Lab Assignment #7

Nick Noel & Liz Villa

Due March 24, 2023

Instructions

The purpose of this lab is to introduce several different classification strategies and variations on classification accuracy. In this lab we will work with another staple set of strategies: Naive Bayes and linear/quadratic discriminant analysis.

```
library(ISLR2)
library(ggplot2)
library(dplyr)
library(nycflights13)
library(e1071) # Naive Bayes
library(MASS) # LDA/QDA
library(yardstick) # only tidymodels package we'll need in this lab
```

This lab assignment is worth a total of 25 points.

Problem 1: Naive Bayes

```
Part a (Code: 1 pt)
```

Run the code in ISLR Lab 4.7.5.

```
attach(Smarket)
train <- (Smarket$Year <2005)</pre>
Smarket.2005 <- Smarket[!train,]</pre>
Direction.2005 <- Direction[!train]</pre>
library(e1071)
nb.fit <- naiveBayes(Direction ~ Lag1 + Lag2, data = Smarket, subset = train)
nb.fit
##
## Naive Bayes Classifier for Discrete Predictors
## Call:
## naiveBayes.default(x = X, y = Y, laplace = laplace)
## A-priori probabilities:
## Y
##
       Down
## 0.491984 0.508016
##
```

```
## Conditional probabilities:
##
         Lag1
## Y
                  [,1]
                           [,2]
     Down 0.04279022 1.227446
##
##
         -0.03954635 1.231668
##
##
         Lag2
## Y
                  [,1]
                           [,2]
##
     Down 0.03389409 1.239191
##
         -0.03132544 1.220765
mean(Lag1[train][Direction[train] == "Down"])
## [1] 0.04279022
sd(Lag1[train][Direction[train] == "Down"])
## [1] 1.227446
nb.class <- predict(nb.fit,Smarket.2005)</pre>
table(nb.class, Direction.2005)
##
           Direction.2005
## nb.class Down Up
##
       Down
              28 20
##
              83 121
       Uр
mean(nb.class == Direction.2005)
## [1] 0.5912698
nb.preds <- predict(nb.fit, Smarket.2005, type = "raw")</pre>
nb.preds[1:5,]
##
             Down
## [1,] 0.4873164 0.5126836
## [2,] 0.4762492 0.5237508
## [3,] 0.4653377 0.5346623
## [4,] 0.4748652 0.5251348
## [5,] 0.4901890 0.5098110
```

Part b (Code: 1 pt)

Recall that in Lab 6 we filtered the flights to only the United, American, and Delta carriers. Here we add another variable, arr_ontime, to represent whether the flight arrived on time or not.

```
flights2 <- flights %>% filter(
  carrier %in% c("UA", "AA", "DL"),
  !is.na(dep_delay),
  !is.na(arr_delay)
) %>%
  mutate(
    arr_ontime = as.factor(if_else(arr_delay <= 0, "yes", "no"))
)</pre>
```

Non-randomly divide the flights2 dataset into flights_training, which contains all flights through October, and flights_test, which contains all flights in November and December. You should be able to use the filter function to do this.

```
flights2$arr_ontime <- relevel(flights2$arr_ontime, ref = "yes")
flights_training <- flights2 %>%
  filter(month == 10)
flights_test <- flights2 %>%
  filter(month == 11 | month == 12)
```

Then, fit a Naive Bayes model on the training set predicting whether a flight will be delayed (arr_ontime = "no") based on the departure delay (dep_delay), carrier, distance traveled, and origin.

Part c (Code: 1.5 pts)

Unfortunately, there is no easy way to use augment on this model, so we'll have to make the predictions ourselves.

First, make class predictions on the flights_test dataset using similar code to that done in Lab 4.7.5. Then, create the flights_nb_predictions data frame or tibble containing two columns: predicted, representing the predicted classes, and actual, representing the actual classes. Use flights_nb_predictions to obtain the confusion matrix for the model.

```
## Truth
## Prediction yes no
## yes 12787 5043
## no 662 4206
```

Part d (Code: 0.5 pts; Explanation: 2 pts)

Without running any additional code, use the confusion matrix from part (c) to estimate the sensitivity, specificity, positive predictive value, and negative predictive value for the model. Express all answers as fractions and then convert to decimals rounded to the thousandths place (3 decimal places).

```
Sensitivity = 12787/13449 \ 0.951
Specificity = 4206/9249 \ 0.455
Positive Predictive Value = 12787/17830 \ 0.717
Negative Predictive Value = 4206/4868 \ 0.864
```

Then, using the summary function on your confusion matrix, check your answers. Remember that we are trying to predict that a flight will be delayed (arr_ontime = "no").

```
summary(cmtrx)
```

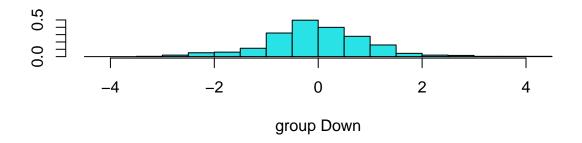
```
0.749
## 1 accuracy
                          binary
## 2 kap
                          binary
                                         0.438
## 3 sens
                          binary
                                         0.951
## 4 spec
                                         0.455
                          binary
## 5 ppv
                          binary
                                         0.717
## 6 npv
                                         0.864
                          binary
## 7 mcc
                          binary
                                         0.485
## 8 j_index
                                         0.406
                          binary
## 9 bal_accuracy
                          binary
                                         0.703
## 10 detection_prevalence binary
                                         0.786
## 11 precision
                          binary
                                         0.717
## 12 recall
                                         0.951
                          binary
## 13 f_meas
                                         0.818
                          binary
```

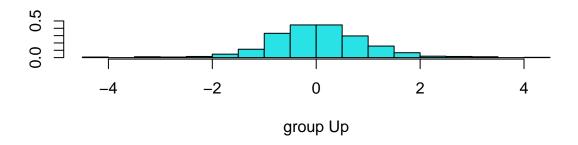
Problem 2: Discriminant Analysis

Part a (Code: 1 pt)

Run the code in ISLR Lab 4.7.3.

```
lda.fit <- lda(Direction ~ Lag1 + Lag2, data = Smarket, subset = train)</pre>
lda.fit
## Call:
## lda(Direction ~ Lag1 + Lag2, data = Smarket, subset = train)
## Prior probabilities of groups:
       Down
## 0.491984 0.508016
##
## Group means:
               Lag1
## Down 0.04279022 0.03389409
      -0.03954635 -0.03132544
## Up
## Coefficients of linear discriminants:
               LD1
## Lag1 -0.6420190
## Lag2 -0.5135293
plot(lda.fit)
```





```
lda.pred <- predict(lda.fit, Smarket.2005)</pre>
names(lda.pred)
## [1] "class"
                    "posterior" "x"
lda.class <- lda.pred$class</pre>
table(lda.class, Direction.2005)
##
            Direction.2005
## lda.class Down Up
        Down
                35
                   35
                76 106
##
        Uр
mean(lda.class == Direction.2005)
## [1] 0.5595238
sum(lda.pred$posterior[,1]>=.5)
## [1] 70
sum(lda.pred$posterior[,1]<.5)</pre>
## [1] 182
lda.pred$posterior[1:20,1]
##
         999
                   1000
                              1001
                                        1002
                                                   1003
                                                              1004
                                                                        1005
                                                                                   1006
## 0.4901792 0.4792185 0.4668185 0.4740011 0.4927877 0.4938562 0.4951016 0.4872861
##
        1007
                   1008
                              1009
                                        1010
                                                   1011
                                                              1012
                                                                        1013
                                                                                   1014
```

```
## 0.4907013 0.4844026 0.4906963 0.5119988 0.4895152 0.4706761 0.4744593 0.4799583
##
        1015
                  1016
                             1017
                                       1018
## 0.4935775 0.5030894 0.4978806 0.4886331
lda.class[1:20]
                                            Up
                                                            Uр
## [1] Up
             Uр
                                  Uр
                                                       Uр
                  Uр
                        Uр
                             Up
                                       Uр
                                                  Uр
                                                                 Down Up
                                                                            Up
                                                                                 Uр
## [16] Up
             Uр
                  Down Up
                             Uр
## Levels: Down Up
sum(lda.pred$posterior[,1]>.9)
## [1] 0
Part b (Code: 1 pt)
Run the code in ISLR Lab 4.7.4.
qda.fit <- qda(Direction ~ Lag1 + Lag2, data = Smarket, subset = train)
qda.fit
## Call:
## qda(Direction ~ Lag1 + Lag2, data = Smarket, subset = train)
## Prior probabilities of groups:
##
       Down
## 0.491984 0.508016
##
## Group means:
##
               Lag1
                            Lag2
## Down 0.04279022 0.03389409
        -0.03954635 -0.03132544
qda.class <- predict(qda.fit, Smarket.2005)$class
table(qda.class, Direction.2005)
##
            Direction.2005
## qda.class Down Up
               30 20
##
        Down
##
        Uр
               81 121
mean(qda.class == Direction.2005)
## [1] 0.5992063
Part c (Code: 1 pt)
Fit a LDA model on the training set predicting whether a flight will be delayed (arr_ontime = "no") based
on the departure delay (dep_delay), carrier, distance traveled, and origin.
lda.flit.fit <-lda(arr_ontime ~ dep_delay + carrier + distance + origin, data = flights_training)</pre>
lda.flit.fit
## Call:
## lda(arr_ontime ~ dep_delay + carrier + distance + origin, data = flights_training)
```

##

```
## Prior probabilities of groups:
##
         yes
## 0.6946888 0.3053112
##
## Group means:
##
       dep delay carrierDL carrierUA distance originJFK originLGA
## yes -2.313854 0.3674215 0.4063794 1359.280 0.2949842 0.3308985
## no 20.626870 0.2969529 0.4700831 1428.542 0.2470914 0.3307479
##
## Coefficients of linear discriminants:
## dep_delay 0.0406933057
## carrierDL -0.2639537167
## carrierUA -0.0556703446
## distance
              0.0002053784
## originJFK -0.2409482989
## originLGA 0.1864510004
```

Part d (Code: 1.5 pts)

Unfortunately, there is no easy way to use augment on this model, so we'll have to make the predictions ourselves.

First, make class predictions on the flights_test dataset using similar code to that done in Lab 4.7.3. Then, create the flights_lda_predictions data frame or tibble containing two columns: predicted, representing the predicted classes, and actual, representing the actual classes. Use flights_lda_predictions to obtain the confusion matrix for the model.

```
lda.flit.pred <- predict(lda.flit.fit, flights_test)</pre>
flights_lda_predictions <- data.frame(</pre>
  predicted = lda.flit.pred$class,
  actual = flights_test$arr_ontime
(cnfsnm <- conf_mat(flights_lda_predictions, truth = actual,</pre>
         estimate = predicted))
##
              Truth
## Prediction
                 yes
                         no
##
           yes 13377
                       6709
##
          no
                  72
                       2540
```

Part e (Code: 0.5 pts; Explanation: 2 pts)

Without running any additional code, use the confusion matrix from part (d) to estimate the sensitivity, specificity, positive predictive value, and negative predictive value for the model. Express all answers as fractions and then convert to decimals rounded to the thousandths place (3 decimal places).

```
Sensitivity = 13377/13449 0.995
Specificity = 2541/9249 0.275
Positive Predictive Value = 13377/20085 0.666
Negative Predictive Value = 2541/2613 0.972
```

Then, using the summary function on your confusion matrix, check your answers. Remember that we are trying to predict that a flight will be delayed (arr_ontime = "no").

```
summary(cnfsnm)
```

```
## # A tibble: 13 x 3
##
      .metric
                           .estimator .estimate
##
      <chr>
                           <chr>
                                          <dbl>
                                          0.701
## 1 accuracy
                           binary
## 2 kap
                                          0.303
                           binary
## 3 sens
                           binary
                                          0.995
## 4 spec
                           binary
                                          0.275
## 5 ppv
                           binary
                                          0.666
## 6 npv
                                          0.972
                           binary
## 7 mcc
                           binary
                                          0.415
## 8 j_index
                                          0.269
                           binary
## 9 bal_accuracy
                           binary
                                          0.635
## 10 detection_prevalence binary
                                          0.885
## 11 precision
                           binary
                                          0.666
## 12 recall
                           binary
                                          0.995
## 13 f_meas
                           binary
                                          0.798
```

Part f (Code: 3 pts; Explanation: 2 pts)

Repeat parts (c) through (e) for the QDA model. (Obviously, call your new data frame/tibble flights_qda_predictions instead.)

```
(c) qda.flit.fit <-qda(arr_ontime ~ dep_delay + carrier + distance + origin, data = flights_training)
```

```
##
               Truth
## Prediction
                  yes
                          no
##
           yes 12801
                        4922
##
           no
                  648
                       4327
Sensitivity = 12801/13449 \ 0.952
Specificity = 4327/9249 \ 0.468
Positive Predictive Value = 12801/17723 \ 0.722
Negative Predictive Value = 4327/4975 \ 0.87
summary(cnfsnmq)
```

```
## # A tibble: 13 x 3
      .metric
##
                           .estimator .estimate
                                          <dbl>
##
      <chr>>
                           <chr>
                                          0.755
## 1 accuracy
                           binary
## 2 kap
                           binary
                                          0.452
## 3 sens
                                          0.952
                           binary
## 4 spec
                                          0.468
                           binary
                                          0.722
## 5 ppv
                           binary
## 6 npv
                           binary
                                          0.870
## 7 mcc
                           binary
                                          0.498
## 8 j_index
                           binary
                                          0.420
## 9 bal_accuracy
                                          0.710
                           binary
## 10 detection_prevalence binary
                                          0.781
## 11 precision
                                          0.722
                           binary
## 12 recall
                                          0.952
                           binary
## 13 f_meas
                           binary
                                          0.821
```

Problem 3: Model Selection

Part a (Code: 2 pts)

Add a column to the flights_nb_predictions, flights_lda_predictions, and flights_qda_predictions indicating the probability of not arriving on time (arr_ontime == "no"). It may be easiest to first obtain the predicted probabilities of being in each class, then add the column to the relevant data frame using cbind or mutate.

Then, compute the Brier scores for each model. As shown in the class activity, it is easiest to use the mutate function to obtain the "squared error" for each observation and then average the squared error.

```
nb.flassprob <- predict(nb.flit, flights_test, type = "raw")</pre>
flights_nb_predictions <- flights_nb_predictions %>%
  mutate(prob_not_aot = nb.flassprob[,"no"])
flights_lda_predictions <- flights_lda_predictions %>%
  mutate(prob_not_aot = lda.flit.pred$posterior[,2])
flights_qda_predictions <- flights_qda_predictions %>%
  mutate(prob not aot = qda.flit.pred$posterior[,2])
brier_nb <- flights_nb_predictions %>%
  mutate(squared error = case when(
    predicted == "yes" ~ (prob_not_aot)^2,
    predicted == "no" ~ (1 - prob_not_aot)^2))
brs_nb <- mean(brier_nb$squared_error)</pre>
brier_lda <- flights_lda_predictions %>%
  mutate(squared_error = case_when(
    predicted == "yes" ~ (prob_not_aot)^2,
    predicted == "no" ~ (1 - prob_not_aot)^2))
brs_lda <- mean(brier_lda$squared_error)</pre>
```

```
brier_qda <- flights_qda_predictions %>%
  mutate(squared_error = case_when(
    predicted == "yes" ~ (prob_not_aot)^2,
    predicted == "no" ~ (1 - prob_not_aot)^2))

brs_qda <- mean(brier_qda$squared_error)</pre>
```

Part b (Code: 1 pt)

Using the mn_log_loss function, obtain the cross-entropy/log loss for each of the three models.

Part c (Code: 1 pt)

Using the mcc function, obtain the Matthews Correlation Coefficient for each of the three models.

```
mcc_nb <- mcc(flights_nb_predictions, actual, predicted)
mcc_lda <- mcc(flights_lda_predictions, actual, predicted)
mcc_qda <- mcc(flights_qda_predictions, actual, predicted)</pre>
```

Part d (Explanation: 1.5 pts)

Compare the Brier score, log loss, and Matthews correlation coefficient for the three models by filling in the table below. Round all numbers to 3 decimal places.

Model	Brier	$\log \log $	MCC
Naive Bayes	0.012	0.823	0.485
LDA	0.068	0.58	0.415
QDA	0.012	0.746	0.498

Which of the three models performs the best on this test set by each measure?

Part e (Explanation: 1.5 pts)

If you had to recommend one of the three models to use to predict whether a flight would be delayed, would you use the Naive Bayes, LDA, or QDA model? Explain.