

In Problems 1–20 determine whether the given differential equation is exact. If it is exact, solve it.

3.

$$(5x + 4y) dx + (4x - 8y^3) dy = 0$$

7.

$$(x^2 - y^2) dx + (x^2 - 2xy) dy = 0$$

12.

$$(3x^2y + e^y) dx + (x^3 + xe^y - 2y) dy = 0$$

13.

$$x \frac{dy}{dx} = 2xe^x - y + 6x^2$$

In Problems 21–26 solve the given initial-value problem.

23)

$$(4y + 2t - 5) dt + (6y + 4t - 1) dy = 0, \quad y(-1) = 2$$

In Problems 31–36 solve the given differential equation by finding, as in Example 4, an appropriate integrating factor.

31)

$$(2y^2 + 3x) dx + 2xy dy = 0$$

34)

$$\cos(x)dx + \left(1 + \frac{2}{y}\right) \sin(x)dy = 0$$

In Problems 37 and 38 solve the given initial-value problem by finding, as in Example 4, an appropriate integrating factor.

37)

$$x dx + (x^2y + 4y) dy = 0, \quad y(4) = 0$$