# Lab Assignment #7

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Due March 24, 2023

#### Instructions

The purpose of this lab is to introduce several different classification strategies and variations on classification accuracy. In this lab we will work with another staple set of strategies: Naive Bayes and linear/quadratic discriminant analysis.

```
library(ISLR2)
library(ggplot2)
library(dplyr)
library(nycflights13)
library(e1071) # Naive Bayes
library(MASS) # LDA/QDA
library(yardstick) # only tidymodels package we'll need in this lab
```

This lab assignment is worth a total of 25 points.

### Problem 1: Naive Bayes

```
Part a (Code: 1 pt)
```

Run the code in ISLR Lab 4.7.5.

```
attach(Smarket)
train <- (Smarket$Year <2005)</pre>
Smarket.2005 <- Smarket[!train,]</pre>
Direction.2005 <- Direction[!train]</pre>
library(e1071)
nb.fit <- naiveBayes(Direction ~ Lag1 + Lag2, data = Smarket, subset = train)
nb.fit
##
## Naive Bayes Classifier for Discrete Predictors
## Call:
## naiveBayes.default(x = X, y = Y, laplace = laplace)
## A-priori probabilities:
## Y
##
       Down
## 0.491984 0.508016
##
```

```
## Conditional probabilities:
##
         Lag1
## Y
                  [,1]
                           [,2]
     Down 0.04279022 1.227446
##
##
         -0.03954635 1.231668
##
##
         Lag2
## Y
                  [,1]
                           [,2]
##
     Down 0.03389409 1.239191
##
         -0.03132544 1.220765
mean(Lag1[train][Direction[train] == "Down"])
## [1] 0.04279022
sd(Lag1[train][Direction[train] == "Down"])
## [1] 1.227446
nb.class <- predict(nb.fit,Smarket.2005)</pre>
table(nb.class, Direction.2005)
##
           Direction.2005
## nb.class Down Up
##
       Down
              28 20
##
              83 121
       Uр
mean(nb.class == Direction.2005)
## [1] 0.5912698
nb.preds <- predict(nb.fit, Smarket.2005, type = "raw")</pre>
nb.preds[1:5,]
##
             Down
## [1,] 0.4873164 0.5126836
## [2,] 0.4762492 0.5237508
## [3,] 0.4653377 0.5346623
## [4,] 0.4748652 0.5251348
## [5,] 0.4901890 0.5098110
```

### Part b (Code: 1 pt)

Recall that in Lab 6 we filtered the flights to only the United, American, and Delta carriers. Here we add another variable, arr\_ontime, to represent whether the flight arrived on time or not.

```
flights2 <- flights %>% filter(
  carrier %in% c("UA", "AA", "DL"),
  !is.na(dep_delay),
  !is.na(arr_delay)
) %>%
  mutate(
    arr_ontime = as.factor(if_else(arr_delay <= 0, "yes", "no"))
)</pre>
```

Non-randomly divide the flights2 dataset into flights\_training, which contains all flights through October, and flights\_test, which contains all flights in November and December. You should be able to use the filter function to do this.

```
flights2$arr_ontime <- relevel(flights2$arr_ontime, ref = "yes")
flights_training <- flights2 %>%
  filter(month == 10)
flights_test <- flights2 %>%
  filter(month == 11 | month == 12)
```

Then, fit a Naive Bayes model on the training set predicting whether a flight will be delayed (arr\_ontime = "no") based on the departure delay (dep\_delay), carrier, distance traveled, and origin.

### Part c (Code: 1.5 pts)

Unfortunately, there is no easy way to use augment on this model, so we'll have to make the predictions ourselves.

First, make class predictions on the flights\_test dataset using similar code to that done in Lab 4.7.5. Then, create the flights\_nb\_predictions data frame or tibble containing two columns: predicted, representing the predicted classes, and actual, representing the actual classes. Use flights\_nb\_predictions to obtain the confusion matrix for the model.

```
## Truth
## Prediction yes no
## yes 12787 5043
## no 662 4206
```

#### Part d (Code: 0.5 pts; Explanation: 2 pts)

Without running any additional code, use the confusion matrix from part (c) to estimate the sensitivity, specificity, positive predictive value, and negative predictive value for the model. Express all answers as fractions and then convert to decimals rounded to the thousandths place (3 decimal places).

```
Sensitivity = 4206/9249 0.455
Specificity = 12787/13449 0.951
Positive Predictive Value = 4206/4868 0.864
Negative Predictive Value = 12787/17830 0.717
```

Then, using the summary function on your confusion matrix, check your answers. Remember that we are trying to predict that a flight will be delayed (arr\_ontime = "no").

```
## 1 accuracy
                           binary
                                          0.749
  2 kap
##
                           binary
                                          0.438
##
  3 sens
                           binary
                                          0.455
##
  4 spec
                                          0.951
                           binary
## 5 ppv
                           binary
                                          0.864
##
  6 npv
                           binary
                                          0.717
##
  7 mcc
                                          0.485
                           binary
## 8 j_index
                                          0.406
                           binary
                                          0.703
## 9 bal_accuracy
                           binary
## 10 detection_prevalence binary
                                          0.214
## 11 precision
                           binary
                                          0.864
## 12 recall
                                          0.455
                           binary
## 13 f_meas
                           binary
                                          0.596
```

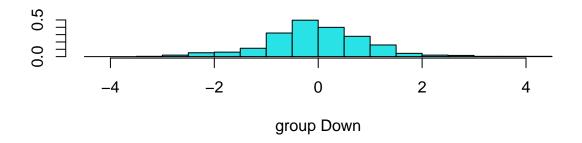
Looking at the summary, the sens row estimate matches our sensitivity, the spec row estimate matches our specificity, the ppv row estimate matches our positive predictive value, the npv row estimate matches our negative predictive value. :)

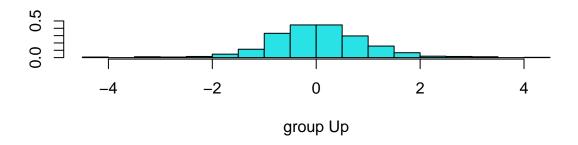
## Problem 2: Discriminant Analysis

### Part a (Code: 1 pt)

Run the code in ISLR Lab 4.7.3.

```
lda.fit <- lda(Direction ~ Lag1 + Lag2, data = Smarket, subset = train)</pre>
lda.fit
## Call:
## lda(Direction ~ Lag1 + Lag2, data = Smarket, subset = train)
## Prior probabilities of groups:
##
       Down
## 0.491984 0.508016
##
## Group means:
               Lag1
## Down 0.04279022 0.03389409
## Up
       -0.03954635 -0.03132544
##
## Coefficients of linear discriminants:
##
               LD1
## Lag1 -0.6420190
## Lag2 -0.5135293
plot(lda.fit)
```





```
lda.pred <- predict(lda.fit, Smarket.2005)</pre>
names(lda.pred)
## [1] "class"
                    "posterior" "x"
lda.class <- lda.pred$class</pre>
table(lda.class, Direction.2005)
##
            Direction.2005
## lda.class Down Up
        Down
                35
                   35
                76 106
##
        Uр
mean(lda.class == Direction.2005)
## [1] 0.5595238
sum(lda.pred$posterior[,1]>=.5)
## [1] 70
sum(lda.pred$posterior[,1]<.5)</pre>
## [1] 182
lda.pred$posterior[1:20,1]
##
         999
                   1000
                              1001
                                        1002
                                                   1003
                                                              1004
                                                                        1005
                                                                                   1006
## 0.4901792 0.4792185 0.4668185 0.4740011 0.4927877 0.4938562 0.4951016 0.4872861
##
        1007
                   1008
                              1009
                                        1010
                                                   1011
                                                              1012
                                                                        1013
                                                                                   1014
```

```
## 0.4907013 0.4844026 0.4906963 0.5119988 0.4895152 0.4706761 0.4744593 0.4799583
##
        1015
                  1016
                             1017
                                       1018
## 0.4935775 0.5030894 0.4978806 0.4886331
lda.class[1:20]
                                            Up
                                                            Uр
## [1] Up
             Uр
                                  Uр
                                                       Uр
                  Uр
                        Uр
                             Up
                                       Uр
                                                  Uр
                                                                 Down Up
                                                                            Up
                                                                                 Uр
## [16] Up
             Uр
                  Down Up
                             Uр
## Levels: Down Up
sum(lda.pred$posterior[,1]>.9)
## [1] 0
Part b (Code: 1 pt)
Run the code in ISLR Lab 4.7.4.
qda.fit <- qda(Direction ~ Lag1 + Lag2, data = Smarket, subset = train)
qda.fit
## Call:
## qda(Direction ~ Lag1 + Lag2, data = Smarket, subset = train)
## Prior probabilities of groups:
##
       Down
## 0.491984 0.508016
##
## Group means:
##
               Lag1
                            Lag2
## Down 0.04279022 0.03389409
        -0.03954635 -0.03132544
qda.class <- predict(qda.fit, Smarket.2005)$class
table(qda.class, Direction.2005)
##
            Direction.2005
## qda.class Down Up
               30 20
##
        Down
##
        Uр
               81 121
mean(qda.class == Direction.2005)
## [1] 0.5992063
Part c (Code: 1 pt)
Fit a LDA model on the training set predicting whether a flight will be delayed (arr_ontime = "no") based
on the departure delay (dep_delay), carrier, distance traveled, and origin.
lda.flit.fit <-lda(arr_ontime ~ dep_delay + carrier + distance + origin, data = flights_training)</pre>
lda.flit.fit
## Call:
## lda(arr_ontime ~ dep_delay + carrier + distance + origin, data = flights_training)
```

##

```
## Prior probabilities of groups:
##
         yes
## 0.6946888 0.3053112
##
## Group means:
##
       dep delay carrierDL carrierUA distance originJFK originLGA
## yes -2.313854 0.3674215 0.4063794 1359.280 0.2949842 0.3308985
## no 20.626870 0.2969529 0.4700831 1428.542 0.2470914 0.3307479
##
## Coefficients of linear discriminants:
## dep_delay 0.0406933057
## carrierDL -0.2639537167
## carrierUA -0.0556703446
## distance
              0.0002053784
## originJFK -0.2409482989
## originLGA 0.1864510004
```

#### Part d (Code: 1.5 pts)

##

no

Unfortunately, there is no easy way to use augment on this model, so we'll have to make the predictions ourselves.

First, make class predictions on the flights\_test dataset using similar code to that done in Lab 4.7.3. Then, create the flights\_lda\_predictions data frame or tibble containing two columns: predicted, representing the predicted classes, and actual, representing the actual classes. Use flights\_lda\_predictions to obtain the confusion matrix for the model.

### Part e (Code: 0.5 pts; Explanation: 2 pts)

2541

72

Without running any additional code, use the confusion matrix from part (d) to estimate the sensitivity, specificity, positive predictive value, and negative predictive value for the model. Express all answers as fractions and then convert to decimals rounded to the thousandths place (3 decimal places).

```
Sensitivity = 2541/9249 = 0.275
Specificity = 13377/13449 = 0.995
Positive Predictive Value = 2541/2613 = 0.972
Negative Predictive Value = 13377/20085 = 0.666
```

Then, using the summary function on your confusion matrix, check your answers. Remember that we are trying to predict that a flight will be delayed (arr\_ontime = "no").

```
summary(cnfsnm, event_level = "second")
```

```
## # A tibble: 13 x 3
##
      .metric
                            .estimator .estimate
##
      <chr>
                           <chr>>
                                           <dbl>
                                           0.701
##
  1 accuracy
                           binary
## 2 kap
                                           0.303
                           binary
## 3 sens
                           binary
                                           0.275
## 4 spec
                           binary
                                           0.995
## 5 ppv
                           binary
                                           0.972
## 6 npv
                                           0.666
                           binary
## 7 mcc
                           binary
                                           0.415
## 8 j_index
                                           0.269
                           binary
## 9 bal_accuracy
                           binary
                                           0.635
## 10 detection_prevalence binary
                                           0.115
## 11 precision
                           binary
                                           0.972
## 12 recall
                           binary
                                           0.275
## 13 f_meas
                           binary
                                           0.428
```

Looking at the summary, the sens row estimate matches our sensitivity, the spec row estimate matches our specificity, the ppv row estimate matches our positive predictive value, the npv row estimate matches our negative predictive value. :)

### Part f (Code: 3 pts; Explanation: 2 pts)

(d)

Repeat parts (c) through (e) for the QDA model. (Obviously, call your new data frame/tibble flights qda predictions instead.)

```
(c) qda.flit.fit <-qda(arr_ontime ~ dep_delay + carrier + distance + origin, data = flights_training)
```

```
## Truth
## Prediction yes no
## yes 12801 4922
## no 648 4327
Sensitivity = 4327/9249 = 0.468
Specificity = 12801/13449 = 0.952
Positive Predictive Value = 4327/4975 = 0.87
```

```
summary(cnfsnmq, event_level = "second")
```

```
## # A tibble: 13 x 3
##
      .metric
                           .estimator .estimate
##
      <chr>
                           <chr>
                                          <dbl>
## 1 accuracy
                           binary
                                          0.755
## 2 kap
                           binary
                                          0.452
## 3 sens
                                          0.468
                           binary
## 4 spec
                           binary
                                          0.952
## 5 ppv
                           binary
                                          0.870
## 6 npv
                                          0.722
                           binary
## 7 mcc
                                          0.498
                           binary
## 8 j_index
                                          0.420
                           binary
## 9 bal_accuracy
                                          0.710
                           binary
## 10 detection_prevalence binary
                                          0.219
## 11 precision
                                          0.870
                           binary
## 12 recall
                           binary
                                          0.468
## 13 f_meas
                           binary
                                          0.608
```

### **Problem 3: Model Selection**

### Part a (Code: 2 pts)

Add a column to the flights\_nb\_predictions, flights\_lda\_predictions, and flights\_qda\_predictions indicating the probability of not arriving on time (arr\_ontime == "no"). It may be easiest to first obtain the predicted probabilities of being in each class, then add the column to the relevant data frame using cbind or mutate.

Then, compute the Brier scores for each model. As shown in the class activity, it is easiest to use the mutate function to obtain the "squared error" for each observation and then average the squared error.

```
nb.flassprob <- predict(nb.flit, flights_test, type = "raw")</pre>
flights_nb_predictions <- flights_nb_predictions %>%
  mutate(prob_not_aot = nb.flassprob[,"no"])
flights lda predictions <- flights lda predictions %>%
  mutate(prob_not_aot = lda.flit.pred$posterior[,2])
flights_qda_predictions <- flights_qda_predictions %>%
  mutate(prob_not_aot = qda.flit.pred$posterior[,2])
brier_nb <- flights_nb_predictions %>%
  mutate(squared_error = case_when(
   predicted == "yes" ~ (prob_not_aot)^2,
   predicted == "no" ~ (1 - prob_not_aot)^2))
brs_nb <- mean(brier_nb$squared_error)</pre>
brier_lda <- flights_lda_predictions %>%
  mutate(squared_error = case_when(
   predicted == "yes" ~ (prob_not_aot)^2,
   predicted == "no" ~ (1 - prob_not_aot)^2))
```

```
brs_lda <- mean(brier_lda$squared_error)

brier_qda <- flights_qda_predictions %>%
   mutate(squared_error = case_when(
    predicted == "yes" ~ (prob_not_aot)^2,
    predicted == "no" ~ (1 - prob_not_aot)^2))

brs_qda <- mean(brier_qda$squared_error)</pre>
```

### Part b (Code: 1 pt)

Using the mn\_log\_loss function, obtain the cross-entropy/log loss for each of the three models.

### Part c (Code: 1 pt)

Using the mcc function, obtain the Matthews Correlation Coefficient for each of the three models.

```
mcc_nb <- mcc(flights_nb_predictions, actual, predicted)
mcc_lda <- mcc(flights_lda_predictions, actual, predicted)
mcc_qda <- mcc(flights_qda_predictions, actual, predicted)</pre>
```

#### Part d (Explanation: 1.5 pts)

Compare the Brier score, log loss, and Matthews correlation coefficient for the three models by filling in the table below. Round all numbers to 3 decimal places.

Model	Brier	log loss	MCC
Naive Bayes	0.012	0.823	0.485
LDA	0.068	0.58	0.415
QDA	0.012	0.746	0.498

Which of the three models performs the best on this test set by each measure?

By Brier Scores, the Naive Bayes and QDA model are tied for best. By log loss, the LDA model performs best. By MCC, the QDA model performs best.

### Part e (Explanation: 1.5 pts)

If you had to recommend one of the three models to use to predict whether a flight would be delayed, would you use the Naive Bayes, LDA, or QDA model? Explain.

If we can reasonably assume that our predictors are independent, I would use the Naive Bayes model since it is performing almost as well as the QDA model and is less computationally demanding. If we could not make this assumption, or we were working with small data, I would use the QDA model.