

# OSTSC

## ESPO

1. Calculating the mean vector for each column of the positive data, which is the mean value for each time point

M

|   | 1      | 2      | 3      | 4      | 5      | 6      | 7      | 8      | 9      | 10     |
|---|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 1 | 0.5336 | 0.5509 | 0.5539 | 0.5843 | 0.5990 | 0.6166 | 0.6228 | 0.6582 | 0.7218 | 0.7820 |

R

```
> Me  
[1] 0.5336481 0.5509333 0.5538938 0.5843321 0.5990064 0.6165761 0.6227543 0.6581734 0.7218326 0.7819764
```

2. Calculating the covariance matrix of the positive data (column)

M

|    | 1           | 2       | 3       | 4       | 5      | 6       | 7           | 8      | 9           | 10          |
|----|-------------|---------|---------|---------|--------|---------|-------------|--------|-------------|-------------|
| 1  | 0.1349      | 0.0885  | 0.0666  | 0.0450  | 0.0301 | 0.0178  | 0.0119      | 0.0021 | -8.8018e-05 | -0.0041     |
| 2  | 0.0885      | 0.1301  | 0.0877  | 0.0577  | 0.0432 | 0.0296  | 0.0220      | 0.0033 | 0.0022      | -0.0021     |
| 3  | 0.0666      | 0.0877  | 0.1370  | 0.0797  | 0.0534 | 0.0399  | 0.0291      | 0.0177 | 0.0110      | -0.0019     |
| 4  | 0.0450      | 0.0577  | 0.0797  | 0.1337  | 0.0931 | 0.0642  | 0.0451      | 0.0305 | 0.0212      | -0.0031     |
| 5  | 0.0301      | 0.0432  | 0.0534  | 0.0931  | 0.1362 | 0.0854  | 0.0578      | 0.0344 | 0.0233      | 0.0010      |
| 6  | 0.0178      | 0.0296  | 0.0399  | 0.0642  | 0.0854 | 0.1345  | 0.0862      | 0.0506 | 0.0293      | -0.0037     |
| 7  | 0.0119      | 0.0220  | 0.0291  | 0.0451  | 0.0578 | 0.0862  | 0.1399      | 0.0782 | 0.0472      | -4.0324e-04 |
| 8  | 0.0021      | 0.0033  | 0.0177  | 0.0305  | 0.0344 | 0.0506  | 0.0782      | 0.1359 | 0.0663      | 0.0058      |
| 9  | -8.8018e-05 | 0.0022  | 0.0110  | 0.0212  | 0.0233 | 0.0293  | 0.0472      | 0.0663 | 0.1269      | 0.0156      |
| 10 | -0.0041     | -0.0021 | -0.0019 | -0.0031 | 0.0010 | -0.0037 | -4.0324e-04 | 0.0058 | 0.0156      | 0.0679      |

R

|               |              |              |              |             |              |               |             |               |               |
|---------------|--------------|--------------|--------------|-------------|--------------|---------------|-------------|---------------|---------------|
| 1.348631e-01  | 0.088459918  | 0.066609461  | 0.045016128  | 0.030148237 | 0.017843393  | 0.0118544017  | 0.002104608 | -8.801822e-05 | -0.0041297934 |
| 8.845992e-02  | 0.130085605  | 0.087697139  | 0.057655225  | 0.043202252 | 0.029569199  | 0.0219744459  | 0.003333716 | 2.236872e-03  | -0.0021233176 |
| 6.660946e-02  | 0.087697139  | 0.136970050  | 0.079659664  | 0.053411609 | 0.039911509  | 0.0290948953  | 0.017745992 | 1.101591e-02  | -0.0019177316 |
| 4.501613e-02  | 0.057655225  | 0.079659664  | 0.133735282  | 0.093117489 | 0.064167345  | 0.0451460214  | 0.030523237 | 2.116930e-02  | -0.0031046857 |
| 3.014824e-02  | 0.043202252  | 0.053411609  | 0.093117489  | 0.136227948 | 0.085361608  | 0.0578129402  | 0.034435713 | 2.332335e-02  | 0.0010167466  |
| 1.784339e-02  | 0.029569199  | 0.039911509  | 0.064167345  | 0.085361608 | 0.134545603  | 0.0861548370  | 0.050641261 | 2.925992e-02  | -0.0037260883 |
| 1.185440e-02  | 0.021974446  | 0.029094895  | 0.045146021  | 0.057812940 | 0.086154837  | 0.1398524642  | 0.078195882 | 4.724219e-02  | -0.0004032377 |
| 2.104608e-03  | 0.003333716  | 0.017745992  | 0.030523237  | 0.034435713 | 0.050641261  | 0.0781958817  | 0.135866161 | 6.628068e-02  | 0.0057526227  |
| -8.801822e-05 | 0.002236872  | 0.011015912  | 0.021169301  | 0.023323347 | 0.029259920  | 0.0472421896  | 0.066280679 | 1.269116e-01  | 0.0156174350  |
| -4.129793e-03 | -0.002123318 | -0.001917732 | -0.003104686 | 0.001016747 | -0.003726088 | -0.0004032377 | 0.005752623 | 1.561744e-02  | 0.0678758833  |

3. Calculating eigenvalues and eigenvectors of the covariance matrix PCov

D: diagonal matrix D of eigenvalues

V: matrix V whose columns are the relating eigenvectors

$$PCov * V = V * D$$

D:

M

|        |        |        |        |        |        |        |        |        |        |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 0.4964 | 0.2599 | 0.1347 | 0.0925 | 0.0682 | 0.0614 | 0.0555 | 0.0409 | 0.0373 | 0.0302 |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|

R

```
> D
[1] 0.49636325 0.25985357 0.13466144 0.09252087 0.06820998 0.06144125 0.05551067 0.04088814 0.03731218
[10] 0.03017229
```

V: (Some columns have opposite +/- , I searched this issue online, and it's because the different algorithm used by Matlab/R. The source codes of Matlab eig() was in C/C++, so there's no way to find how Matlab calculates the eigenvectors. I don't know how to make the eigenvectors of Matlab and R exactly same.)

M

|         |         |         |         |         |         |         |         |         |         |
|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|
| -0.2615 | -0.4298 | 0.3494  | -0.2816 | -0.3661 | -0.3719 | -0.2849 | -0.0575 | -0.4048 | 0.1575  |
| -0.3179 | -0.4200 | 0.2442  | -0.1462 | -0.0952 | 0.1241  | 0.1559  | 0.0810  | 0.6713  | -0.3682 |
| -0.3656 | -0.3296 | 0.1321  | 0.1609  | 0.4690  | 0.4117  | 0.2535  | 0.1692  | -0.2583 | 0.4066  |
| -0.4100 | -0.1096 | -0.2534 | 0.4043  | 0.2328  | -0.1324 | -0.1908 | -0.3938 | -0.2230 | -0.5285 |
| -0.4030 | 0.0426  | -0.4375 | 0.2673  | -0.2364 | -0.1995 | -0.1994 | 0.0525  | 0.3887  | 0.5326  |
| -0.3808 | 0.2235  | -0.3491 | -0.2654 | -0.2513 | 0.0478  | 0.2658  | 0.5503  | -0.3017 | -0.2878 |
| -0.3483 | 0.3704  | 0.0169  | -0.4887 | -0.0248 | 0.2410  | 0.1517  | -0.6317 | 0.0266  | 0.1448  |
| -0.2583 | 0.4407  | 0.3734  | -0.0966 | 0.3638  | -0.0158 | -0.5832 | 0.3174  | 0.1177  | -0.0555 |
| -0.1827 | 0.3631  | 0.5129  | 0.4623  | -0.1967 | -0.3025 | 0.4763  | -0.0211 | -0.0174 | 0.0144  |
| 0.0013  | 0.0568  | 0.1434  | 0.3259  | -0.5405 | 0.6836  | -0.3058 | -0.0266 | -0.1096 | -0.0651 |

R

|              |             |             |             |             |             |            |             |             |             |
|--------------|-------------|-------------|-------------|-------------|-------------|------------|-------------|-------------|-------------|
| -0.261507059 | 0.42978637  | 0.34936596  | -0.28157959 | 0.36613636  | -0.37192209 | 0.2849205  | -0.05746296 | -0.40483146 | 0.15748660  |
| -0.317875818 | 0.41997455  | 0.24424110  | -0.14620661 | 0.09520869  | 0.12411448  | -0.1558977 | 0.08098279  | 0.67130860  | -0.36818422 |
| -0.365638105 | 0.32964422  | 0.13214446  | 0.16088133  | -0.46895140 | 0.41168024  | -0.2534569 | 0.16920526  | -0.25827333 | 0.40660369  |
| -0.409965114 | 0.10963756  | -0.25339974 | 0.40429130  | -0.23280013 | -0.13237739 | 0.1907754  | -0.39377525 | -0.22303791 | -0.52851257 |
| -0.402959415 | -0.04264977 | -0.43749067 | 0.26729884  | 0.23640917  | -0.19948974 | 0.1993740  | 0.05248792  | 0.38870072  | 0.53261549  |
| -0.380849819 | -0.22346112 | -0.34912902 | -0.26537676 | 0.25125837  | 0.04778463  | -0.2658154 | 0.55025136  | -0.30172641 | -0.28777646 |
| -0.348284214 | -0.37037456 | 0.01685378  | -0.48869311 | 0.02484174  | 0.24099872  | -0.1516519 | -0.63169786 | 0.02655727  | 0.14481887  |
| -0.258282371 | -0.44069087 | 0.37342230  | -0.09657748 | -0.36376604 | -0.01579662 | 0.5831573  | 0.31737148  | 0.11774244  | -0.05545024 |
| -0.182675296 | -0.36311444 | 0.51286172  | 0.46234022  | 0.19665053  | -0.30247974 | -0.4763104 | -0.02111650 | -0.01735701 | 0.01441772  |
| 0.001260301  | -0.05681208 | 0.14342790  | 0.32591741  | 0.54049405  | 0.68363859  | 0.3058275  | -0.02657336 | -0.10958249 | -0.06508919 |

4. Calculating the covariance matrix of the total data (column) TCov.

Then calculating dT. (dT = V' \* TCov \* V)

Turning the diagonal of matrix dT to a vector.

M

|        |        |        |        |        |        |        |        |        |        |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 0.4579 | 0.1638 | 0.0867 | 0.0528 | 0.0527 | 0.0413 | 0.0214 | 0.0177 | 0.0185 | 0.0148 |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|

R

```
> dT
[1] 0.45788128 0.16378062 0.08665568 0.05279657 0.05266202 0.04133698 0.02141124 0.01769672 0.01845588
[10] 0.01477735
```

##### 5. Modifying the eigen spectrum values

M = index of the first number in d which  $\leq 0.005$  (index starts from 1)

n = the original data column number (time series length)

$\text{Alpha} = d(1) * d(M) * (M-1) / (d(1) - d(M))$

$\text{Beta} = (M * d(M) - d(1)) / (d(1) - d(M))$

dMod = a new created array with length n

For i from 1 to n

    if i < M           # the reliable portion of the eigen spectrum

        dMod(i) = d(i)

    else

        dMod(i) = Alpha/(i+Beta)

        if dMod(i) > dT(i)

            dMod(i) = dT(i)

        end

    end

end

DD = the square root of dMod

M

| Name ▲ | Value   |
|--------|---------|
| Alpha  | 0.2891  |
| Beta   | -0.4175 |

dMod

|        |        |        |        |        |        |        |        |        |        |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 0.4964 | 0.2599 | 0.1347 | 0.0925 | 0.0682 | 0.0614 | 0.0555 | 0.0409 | 0.0373 | 0.0148 |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|

DD

|        |        |        |        |        |        |        |        |        |        |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 0.7045 | 0.5098 | 0.3670 | 0.3042 | 0.2612 | 0.2479 | 0.2356 | 0.2022 | 0.1932 | 0.1216 |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|

R

| values |                    |
|--------|--------------------|
| Alpha  | 0.28912563282355   |
| Beta   | -0.417512013265098 |

dMod

|           |           |           |            |            |            |            |            |            |            |
|-----------|-----------|-----------|------------|------------|------------|------------|------------|------------|------------|
| 0.4963633 | 0.2598536 | 0.1346614 | 0.09252087 | 0.06820998 | 0.06144125 | 0.05551067 | 0.04088814 | 0.03731218 | 0.01477735 |
|-----------|-----------|-----------|------------|------------|------------|------------|------------|------------|------------|

DD

|           |           |           |           |           |           |          |           |           |           |
|-----------|-----------|-----------|-----------|-----------|-----------|----------|-----------|-----------|-----------|
| 0.7045305 | 0.5097583 | 0.3669625 | 0.3041724 | 0.2611704 | 0.2478735 | 0.235607 | 0.2022082 | 0.1931636 | 0.1215621 |
|-----------|-----------|-----------|-----------|-----------|-----------|----------|-----------|-----------|-----------|

- Starting from here is generating random vectors from the multivariate normal distribution. Even given a same seed number, the vector generated by Matlab and R are different. So for comparison, I used a same vector for both rest test.

The vector is:

|        |         |        |        |        |         |        |        |         |        |
|--------|---------|--------|--------|--------|---------|--------|--------|---------|--------|
| 1.5118 | -0.3054 | 0.5758 | 0.7383 | 0.4874 | -0.8205 | 0.3295 | 1.5953 | -0.8356 | 0.1836 |
|--------|---------|--------|--------|--------|---------|--------|--------|---------|--------|

Before Euclidean distance checking, the generated vector need to be modified by

$$x = \text{vector} * DD * V' + Me$$

DD and Me are the same in R and Matlab. Only V has minor different. I used same V for comparison.

x:

M

|        |        |        |        |        |        |         |        |        |        |
|--------|--------|--------|--------|--------|--------|---------|--------|--------|--------|
| 0.3935 | 0.0501 | 0.1194 | 0.0771 | 0.1963 | 0.3338 | -0.0592 | 0.5932 | 0.8419 | 0.8568 |
|--------|--------|--------|--------|--------|--------|---------|--------|--------|--------|

R

|          |            |           |            |          |           |             |           |           |           |
|----------|------------|-----------|------------|----------|-----------|-------------|-----------|-----------|-----------|
| 0.393485 | 0.05007858 | 0.1194362 | 0.07714205 | 0.196272 | 0.3337652 | -0.05918221 | 0.5932051 | 0.8418713 | 0.8568402 |
|----------|------------|-----------|------------|----------|-----------|-------------|-----------|-----------|-----------|

- The Euclidean distance between x and positive data:

M

First 10 elements from total 600:

|        |        |        |        |        |        |        |        |        |        |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 1.6736 | 1.3246 | 1.9920 | 1.8604 | 2.0885 | 1.2420 | 1.0674 | 1.4747 | 2.1704 | 1.9786 |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|

Sum & Mean:

```
>> temp = sum(PDist);  
>> temp  
  
temp =  
  
    955.6397  
  
>> temp = temp/600  
  
temp =  
  
    1.5927
```

R

First 10 elements from total 600:

|         |          |          |          |          |          |          |          |          |         |
|---------|----------|----------|----------|----------|----------|----------|----------|----------|---------|
| 1.67361 | 1.324554 | 1.991967 | 1.860365 | 2.088549 | 1.242046 | 1.067399 | 1.474712 | 2.170398 | 1.97859 |
|---------|----------|----------|----------|----------|----------|----------|----------|----------|---------|

Sum & Mean:

```
> temp = sum(PDist)  
> temp  
[1] 955.6397  
> temp/600  
[1] 1.592733
```

8. Index & value of the smallest element in the Euclidean distance between x and negative data

M

```

>> [tmp ind] = min(NDist);
>> tmp

tmp =

    0.3418

>> ind

ind =

    27426

```

R

```

> tmp <- min(NDist)
> tmp
[1] 0.341785
> ind <- which.min(NDist)
> ind
[1] 27426

```

## ADASYN

9. Calculating the positive data's number of samples and time series length

M

```

>> NT

NT =

    600

>> NumAtt

NumAtt =

    10

```

R

```

> NT
[1] 600
> NumAtt
[1] 10

```

10. Calculating the number of samples should be generated upon each positive sample. The number of all samples would be generated was set 10,000 in this testing experiment.

M

Samples:

|    |
|----|
| 95 |
| 15 |
| 18 |
| 12 |
| 18 |
| 18 |
| 15 |
| 19 |
| 18 |
| 1  |

Sum:

```
>> sum(No)

ans =

    10000
```

R

Samples:

|    |
|----|
| 95 |
| 15 |
| 18 |
| 12 |
| 18 |
| 18 |
| 15 |
| 19 |
| 18 |
| 1  |

Sum:

```
> sum(No)
[1] 10000
```

11. Finding the k indices corresponding to the closest indices. K default set to 5.

For the first positive data sample:

M

|     |     |    |     |     |
|-----|-----|----|-----|-----|
| 128 | 243 | 87 | 221 | 408 |
|-----|-----|----|-----|-----|

R

|     |     |    |     |     |
|-----|-----|----|-----|-----|
| 128 | 243 | 87 | 221 | 408 |
|-----|-----|----|-----|-----|

12. Generating data using a same random generated order list rn.

M (1:10 rows, 1:10 cols)

|        |        |        |        |        |        |        |        |        |        |
|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 0.7215 | 0.7126 | 0.7342 | 0.7102 | 0.6910 | 0.7024 | 0.7158 | 0.7248 | 0.6664 | 0.6945 |
| 0.7342 | 0.8027 | 0.7612 | 0.7330 | 0.7579 | 0.7523 | 0.7359 | 0.7631 | 0.7834 | 0.8121 |
| 0.7196 | 0.7890 | 0.7795 | 0.7484 | 0.7489 | 0.7399 | 0.7493 | 0.7889 | 0.7790 | 0.7878 |
| 0.7460 | 0.7816 | 0.7890 | 0.7366 | 0.7686 | 0.7372 | 0.7775 | 0.7855 | 0.7865 | 0.7836 |
| 0.7241 | 0.7831 | 0.7930 | 0.7796 | 0.7811 | 0.7688 | 0.7759 | 0.7786 | 0.7802 | 0.7821 |
| 0.7325 | 0.7812 | 0.7762 | 0.7652 | 0.7642 | 0.7647 | 0.7700 | 0.7784 | 0.7748 | 0.7783 |
| 0.7376 | 0.7531 | 0.7599 | 0.7549 | 0.7496 | 0.7567 | 0.7564 | 0.7557 | 0.7573 | 0.7567 |
| 0.7778 | 0.7136 | 0.7112 | 0.7567 | 0.7657 | 0.7664 | 0.7622 | 0.7413 | 0.7372 | 0.7637 |
| 0.8009 | 0.7595 | 0.7454 | 0.7576 | 0.7710 | 0.7734 | 0.7711 | 0.7674 | 0.7507 | 0.7378 |
| 0.7814 | 0.7497 | 0.7761 | 0.7924 | 0.8453 | 0.7675 | 0.8614 | 0.7475 | 0.7667 | 0.7590 |

R(1:10 rows, 1:10 cols)

|           |           |           |           |           |           |           |           |           |           |
|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|
| 0.7215364 | 0.7126133 | 0.7342486 | 0.7102273 | 0.6909929 | 0.7024262 | 0.7158408 | 0.7247686 | 0.6663753 | 0.6945394 |
| 0.7341552 | 0.8026660 | 0.7612480 | 0.7330197 | 0.7579490 | 0.7523210 | 0.7359235 | 0.7631486 | 0.7833597 | 0.8120859 |
| 0.7195918 | 0.7890007 | 0.7795359 | 0.7483930 | 0.7489327 | 0.7399240 | 0.7493385 | 0.7888918 | 0.7789952 | 0.7877711 |
| 0.7459861 | 0.7815557 | 0.7890041 | 0.7366452 | 0.7685508 | 0.7371588 | 0.7775313 | 0.7854667 | 0.7865363 | 0.7836255 |
| 0.7241203 | 0.7831127 | 0.7929627 | 0.7796013 | 0.7810818 | 0.7688142 | 0.7759419 | 0.7786340 | 0.7801665 | 0.7821185 |
| 0.7324621 | 0.7812004 | 0.7762187 | 0.7652379 | 0.7642392 | 0.7647131 | 0.7700056 | 0.7783545 | 0.7747617 | 0.7783241 |
| 0.7376493 | 0.7530557 | 0.7598970 | 0.7548852 | 0.7495982 | 0.7567323 | 0.7564003 | 0.7557472 | 0.7572656 | 0.7566980 |
| 0.7777677 | 0.7136331 | 0.7111698 | 0.7566517 | 0.7656592 | 0.7663729 | 0.7622274 | 0.7413278 | 0.7372196 | 0.7636958 |
| 0.8008719 | 0.7594832 | 0.7453702 | 0.7575589 | 0.7709697 | 0.7734069 | 0.7711179 | 0.7674259 | 0.7507091 | 0.7377854 |
| 0.7813701 | 0.7497223 | 0.7761397 | 0.7924465 | 0.8452980 | 0.7675219 | 0.8614060 | 0.7474998 | 0.7666955 | 0.7590476 |