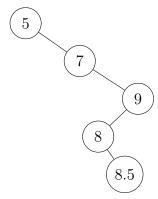
CS 430 Lecture 10 Activities

Opening Questions

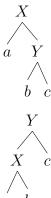
- 1. In your own words explain how you insert a new key in a binary search tree.
 - When you have a value, you compare the value you're inserting to the value in the node. If the inserting value is less than the value, you recursively call the Insert function with the left node. If the value was greater, you recursively call Insert on the right node.
- 2. Give an example of a series of 5 keys inserted one at a time into a binary search tree that will yield a tree of height 5.



The runtime of Insert is O(h) where h is the height of

the tree.

3. If we do a left rotate on node X below, explain which left and/or right child links need to be changed.



a b This tree maintains the relationships of the first tree. c was already larger than Y, which is maintained. b was smaller than Y but larger than X, which has also been maintained. But now the height of C has been decreased by 1.

Tree depth vs Tree Height

The length of the path from the root r to a node x is the depth of x in T. The height of a node in a tree is the number of edges on the longest simple downward path from the node to a leaf, and the height of a tree is the height of its root. The height of a tree is also equal to the largest depth of any node in the tree.

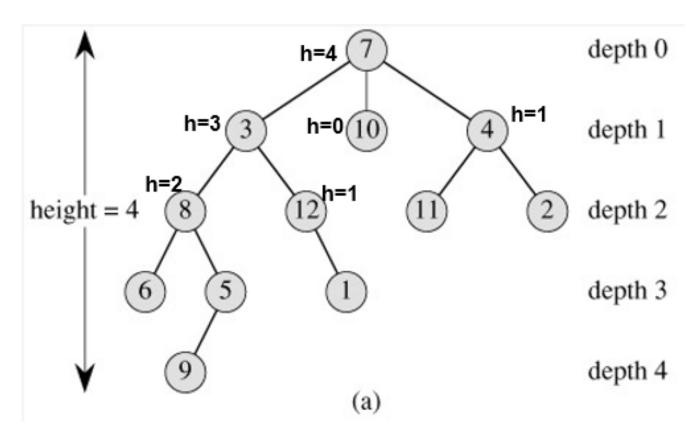
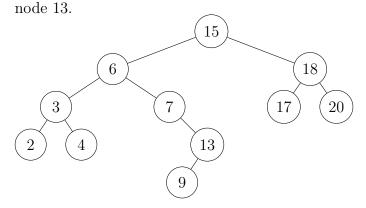


Figure 10.1: Height vs Depth of a Tree

BST Operations

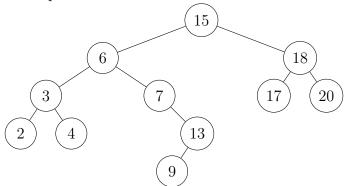
1) Write pseudocode for BST Successor (next larger value) (or Predecessor). Demonstrate on the below tree from node 15 and then



Algorithm 10.1 Binary Search Tree Successor (Best: O(1), Worst: O(h))

```
1: function Successor(p: Node) ▷ The Successor is usually the min of the graph in the right
   node, essentially, right than left-left-...-left.
      if p.right exists then
2:
3:
          return Min(p.right)
4:
       else
          go up until you go up on left pointer
5:
          if never go up left then
6:
                                                               ▶ You started in the largest value.
              return null
7:
          end if
8:
9:
       end if
10: end function
```

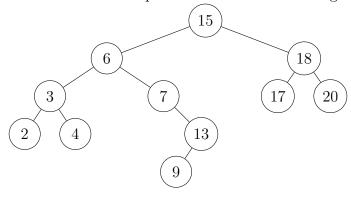
2) Write pseudocode for BST Insert. Demonstrate on the below tree to insert 5 and then 19.



Algorithm 10.2 Binary Search Tree Insert (O(h))

```
1: function Insert(key)
         if root == null then
 2:
             root \leftarrow Node(key)
 3:
             return
 4:
 5:
         end if
         p \leftarrow root
 6:
         q \leftarrow \text{null}
 7:
                                                                                         ▶ Following the parent node
         while p \neq \text{null do}
 8:
             q \leftarrow p
 9:
             if key < p.val then
10:
                                                                                                                 \triangleright Go Left
                 p \leftarrow p.left
11:
12:
             else
                  p \leftarrow p.right
                                                                                                               ▶ Go Right
13:
             end if
14:
         end while
15:
         if q.val > key then
16:
             q.left \leftarrow \text{Node}(key)
17:
18:
             q.right \leftarrow \text{Node}(key)
19:
         end if
20:
21: end function
```

3) What are the three possible cases when deleting a node from a BST?



- No children
 - Set the parent.left or parent.right (depending on where you came from) to null; O(1).
- One child
 - Make the parent of the child point to the child of the node you're deleting (essentially splicing out the node you're deleting); O(1).
- Two children
 - Swap the predecessor or successor value into the node, and then deleting the value where the predecessor successor was.

Algorithm 10.3 Delete A Node with 2 Children from a BST

- 1: **function** Delete 2Child (p: Node)2: $successor \leftarrow Successor(p)$ \triangleright Or Predeccesor, O(h)3: $p.value \leftarrow successor.value$ \triangleright O(1)4: Delete(successor) \triangleright O(h)
- 5: end function
- 4) Write pseudocode for BST Delete (assume you already have a pointer to the node)

Algorithm 10.4 Binary Search Tree Delete

1: **function** Delete (p: Node)

2:

3: end function

BST Rotations

Local operation in a search tree that maintains the BST property and possibly alters the height of the BST.

x and y are nodes; a, b, c are sub trees

5. Write pseudocode for LeftRotate (or RightRotate). What is the worst case runtime?

Algorithm 10.5 Binary Search Tree Left Rotate

```
1: function LeftRotate(p:Node, z:Node)
                                                         ▶ To make this right rotate, switch all lefts with
    rights and rights with left.
 2:
        savey \leftarrow p.right
                                                                                          \triangleright z is the parent of p
        if z.left = p then
 3:
            z.left \leftarrow savey
 4:
        else
 5:
 6:
            z.right \leftarrow savey
 7:
        end if
        p.right \leftarrow z.left
 8:
        y.left \leftarrow p
 9:
        savey.left \leftarrow p
10:
11: end function
```