45	63.43%
cs2	87	65	62	49	72	56	59	64.29%
cs3	90	89	74	64	77	72	72	76.86%
cs4	93	77	67	63	68	68	59	70.71%
cs5	94	85	78	77	91	80	71	82.29%

We recommend custom_score_5:

- It achieve best result when matching with random opponent, with chance 94%.
- It achieve good result when matching with intelligent opponents such as open_move_score and improved_score, with higher than 70% chance. Although the winning rate versus AB_Imp is slightly lower, it perform best when versus MM_Open, MM_Improve and AB_Open.
- It's result % is the best among all other custom score.

In CPU limited environment, we recommend custom_score_0, as the evaluate function can run in constant time in larger board.

In extreme limited environment, `custom_score_2b` would be a choice as it does not require much calculation.

tournament.py output

This script evaluates the performance of the custom heuristic function by comparing the strength of an agent using iterative deepening (ID) search with alpha-beta pruning against the strength rating of agents using other heuristic functions. The `ID_Improved` agent provides a baseline by measuring the performance of a basic agent using Iterative Deepening and the "improved" heuristic (from lecture) on your hardware. The `Student` agent then measures the performance of Iterative Deepening and the custom heuristic against the same opponents.

```
*************************
 Evaluating: ID_Improved
*************************

Playing Matches:
----------
  Match 1: ID_Improved vs   Random      Result: 17 to 3
  Match 2: ID_Improved vs   MM_Null     Result: 14 to 6
  Match 3: ID_Improved vs   MM_Open     Result: 11 to 9
  Match 4: ID_Improved vs MM_Improved   Result: 12 to 8
  Match 5: ID_Improved vs   AB_Null     Result: 15 to 5
  Match 6: ID_Improved vs   AB_Open     Result: 12 to 8
  Match 7: ID_Improved vs AB_Improved   Result: 12 to 8


Results:
----------
ID_Improved          66.43%

*************************
   Evaluating: Student
*************************

Playing Matches:
----------
  Match 1:   Student   vs   Random      Result: 18 to 2
  Match 2:   Student   vs   MM_Null     Result: 18 to 2
  Match 3:   Student   vs   MM_Open     Result: 16 to 4
  Match 4:   Student   vs MM_Improved   Result: 14 to 6
  Match 5:   Student   vs   AB_Null     Result: 17 to 3
  Match 6:   Student   vs   AB_Open     Result: 15 to 5
  Match 7:   Student   vs AB_Improved   Result: 17 to 3


Results:
----------
Student              82.14%
```