HW Section 4.3

Section 4.3

In Problems 1–14 find the general solution of the given second-order differential equation.

3.

$$y'' - y' - 6y = 0$$

5.

$$y'' + 8y' + 16y = 0$$

6.

$$y'' - 10y' + 25y = 0$$

9.

$$y'' + 9y = 0$$

11.

$$y'' - 4y' + 5y = 0$$

12.

$$2y'' + 2y' + y = 0$$

In Problems 15–28 find the general solution of the given higher-order differential equation.

15.

$$y''' - 4y'' - 5y' = 0$$

17.

$$y''' - 5y'' + 3y' + 9y = 0$$

25.

$$16\frac{d^4y}{dx^4} + 24\frac{d^2y}{dx^2} + 9y = 0$$

26.

$$\frac{d^4y}{dx^4} - 7\frac{d^2y}{dx^2} - 18y = 0$$

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In Problems 29–36 solve the given initial-value problem.

31.

$$\frac{d^2y}{dt^2} - 4\frac{dy}{dt} - 5y = 0, \quad y(1) = 0, \quad y'(1) = 2$$

32.

$$4y'' - 4y' - 3y = 0$$
, $y(0) = 1$, $y'(0) = 5$

In Problems 49–58 find a homogenous linear differential equation with constant coefficients whose general solution is given.

49.

$$y = c_1 e^x + c_2 e^{5x}$$

50.

$$y = c_1 e^{-4x} + c_2 e^{-3x}$$

53.

$$y = c_1 \cos(3x) + c_2 \sin(3x)$$

56.

$$y = c_1 + c_2 e^{2x} \cos(5x) + c_3 e^{2x} \sin(5x)$$

Section 4.1

In Problems 23–30 verify that the given functions form a fundamental set of solutions of the differential equation on the indicated interval. Form the general solution.

23.

$$y'' - y' - 12y = 0$$
; e^{-3x} , e^{4x} , $(-\infty, \infty)$

25.

$$y'' - 2y' + 5y = 0$$
; $e^x \cos(2x)$, $e^x \sin(2x)$, $(-\infty, \infty)$

- 40. Is the set of functions $f_1(x) = e^{x+2}$, $f_2(x) = e^{x-3}$ linearly dependent or linearly independent on $(-\infty, \infty)$? Discuss.
- 41. Suppose y_1, y_2, \ldots, y_k are k linearly independent solutions on $(-\infty, \infty)$ of a homogeneous linear nth-order differential equation with constant coefficients. By Theorem 4.1.2 it follows that $y_{k+1} = 0$ is also a solution of the differential equation. Is the set of functions $y_1, y_2, \ldots, y_k, y_{k+1}$ linearly dependent or linearly independent on $(-\infty, \infty)$? Discuss.
- 42. Suppose that y_1, y_2, \ldots, y_k are k nontrivial solutions of a homogeneous linear nth-order differential equation with constant coefficients and that k = n + 1. Is the set of solutions y_1, y_2, \ldots, y_k linearly dependent or linearly independent on $(-\infty, \infty)$? Discuss.