

Multivariate Analysis Publication Code Part 2: Bayesian Networks

Jerry Z. Zhang, Lacey W. Heinsberg, and Daniel E. Weeks
Department of Human Genetics
University of Pittsburgh

April 05, 2022

Contents

1	Overview	1
2	Load Libraries	2
3	Read in the synthetic dataset	2
4	Bayesian Network estimation	3
4.1	Define function to fit the model	3
4.1.1	fit.the.model	3
4.2	Define plotting functions	7
4.2.1	f_run_plot_graph	7
4.2.2	redraw.graph	9
4.2.3	match.arcs.and.directions	9
4.2.4	redraw.graph.labels	10
4.2.5	redraw.label.ggnet	11
4.3	mvBIMBAM results	14
5	Results	14
5.1	Data summaries	14
5.2	Visualize learned networks as graphs	16
5.2.1	Regular graph	16
5.2.2	Labeled high-strength graph	17
5.2.3	ggnetwork graph	19
6	Session information	21

1 Overview

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Here we illustrate how we estimated our Bayesian Networks.

As laid out in our README.md, this .Rmd file builds upon another example .Rmd file

`cleancode_paper_phenotypes_mvBIMBAM_run.Rmd`,

which will need to be ran first as it creates two data files that are read in below.

As stated in our README.md, the code within this document was adapted from <http://www.bnlearn.com/research/genetics14/> under the Creative Commons Attribution-Share Alike License(<https://creativecommons.org/licenses/by-sa/3.0/>) which accompanies the paper “Multiple Quantitative Trait Analysis Using Bayesian Networks” by Scutari, Howell, Balding, Mackay (Genetics, 2014).

2 Load Libraries

```
library(tidyverse)
library(lme4)
library(bnlearn)
library(parallel)
# The 'graph' package has been archived from CRAN
# To install use
#if (!require("BiocManager", quietly = TRUE))
#install.packages("BiocManager")
#BiocManager::install("graph")
library(graph)
library(pander)
library(ggnetwork)
```

3 Read in the synthetic dataset

Please see the README.md for information regarding the example synthetic data set and pre-processing instructions if you will be adapting this code to perform the analyses in your own data set.

As detailed in the README.md and demonstrated in `cleancode_paper_phenotypes_mvBIMBAM_run.Rmd`, the synthetic phenotype data created for this example .Rmd were adjusted for age and sex, quantile normalized, and outliers were removed. The quantile normalized adjusted data set is read in below.

```
# Read in the quantile normalized adjusted synthetic data set
# (Created for use with this example analysis code and processed in the
# previous .Rmd)
df_synth <- readRDS("SyntheticQuantNorm.rds") %>%
  mutate(rs373863828 = case_when(rs373863828 == "AA" ~ 2,
                                rs373863828 == "AG" ~ 1,
                                rs373863828 == "GG" ~ 0))

# The package to learn the Bayesian networks (bnlearn) does not support integer data,
# so convert integer columns to numeric
df_synth[sapply(df_synth, class) == "integer"] <-
  sapply(df_synth[sapply(df_synth, class) == "integer"], as.numeric)

# Define the phenotypes of interest
# Anthropometry
anthro.traits <- c("BMI", "Height", "Weight", "FFM", "FM", "WHR", "Abd_Circ", "Hip_Circ")
# Lipids
lipids.traits <- c("HDL_C", "NetTG", "Cholesterol")
# Both
traits <- c(anthro.traits, lipids.traits)
# Phenotype abbreviations
# BMI=body mass index; FFM=fat-free mass; FM=fat mass; WHR=waist hip ratio;
```

```
# Abd_Circ=abdominal circumference; Hip_Circ=hip circumference;
# HDL_C=HDL cholesterol; NetTG=net triglycerides

# Define variant of interest
genes <- c("rs373863828")
```

Here we will analyze all traits which are loaded into the ‘traits’ object.

4 Bayesian Network estimation

As described in our paper, we further explored the relationships between the variant and the correlated phenotypes of interest with a Bayesian network learned using the R package bnlearn. The final quantile normalized data (created in `cleancode_paper_phenotypes_mvBIMBAM_run.Rmd` and loaded above) are used to learn the Bayesian networks.

4.1 Define function to fit the model

4.1.1 fit.the.model

The Bayesian networks model is fitted by the `fit.the.model()` function defined below. A constrained learning algorithm based on conditional independence testing (semi-interleaved HITON-PC) is used to infer association and potential causal relationships within the network.

In this approach “parent-child” relationships are learned based on `learn.nbr`, which depends on `ci.test` (independence and conditional independence tests). Phenotypes and the variant are modeled as nodes, with edges representing associations between nodes. In our analyses below, the “parents” of a trait can be either variants or other traits while “children” can only be traits. In other words, the analyses are restricted so the variant can have only outgoing edges connecting to phenotypes, and phenotypes cannot act on gene(s). This is specified through the use of the `tiers2blacklist()` function which creates a “blacklist” that prevents arcs from going to specific nodes. This option restricts the space of the candidate models with the intention of forcing known causal relationships to flow in the right direction while learning them from the data. Here we are only forcing the direction of the flow from variant to traits (preventing trait to variants), but this could be customized further as shown at <http://www.bnlearn.com/research/genetics14/>.

Once networks are learned, the nodes are partitioned into subsets for plotting and structures are learned by maximizing the Bayesian Information Criteria (BIC).

```
# Define model function to return a Bayesian network based on a conditional correlation
# test and si.hiton.pc structure learning algorithm
fit.the.model <- function(data, alpha) {
  cpc = vector(length(traits), mode = "list")
  names(cpc) = traits

  # Find the "parents" of each trait (which might be genes/variants or other traits)
  # The parents of a trait can be either markers or other traits
  # Children can only be traits
  # The test used to assess (conditional) independence is the exact t test for
  # Pearson' correlation (test = "cor") with the specified alpha threshold.
  for (t in seq_along(traits)) {
    # Discover parents
    cpc[[t]] = learn.nbr(
      data[, c(traits, genes)],
      node = traits[t],
```

```

    debug = FALSE,
    method = "si.hiton.pc",
    test = "cor",
    alpha = alpha
  )
} #FOR
# Merge the relevant variables to use for learning
# Since we are performing a candidate SNP study, force in SNP of interest
# In the original code, markers that are not included in this list have not
# been found to be directly related to any trait and are therefore discarded
# from the analysis - which would be appropriate in a study of many genes/SNPs
nodes = unique(c(traits, unlist(cpc), "rs373863828"))

# Create a blacklist of edges
# Manually define trait to gene
# If the gene is not a node in the graph, run without a blacklist
# Else no blacklist
if (!(("rs373863828" %in% nodes))) {
  bn = hc(data[, c(nodes)])
} else {
  blacklist = tiers2blacklist(list(nodes[!(nodes %in% traits)], traits))
  bn = hc(data[, c(nodes)], blacklist = blacklist)
}
return(bn)
} #FIT.THE.MODEL

# Create a function to train the model with n fold cross validation,
# 100-100/n% train and 100/n% test for 10 partitions
# Hold out each partition iteratively so that no data are totally held out
xval.the.model <- function(data,
                           k = 10,
                           alpha = 0.15,
                           ridge,
                           verbose = F) {
  n = nrow(data)
  predcor = numeric(length(traits))
  names(predcor) = traits
  postcor = numeric(length(traits))
  names(postcor) = traits

  # Shuffle the data to get unbiased splits
  # Suppress: data length is not a multiple of split variable
  # kcv = suppressWarnings(split(sample(n), seq_len(k)))

  # Stratified sampling by genotype
  list_strat = suppressWarnings(split(1:n, data$rs373863828) %>% lapply(split, seq_len(k)))
  # Shuffle the list so that group sizes are more random,
  # Otherwise first group will always be largest group
  # Up to levels(genotype) larger. This only ensures size
  # Instead of minimized group size difference
  list_strat = lapply(list_strat, function(x)
    x[sample(k)])
  kcv = sapply(1:k, function(i)

```

```

c(list_strat[[1]][[i]],
  list_strat[[2]][[i]],
  list_strat[[3]][[i]])
names(kcv) = 1:length(kcv)

# Store the length of each test set
kcv.length = sapply(kcv, length)

predicted = lapply(kcv, function(test) {
  # Create a matrix to store the predicted values
  pred = matrix(0, nrow = length(test), ncol = length(trait))
  colnames(pred) = trait
  # Create a matrix to store posterior estimates.
  post = matrix(0, nrow = length(test), ncol = length(trait))
  colnames(post) = trait

  if (verbose)
    cat("* beginning cross-validation fold.\n")

  # Split training and test
  dtraining = data[-test,]
  dtest = data[test,]
  # Fit the model on the training data
  model = fit.the.model(dtraining, alpha = alpha)
  fitted = bn.fit(model, dtraining[, nodes(model)], debug = F)
  # Maybe re-fit with ridge regression
  # Untested
  if (ridge) {
    if (verbose)
      cat("* re-fit with ridge regression")
    library(penalized)
    for (no in nodes(fitted)) {
      node.parents = parents(fitted, no)

      if (length(node.parents) < 3)
        next

      opt.lambda = optL2(
        response = dtraining[, no],
        penalized = dtraining[, node.parents],
        model = "linear",
        trace = FALSE,
        minlambda2 = 10e-5,
        maxlambda = 500
      )$lambda
      fitted[[no]] = penalized(
        response = dtraining[, no],
        penalized = dtraining[, node.parents],
        model = "linear",
        trace = FALSE,
        lambda1 = 0,
        lambda2 = opt.lambda
      )
    }
  }
})

```

```

    }
  }
  # Subset the test data
  dtest = dtest[, nodes(model)]
  # cat("Subset complete. \n")

  if (verbose)
    cat("  model has", length(nodes(model)), "nodes.\n")

  # Predict each trait in turn, given all the parents
  for (t in traits)
    pred[, t] = predict(fitted, node = t, data = dtest[, nodes(model)])
  # cat(" Predict each trait complete \n")

  for (i in seq(nrow(dtest)))
    post[i, traits] = colMeans(cpdist(
      fitted,
      nodes = traits,
      evidence = as.list(dtest[i, ])[names(dtest) %in% genes],
      method = "lw",
      n = 1000
    ))
  # cat(" Posterior calculation complete \n")

  return(list(
    model = fitted,
    pred = pred,
    post = post
  ))
})

# Merge all the predicted values
posterior = do.call(rbind, lapply(predicted, `[`, "post"))
causal = do.call(rbind, lapply(predicted, `[`, "pred"))

if (verbose)
  cat("* overall cross-validated correlations:\n")
for (t in traits) {
  predcor[t] = cor(causal[, t], data[unlist(kcv), t])
  if (verbose)
    cat("  PREDCOR(", t, "):", predcor[t], "\n")
  postcor[t] = cor(posterior[, t], data[unlist(kcv), t])
  if (verbose)
    cat("  POSTCOR(", t, "):", postcor[t], "\n")
}
return(
  list(
    predicted = causal,
    posterior = posterior,
    observed = data[unlist(kcv), t],
    predcor = predcor,

```

```

    postcor = postcor,
    models = lapply(predicted, `[`, "model")
  )
}

```

4.2 Define plotting functions

4.2.1 f_run_plot_graph

```

# Define function to plot the networks
f_run_plot_graph <- function(data = df_synth,
                             k = 5,
                             alpha = 0.01,
                             use.custom.threshold = FALSE,
                             custom.threshold = 0.90,
                             ncluster = 10,
                             ...) {
  cl = makeCluster(ncluster)
  invisible(clusterEvalQ(cl, library(bnlearn)))
  invisible(clusterEvalQ(cl, library(lme4)))
  clusterExport(cl = cl, c("traits", "genes", "fit.the.model"))
  pr001 = vector(k, mode = "list")
  for (i in seq_along(pr001))
    pr001[[i]] = xval.the.model(data,
                                k = k,
                                alpha = alpha,
                                ridge = FALSE,
                                ...)

  stopCluster(cl)

  pred.summary = sapply(pr001, `[`, "predcor")
  print(rowMeans(pred.summary))
  post.summary = sapply(pr001, `[`, "postcor")
  print(rowMeans(post.summary))
  # Average the network structures
  arclist = list()
  for (i in seq_along(pr001)) {
    # Extract the models
    run = pr001[[i]]$models
    for (j in seq_along(run))
      arclist[[length(arclist) + 1]] = arcs(run[[j]])
  }

  # Compute the arc strengths
  nodes = unique(unlist(arclist))
  # Note: default boot.strength() runs with "cpdag = TRUE" which means
# reversible arcs can have positive strength in both directions
# Use "cpdag = FALSE" to truly make the blacklist work as expected
  strength = custom.strength(arclist, nodes = nodes, cpdag = FALSE)
  # Estimate the threshold and average the networks

```

```

averaged = averaged.network(strength)
# sna::degree will break code
relevant.nodes = bnlearn::nodes(averaged)[sapply(nodes, bnlearn::degree, object = averaged) > 0]
# igraph::subgraph will break code
averaged2 = bnlearn::subgraph(averaged, relevant.nodes)
strength2 = strength[(strength$from %in% relevant.nodes) &
  +(strength$to %in% relevant.nodes),]
cat("threshold: ", attr(strength2, "threshold"), "\n")
t <- attr(strength2, "threshold")
v <- strength2$strength
cat("min strength > threshold: ", min(v[v > t]), "\n")
cat("strength: ", sort(strength2$strength))
if (use.custom.threshold) {
  cat("Using custom threshold of ", custom.threshold, "\n")
  gR = strength.plot(
    averaged2,
    strength2,
    shape = "rectangle",
    layout = "fdp",
    render = F,
    threshold = custom.threshold
  )
} else {
  gR = strength.plot(
    averaged2,
    strength2,
    shape = "rectangle",
    layout = "fdp",
    render = F
  )
}
nodeRenderInfo(gR)$fill = "lightblue"
nodeRenderInfo(gR)$col = "darkblue"
nodeRenderInfo(gR)$fill[traits] = "limegreen"
nodeRenderInfo(gR)$col[traits] = "darkgreen"
a = arcs(bnlearn::subgraph(averaged, traits))
a = as.character(interaction(a[, "from"], a[, "to"], sep = "~"))
edgeRenderInfo(gR)$col = "grey"
edgeRenderInfo(gR)$col[a] = "darkgreen"
Rgraphviz::renderGraph(gR)
results <-
  list(
    averaged2 = averaged2,
    strength2 = strength2,
    averaged = averaged,
    traits = traits,
    threshold = t
  )
return(results)
}

```


4.2.2 redraw.graph

```
# Define function to redraw plots
redraw.graph <-
  function(averaged2,
           strength2,
           averaged,
           traits,
           custom.threshold) {
    gR = strength.plot(
      averaged2,
      strength2,
      shape = "rectangle",
      layout = "fdp",
      render = F,
      threshold = custom.threshold
    )
    nodeRenderInfo(gR)$fill = "lightblue"
    nodeRenderInfo(gR)$fill = "lightblue"
    nodeRenderInfo(gR)$col = "darkblue"
    nodeRenderInfo(gR)$fill[traits] = "limegreen"
    nodeRenderInfo(gR)$col[traits] = "darkgreen"
    a = arcs(bnlearn::subgraph(averaged, traits))
    a = as.character(interaction(a[, "from"], a[, "to"], sep = "~"))
    edgeRenderInfo(gR)$col = "grey"
    edgeRenderInfo(gR)$col[a] = "darkgreen"
    Rgraphviz::renderGraph(gR)
  }
```

4.2.3 match.arcs.and.directions

```
# Define function to match arcs and directions
match.arcs.and.directions <-
  function(arcs, nodes, strengths, keep = FALSE)
  {
    if (nrow(strengths) < nrow(arcs))
      stop("insufficient number of strength coefficients.")
    a_hash = interaction(arcs[, "from"], arcs[, "to"])
    s_hash = interaction(strengths[, "from"], strengths[, "to"])
    if (keep) {
      s = strengths[match(a_hash, s_hash), , drop = FALSE]
      coef = s$direction
    }
    else {
      s = strengths[match(a_hash, s_hash), "direction"]
      from = strengths[match(a_hash, s_hash), "from"]
      to = strengths[match(a_hash, s_hash), "to"]
      names(s) <- paste0(from, "~", to)
      coef = s
    }
    if (any(is.na(coef))) {
      missing = apply(arcs[is.na(coef), , drop = FALSE], 1,
```

```

        function(x) {
          paste(" (", x[1], ", ", x[2], ")", sep = "")
        })
    stop(
      "the following arcs do not have a corresponding direction coefficients:",
      missing,
      "."
    )
  }
  return(s)
}

```

4.2.4 redraw.graph.labels

```

# Define function to redraw graph labels
redraw.graph.labels <-
  function(averaged2,
           strength2,
           averaged,
           traits,
           custom.threshold) {
    gR = strength.plot(
      averaged2,
      strength2,
      shape = "rectangle",
      layout = "fdp",
      render = F,
      threshold = custom.threshold
    )
    x <- averaged2
    str <-
      match.arcs.and.directions(
        arcs = x$arcs,
        nodes = names(x$nodes),
        strengths = strength2
      )
    str2 = bnlearn::match.arcs.and.strengths(
      arcs = x$arcs,
      nodes = names(x$nodes),
      strengths = strength2
    )
    # labels <- edgeNames(gR)
    labels2 <- paste0(round(str2, 2), "; ", round(str, 2))
    names(labels2) <- names(str)
    gR <-
      Rgraphviz::layoutGraph(gR,
                             edgeAttrs = list(label = labels2),
                             layoutType = "fdp")
    nodeRenderInfo(gR)$fill["rs373863828"] = "grey"
    nodeRenderInfo(gR)$fill = "lightblue"
    nodeRenderInfo(gR)$col = "darkblue"
    nodeRenderInfo(gR)$fill[traits] = "limegreen"
  }

```

```

nodeRenderInfo(gR)$col[traits] = "darkgreen"
a = arcs(bnlearn::subgraph(averaged2, traits))
a = as.character(interaction(a[, "from"], a[, "to"], sep = "~"))
edgeRenderInfo(gR)$col = "grey"
edgeRenderInfo(gR)$col[a] = "darkgreen"
Rgraphviz::renderGraph(gR)
}

```

4.2.5 redraw.label.ggnet

```

# Define function to redraw the graph in ggnetwork/ggplot2 framework
redraw.label.ggnet <-
  function(averaged2,
           strength2,
           averaged,
           traits,
           df_bayes,
           ...) {
    # Relies on bnlearn code to return a directed graph
    x <- averaged2
    # Get the directions and str
    vec_dir <-
      match.arcs.and.directions(
        arcs = x$arcs,
        nodes = names(x$nodes),
        strengths = strength2
      )
    vec_str = bnlearn::match.arcs.and.strengths(
      arcs = x$arcs,
      nodes = names(x$nodes),
      strengths = strength2
    )

    # Create data.frame with node/dir/str
    # Need to join this to the data.frame created by ggnetwork
    df_dir_str = data.frame(do.call(rbind, str_split(names(vec_dir), "~")),
                           vec_dir,
                           vec_str,
                           stringsAsFactors = F)

    names(df_dir_str)

    # Convert NEL graph to iGraph to ggnetwork data.frame
    # This step 'shuffles' the edge orders so vec_dir, vec_str is not in same order
    # as df_ggnetwork
    graph_igraph = igraph::igraph.from.graphNEL(as.graphNEL(averaged2))
    df_ggnetwork = ggnetwork(graph_igraph, ...)
    # df_ggnetwork$vertex.names = as.character(df_ggnetwork$vertex.names)
    df_ggnetwork$vertex.names = as.character(df_ggnetwork$name)
    df_ggnetwork$xend = as.numeric(df_ggnetwork$xend)
    df_ggnetwork$yend = as.numeric(df_ggnetwork$yend)
    df_ggnetwork$x = as.numeric(df_ggnetwork$x)
    df_ggnetwork$y = as.numeric(df_ggnetwork$y)
  }

```

```

# Data.frame of node coordinates, will need to this to figure out the
# destination node/end vertex
df_node_coord = df_ggnetwork %>% filter(is.na(weight)) %>% select(vertex.names, x, y) %>%
  transmute(vertex.names.end = vertex.names,
            xend = x,
            yend = y)

# Join back to form end vertex
# Relies on fuzzyjoin with L2 norm < 0.05 since ggnetwork shifts node
# positions around randomly
df_ggnetwork = df_ggnetwork %>%
  fuzzyjoin::distance_left_join(df_node_coord,
                              by = c("xend", "yend"),
                              max_dist = 0.05)

# Join the dir/prob table
# Based on source node and end node
df_ggnetwork = df_ggnetwork %>% left_join(df_dir_str,
                                          by = c("vertex.names" = "X1", "vertex.names.end" = "X2"))

# Add on Bayes factors
df_ggnetwork = df_ggnetwork %>% left_join(df_bayes, by = "vertex.names")

# Change formatting for some names
df_ggnetwork$vertex.names[df_ggnetwork$vertex.names == "Abd_Circ"] = "Abd Circ"
df_ggnetwork$vertex.names[df_ggnetwork$vertex.names == "Hip_Circ"] = "Hip Circ"
df_ggnetwork$vertex.names[df_ggnetwork$vertex.names == "HDL_C"] = "HDL-C"
df_ggnetwork$vertex.names[df_ggnetwork$vertex.names == "Cholesterol2"] = "Cholesterol"

# Create a node type lookup table for node coloring
df_vertex_table = data.frame(
  vertex.names = c(
    "BMI",
    "Height",
    "Weight",
    "FFM",
    "FM",
    "WHR",
    "Abd Circ",
    "Hip Circ",
    "HDL-C",
    "NetTG",
    "rs373863828",
    "Cholesterol"
  ),
  type = c(
    "Anthropometric",
    "Anthropometric",
    "Anthropometric",
    "Anthropometric",
    "Anthropometric",
    "Anthropometric",
    "Anthropometric",
    "Anthropometric",
    "Anthropometric",
    "Anthropometric",
    "Anthropometric",
    "Anthropometric"
  )
)

```

```

    "Anthropometric",
    "Lipids",
    "Lipids",
    "Genotype",
    "Lipids"
  ),
  stringsAsFactors = F
)

# Join node type table
df_ggnetwork = df_ggnetwork %>% left_join(df_vertex_table, by = "vertex.names")

# Fix the data.frame column names, fuzzyjoin appended .x and .y to column names
# names(df_ggnetwork) = c("x", "y", "na.x", "vertex.names", "xend", "yend", "na",
#                          "weight", "vertex.names.end", "xend.y", "yend.y", "vec_dir",
#                          "vec_str", "BF", "type")
names(df_ggnetwork)[names(df_ggnetwork) == "xend.x"] <- "xend"
names(df_ggnetwork)[names(df_ggnetwork) == "yend.x"] <- "yend"

# Function to ceiling the bayes factor at v (5 in this case)
f_ceil = function(x, v) {
  x[x > v] = v
  x
}

# Plot with ggplot and ggnetwork geoms
ggplot(df_ggnetwork, aes(
  x = x,
  y = y,
  xend = xend,
  yend = yend
)) +
  geom_edges(aes(linetype = (vec_str > 0.9)),
             color = "grey50",
             arrow = arrow(length = unit(8, "pt"), type = "open")) +
  geom_nodes(size = 10,
             aes(shape = type, fill = f_ceil(BF, 5)),
             color = "black") +
  geom_edgelabel_repel(aes(label = paste0(
    round(vec_str, 2), ":", round(vec_dir, 2)
  ))) +
  geom_nodelabel_repel(
    aes(label = vertex.names),
    force = 1,
    fontface = "bold",
    box.padding = unit(1.2, "lines"),
    color = "black"
  ) +
  scale_fill_gradientn("Node Type",
                      colors = c("white", "grey", "black"),
                      limits = c(0, 5)) +
  scale_linetype_manual(
    "Node Signif.",
    values = c("FALSE" = "dotted", "TRUE" = "solid"),

```

```

    label = c("<= 90 Strength", "> 0.90 Strength")
  ) +
  scale_shape_manual(values = c(21:23)) + theme_blank(legend.position = "none")
}

```

4.3 mvBIMBAM results

The Bayes factors calculated by mvBIMBAM in the previous .Rmd are used to color the nodes in the final graph.

When reading setting up the Bayes factors for coloring, set negative BF's to zero.

```

# Load mvBIMBAM results calculated from mvBIMBAM runs
# Used only for plotting purposes
load('mvBimBam_Results.RDdata', verbose = TRUE)

## Loading objects:
##   m1
##   m2
##   table1

results <- data.frame(vertex.names = colnames(m1), BF = t(m1))
rownames(results) <- NULL
df_bayes_expand <- results[-c(1:2),]
rownames(df_bayes_expand) <- NULL
# Set negative BF's to zero
df_bayes_expand$BF[df_bayes_expand$BF<0] <- 0
kable(df_bayes_expand, caption= "Bayes factors as estimated by mvBIMBAM")

```

Table 1: Bayes factors as estimated by mvBIMBAM

vertex.names	BF
BMI	7.44413
Height	0.19346
Weight	5.49124
FFM	2.40668
FM	5.86814
WHR	0.18422
Abd_Circ	3.44936
Hip_Circ	6.31858
HDL_C	0.00000
NetTG	0.00000
Cholesterol	0.00000

5 Results

5.1 Data summaries

```

# Check dimensions of the synthetic data used here
dim(df_synth)

```

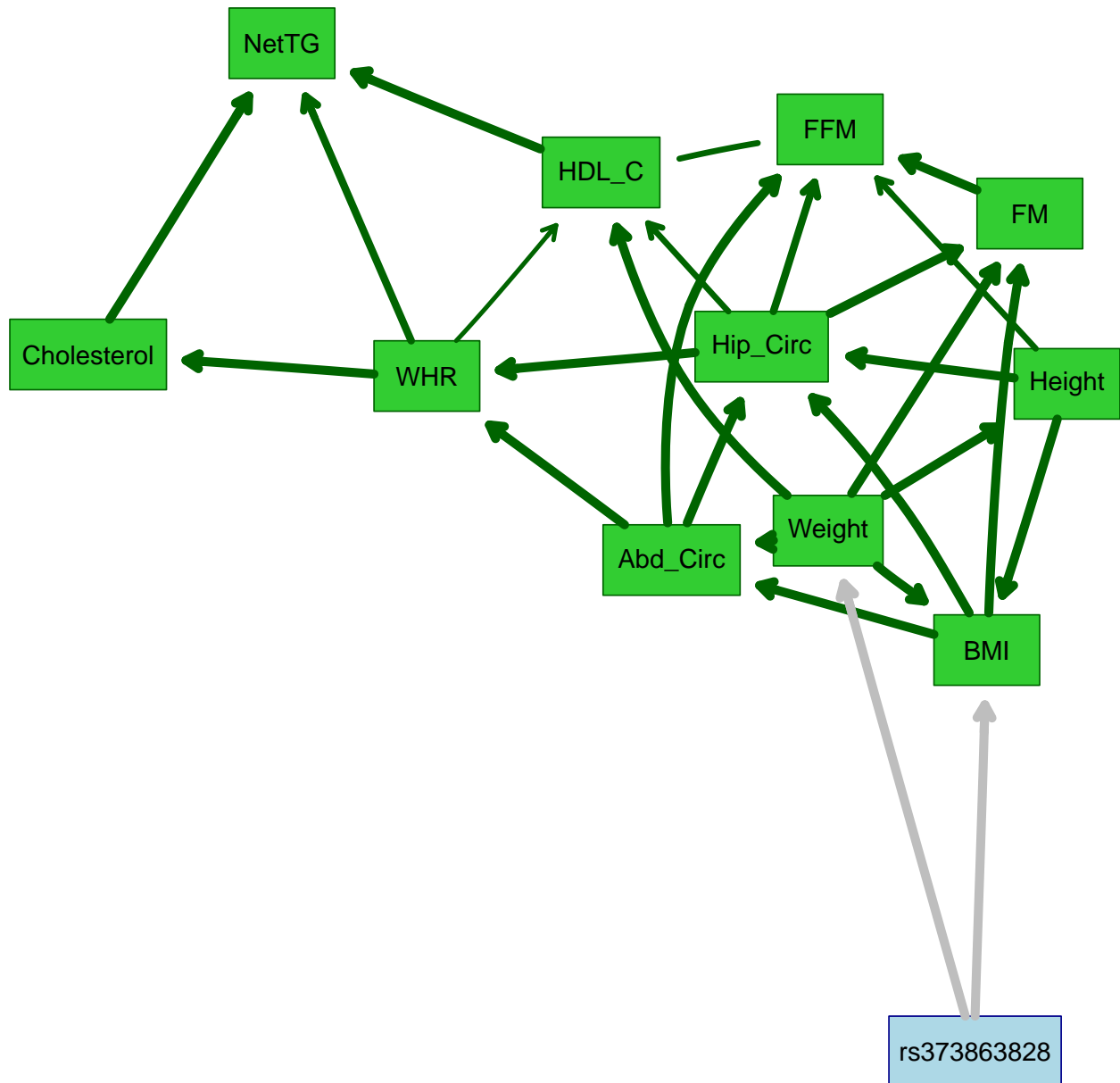
```
## [1] 1356 12
```

```
# Summary of data  
summary(df_synth)
```

```
##      rs373863828      BMI      Height      Weight  
## Min.   :0.0000   Min.   :-49.3494   Min.   :-49.3494   Min.   :-49.3494  
## 1st Qu.:0.0000   1st Qu.: -13.8366   1st Qu.: -13.9033   1st Qu.: -13.9033  
## Median :0.0000   Median : -1.6261   Median : -1.9481   Median : -1.5709  
## Mean   :0.5361   Mean    : 0.3903   Mean    : 0.1986   Mean    : 0.3395  
## 3rd Qu.:1.0000   3rd Qu.: 11.2919   3rd Qu.: 11.2332   3rd Qu.: 11.2919  
## Max.   :2.0000   Max.    :151.5049   Max.    :151.5049   Max.    :151.5049  
##      FFM      FM      WHR      Abd_Circ  
## Min.   :-49.34942   Min.   :-49.3494   Min.   :-49.3494   Min.   :-49.3494  
## 1st Qu.: -14.10627   1st Qu.: -13.7759   1st Qu.: -13.9973   1st Qu.: -13.7234  
## Median : -2.40400   Median : -1.6261   Median : -1.9361   Median : -1.4368  
## Mean    : -0.01652   Mean    : 0.3376   Mean    : 0.1208   Mean    : 0.4066  
## 3rd Qu.: 10.93342   3rd Qu.: 11.4142   3rd Qu.: 11.0231   3rd Qu.: 11.3717  
## Max.    :151.50491   Max.    :151.5049   Max.    :151.5049   Max.    :151.5049  
##      Hip_Circ      HDL_C      NetTG      Cholesterol  
## Min.   :-49.3494   Min.   :-49.34942   Min.   :-49.3494   Min.   :-49.34942  
## 1st Qu.: -13.7999   1st Qu.: -14.16725   1st Qu.: -14.1307   1st Qu.: -13.97325  
## Median : -1.5492   Median : -2.12963   Median : -1.8848   Median : -2.09169  
## Mean    : 0.4109   Mean    : -0.01787   Mean    : 0.1294   Mean    : -0.01349  
## 3rd Qu.: 11.4142   3rd Qu.: 10.94681   3rd Qu.: 11.0820   3rd Qu.: 10.96894  
## Max.    :151.5049   Max.    :151.50491   Max.    :151.5049   Max.    :151.50491
```

```
# Correlation structure of data  
cor(df_synth[,traits])
```

```
##      BMI      Height      Weight      FFM      FM  
## BMI      1.00000000  0.05654999  0.89115448 -0.77803102  0.90689781  
## Height   0.05654999  1.00000000  0.34823176 -0.13094969  0.26978131  
## Weight   0.89115448  0.34823176  1.00000000 -0.77086403  0.95703031  
## FFM      -0.77803102 -0.13094969 -0.77086403  1.00000000 -0.80125959  
## FM        0.90689781  0.26978131  0.95703031 -0.80125959  1.00000000  
## WHR       0.35825726  0.02561132  0.38019540 -0.38299136  0.35161851  
## Abd_Circ  0.87050789  0.13256381  0.83692435 -0.74651551  0.84175720  
## Hip_Circ  0.86795388  0.18805683  0.82552248 -0.74289334  0.85623153  
## HDL_C     -0.29538767 -0.13061223 -0.32741249  0.30757979 -0.30175714  
## NetTG     0.21113450  0.09693125  0.23353713 -0.22050883  0.21727328  
## Cholesterol 0.05390981  0.01655032  0.05012822 -0.06355734  0.04560803  
##      WHR      Abd_Circ      Hip_Circ      HDL_C      NetTG  
## BMI      0.35825726  0.87050789  0.86795388 -0.2953877  0.21113450  
## Height   0.02561132  0.13256381  0.18805683 -0.1306122  0.09693125  
## Weight   0.38019540  0.83692435  0.82552248 -0.3274125  0.23353713  
## FFM      -0.38299136 -0.74651551 -0.74289334  0.3075798 -0.22050883  
## FM        0.35161851  0.84175720  0.85623153 -0.3017571  0.21727328  
## WHR       1.00000000  0.53958553  0.18112236 -0.2560829  0.27459864  
## Abd_Circ  0.53958553  1.00000000  0.79772319 -0.3114177  0.25445384  
## Hip_Circ  0.18112236  0.79772319  1.00000000 -0.2110896  0.13197904  
## HDL_C     -0.25608291 -0.31141766 -0.21108962  1.0000000 -0.51564497  
## NetTG     0.27459864  0.25445384  0.13197904 -0.5156450  1.00000000  
## Cholesterol 0.14831410  0.06370297  0.03079216  0.0148836  0.31223519  
## Cholesterol  
## BMI      0.05390981
```

5.2.2 Labeled high-strength graph

Redraw graph adding strengths/directions to association lines.

The strength and directionalities of the edges of the Bayesian networks are inferred through a bootstrapped process so resulting networks vary a bit from run to run. As such, representative networks (i.e., averaged) are plotted.

The code below calls in the function created above to add specific details on the strength (Es) and direction (Ed) of each edge that summarize the results across the total number of bootstrapped realizations.

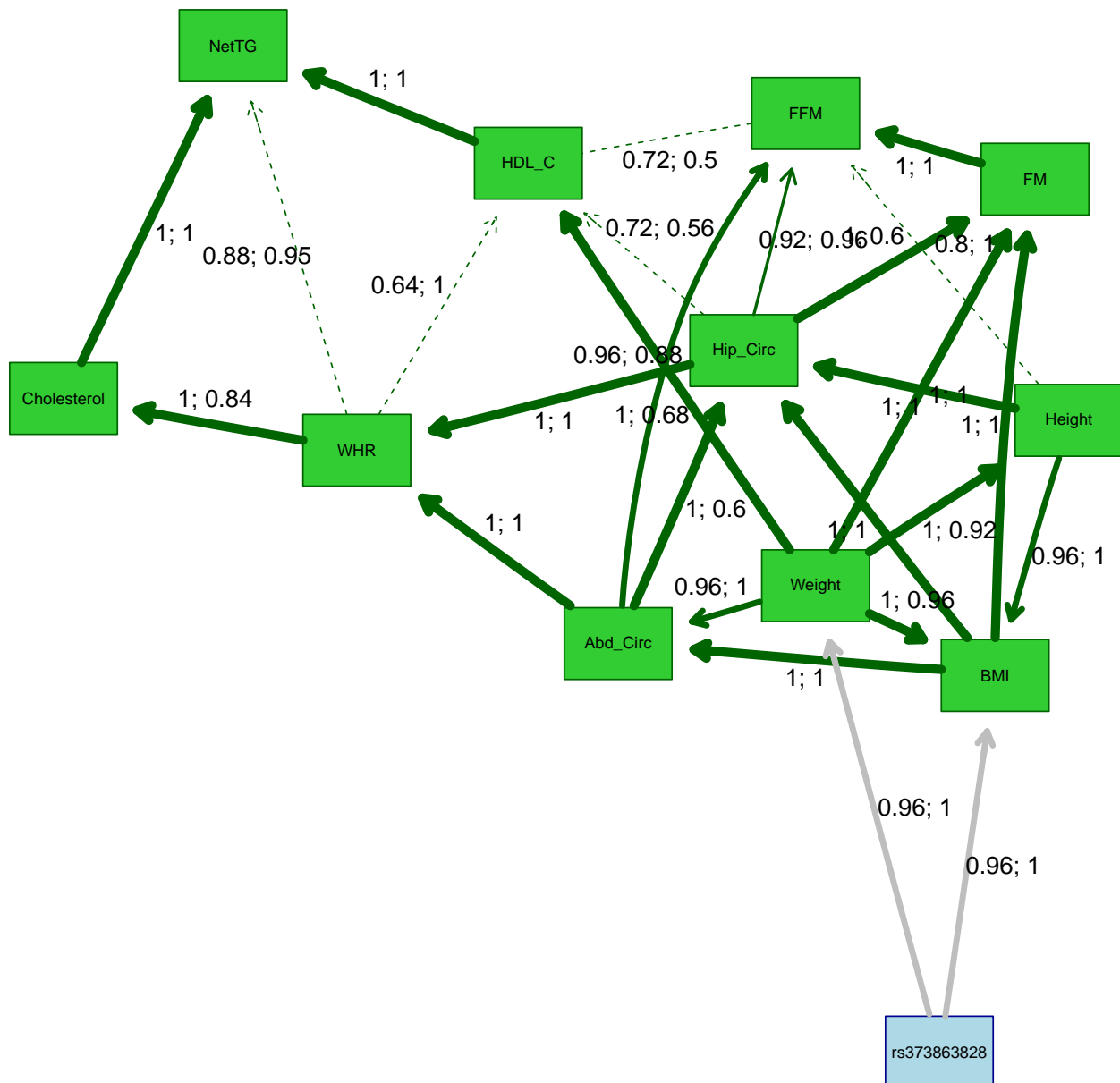
Edge strength is a measure of confidence of that edge while fixing the rest of the network structure and is defined as the empirical frequency a specific edge is observed over a set of networks learned from bootstrapped samples (i.e., the number of times the edge was present out of the total number of bootstrapped realizations).

Edge direction represents the probability of the edge's direction conditional on the edge's presence within

the network (i.e., the number of times the edge traveled in a specific direction out of the total number of bootstrapped realizations in which it was present).

An edge is included in the network graph if its strength is larger than a significance threshold learned from the bootstrapped samples.

```
# Redraw graph adding strengths/directions to association lines using function created above
# Here, we use a threshold of 0.9 to indicate "strong" associations
# In this case, edges with a strength >0.9 will be solid, while edges with a strength <0.9 will be dash
redraw.graph.labels(
  results$averaged2,
  results$strength2,
  results$averaged,
  results$traits,
  custom.threshold = 0.90
)
```



```
# Visualize strengths/directions as a table
```

```
results$strength2 %>%
  filter(strength > 0 & direction > 0 & strength > results$threshold) %>%
  arrange(strength) %>% pander()
```

from	to	strength	direction
WHR	HDL_C	0.64	1
FFM	HDL_C	0.72	0.5
Hip_Circ	HDL_C	0.72	0.5556
HDL_C	FFM	0.72	0.5
HDL_C	Hip_Circ	0.72	0.4444
Height	FFM	0.8	1
WHR	NetTG	0.88	0.9545
NetTG	WHR	0.88	0.04545
FFM	Hip_Circ	0.92	0.04348
Hip_Circ	FFM	0.92	0.9565
Height	BMI	0.96	1
Weight	Abd_Circ	0.96	1
FFM	Abd_Circ	0.96	0.125
Abd_Circ	FFM	0.96	0.875
rs373863828	BMI	0.96	1
rs373863828	Weight	0.96	1
BMI	Weight	1	0.04
BMI	FM	1	1
BMI	Abd_Circ	1	1
BMI	Hip_Circ	1	1
Height	Weight	1	0.08
Height	Hip_Circ	1	1
Weight	BMI	1	0.96
Weight	Height	1	0.92
Weight	FM	1	1
Weight	HDL_C	1	0.68
FFM	WHR	1	0.96
FM	FFM	1	1
FM	Hip_Circ	1	0.4
WHR	FFM	1	0.04
WHR	Cholesterol	1	0.84
Abd_Circ	WHR	1	1
Abd_Circ	Hip_Circ	1	0.6
Hip_Circ	FM	1	0.6
Hip_Circ	WHR	1	1
Hip_Circ	Abd_Circ	1	0.4
HDL_C	Weight	1	0.32
HDL_C	NetTG	1	1
Cholesterol	WHR	1	0.16
Cholesterol	NetTG	1	1

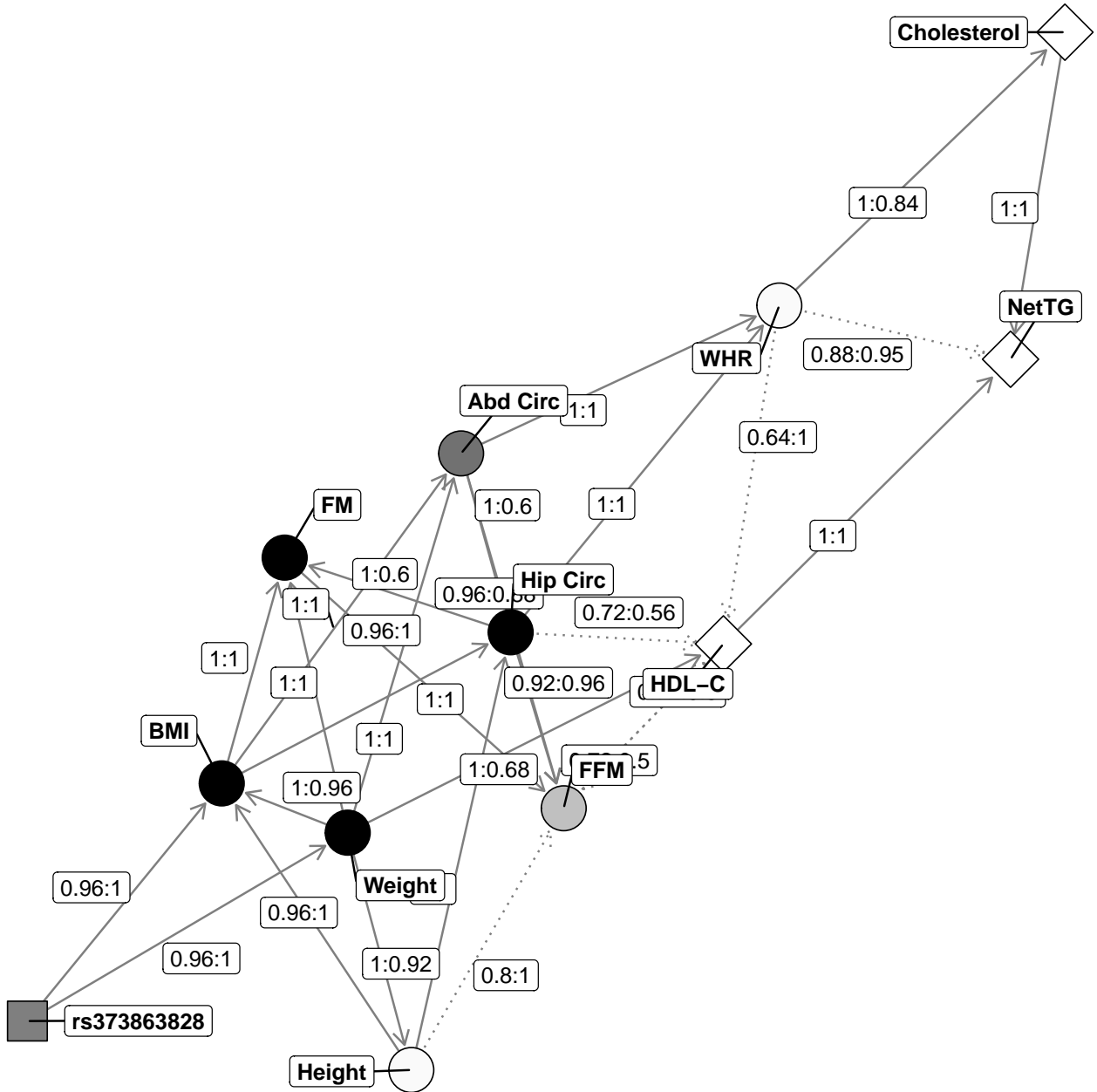
5.2.3 ggnetwork graph

```
# Redraw graph in black and white using ggnetwork through the function created above
redraw.label.ggnet(results$averaged2,
```

```

results$strength2,
results$averaged,
results$traits,
df_bayes = df_bayes_expand)

```



A note about interpretation: In this example figure, we see direct associations between the rs373863828 and weight and BMI with indirect associations with fat mass, hip circumference, and abdominal circumference, height, and HDL cholesterol. An indirect association like the one observed between the variant and HDL cholesterol can be interpreted as HDL cholesterol being conditionally independent of rs373863828 given the presence of weight.

In this figure, the strengths (Es) and directions (Ed) of the relationships are depicted along the edges (Es:Ed).

As described above, the strength is a measure of confidence of that edge while fixing the rest of the network structure and is defined as the empirical frequency a specific edge is observed over a set of networks learned

from bootstrapped samples (i.e., the number of times the edge was present out of the total number of bootstrapped realizations).

Edge direction represents the probability of the edge’s direction conditional on the edge’s presence within the network (i.e., the number of times the edge traveled in a specific direction out of the total number of bootstrapped realizations in which it was present).

So in the example figure created using the synthetic data, we see an association between rs373863828 and body mass index with Es:Ed values of 0.96:1. This means that the edge was present in 96% of all bootstrapped realizations and the relationship traveled from the variant (“parent”) to BMI (“child”) 100% of the time. Note that in our “blacklist” code above, we specified that the variant of interest (rs373863828) could only be a “parent” and not a “child” – so directions of 1 are expected.

This is not the case with the arrow traveling from waist-hip ratio (WHR) to cholesterol. With Es:Ed values of 1:0.84, this relationship was observed in 100% of bootstrapped realizations but traveled from WHR to cholesterol in 84% of realizations.

Finally, note that (1) edges with a strength >0.9 are solid, while edges with a strength <0.9 are dashed and (2) nodes are colored by Bayes factors computed via mvBIMBAM (darker nodes indicate stronger levels of evidence of association).

6 Session information

```
sessioninfo::session_info()

## - Session info -----
## hash: bow and arrow, name badge, broccoli
##
## setting value
## version R version 4.1.2 (2021-11-01)
## os CentOS Linux 7 (Core)
## system x86_64, linux-gnu
## ui X11
## language (EN)
## collate en_US.UTF-8
## ctype en_US.UTF-8
## tz America/New_York
## date 2022-04-05
## pandoc 2.14.0.3 @ /usr/lib/rstudio-server/bin/pandoc/ (via rmarkdown)
##
## - Packages -----
## package * version date (UTC) lib source
## assertthat 0.2.1 2019-03-21 [2] CRAN (R 4.1.2)
## backports 1.3.0 2021-10-27 [2] CRAN (R 4.1.2)
## BiocGenerics * 0.40.0 2021-10-26 [2] Bioconductor
## bnlearn * 4.7 2021-09-06 [2] CRAN (R 4.1.2)
## boot 1.3-28 2021-05-03 [2] CRAN (R 4.1.2)
## broom 0.7.10 2021-10-31 [2] CRAN (R 4.1.2)
## cellranger 1.1.0 2016-07-27 [2] CRAN (R 4.1.2)
## cli 3.1.0 2021-10-27 [2] CRAN (R 4.1.2)
## colorspace 2.0-2 2021-06-24 [2] CRAN (R 4.1.2)
## crayon 1.4.2 2021-10-29 [2] CRAN (R 4.1.2)
## DBI 1.1.1 2021-01-15 [2] CRAN (R 4.1.2)
## dbplyr 2.1.1 2021-04-06 [2] CRAN (R 4.1.2)
```

##	digest	0.6.28	2021-09-23	[2]	CRAN (R 4.1.2)
##	dplyr	* 1.0.7	2021-06-18	[2]	CRAN (R 4.1.2)
##	ellipsis	0.3.2	2021-04-29	[2]	CRAN (R 4.1.2)
##	evaluate	0.14	2019-05-28	[2]	CRAN (R 4.1.2)
##	fansi	0.5.0	2021-05-25	[2]	CRAN (R 4.1.2)
##	farver	2.1.0	2021-02-28	[2]	CRAN (R 4.1.2)
##	fastmap	1.1.0	2021-01-25	[2]	CRAN (R 4.1.2)
##	forcats	* 0.5.1	2021-01-27	[2]	CRAN (R 4.1.2)
##	fs	1.5.0	2020-07-31	[2]	CRAN (R 4.1.2)
##	fuzzyjoin	0.1.6	2020-05-15	[2]	CRAN (R 4.1.2)
##	generics	0.1.1	2021-10-25	[2]	CRAN (R 4.1.2)
##	ggnetwork	* 0.5.10	2021-07-06	[2]	CRAN (R 4.1.2)
##	ggplot2	* 3.3.5	2021-06-25	[2]	CRAN (R 4.1.2)
##	ggrepel	0.9.1	2021-01-15	[2]	CRAN (R 4.1.2)
##	glue	1.5.0	2021-11-07	[2]	CRAN (R 4.1.2)
##	graph	* 1.72.0	2021-10-26	[2]	Bioconductor
##	gtable	0.3.0	2019-03-25	[2]	CRAN (R 4.1.2)
##	haven	2.4.3	2021-08-04	[2]	CRAN (R 4.1.2)
##	highr	0.9	2021-04-16	[2]	CRAN (R 4.1.2)
##	hms	1.1.1	2021-09-26	[2]	CRAN (R 4.1.2)
##	htmltools	0.5.2	2021-08-25	[2]	CRAN (R 4.1.2)
##	httr	1.4.2	2020-07-20	[2]	CRAN (R 4.1.2)
##	igraph	1.2.8	2021-11-07	[2]	CRAN (R 4.1.2)
##	jsonlite	1.7.2	2020-12-09	[2]	CRAN (R 4.1.2)
##	knitr	* 1.36	2021-09-29	[2]	CRAN (R 4.1.2)
##	labeling	0.4.2	2020-10-20	[2]	CRAN (R 4.1.2)
##	lattice	0.20-45	2021-09-22	[2]	CRAN (R 4.1.2)
##	lifecycle	1.0.1	2021-09-24	[2]	CRAN (R 4.1.2)
##	lme4	* 1.1-27.1	2021-06-22	[2]	CRAN (R 4.1.2)
##	lubridate	1.8.0	2021-10-07	[2]	CRAN (R 4.1.2)
##	magrittr	2.0.1	2020-11-17	[2]	CRAN (R 4.1.2)
##	MASS	7.3-54	2021-05-03	[2]	CRAN (R 4.1.2)
##	Matrix	* 1.3-4	2021-06-01	[2]	CRAN (R 4.1.2)
##	minqa	1.2.4	2014-10-09	[2]	CRAN (R 4.1.2)
##	modelr	0.1.8	2020-05-19	[2]	CRAN (R 4.1.2)
##	munsell	0.5.0	2018-06-12	[2]	CRAN (R 4.1.2)
##	nlme	3.1-153	2021-09-07	[2]	CRAN (R 4.1.2)
##	nloptr	1.2.2.3	2021-11-02	[2]	CRAN (R 4.1.2)
##	pander	* 0.6.4	2021-06-13	[2]	CRAN (R 4.1.2)
##	pillar	1.6.4	2021-10-18	[2]	CRAN (R 4.1.2)
##	pkgconfig	2.0.3	2019-09-22	[2]	CRAN (R 4.1.2)
##	purrr	* 0.3.4	2020-04-17	[2]	CRAN (R 4.1.2)
##	R6	2.5.1	2021-08-19	[2]	CRAN (R 4.1.2)
##	Rcpp	1.0.7	2021-07-07	[2]	CRAN (R 4.1.2)
##	readr	* 2.1.0	2021-11-11	[2]	CRAN (R 4.1.2)
##	readxl	1.3.1	2019-03-13	[2]	CRAN (R 4.1.2)
##	reprex	2.0.1	2021-08-05	[2]	CRAN (R 4.1.2)
##	Rgraphviz	2.38.0	2021-10-26	[2]	Bioconductor
##	rlang	0.4.12	2021-10-18	[2]	CRAN (R 4.1.2)
##	rmarkdown	2.11	2021-09-14	[2]	CRAN (R 4.1.2)
##	rstudioapi	0.13	2020-11-12	[2]	CRAN (R 4.1.2)
##	rvest	1.0.2	2021-10-16	[2]	CRAN (R 4.1.2)
##	scales	1.1.1	2020-05-11	[2]	CRAN (R 4.1.2)
##	sessioninfo	1.2.1	2021-11-02	[2]	CRAN (R 4.1.2)

```

## stringi      1.7.5      2021-10-04 [2] CRAN (R 4.1.2)
## stringr      * 1.4.0      2019-02-10 [2] CRAN (R 4.1.2)
## tibble       * 3.1.6      2021-11-07 [2] CRAN (R 4.1.2)
## tidyr        * 1.1.4      2021-09-27 [2] CRAN (R 4.1.2)
## tidyselect   1.1.1      2021-04-30 [2] CRAN (R 4.1.2)
## tidyverse    * 1.3.1      2021-04-15 [2] CRAN (R 4.1.2)
## tzdb         0.2.0      2021-10-27 [2] CRAN (R 4.1.2)
## utf8         1.2.2      2021-07-24 [2] CRAN (R 4.1.2)
## vctrs        0.3.8      2021-04-29 [2] CRAN (R 4.1.2)
## withr        2.4.2      2021-04-18 [2] CRAN (R 4.1.2)
## xfun         0.28       2021-11-04 [2] CRAN (R 4.1.2)
## xml2         1.3.2      2020-04-23 [2] CRAN (R 4.1.2)
## yaml         2.2.1      2020-02-01 [2] CRAN (R 4.1.2)
##
## [1] /home/law145/R/x86_64-pc-linux-gnu-library/4.1
## [2] /usr/local/lib64/R/library
##
## -----

```