

Attention Mechanism



W

Machine Translation

- Before 2014: Statistical Machine Translation (SMT)
 - Extremely complex systems that require massive human efforts
 - Separately designed components
 - A lot of feature engineering
 - Lots of linguistic domain knowledge and expertise
- Before 2016:
 - Google Translate is based on statistical machine learning
- What happened in 2014?
 - Neural machine translation (NMT)

Sequence to Sequence Model

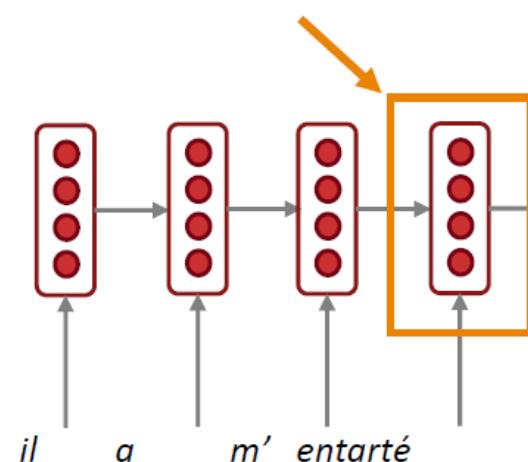
- Neural Machine Translation (NMT)
 - Learning to translate via a single end-to-end neural network.
 - Source language sentence \underline{X} , target language sentence $\underline{Y} = f(\underline{X}; \theta)$
- Sequence to Sequence Model (Seq2Seq, Sutskever et al. , '14)
 - Two RNNs: f_{enc} and f_{dec}
 - Encoder f_{enc} :
 - Takes X as input, and output the initial hidden state for decoder
 - Can use bidirectional RNN
 - Decoder f_{dec} :
 - It takes in the hidden state from f_{enc} to generate Y
 - Can use autoregressive language model

Sequence to Sequence Model

The sequence-to-sequence model

Encoding of the source sentence.
Provides initial hidden state
for Decoder RNN.

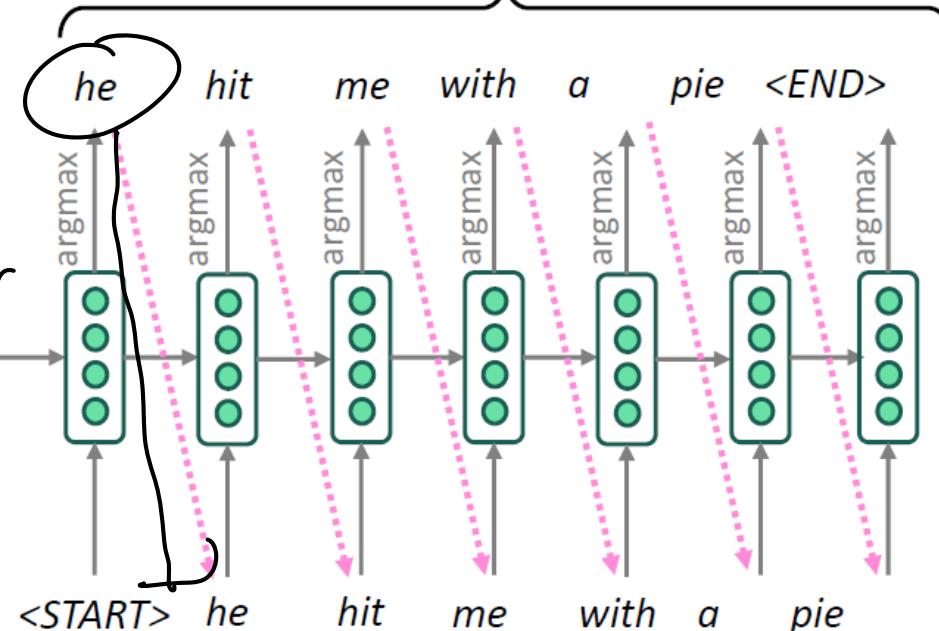
Encoder RNN



Source sentence (input)

Encoder RNN produces
an encoding of the
source sentence.

Target sentence (output)



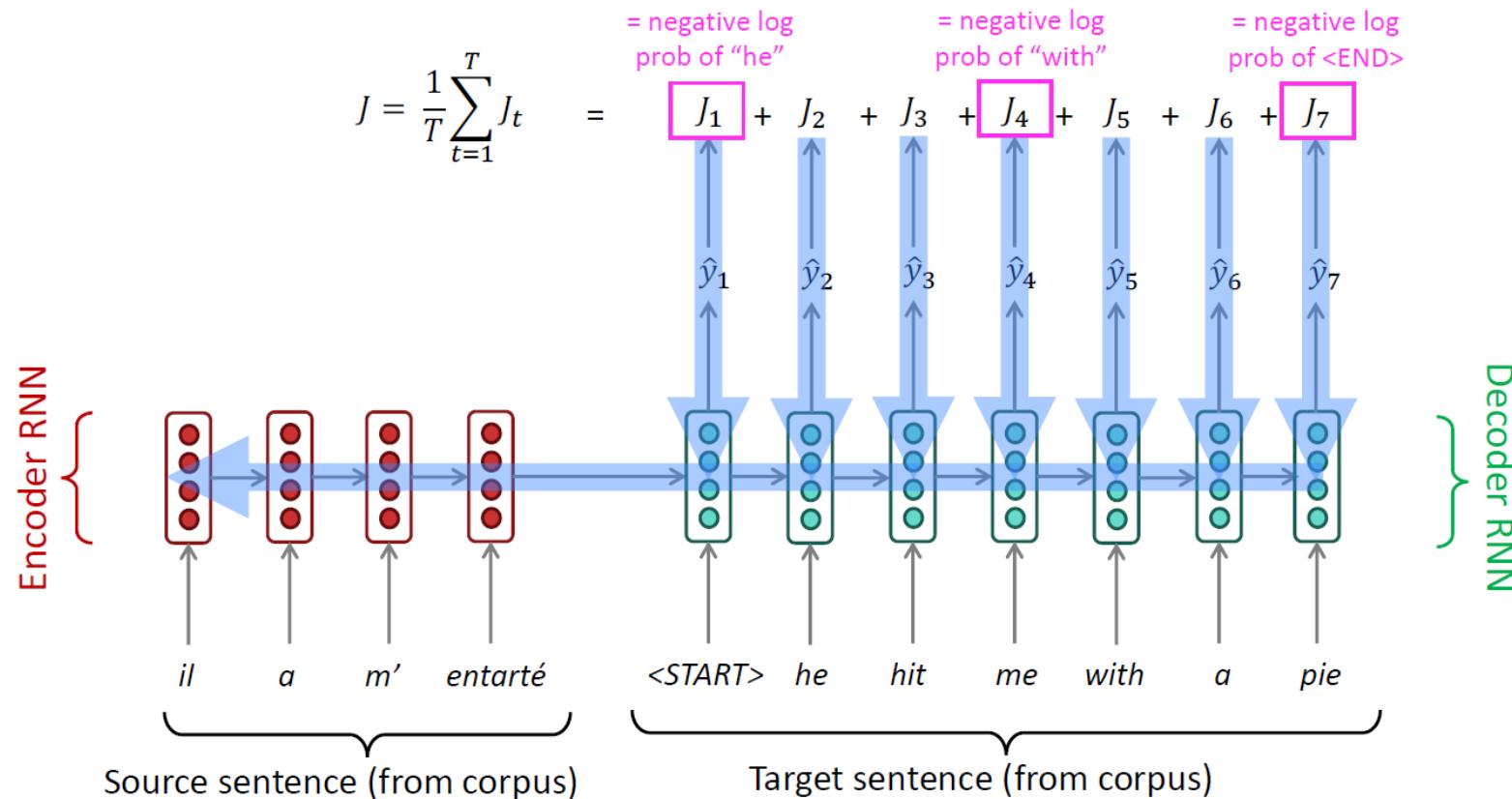
Decoder RNN

Decoder RNN is a Language Model that generates target sentence, *conditioned on encoding*.

Note: This diagram shows **test time** behavior: decoder output is fed in as next step's input

Training Sequence to Sequence Model

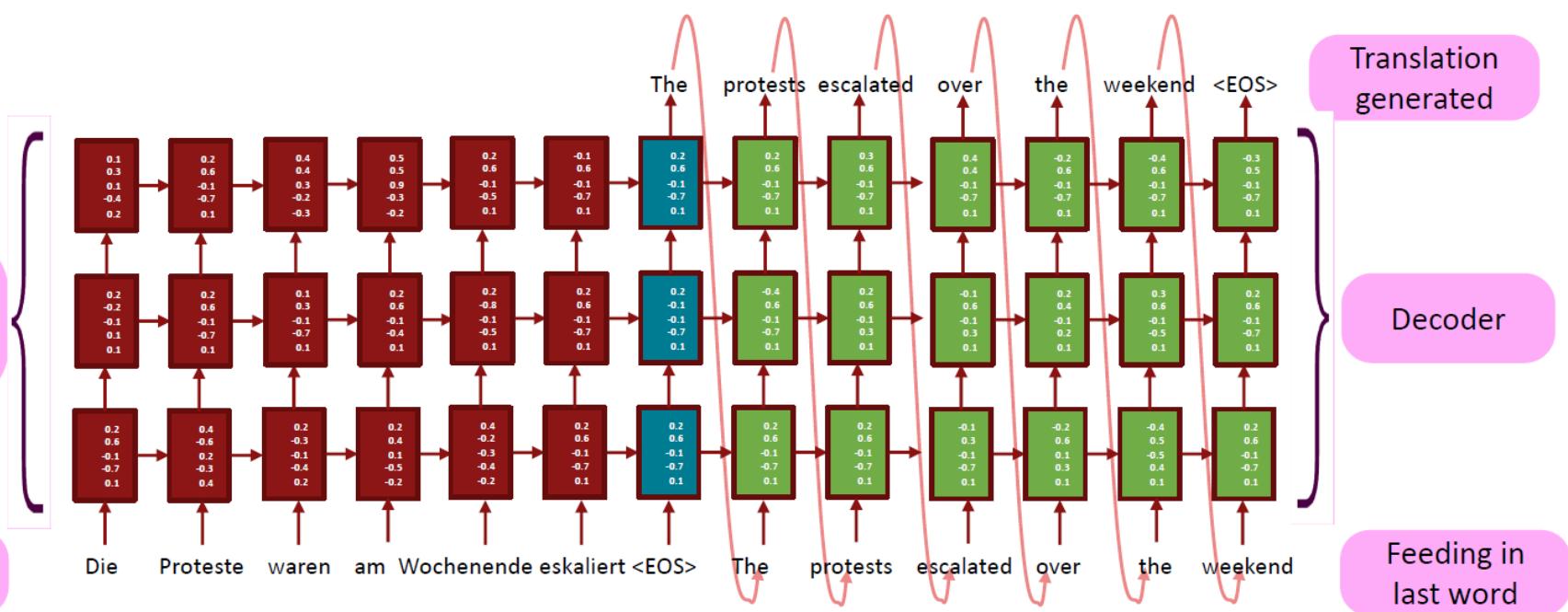
- Collect a huge paired dataset and train it end-to-end via BPTT
- Loss induced by MLE $P(Y|X) = P(Y|f_{enc}(X))$



Seq2seq is optimized as a **single system**. Backpropagation operates “*end-to-end*”.

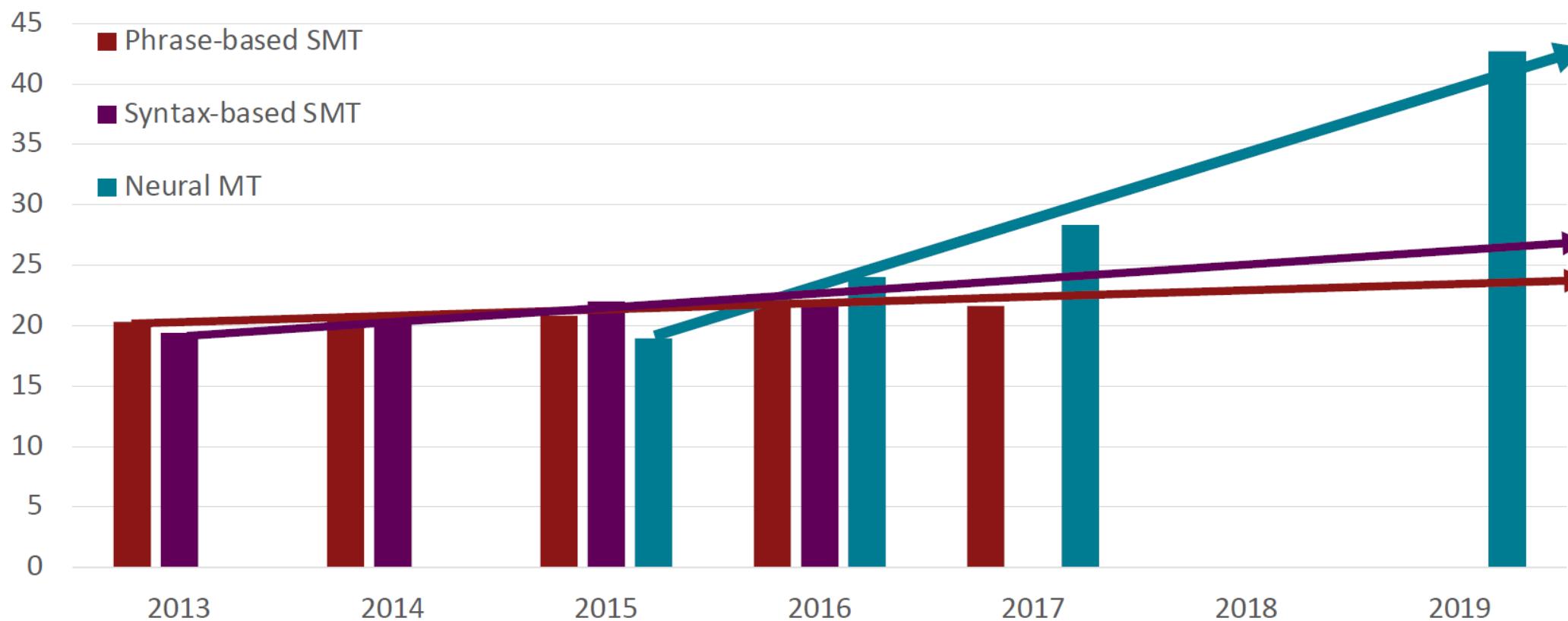
Deep Sequence to Sequence Model

- Stacked seq2seq model



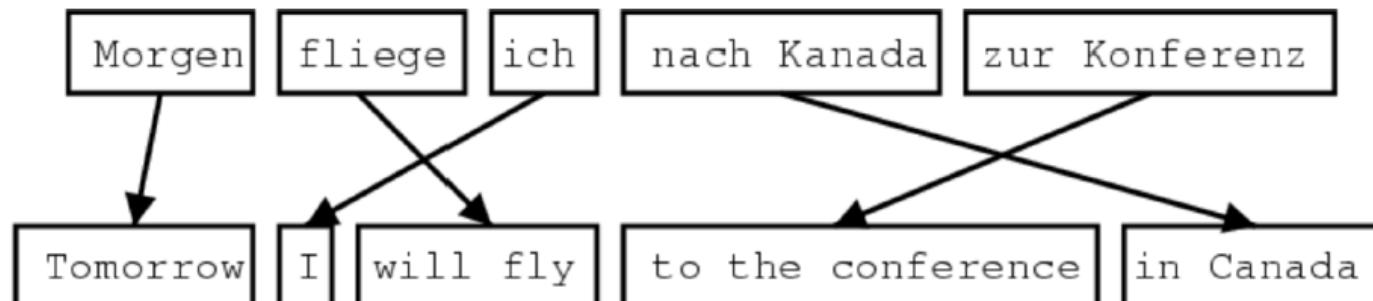
Machine Translation

- 2016: Google switched Google Translate from SMT to NMT



Alignment

- Alignment: the word-level correspondence between X and Y
- Can have complex long-term dependencies



The ————— Les
poor ————— pauvres
don't ————— sont
have ————— démunis
any —————
money —————

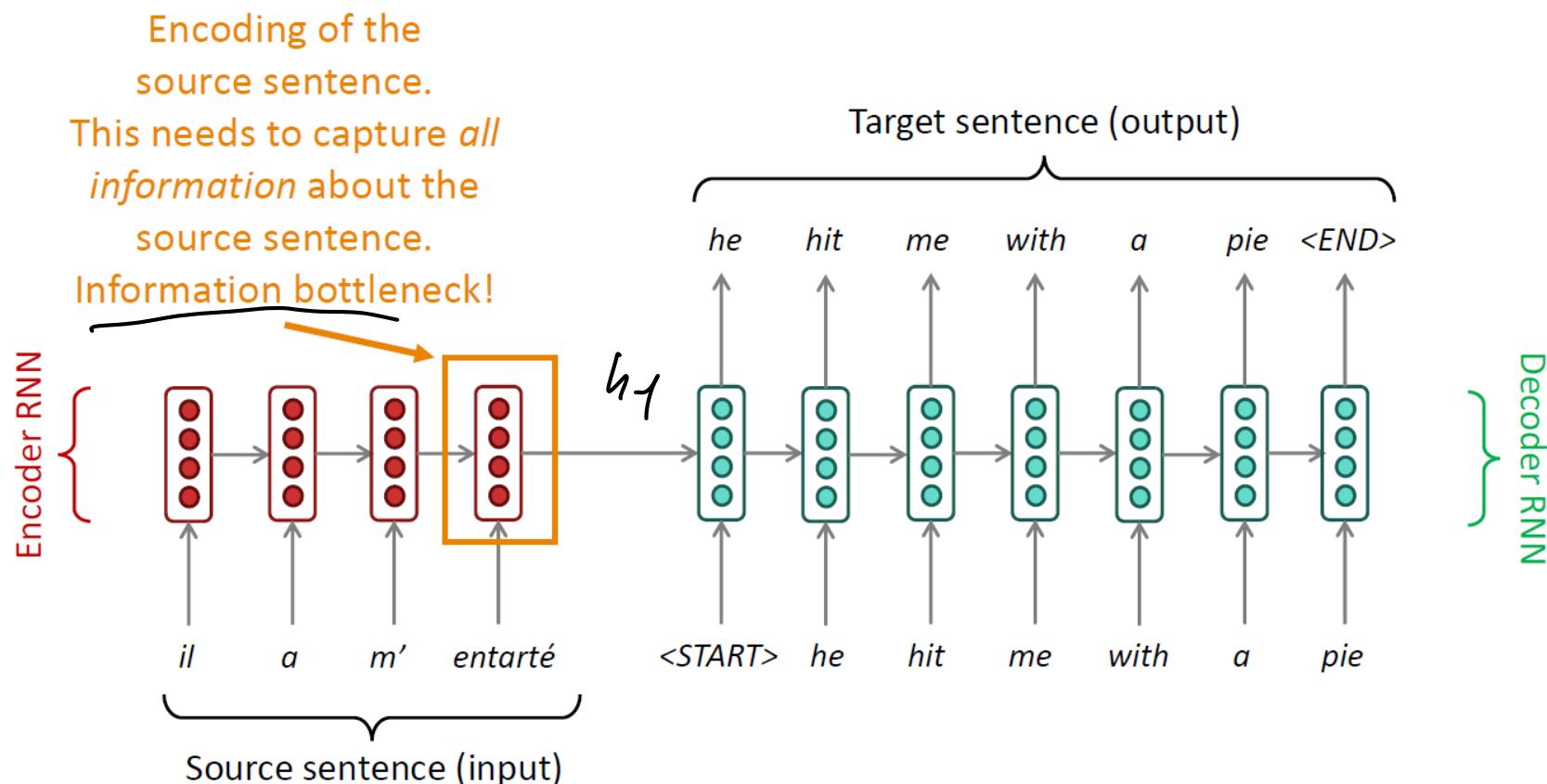
many-to-many alignment

	Lé	pau	sor	dér
The				
poor				
don't				
have				
any				
money				

phrase alignment

Issue in Seq2Seq

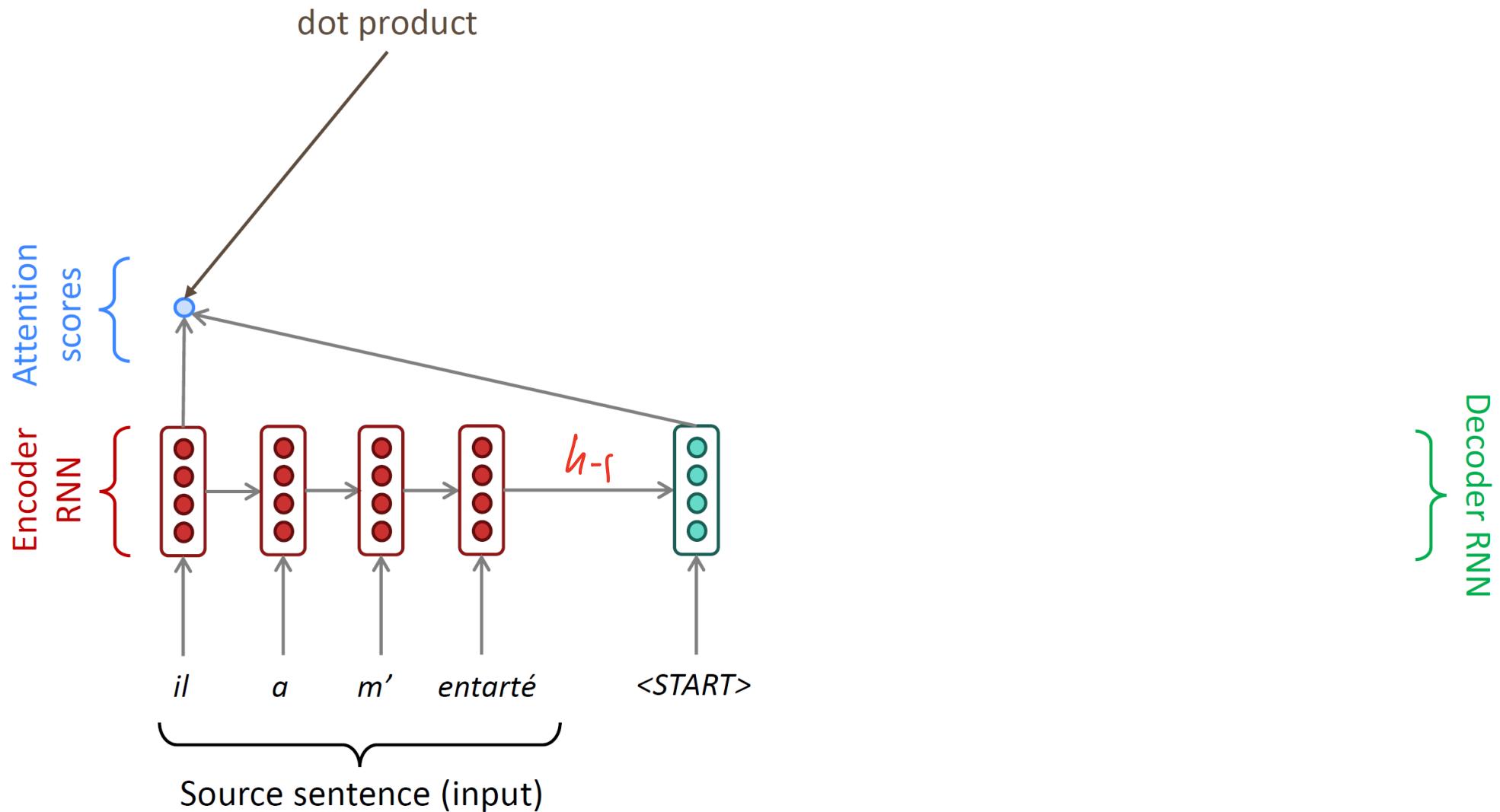
- Alignment: the word-level correspondence between X and Y
 - The information bottleneck due to the hidden state h
 - We want each Y_t to also focus on some X_i that it is aligned with



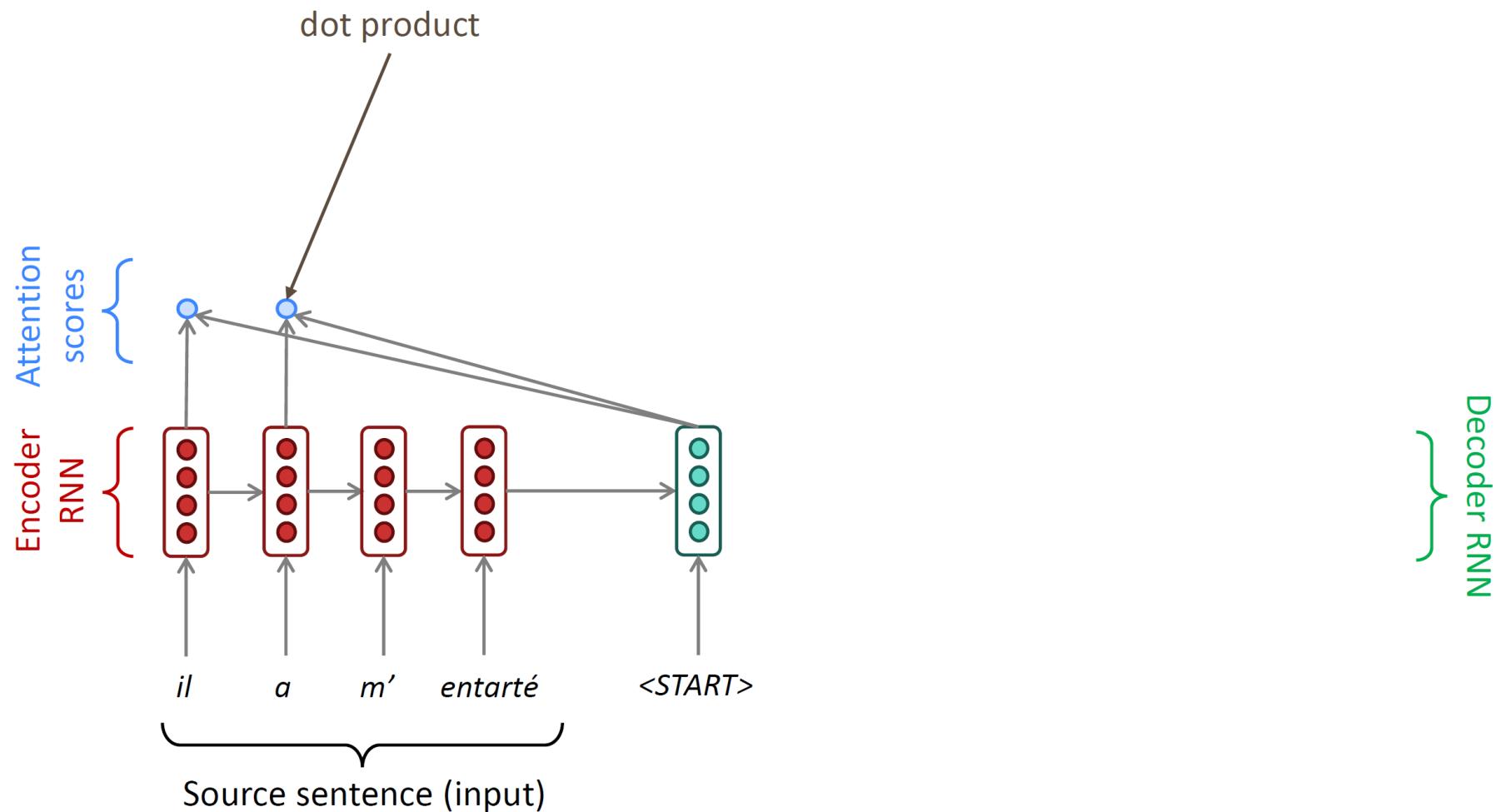
Seq2Seq with Attention

- NMT by jointly learning to align and translate (Bahdanau, Cho, Bengio, '15)
- Core idea:
 - When decoding $\underline{Y_t}$, consider both hidden states and alignment:
 - Hidden state: $\underline{h_t} = f_{dec}(Y_{i < t})$
 - Alignment: connect to a portion of \underline{X}
 - When portion of X to focus on?
 - Learn a softmax weight over X : attention distribution $\underline{P_{att}}$
 - $P_{att}(X_i | \underline{h_t})$: how much attention to put on word X_i
 - Attention output $\underline{h_{att}} = \sum_i f_{enc}(X_i | X_{j < i}) \cdot P_{att}(X_i | h_{t-1})$
 - Use $\underline{h_{t-1}}$ and $\underline{h_{att}}$ to compute $\underline{Y_t}$

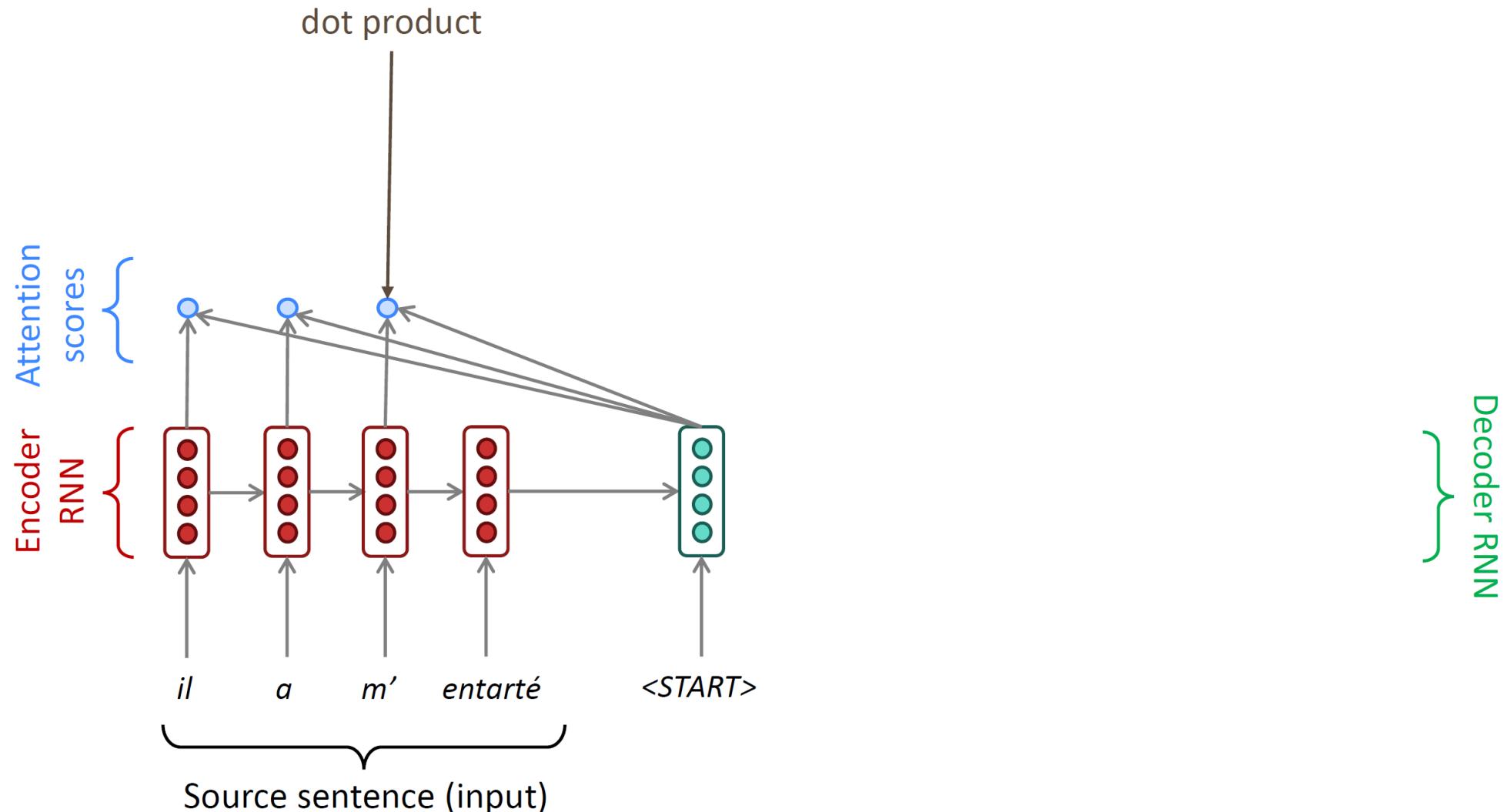
Seq2Seq with Attention



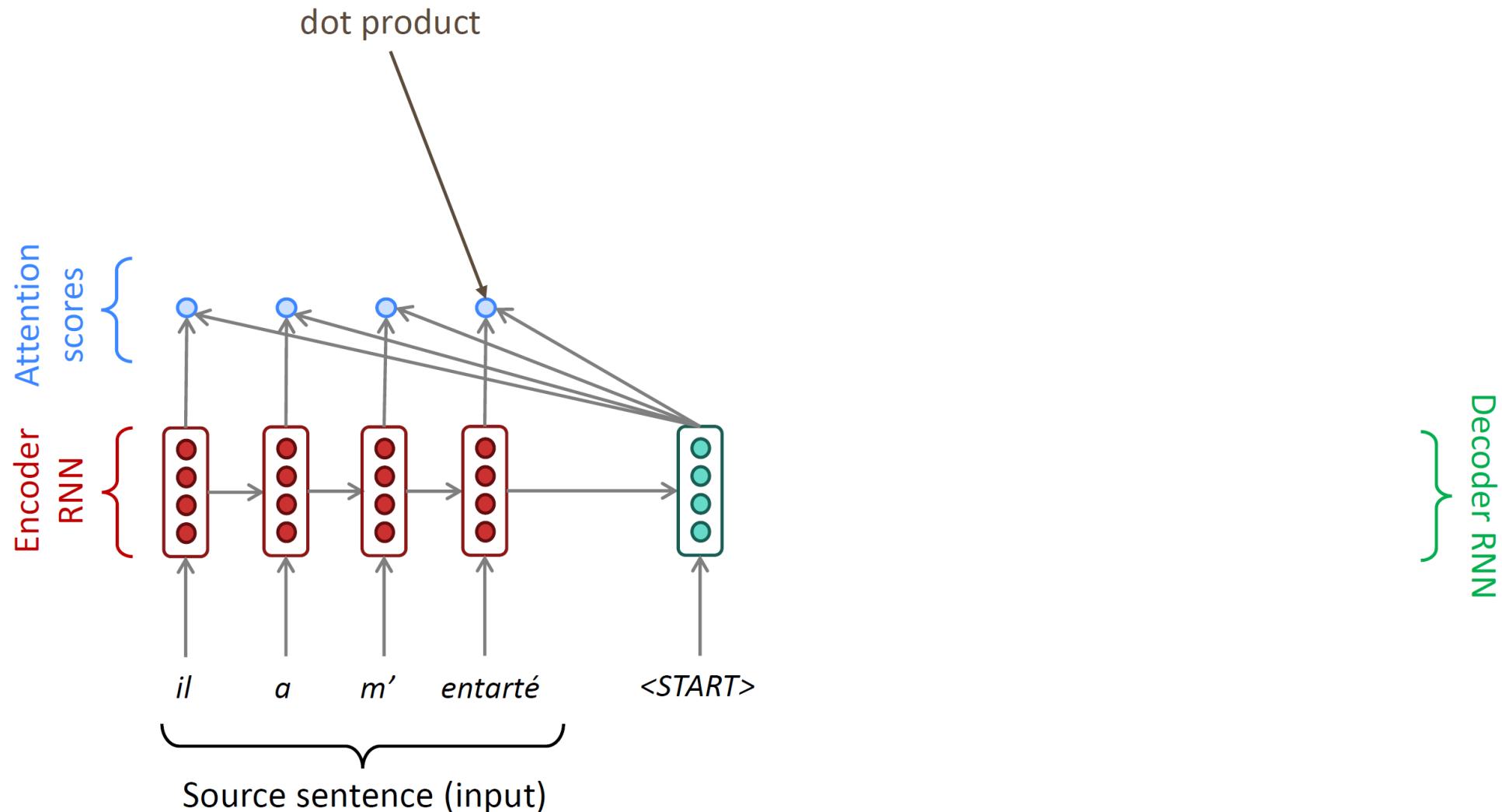
Seq2Seq with Attention



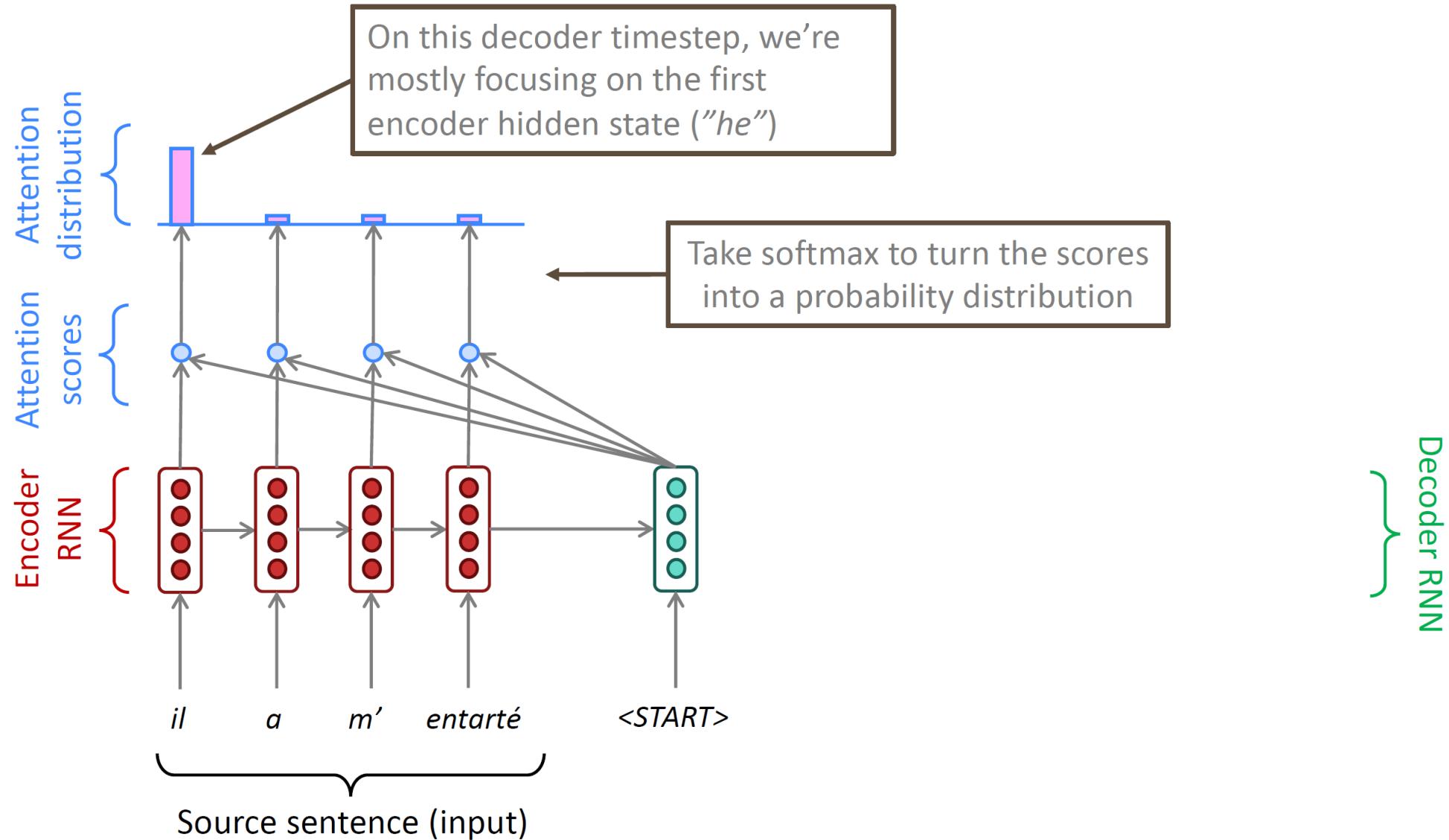
Seq2Seq with Attention



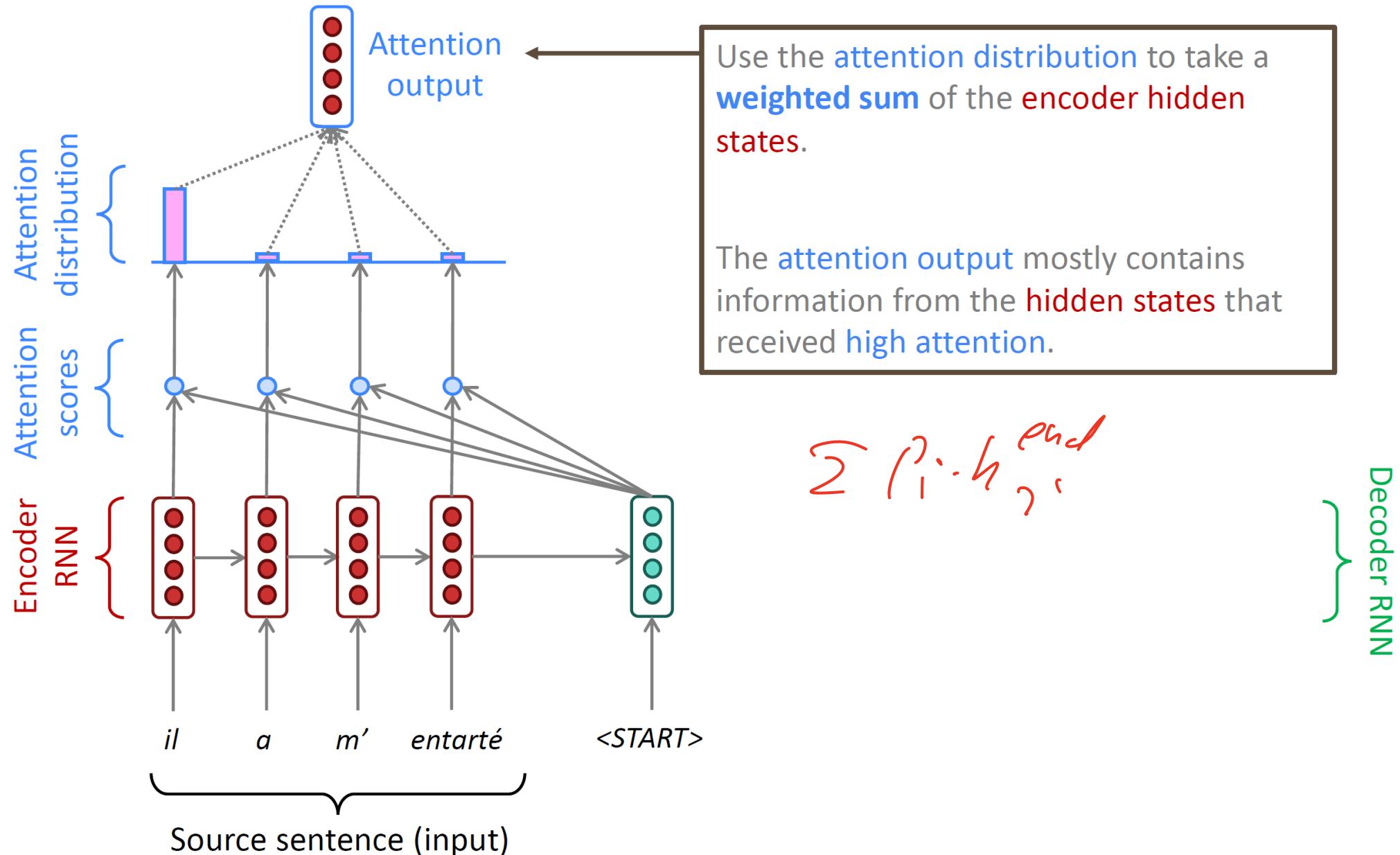
Seq2Seq with Attention



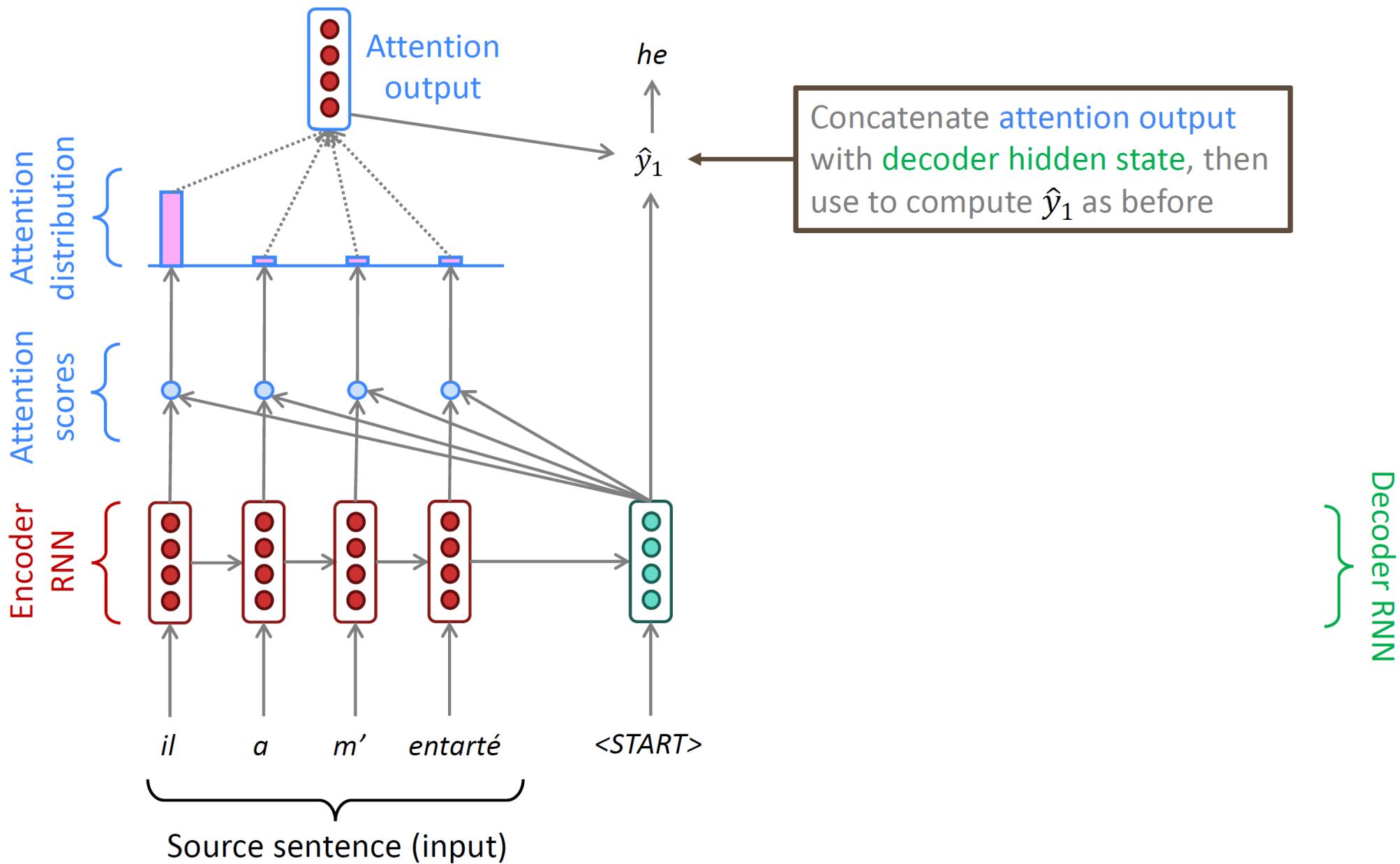
Seq2Seq with Attention



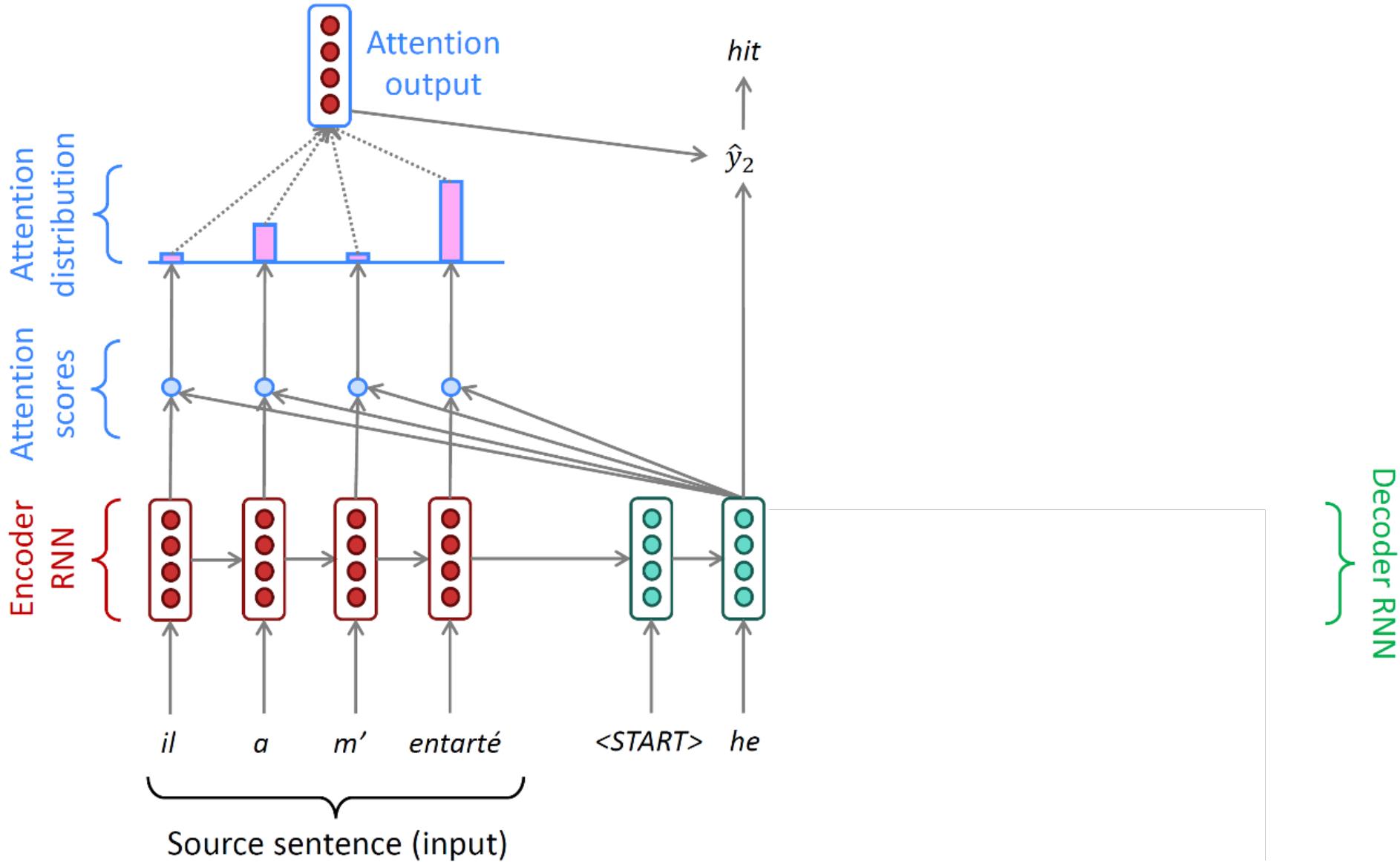
Seq2Seq with Attention



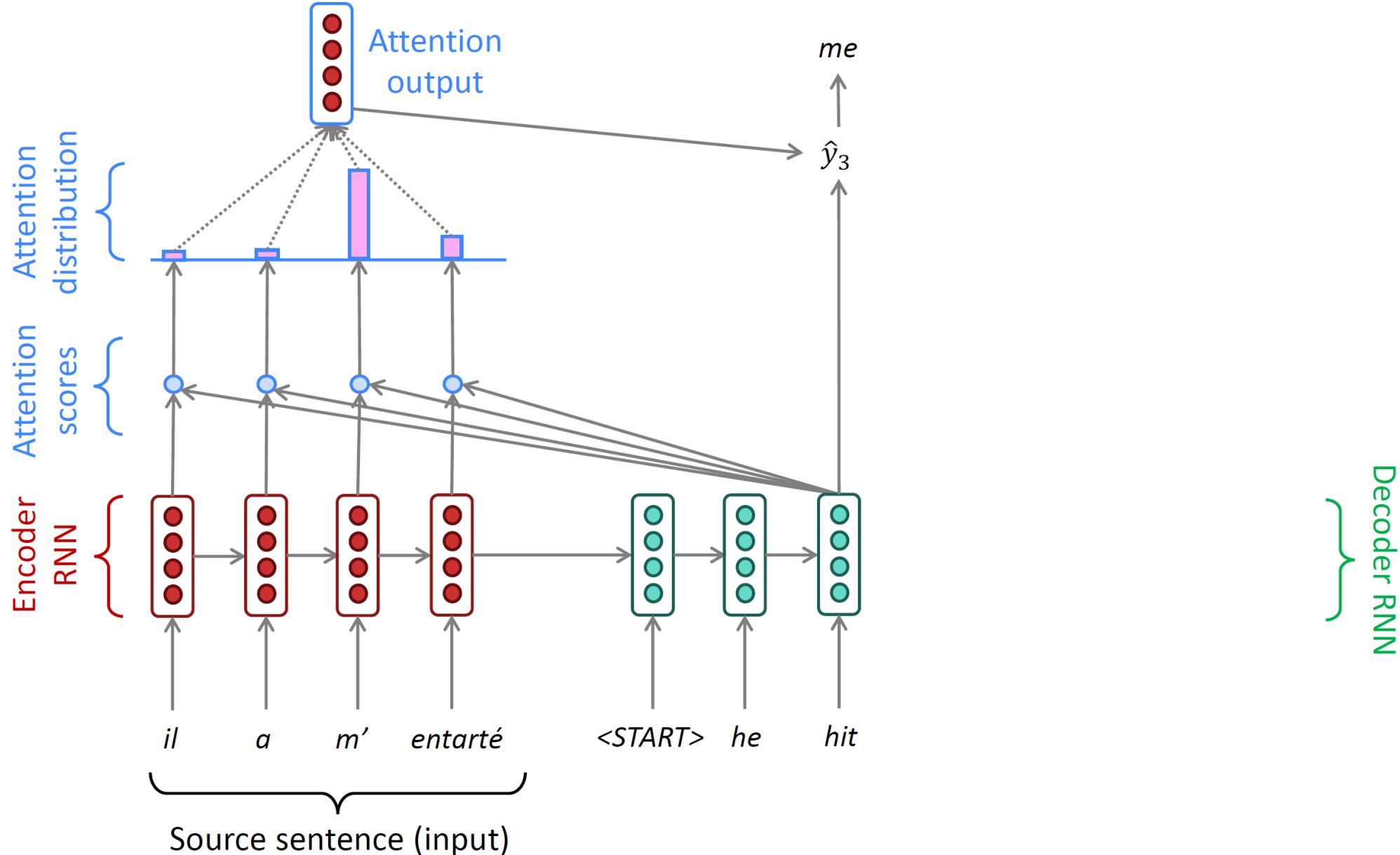
Seq2Seq with Attention



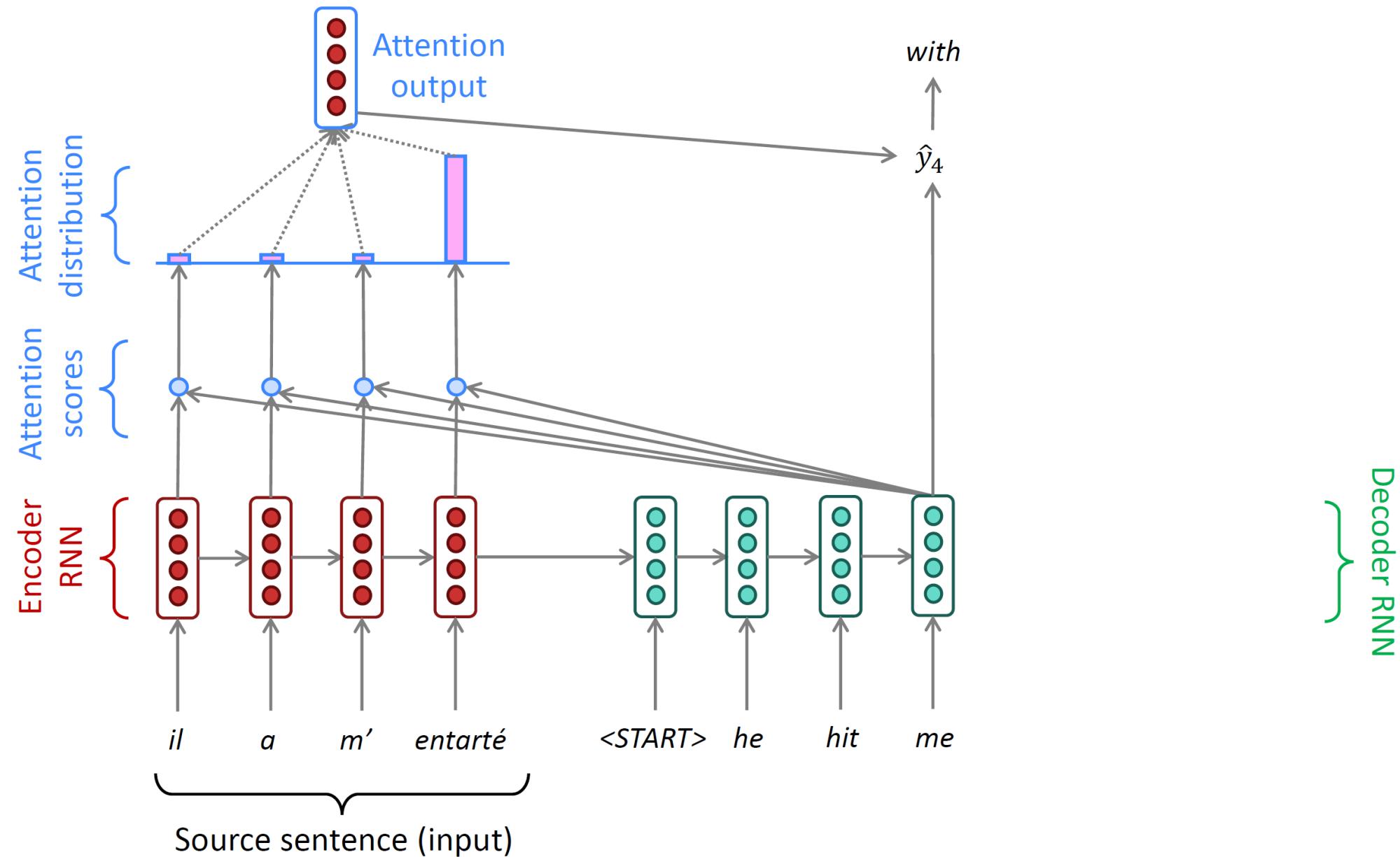
Seq2Seq with Attention



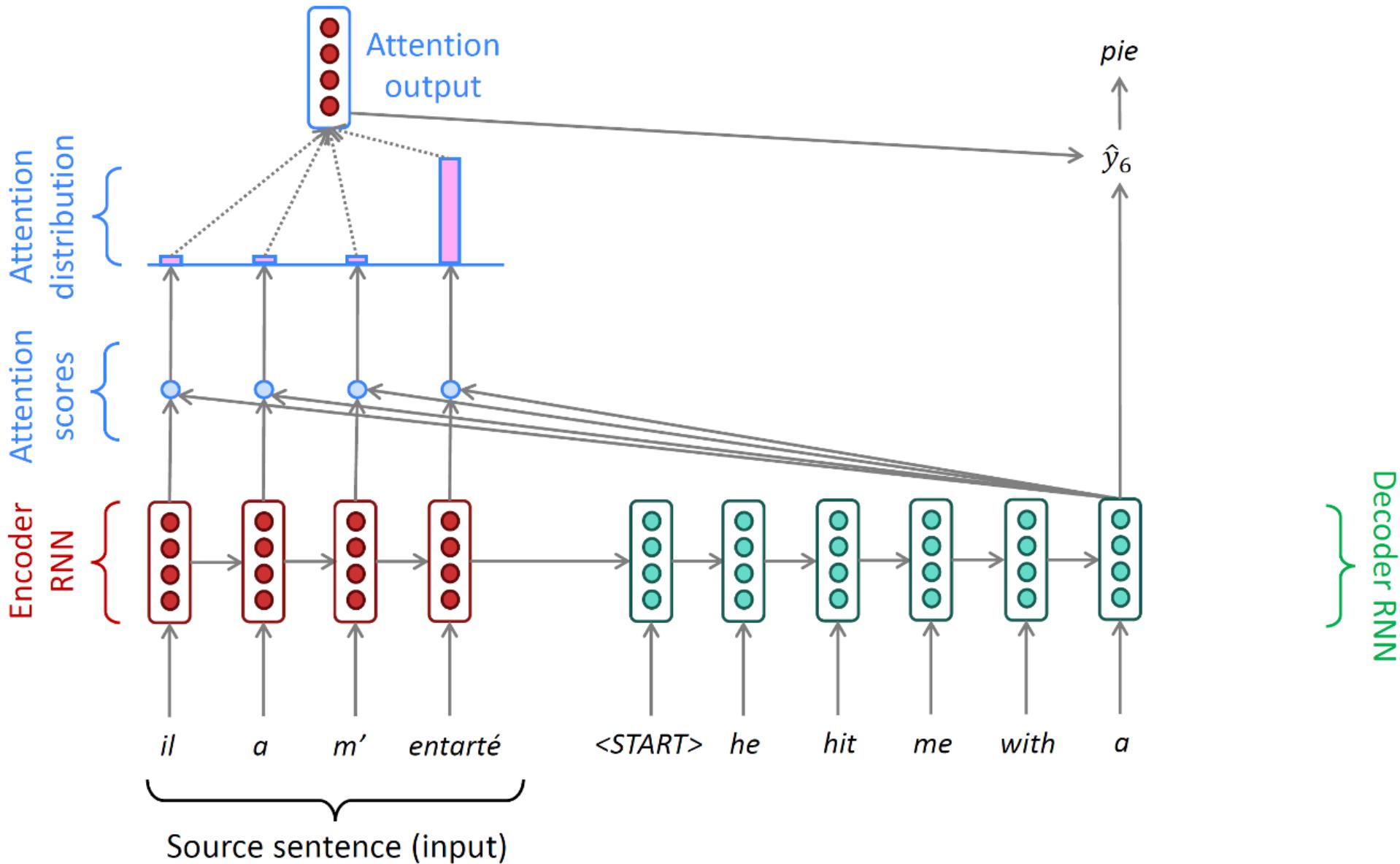
Seq2Seq with Attention



Seq2Seq with Attention



Seq2Seq with Attention



Seq2Seq with Attention

Summary

- Input sequence X , encoder f_{enc} , and decoder f_{dec}
- $f_{enc}(X)$ produces hidden states $h_1^{enc}, h_2^{enc}, \dots, h_N^{enc}$
- On time step t , we have decoder hidden state $\underline{h_t}$
- Compute attention score $e_i = h_t^\top h_i^{enc}$
- Compute attention distribution $\alpha_i = P_{att}(X_i) = \text{softmax}(e_i)$
- Attention output: $h_{att}^{enc} = \sum_i \alpha_i h_i^{enc}$
- $Y_t \sim g(h_t, h_{att}^{enc}; \theta)$
 - Sample an output using both h_t and h_{att}^{enc}

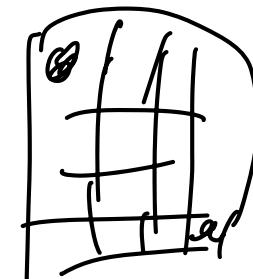
Attention

- It significantly improves NMT.
- It solves the bottleneck problem and the long-term dependency issue.
- Also helps gradient vanishing problem.
- Provides some interpretability
 - Understanding which word the RNN encoder focuses on
- Attention is a general technique
 - Given a set of vector values V_i and vector query q
 - Attention computes a weighted sum of values depending on q

	he	hit	me	with	a	pie
il	█					
a						
m'			█			
entarté		█	█		█	█

Other use cases:

- Attention can be viewed as a module.
- In encoder and decoder (more on this later)
- A representation of a set of points
 - Pointer network (Vinyals, Forunato, Jaitly '15)
 - Deep Sets (Zaheer et al., '17)
- Convolutional neural networks
 - To include non-local information in CNN (Non-local network, '18)



Attention

- Representation learning:
 - A method to obtain a fixed representation corresponding to a query q from an arbitrary set of representations $\{V_i\}$
 - Attention distribution: $\alpha_i = \text{softmax}(\underline{f(v_i, q)})$
 - Attention output: $v_{att} = \sum_i \alpha_i v_i$
- Attent variant: $f(v_i, q)$
 - Multiplicative attention: $f(v_i, q) = q^\top W h_i$, W is a weight matrix
 - Additive attention: $f(v_i, q) = u^\top \tanh(W_1 v_i + W_2 q)$

Key-query-value attention

$$X_t \in \mathbb{R}^{T \times d}$$
$$W^q, W^K, W^V \in \mathbb{R}^{d \times d}$$

- Obtain q_t, v_t, k_t from X_t
- $q_t = W^q X_t; v_t = W^v X_t; k_t = W^k X_t$ (position encoding omitted)
 - W^q, W^v, W^k are learnable weight matrices
- $\alpha_{i,j} = \text{softmax}(q_i^\top k_j); \text{out}_i = \sum_k \alpha_{i,j} v_j$
- Intuition: key, query, and value can focus on different parts of input

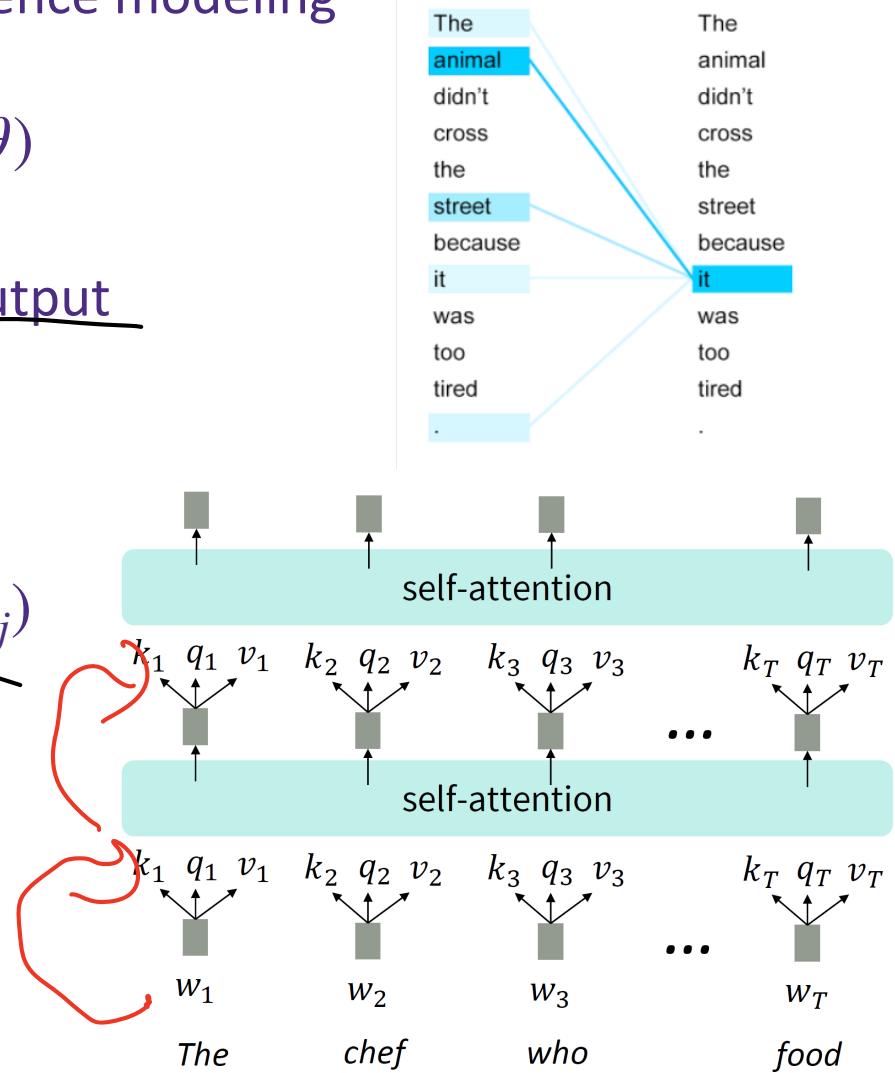
$$XQ \quad K^\top X^\top = XQK^\top X^\top \in \mathbb{R}^{T \times T}$$

All pairs of
attention scores!

$$\text{softmax} \left(\begin{matrix} XQK^\top X^\top \\ XV \end{matrix} \right) = \text{output} \in \mathbb{R}^{T \times d}$$

Attention is all you need (Vaswani '17)

- A pure attention-based architecture for sequence modeling
 - No RNN at all!
- Basic component: self-attention, $Y = f_{SA}(X; \theta)$
 - X_t uses attention on entire X sequence
 - Y_t computed from X_t and the attention output
- Computing Y_t
 - Key k_t , value v_t , query q_t from X_t
 - $(k_t, v_t, q_t) = g_1(X_t; \theta)$
 - Attention distribution $\alpha_{t,j} = \text{softmax}(q_t^\top k_j)$
 - Attention output $out_t = \sum_j \alpha_{t,j} v_j$
 - $Y_t = g_2(out_t; \theta)$



Issues of Vanilla Self-Attention

- Attention is order-invariant



- Lack of non-linearities
 - All the weights are simple weighted average



- Capability of autoregressive modeling
 - In generation tasks, the model cannot “look at the future”
 - e.g. Text generation:
 - Y_t can only depend on $X_{i < t}$
 - But vanilla self-attention requires the entire sequence

Position Encoding

- Vanilla self-attention

- $(\underline{k}_t, \underline{v}_t, \underline{q}_t) = g_1(X_t; \theta)$
- $\alpha_{t,j} = \text{softmax}(q_t^\top k_j)$
- Attention output $out_t = \sum_j \alpha_{t,j} v_j$

- Idea: position encoding:

- p_i : an embedding vector (feature) of position i
- $(\tilde{k}_t, \tilde{v}_t, \tilde{q}_t) = g_1([X_t, p_t]; \theta)$

- In practice: Additive is sufficient: $k_t \leftarrow \tilde{k}_t + p_t, q_t \leftarrow \tilde{q}_t + p_t, v_t \leftarrow \tilde{v}_t + p_t;$
 $(\tilde{k}_t, \tilde{v}_t, \tilde{q}_t) = g_1(X_t; \theta)$

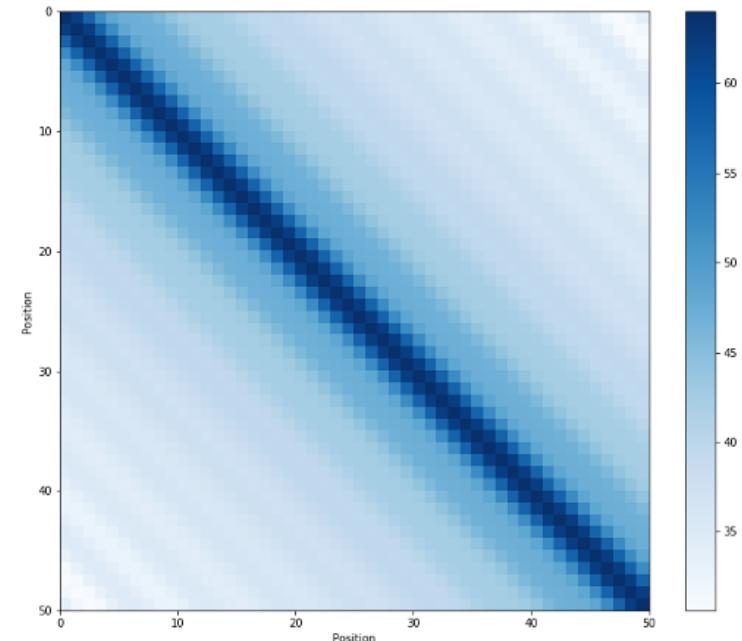
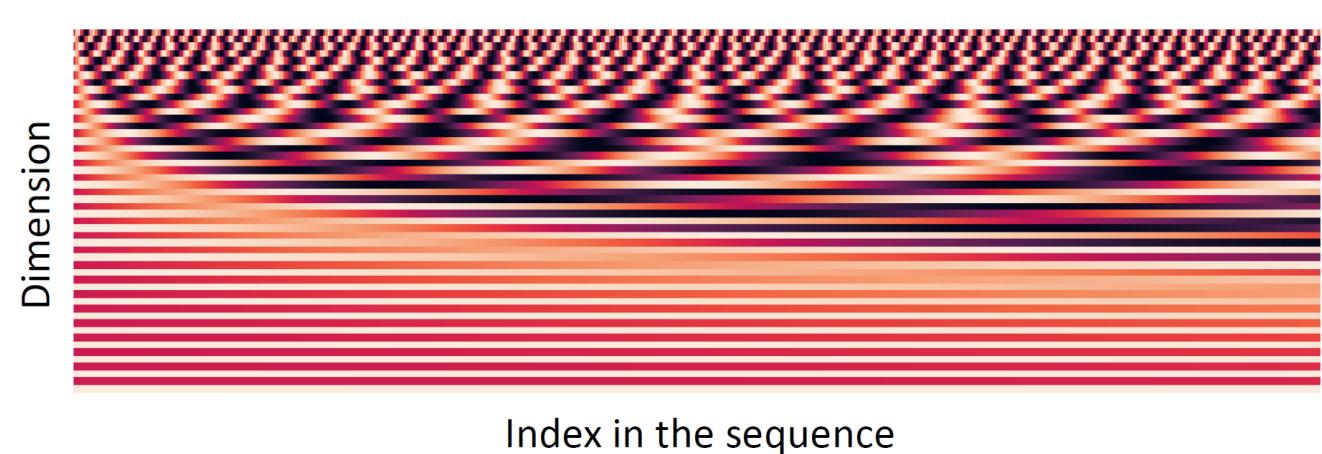
- p_t is only included in the first layer

Position Encoding

p_t design 1: Sinusoidal position representation

- Pros:
 - simple
 - naturally models “relative position”
 - Easily applied to long sequences
- Cons:
 - Not learnable
 - Generalization poorly to sequences longer than training data

$$p_i = \begin{pmatrix} \sin(i/10000^{2*1/d}) \\ \cos(i/10000^{2*1/d}) \\ \vdots \\ \sin(i/10000^{2*\frac{d}{2}/d}) \\ \cos(i/10000^{2*\frac{d}{2}/d}) \end{pmatrix}$$



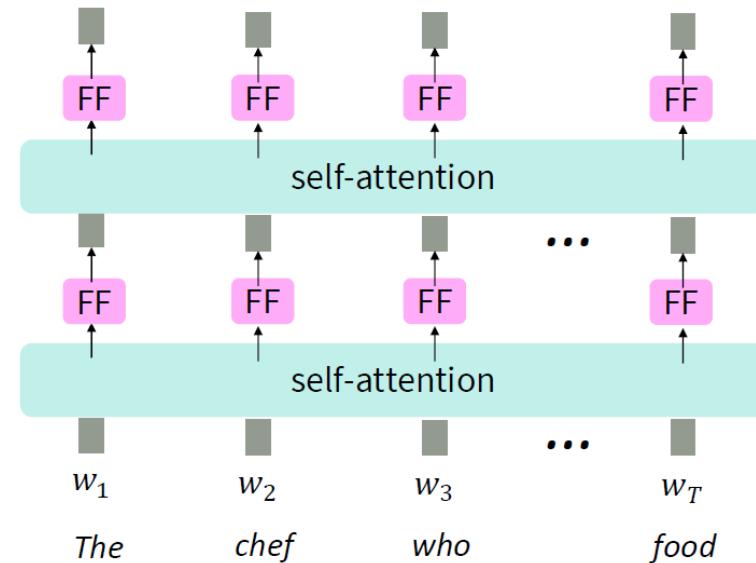
Position Encoding

p_t design 2: Learned representation

- Assume maximum length L , learn a matrix $p \in \mathbb{R}^{d \times T}$, p_t is a column of p
- Pros:
 - Flexible
 - Learnable and more powerful
- Cons:
 - Need to assume a fixed maximum length L
 - Does not work at all for length above L

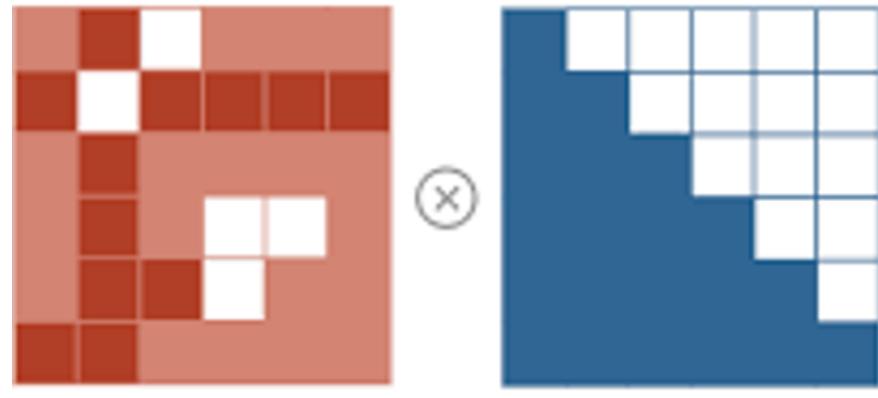
Combine Self-Attention with Nonlinearity

- Vanilla self-attention
 - No element-wise activation (e.g., ReLU, tanh)
 - Only weighted average and softmax operator
- Fix:
 - Add an MLP to process out_i
 - $m_i = MLP(out_i) = W_2 \text{ReLU}(W_1 out_i + b_1) + b_2$
 - Usually do not put activation layer before softmax



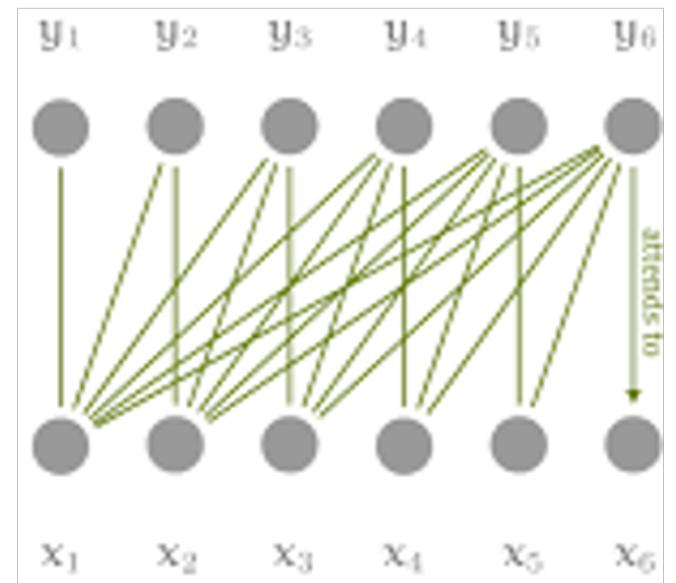
Masked Attention

- In language model decoder: $P(Y_t | X_{i < t})$
 - out_t cannot look at future $X_{i > t}$
- Masked attention
 - Compute $e_{i,j} = q_i^\top k_j$ as usual
 - Mask out $e_{i>j}$ by setting $e_{i>j} = -\infty$
 - $e \odot (1 - M) \leftarrow -\infty$
 - M is a fixed 0/1 mask matrix
 - Then compute $\alpha_i = \text{softmax}(e_i)$
 - Remarks:
 - $M = 1$ for full self-attention
 - Set M for arbitrary dependency ordering



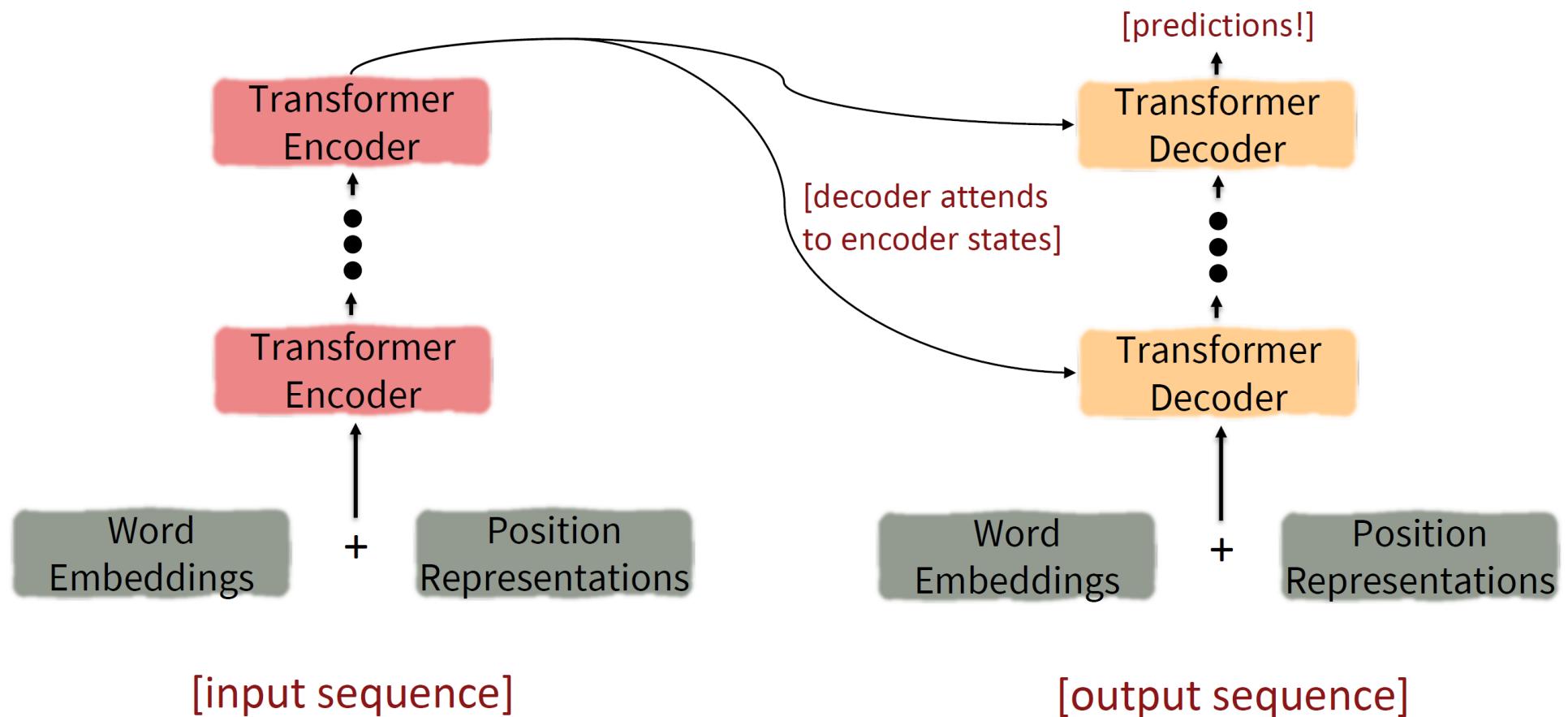
raw attention weights

mask



Transformer

Transformer-based sequence-to-sequence modeling



Key-query-value attention

- Obtain q_t, v_t, k_t from X_t
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$$\begin{array}{c} XQ \quad K^\top X^\top = XQK^\top X^\top \in \mathbb{R}^{T \times T} \\ \text{All pairs of attention scores!} \\ \text{softmax} \left(\begin{array}{c} XQK^\top X^\top \\ XV \end{array} \right) = \text{output} \in \mathbb{R}^{T \times d} \end{array}$$

Multi-headed attention

- Standard attention: single-headed attention
 - $X_t \in \mathbb{R}^d, Q, K, V \in \mathbb{R}^{d \times d}$
 - We only look at a single position j with high $\alpha_{i,j}$
 - What if we want to look at different j for different reasons?
- Idea: define h separate attention heads
 - h different attention distributions, keys, values, and queries
 - $Q^\ell, K^\ell, V^\ell \in \mathbb{R}^{d \times \frac{d}{h}}$ for $1 \leq \ell \leq h$
 - $\alpha_{i,j}^\ell = \text{softmax}((q_i^\ell)^\top k_j^\ell); out_i^\ell = \sum_j \alpha_{i,j}^\ell v_j^\ell$

#Params Unchanged!

Single-head attention
(just the query matrix)

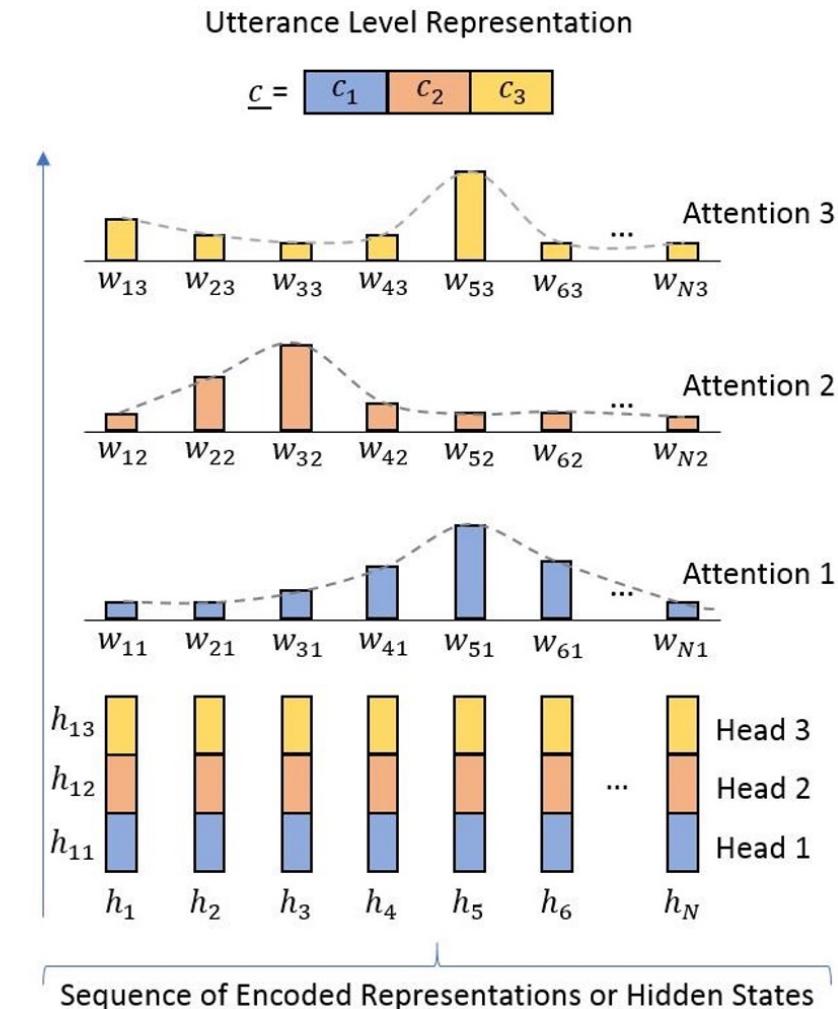
$$X \quad Q = XQ$$

Multi-head attention
(just two heads here)

$$X \quad Q_1 \quad Q_2 = XQ_1 \quad XQ_2$$

Multi-headed attention

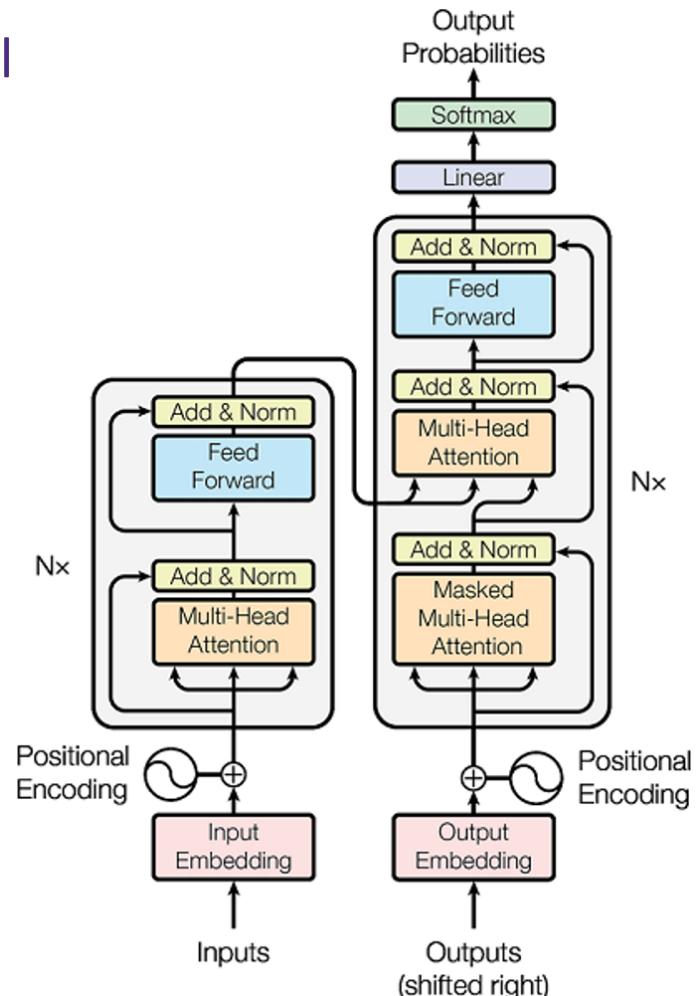
- Standard attention: single-headed attention
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Transformer

Transformer-based sequence-to-sequence model

- Basic building blocks: self-attention
 - Position encoding
 - Post-processing MLP
 - Attention mask
- Enhancements:
 - Key-query-value attention
 - Multi-headed attention
 - Architecture modifications:
 - Residual connection
 - Layer normalization



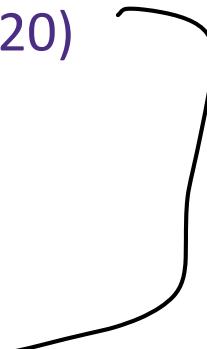
Transformer

Machine translation with transformer

Model	BLEU		Training Cost (FLOPs)	
	EN-DE	EN-FR	EN-DE	EN-FR
ByteNet [18]	23.75			
Deep-Att + PosUnk [39]		39.2		$1.0 \cdot 10^{20}$
GNMT + RL [38]	24.6	39.92	$2.3 \cdot 10^{19}$	$1.4 \cdot 10^{20}$
ConvS2S [9]	25.16	40.46	$9.6 \cdot 10^{18}$	$1.5 \cdot 10^{20}$
MoE [32]	26.03	40.56	$2.0 \cdot 10^{19}$	$1.2 \cdot 10^{20}$
Deep-Att + PosUnk Ensemble [39]		40.4		$8.0 \cdot 10^{20}$
GNMT + RL Ensemble [38]	26.30	41.16	$1.8 \cdot 10^{20}$	$1.1 \cdot 10^{21}$
ConvS2S Ensemble [9]	26.36	41.29	$7.7 \cdot 10^{19}$	$1.2 \cdot 10^{21}$
Transformer (base model)	27.3	38.1		$3.3 \cdot 10^{18}$
Transformer (big)	28.4	41.8		$2.3 \cdot 10^{19}$

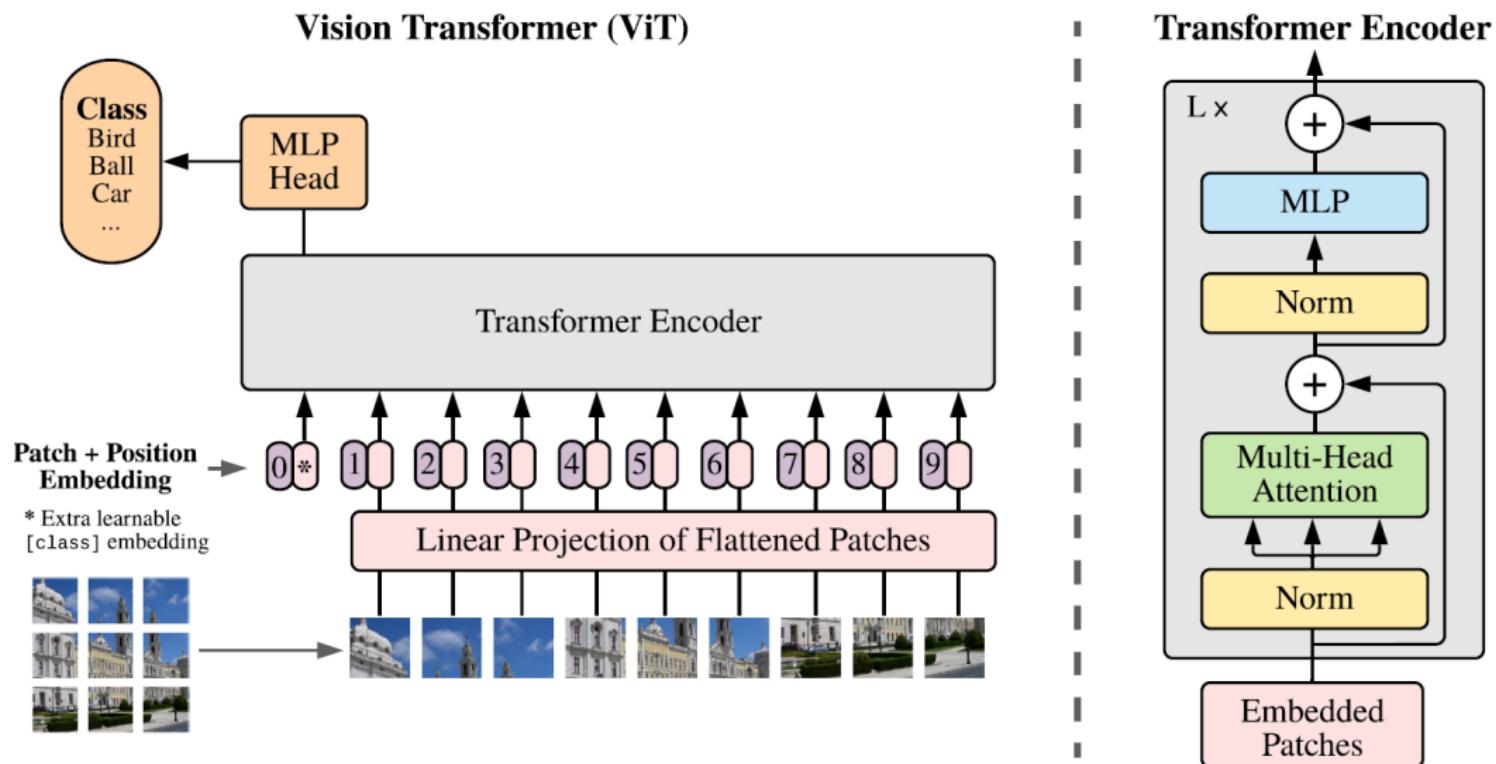
Transformer

- Limitations of transformer: Quadratic computation cost
 - Linear for RNNs
 - Large cost for large sequence length, e.g., $L > 10^4$
- Follow-ups:
 - Large-scale training: transformer-XL; XL-net ('20)
 - Projection tricks to $O(L)$: Linformer ('20)
 - Math tricks to $O(L)$: Performer ('20)
 - Sparse interactions: Big Bird ('20)
 - Deeper transformers: DeepNet ('22)



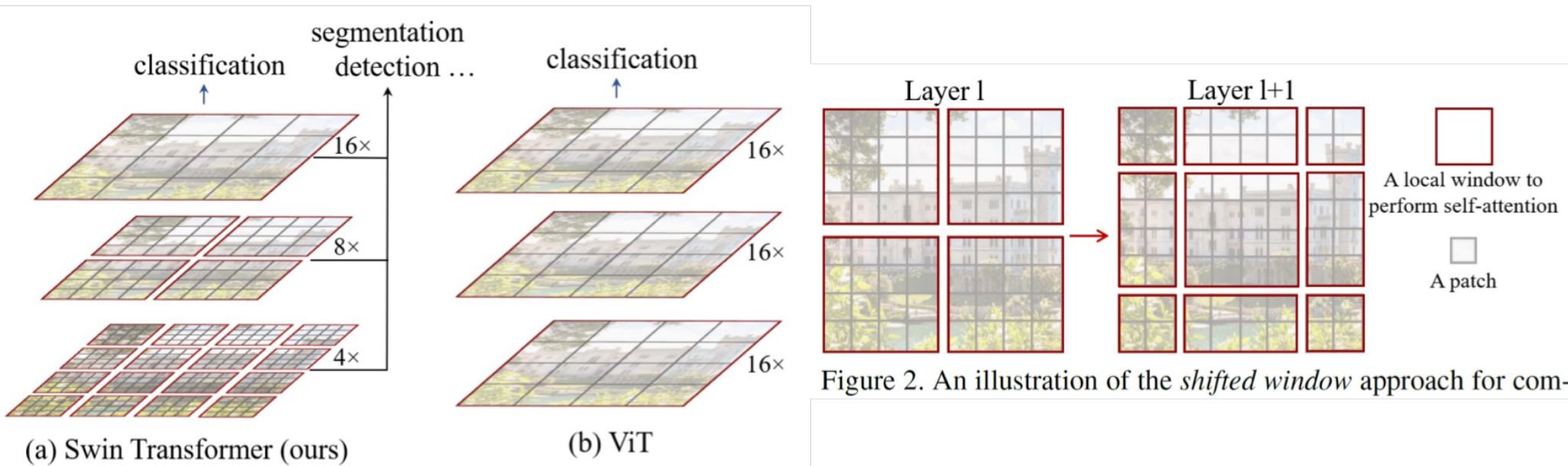
Transformer for Images

- Vision Transformer ('21)
 - Decompose an image to 16x16 patches and then apply transformer encoder

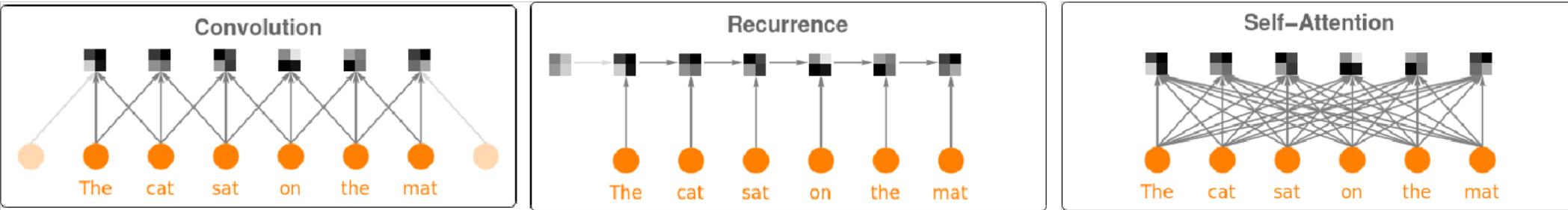


Transformer for Images

- Swin Transformer ('21)
 - Build hierarchical feature maps at different resolution
 - Self-attention only within each block
 - Shifted block partitions to encode information between blocks



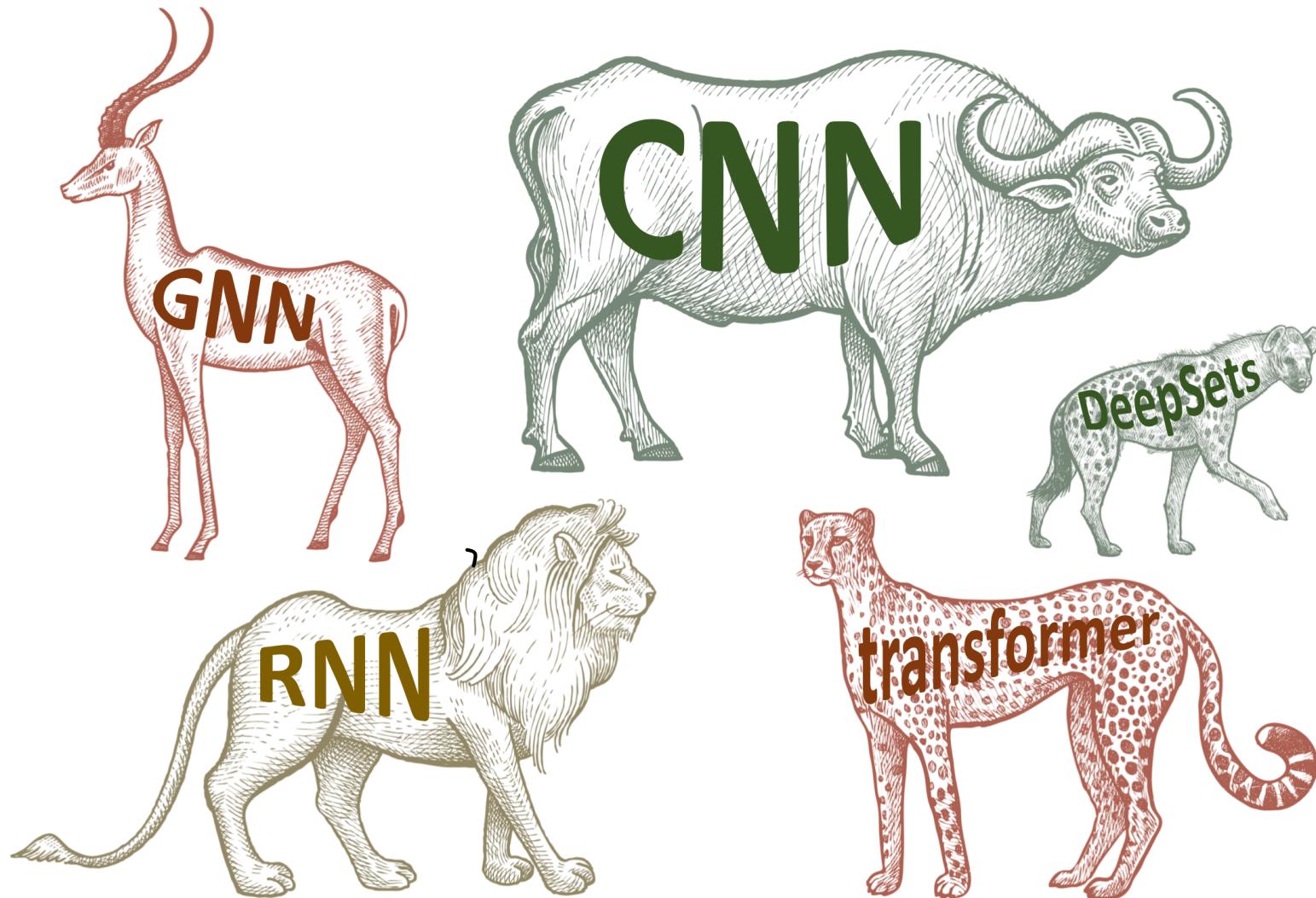
CNN vs. RNN vs. Attention



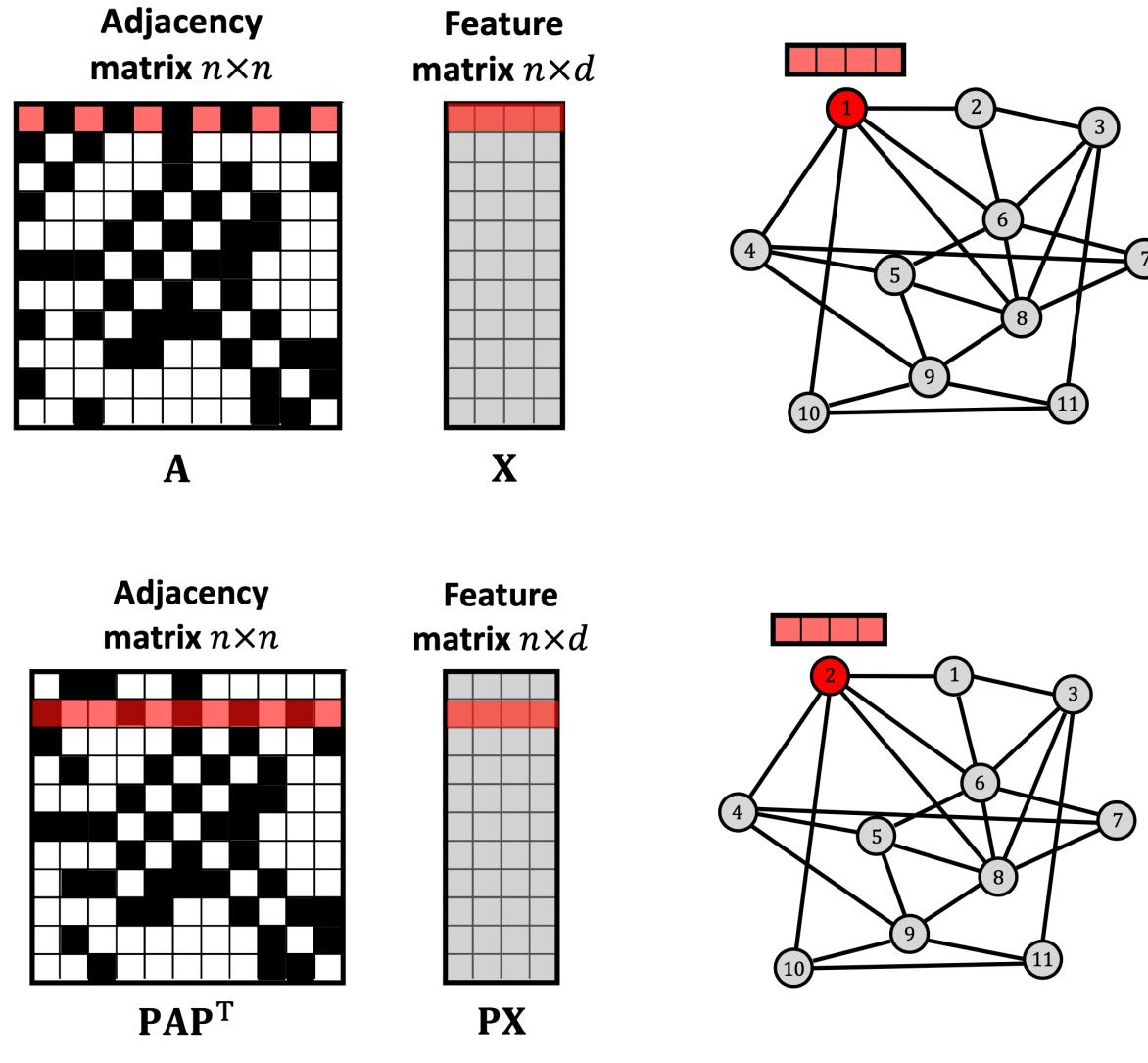
Summary

- Language model & sequence to sequence model:
 - Fundamental ideas and methods for sequence modeling
 - Attention mechanism
 - So far the most successful idea for sequence data in deep learning
 - A scale/order-invariant representation
 - Transformer: a fully attention-based architecture for sequence data
 - Transformer + Pretraining: the core idea in today's NLP tasks
 - LSTM is still useful in lightweight scenarios
-

Other architectures



Graph Neural Networks



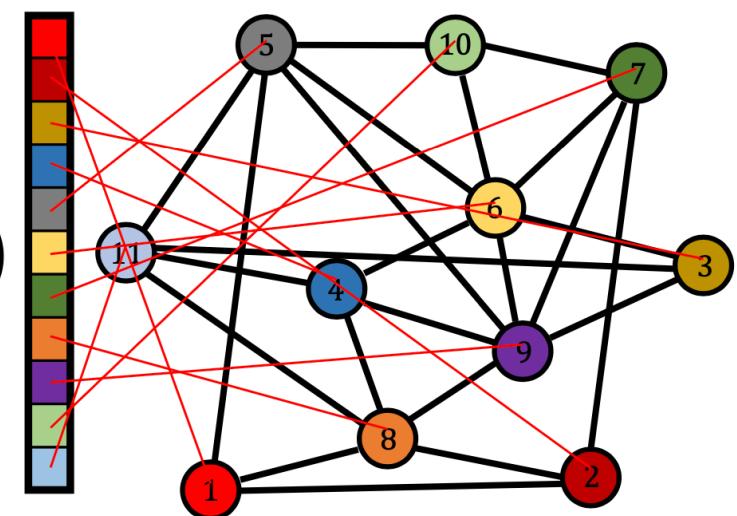
Graph Neural Networks

permutation-equivariant

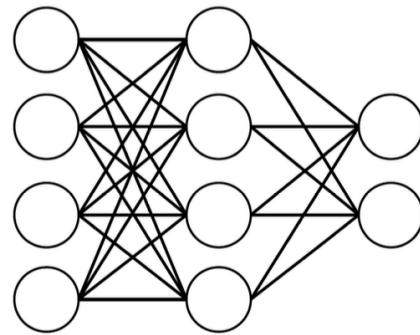
$$F(PX, PAP^T) = PF(X, A)$$

X : input $n \times d$

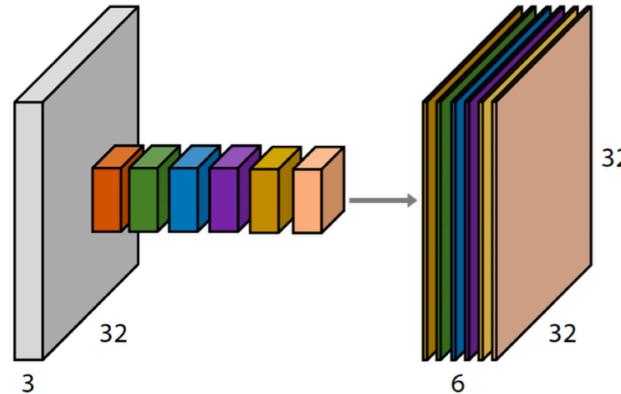
A : adj matrix



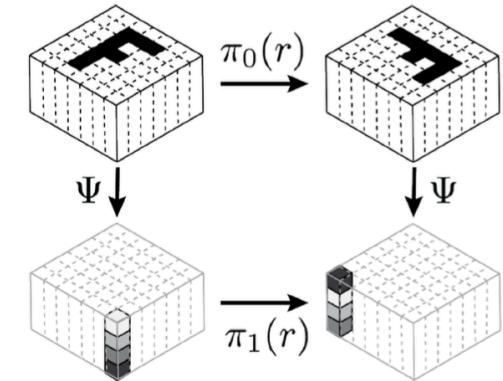
Geometric Deep Learning



Perceptrons
Function regularity



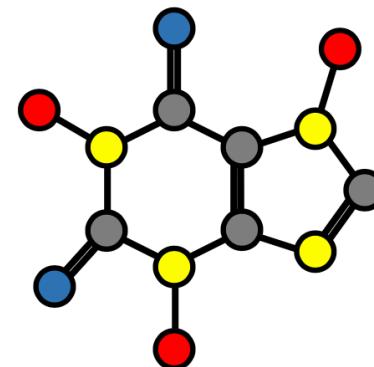
CNNs
Translation



Group-CNNs
Translation+Rotation



DeepSets / Transformers
Permutation



GNNs
Permutation



Intrinsic CNNs
Local frame choice