# Lecture 1: Electromagnetic Interactions

### Electric Force (Coulombs Law)

$$F = \frac{1}{4\pi\epsilon_0} \cdot \frac{|q_1||q_2|}{r^2}$$
, Newtons (N)

 $F = \frac{1}{4\pi\epsilon_0} \cdot \frac{|q_1||q_2|}{r^2}, \text{ Newtons (N)}$   $\epsilon_0 = 8.85 \times 10^{-12} \ C^2/Nm^2, \text{ Permittivity of free space.}$   $\frac{1}{4\pi\epsilon_0} = 8.99 \times 10^9 Nm^2/C^2, \text{ Coulomb's Constant}$ 

#### **Fundamentals of Charges**

Fundament charge:  $e = 1.60 \times 10^{-19} C$ 

$$q = (N_p - N_e)e$$

q: charge,  $N_p$ : No. of protons,  $N_e$ : No. of electrons

# Lecture 2: Electric Force and Field

### **Electric Field**

$$E = \frac{1}{4\pi\epsilon_0} \cdot \frac{|q|}{r^2}$$

 $E = \frac{1}{4\pi\epsilon_0} \cdot \frac{|q|}{r^2}$  S.I unit: Newtons/Coulombs (N/C)

\*Direction of electric field: positive (outwards), negative (inwards)

#### Large charged plate

$$E = \frac{\sigma}{2\epsilon_0}, \sigma = \frac{Q}{A}.$$

 $E = \frac{\sigma}{2\epsilon_0}, \sigma = \frac{Q}{A}.$   $\sigma$  is Surface Charge Density

Q is charge.

A is area of plate.

\*No. of field lines entering/leaving the charge is proportional to the amount of charge.

#### Lecture 3: Electric Potential

# Work done

$$W_{a \to b} = -\Delta U = U_a - U_b$$

Potential energy of charge 
$$q_0$$
 in a uniform electric field

$$U = q_0 E y$$

y: distance from negative plate.

# Electric potential energy between 2 point charges

$$U = \frac{1}{4\pi\epsilon_0} \cdot \frac{q_1 \cdot q_2}{r}$$

\*For shells, r is distance between centers.

$$U = \frac{1}{4} \cdot \sum_{i \neq j} \frac{q_i \cdot q_j}{q_j}$$

$$U = \frac{1}{4\pi\epsilon_0} \cdot \sum_{i < j} \frac{q_i \cdot q_j}{r_{ij}}$$

$$U = q\Delta V = q(V_f - V_i)$$

# **Electric Potential**

$$V = \frac{1}{4\pi\epsilon_0} \cdot \frac{q}{r}$$

\*Electric **force** on a charge is always in the direction of **lower** electric **potential energy**.

\*Electric field is always in the direction of lower potential.

 $V = \frac{1}{4\pi\epsilon_0} \cdot \sum_i \frac{q_i}{r_i}$  (scalar sum)

#### Total energy conservation

$$K_i + qV_i = K_f + qV_f$$

K: kinetic energy

qV: potential energy

V: potential

#### Kinetic Energy

$$E_k = \frac{1}{2}mv^2$$

\*Mass of proton:  $1.67 \times 10^{-27} \ kg$ 

\*Mass of electron:  $9.11 \times 10^{-31} \ kg$ 

#### Electric Field vs Potential

$$E = \frac{\Delta V}{d}$$

d: distance between 2 equipotential surfaces

#### Lecture 4: Capacitance

\*Any 2 conductors (regardless of shape) separated by an insulator (or vacuum) form a Capacitor.

\*The 2 conductors have charges with equal magnitude but opposite signs.

#### Capacitance

 $C = \frac{Q}{\Delta V}$ , Coulomb per Volt (C/V), Farad (F).

 $C = \frac{\epsilon_0 A}{d}$ , A: Area, d: distance between

# **Energy Storage in Capacitor**

$$U=rac{1}{2}QV=rac{Q^2}{2C}=rac{1}{2}CV^2,$$
 Joules (J) Energy Density in Electric Field

 $u = \frac{1}{2}\epsilon_0 E^2, (J/m^3)$ 

u: amount of energy per unit volume

#### Capacitors with Dielectrics

$$C = \kappa C_0, \kappa > 1$$

 $\kappa$ : dielectric constant

$$\Rightarrow V = \frac{Q_0}{C} = \frac{Q_0}{\kappa C_0} = \frac{V_0}{\kappa}$$

$$\Rightarrow V = \frac{Q_0}{C} = \frac{Q_0}{\kappa C_0} = \frac{V_0}{\kappa}$$

$$\Rightarrow E = \frac{V}{d} = \frac{V_0}{\kappa d} = \frac{E_0}{\kappa}$$

$$\Rightarrow U = \frac{U_0}{\kappa} < U_0$$

$$\Rightarrow U = \frac{1}{\kappa} < U_0$$
Inserting dielectric w

Inserting dielectric with battery

$$\Rightarrow Q = CV_0 = (\kappa C_0)V_0 = \kappa Q_0$$

$$\Rightarrow U = \kappa U_0 > U_0$$

\*Dielectric strength of Dry Air =  $3 \times 10^6 \ V/m$ 

### Find Maximum Charge on Capacitor

\*Given dielectric strength of medium:

$$Q_{max} = \kappa \times \frac{\epsilon_0 A}{d} \times d$$

# Capacitor Network

In parallel:  $C = C_1 + C_2$ 

In series:  $\frac{1}{C} = \frac{1}{C_1} + \frac{1}{C_2}$ 

### Lecture 5: Current and Resistance

#### Ohm's Law

$$I = \frac{\Delta V}{R}$$
 In series:

$$V = V_1 + \ldots + V_n$$

$$I = I_1 = \ldots = I_n$$

$$R = R_1 + \ldots + R_n$$

In parallel:

$$V_1 = V_2 = \ldots = V_n$$

$$I = I_1 + \ldots + I_n$$

$$I = I_1 + \ldots + I_n$$
  
 $\frac{1}{R} = \frac{1}{R_1} + \ldots + \frac{1}{R_n}$   
Currents and Charges

$$I = \frac{\Delta Q}{\Delta t} = |q| nAv_{e}$$

 $I = \frac{\Delta Q}{\Delta t} = |q| n A v_d$  n: no. of charge carriers per unit volume

A: cross section area

 $v_d$ : drift speed of current

#### Resistance

$$R = \frac{\rho L}{A}$$
, (Ohms,  $\Omega$ )

 $\rho$ : resistivity, (Ohms meter,  $\Omega \cdot m$ )

L: length

A: cross section area

#### Resistance and Temperature

$$\rho = \rho_0 [1 + \alpha (T - T_0)]$$

$$R = R_0[1 + \alpha(T - T_0)]$$
  
 $\rho_0$ : resistivity at  $T_0$ 

 $T_0$ : usually  $20^{\circ}C$ 

 $\alpha$ : temp. coefficient of resistivity  $({}^{\circ}C)^{-1}$ 

$$P = \frac{\Delta Q \Delta V}{\Delta t} = \Delta V I = I^2 R = \frac{\Delta V^2}{R}$$
, (Watts, W).

# Lecture 6: DC Circuits

$$I = \frac{\varepsilon}{R+r}$$

 $\varepsilon$ : EMF

R: external resistor

r: internal resistor (in battery)

#### Kirchhoff's Rules

\* $\sum I_i$  into junction =  $\sum I_i$  out of junction

\*Sum of voltage drops around a loop is zero,  $\varepsilon = Ir + IR$ 

\*Intuition: Applying Kirchhoff is to form equations of emf = 0.

\*Recall: Can use Row Operations from Linear Algebra to reduce to Reduced Row Echelon form.

#### **RC** Circuits

RC Circuit: Charging

 $\varepsilon - I(t)R - \frac{q(t)}{c} = 0$ 

Just after switch closed:

 $q(t) = q_0 = 0 \Rightarrow \varepsilon - I_0 R = 0 \Rightarrow I_0 = \frac{\varepsilon}{R}$ 

Long after switch closed:

 $I(t) = I_{\infty} = 0 \Rightarrow \varepsilon - \frac{q_{\infty}}{C} = 0 \Rightarrow = q_{\infty} = C\varepsilon$ 

Intermediate:

 $q(t) = q_{\infty}(1 - e^{-t/RC}), I(t) = I_0 e^{-t/RC}$ 

RC Circuit: Discharging

 $\frac{q(t)}{C} + I(t)R = 0$ Just after switch closed:

 $q(t) = q_0 \Rightarrow \frac{q_0}{C} + I_0 R = 0 \Rightarrow I_0 = -\frac{q_0}{RC}$ 

Long after switch closed:

 $I(t) = I_{\infty} = 0 \Rightarrow \frac{q_{\infty}}{C} = 0 \Rightarrow q_{\infty} = 0$ 

Intermediate:

 $q(t) = q_0 e^{-t/RC}, \ I(t) = I_0 e^{-t/RC}$ 

# Lecture 7: Magnetism

# Magnetic Flux

 $\Phi = BA\cos\theta$ , SI unit:  $Tm^2 \equiv Wb$ 

B: magnetic field strength (Teslas, T)

A: area of plane

 $\theta$ : angle between B and normal to plane

### Magnetic Force on ONE moving charge

 $F = |q|vB\sin\theta$ , Newtons

 $\theta$ : angle between v and B.

(recall:  $E = \frac{F}{q} \Rightarrow E = vB$ , when  $\theta = 90^{\circ}$ )

# Right-hand Rule

Thumb: F, Index: v, Middle: B

\*If negative charge, F is in opposite direction to thumb

#### Radius of circular orbit

 $R = \frac{mv}{B|a|}$ 

# Lecture 8: Currents and Magnetism

# Magnetic Force on MANY moving charges

 $F = ILB \sin \theta$ 

L: length of wire

 $\theta$ : angle between I and B

# **Gravity Force**

F = mq

# Magnetic Field of a Long Straight Wire

 $B = \frac{\mu_0 I}{2\pi r}$ 

 $\mu_0$ : permeability of vacuum,  $\mu_0 = 4\pi \times 10^{-7} \ Tm/A$ 

r: distance from wire

\*Right-hand rule: Thumb: direction of I, fingers: direction of B.

#### Force between parallel wires with length L

\*Consider I directed to the right, wire a is d meters from b.

Magnetic force on wire a and b:

 $F_a = I_a L B_b = \frac{\mu_0 I_a I_b L}{2\pi d}$ , (downward)  $F_a = I_a L B_b = \frac{-2\pi d}{2\pi d}$ , (downwa)  $F_b = I_b L B_a = \frac{\mu_0 I_a I_b L}{2\pi d}$ , (upward)

#### Bar magnet vs Current Loop

\*If wrap fingers around wire in loop, Thumb: I, fingers: B\*If put fingers on loop, Thumb:B, fingers: I, like inside of a Bar

\*The side of the current loop from which B emerges is North pole.

### Magnetic Field at CENTER of current loop

 $B = \frac{\mu_0 NI}{2R}$ 

N: number of loops

#### Interaction between Current Loops

\*Same I direction: attract

\*Different I direction: repel

n: no. of turns per unit length

# Magnetic Field INSIDE ideal solenoid

 $B = \mu_0 nI$ 

\*Solenoid becomes like a Bar Magnet

#### Cosine Rule

 $c^2 = a^2 + b^2 - 2ab\cos C$ , C is angle between a and b

### Lecture 9: Electromagnetic Induction

 $\Delta\Phi \to \varepsilon_{induced} \to I_{induced} \to B_{induced} \to \Phi_{induced}$ 

#### Len's Law

The direction of  $I_{induced}$  is such that the  $B_{induced}$  opposes the **change** in the flux that induces the current.

### Faraday's Law of Induction

$$|arepsilon|=Nrac{|\Delta\Phi|}{\Delta t}=Nrac{|\Phi_f-\Phi_i|}{\Delta t},\,N$$
 is no. of loops Motional Electromotive Force

$$\Delta V = \varepsilon = vBL$$
, (recall  $E = vB$ ,  $E = \frac{\varepsilon}{L}$ )

To have motional emf, conductor must **cut** through magnetic field

#### **Induced Current**

$$I = \frac{\varepsilon}{R} = \frac{vBL}{R}$$

# $I=rac{arepsilon}{R}=rac{vBL}{R}$ Magnetic Force (magnitude) on bar

$$F = ILB = \frac{vB^2L^2}{R}$$

# Lecture 10: Electromagnetic Waves (EM Waves)

# Speed of EM Waves

$$c = \frac{1}{\sqrt{\varepsilon_0 \mu_0}}, E = cB$$

Transverse wave:  $\vec{E}$  and  $\vec{B}$  fields are **perpendicular**.

#### Energy in EM Waves

$$u_E = \frac{1}{2}\epsilon_0 E^2, u_B = \frac{1}{2}\frac{B^2}{\mu_0}, u_E = u_B$$

So total,  $u_{EM} = u_E + u_B = \epsilon_0 E^2 = \frac{B^2}{u_0}$ 

#### Intensity of EM Waves

 $I=\frac{U}{A\Delta t}=\frac{P}{A}=u_{EM}c=c\varepsilon_0E^2=\frac{c}{\mu_0B^2},$  (Watts/ $m^2$  or  $W/m^2$ ) Here I is Intensity, not Current

#### EM Spectrum

 $c = f\lambda$ , f: frequency,  $\lambda$ : wavelength

# Doppler Equation for EM Waves

 $f_o = f_s(1 \pm \frac{u}{c})$ , only valid for  $u \ll c$ 

 $f_o$ : observed frequency

 $f_s$ : frequency emitted by the source

u: relative speed between source and observer

 $u = |v_1 + v_2| \Rightarrow$  moving in opposite directions

 $u = |v_1 - v_2| \Rightarrow$  moving in same directions

\*Important intuition: As objects come closer, frequency increase

#### Polarization of EM Waves

\*Direction of polarization of an EM wave is defined to be the direction of  $\vec{E}$  field. A wave propagates with FIXED polarization  $\rightarrow$  linearly polarized.

#### Unpolarized Light on Linear Polarizer

 $I_{transmitted} = \frac{1}{2}I_{incident}$ , here I is Intensity

#### Linearly Polarized Light on Linear Polarizer, Malus' Law

 $E_{transmitted} = E_{incident} \cos \theta \Rightarrow I_{transmitted} = I_{incident} \cos^2 \theta$  $\theta$ : angle between the incoming light's polarization and the transmission axis (TA)

#### **Optical Activity**

The ability of a substance to rotate the polarization direction of linearly polarization light. This ability depends on the molecular structure of the substance.

#### Lecture 11: Reflection Of Light

#### Law of Reflection

 $\theta_i = \theta_r$ 

 $\theta_i$ : Incident angle

 $\theta_r$ : Reflected angle

Specular vs Diffuse reflection: one is smooth surface, one is rough surface. Diffuse makes dry road easy to see at night.

\*For plane mirrors, basically it's all about similar triangles

# **Spherical Mirrors**

C = center of curvature.

#### Focal Point for Concave/Convex Mirror

Concave:  $f = \frac{R}{2}$ , Convex:  $f = -\frac{R}{2}$ 

Concave converges, Convex diverges

f: focal length, distance from Focal Point, F, to center of mirror

R: distance from C to center of mirror

\*Flat/Plane mirror has  $f = \infty, : R \to \infty$ 

### Ray tracing for Concave/Convex mirror (Find real/virtual image)

Ray#1: Parallel to principal axis, reflects through F.

Ray#2: Through C, center of curvature.

Ray#3: Through F, reflects parallel to principal axis.

\*Intersection point is where the real/virtual image lies.

# **Spherical Mirror Equations**

$$\frac{1}{d_o} + \frac{1}{d_i} = \frac{1}{f}$$
, applies to concave/convex

 $\frac{1}{d_o}+\frac{1}{d_i}=\frac{1}{f},$  applies to concave/convex  $d_o$ : object distance  $d_i$ : image distance f: focal length

#### Magnification

$$m \equiv \frac{h_i}{h_o} = -\frac{d_i}{d_o}$$
  $h_o$ : object height

 $h_i$ : image height,  $(-ve) \rightarrow$  inverted image

m has same sign as  $h_i$ ,  $|m| < 1 \rightarrow \text{reduced}$ ,  $|m| > 1 \rightarrow \text{enlarged}$ .

# Lecture 12: Refraction Of Light

#### **Index of Refraction**

$$n \equiv \frac{c}{v}, n > 1, :: c > v$$

c: speed of light in vacuum

v: speed of light in medium

#### Frequency between media

$$v=f\lambda\Rightarrow rac{\lambda_1}{\lambda_2}=rac{v_1}{v_2}=rac{n_2}{n_1}$$
 Snell's Law of Refraction

 $n_1 \sin \theta_1 = n_2 \sin \theta_2$ 

 $\theta$ : angle between light and normal of incidence

#### Apparent Depth

$$\frac{d'}{d} = \frac{n_1}{n_2}$$

 $\frac{d'}{d} = \frac{n_1}{n_2}$  d': apparent depth

d: actual depth

 $n_1$ : refraction index of medium 1 (before refraction)

 $n_2$ : refraction index of medium 2 (after refraction)

#### Total Internal Reflection

Critical angle:  $n_1 \sin \theta_c = n_2 \sin 90^\circ \Rightarrow \sin \theta_c = \frac{n_2}{n_1}$ 

#### Polarization by Reflection, Brewster's Angle

 $\tan \theta_B = \frac{n_2}{n_1} \Rightarrow \theta_B$ : Brewster's Angle

\*When unpolarized light is reflected from a surface, it can get polarized at  $0^{\circ} < \theta_i < 90^{\circ}$ . At  $0^{\circ}/90^{\circ}$ , light remains unpolarized. \*Reflected light is **totally** polarized **parallel** to the surface when the reflected and refracted rays are at right angles.

\*Dispersion is the dependence of the index of refraction of a transparent medium on the wavelength of light.

# Lecture 13: Optical Instruments

#### Thin Lenses

Principal Rays for Converging/Diverging lens

Ray#1: Parallel to principal axis, passes through F.

Ray#2: Through center of lens.

Ray#3: Through F, emerges parallel to principal axis.

#### Thin Lens Equation

$$\frac{\frac{1}{d_o} + \frac{1}{d_i} = \frac{1}{f}}{d_o: \text{ object distance}}$$

Positive: real object (in front of lens)

Negative: virtual object (behind lens)

 $d_i$ : image distance

Positive: real image (behind lens)

Negative: virtual image (in front of lens)

f: focal length

Positive: convex (converging) lens Negative: concave (diverging) lens

### Magnification equation

$$m \equiv \frac{h_i}{h_o} = -\frac{d_i}{d_o}$$
  
 $h_o$ : object height

 $h_i$ : image height,  $(-ve) \rightarrow$  inverted image

m has same sign as  $h_i$ ,  $|m| < 1 \rightarrow \text{reduced}$ ,  $|m| > 1 \rightarrow \text{enlarged}$ .

#### Combination of Lenses

 $m_{total} = m_1 * m_2$ 

 $m_i$ : magnification by *i*-th lens

#### **Human Eyes**

Focal length of normal human eye  $\approx 2.5$ cm

Near point of normal human eye  $\approx 25 \text{cm}$ 

Far point of normal human eye :  $\infty$ 

#### When you are **near-sighted**:

- 1. Far point is too close
- 2. Need concave (diverging) lens to create an virtual image at that abnormal far point (which is  $< \infty$ ), which acts as new object for vour eve

When you are **far-sighted**:

- 1. Near point is too far
- 2. Need convex (converging) lens to create an virtual image at that abnormal near point (which is > 25cm), which acts as new object for your eye

#### Refractive Power of Lens

 $P = \frac{1}{f}, \text{ Unit: Diopter, } (m^{-1})$  f: focal length of lens

# Magnifying Glass

Angular size,  $\tan \theta = \frac{h_o}{d_o} \Rightarrow \theta \approx \frac{h_o}{d_o} \text{ or } \theta \approx \frac{h_o}{N}$   $h_o$ : object height

N: near point distance

As object is moved closer to eye,  $\theta$  decreases.

 $\theta \approx \frac{h_i}{d_i} \approx \frac{h_o}{d_o}$ , (similar triangles)

Angular Magnification,

$$M = \frac{\theta}{\theta_o}$$

 $\theta_o$ : angular size of object, (without magnifying glass)

 $\theta$ : angular size of image, (with magnifying glass)

$$M = N(\frac{1}{f} - \frac{1}{d_i})$$

 $\Rightarrow M = N(\frac{1}{f} - \frac{1}{-\infty})$  for virtual image at  $\infty$  $\Rightarrow M = N(\frac{1}{f} - \frac{1}{-N})$  for virtual image at N

# Lecture 14: Interference of Light

#### Principle of superposition

Constructive superposition:  $\lambda_2 - \lambda_1 = m\lambda$ , m = 0, 1, 2, ...

Destructive superposition:  $\lambda_2 - \lambda_1 = (m + \frac{1}{2})\lambda$ , m = 0, 1, 2, ...

#### Double Slit Interference

Optical Path Difference:  $\delta = d \sin \theta$ 

# Constructive Interference (Bright Fringes)

$$\delta = d \sin \theta = m\lambda, \ m = 0, 1, 2, \dots$$

#### Destructive Interference (Dark Fringes)

$$\delta = d \sin \theta = (m + \frac{1}{2})\lambda, \ m = 0, 1, 2, \dots$$

d: slit-spacing

 $\theta$ : angle between ray and norm

\*Center Bright is m = 0, 1st Bright usually means m = 1

\*First Dark from Center Bright is m = 0

Small Angle Approx. To Find Bright/Dark Fringes Bright:  $\theta \approx \frac{m\lambda}{d}, \ y \approx \frac{m\lambda L}{d} \ | \ \text{Dark:} \ \theta \approx (m+\frac{1}{2})\frac{\lambda}{d}, \ y \approx (m+\frac{1}{2})\frac{\lambda L}{d}$ L: distance between slit and screen

### Thin Film Interference

Reflection	Distance	Optical path diff
Ray 1 $0(n_0 > n_1)$	0	$\delta_1 = 0 + 0(n_0 > n_1)$
Ray 1 $\frac{\lambda}{2}(n_0 < n_1)$	0	$\delta_1 = \frac{\lambda}{2} + 0(n_0 < n_1)$
Ray 2 $\bar{0}(n_1 > n_2)$	$2n_1t$	$\delta_1 = 0 + 2n_1 t (n_1 > n_2)$
Ray 2 $\frac{\lambda}{2}(n_1 < n_2)$	$2n_1t$	$\delta_1 = \frac{\lambda}{2} + 2n_1 t (n_1 < n_2)$

 $\delta = |\delta_1 - \delta_2|$ : optical path difference between Ray 1 and 2  $\delta_1$ : optical path difference between Ray 1 and incident ray  $\delta_2$ : optical path difference between Ray 2 and incident ray Constructive:  $\delta = m\lambda$ , Destructive:  $\delta = (m + \frac{1}{2})\lambda$ , m = 0, 1, ...

# Lecture 15: Diffraction and Grating

# Single Slit Diffraction - Locating Minima (Dark Fringe)

 $\sin \theta = \frac{m\lambda}{W}, \ y = \frac{m\lambda L}{W}, \ m = 1, 2, 3, \dots$ 

\*First Dark is m = 1 (Notice the difference between Double Slit) Diffraction from Circular Aperture

$$\sin \theta = 1.22 \frac{\lambda}{D}$$

→**First minimum** of a circular diffraction pattern

D: diameter of circular aperture

#### Resolving Power (Rayleigh's Criterion)

 $\theta_{min} = 1.22 \frac{\lambda}{D}$ , **NOTE**:  $\theta_{min}$  will be in Radians

 $\theta_{min}$ : angle between the 2 objects / light sources

 $\lambda$ : the wavelength in the region between the aperture and screen Two point objects are just resolved when the 1st dark fringe in the diffraction pattern of one falls directly on the central bright fringe in the diffraction pattern of the other. So, to see 2 objects distinctively, we need:

 $\theta_{objects} \ge \theta_{min}$ , and  $\theta_{objects} \approx \frac{d}{u}$ 

d: distance between objects

y: distance from objects to the aperture

#### Convert Radians to Degree

$$\theta^{\circ} = \frac{\theta \operatorname{rad} \times 180^{\circ}}{\pi}$$

### Diffraction Grating

 $d\sin\theta = m\lambda$ 

\*Condition for constructive interference

$$\theta = \sin^{-1} \frac{m\lambda}{d}, \ y = L \tan \theta$$

\*Center Bright fringe is m = 0

\*As no. of slits per unit length of grating \(\frac{1}{2}\), fringes get narrower and brighter

 $m: m = 0, 1, 2, \dots$ 

y: distance from center fringe to i-th fringe

L: distance from grating to screen

#### Lecture 16: Photoelectric Effect

#### Photoelectric Equation

 $K_{max} = hf - W_0 \Rightarrow K_{max} = h\frac{c}{\lambda} - W_0 \text{ (units: } eV)$ 

eV: electron volt, 1 electron charge times 1 V

 $K_{max}$ : max kinetic energy of released electrons

h: Planck's constant =  $6.63 \times 10^{-34} Js$  (Joules second)

f: frequency of light source

 $W_0$ : work function of the metal surface (minimum energy needed to free electron)

 $f_0 = \frac{W_0}{h}, \lambda_0 = \frac{hc}{W_0}$ 

 $f_0, \lambda_0$ : cutoff frequency/wavelength (if  $\lambda_0 \uparrow$  then  $W_0 \downarrow$ , no photo-

\*Remember:  $K_{max}$  depend **only** on frequency and work function, not intensity

\*Photon energy  $> W_0 \rightarrow \text{electron freed}$ 

\*Photon energy  $\langle W_0 \rightarrow \text{electron not freed regardless of intensity}$ 

#### **Stopping Potential**

$$eV_0 = K_{max}, V_0 = rac{h}{e}(f-f_0)$$
de Broglie's Matter Wave

$$\lambda = \frac{h}{p} = \frac{h}{mv} = \frac{h}{\sqrt{2meV}}$$
 p: momentum

v: velocity

e: electron charge

Converging lenses 
$$\begin{pmatrix} d_o \\ d_o \\ d_o \end{pmatrix}$$

$d_o < f$	Up.	Mag.	Virt.
$d_o = f$	_	_	_
$d_o = 2f$	Inv.	Same	Real
$d_o > f$	Inv.	Dim.	Real

V: potential

\*Note: eV together may mean, for e.g. 10.2 eV. Need to multiply by electron charge

#### Finding No. of photons per second

$$\frac{\#photons}{second} = \frac{energy/second}{energy/photon} = \frac{power}{energy/photon} = \frac{power}{hf}$$

# Lecture 17: Atomic Physics

#### Line Spectra

Absorption Spectrum:

Bright background with dark lines (Photons were absorbed)

Emission Spectrum:

Dark background with bright lines (Photons were emitted)

#### Balmer Series (Hydrogen)

$$\frac{1}{\lambda} = R_H(\frac{1}{2^2} - \frac{1}{n^2}), \ n = 3, 4, 5, \dots$$
  
\*When  $n = 3, \lambda$  is longest.

#### Lyman Series (Ultraviolet)

$$\frac{1}{\lambda}=R_H(\frac{1}{1^2}-\frac{1}{n^2}),\ n=2,3,4,\dots$$
 Paschen Series (Infrared)

$$\frac{1}{\lambda} = R_H(\frac{1}{3^2} - \frac{1}{n^2}), \ n = 4, 5, 6, \dots$$

#### Brackett Series (Infrared)

$$\frac{1}{\lambda} = R_H(\frac{1}{4^2} - \frac{1}{n^2}), \ n = 5, 6, 7, \dots$$

Pfund Series (Infrared)

$$\frac{1}{\lambda} = R_H(\frac{1}{5^2} - \frac{1}{n^2}), \ n = 6, 7, 8, \dots$$

# $\frac{1}{\lambda}=R_H(\frac{1}{5^2}-\frac{1}{n^2}),\ n=6,7,8,\ldots$ In general... (for the spectral lines in Hydrogen atom)

$$\frac{1}{\lambda} = R_H(\frac{1}{n_f^2} - \frac{1}{n_i^2}), \ n \in \mathbb{Z}^+, n_i > n_f$$

 $R_H$ : Rydberg Constant,  $1.097 \times 10^7 m^{-1}$ 

#### Bohr's Model of Atom

Intuition:

Electron jump from level n = i to  $n = i - 1 \rightarrow$  emits photons Electron jump from level n = i to  $n = i + 1 \rightarrow$  absorbs photons

# Bohr's Angular Momentum Quantization

$$2\pi r=n\lambda~\&~\lambda={h\over p}\Rightarrow mrv={nh\over 2\pi}$$
 Planck-Einstein / Planck's relation

$$E = hf = h\frac{c}{\lambda} \Rightarrow \lambda = \frac{hc}{E}$$

h: Planck's constant,  $6.63 \times 10^{-34} Js$ 

f: frequency

E: energy, so can be in eV or J. (Recall equation in Lect 16)

#### Energy Levels of Hydrogen Atom

$$E_n = -\frac{1}{2} \frac{1}{4\pi\epsilon_0} \frac{e^2}{n^2 a_0} = -\frac{13.6 \text{ eV}}{n^2}, \ (a_0 = \epsilon_0 \frac{h^2}{\pi m e^2}, \ r_n = n^2 a_0)$$
  
 $a_0$ : smallest orbit radius,  $Bohr \ radius = 0.0529 \text{nm}$ 

 $r_n$ : general expression for radius of any orbit

\*Lowest energy level or ground state  $\rightarrow n = 1$ 

\*First excited state  $\rightarrow n = 2$ , and so on...

\*Highest level, electron removed  $\rightarrow n = \infty, E = 0$ 

#### Some Intuition about Spectral Lines

When there is a transition from (e.g.) n=3 to n=2, then there is a wavelength for that photon(s). So for e.g. electron excited to n=3.  $(3 \to 2), (2 \to 1) & (3 \to 1)$  are spectral lines.

# **Energy Levels and Spectrum**

$$\frac{1}{\lambda} = R_H \left| \frac{1}{n_f^2} - \frac{1}{n_i^2} \right|$$

\*Longest  $\lambda$ : e.g.  $\lambda_{32} = \frac{hc}{E_3 - E_2}$  (Balmer series)

\*Shortest  $\lambda$ : e.g.  $\lambda_{\infty 2}$  (Balmer series)

In General, when there's 
$$Z/\text{Protons}$$
 involved..  $E_n = -\frac{1}{4\pi\epsilon_0} \frac{Z^2 e^2}{2n^2 a_0} = -\frac{Z^2 (13.6 \text{ eV})}{n^2}, (r_n = \frac{n^2 a_0}{Z})$   $Z$ : number of protons in nucleus

$$\Rightarrow \frac{1}{\lambda} = Z^2 R_H \left| \frac{1}{n_f^2} - \frac{1}{n_i^2} \right|$$