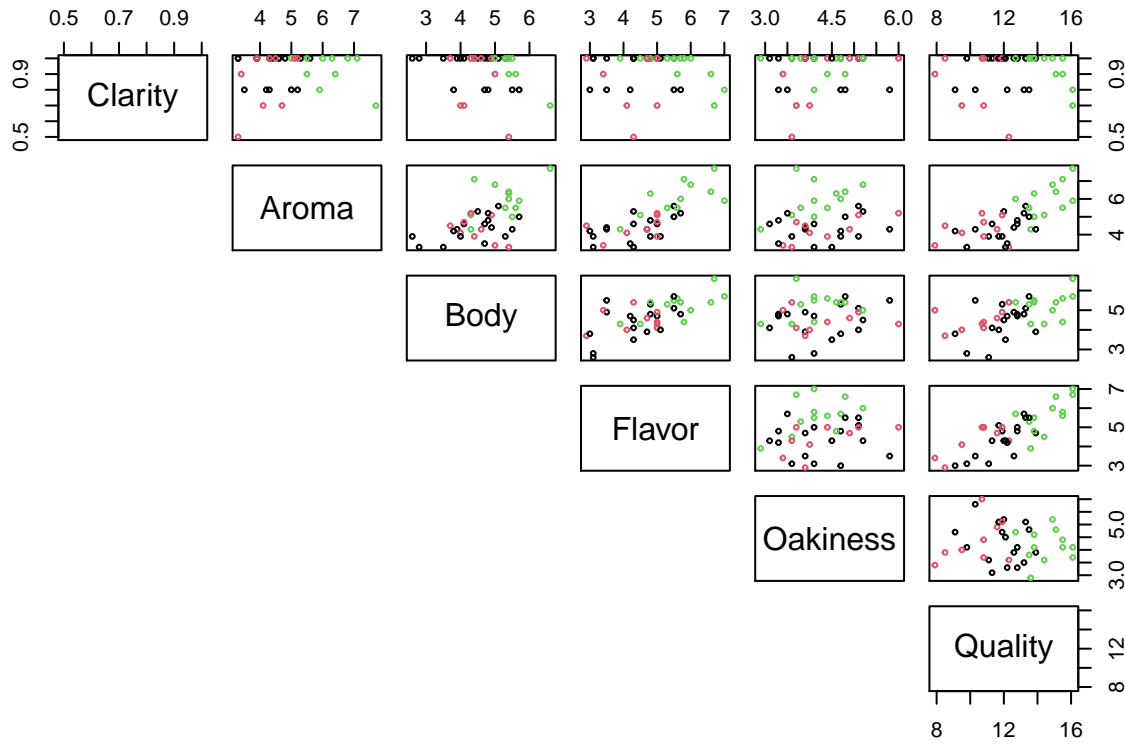


MiniProj_2

Wenxiong Lu

Q1

- (a) There are 17 observations from region 1, 9 observations from region 2 and 12 observations from region 3. It seems observations from region 3 have the highest quality and observations from region 2 and 1 are mixed.



- (b): Yes. Quality is an appropriate variable

(c):

Variable Name	P - Value	95%Confidence Interval
Clarity	0.865	(-5.105130, 6.043584)
Aroma	6.87e-07	(0.8850212 1.787982)
Body	0.000361	(1.159604 1.984177)
Flavor	3.68e-09	(1.159604 1.984177)
Oakiness	0.779	(-1.066083 0.805353)
Region 1	2e-16	(11.330893 12.6220486)
Region 2	0.00757	(-2.629298 -0.4347544)
Region 3	7.01e-06	(1.603271 3.6104546)
Region(overall)		

Comments: As the results shown above, 'Clariy' and 'Oakiness' are not significantly associated to Quality per 95% confidence level. The rest of variables are associated to Quality.

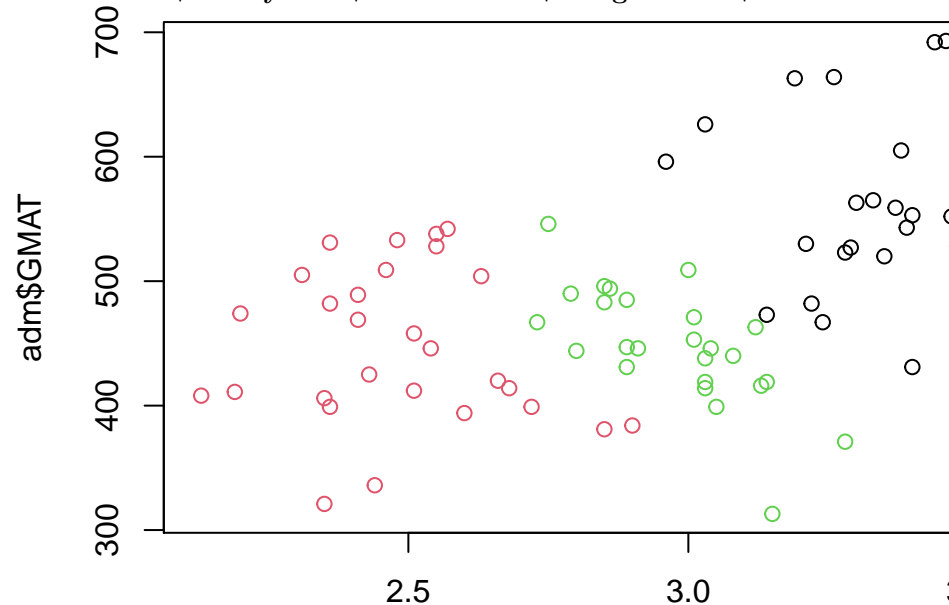
(d): Without considering interaction term, the remaining predictors are 'Flavor' and 'Region'. (The interaction terms will be tested in question e) We can reject H0 for the F test of these parameters. Firstly, fit a full model with all the parameters, then we can find out that Clarity has highest p-value '0.990736'. After removing Clarity, the next highest will be removed. The 'removing sequence' is Clarity(0.990736), Body(0.746249), Aroma(0.70489), Oakiness(0.128060).

(e) Firstly, fit a full model (including all the possible interaction terms). Then remove terms with highest p-value and make anova for the updated model and find the next highest p-value and remove the predictor. By repeating this process we will remove the predictors in sequence: [Body:Flavor(interaction term between Body and Flavor), Aroma:Region, Flavor:Region, Aroma:Flavor:Region, Body:Flavor:Region, Aroma:Flavor, Aroma:Body:Region, Aroma:Body:Flavor:Region, Aroma:Body:Flavor, Aroma:Body, Body:Region]. The remaining predictors are Aroma, Body, Flavor, Region. Then, check the F test for multiple linear model and we can see that the p-value of Aroma and Body changed from significant to insignificant. This is due to Region is a qualitative data, both Aroma and Body have significant interaction to Region 1 and Region 2. The currently reasonably good model is: $Quality = x_0 + Aroma x_1 + Body x_2 + Flavor x_3 + Region x_4$.

```
## Analysis of Variance Table
##
## Response: Quality
##           Df Sum Sq Mean Sq F value    Pr(>F)
## Aroma      1  77.442   77.442  91.2025 6.909e-11 ***
## Body       1   5.703    5.703   6.7163  0.01428 *
## Flavor     1  18.878   18.878  22.2329 4.539e-05 ***
## Region     2  25.593   12.797  15.0706 2.445e-05 ***
## Residuals 32  27.172    0.849
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Call:
## lm(formula = Quality ~ Aroma + Body + Flavor + Region, data = wine)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -1.98279 -0.59142  0.02005  0.55790  1.87722
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   7.00195     1.11063   6.304 4.51e-07 ***
## Aroma        -0.01643     0.24448  -0.067 0.946855
## Body          0.05253     0.24509   0.214 0.831664
## Flavor        1.10027     0.24136   4.559 7.13e-05 ***
## Region2      -1.53977     0.38117  -4.040 0.000313 ***
## Region3       1.22420     0.47800   2.561 0.015352 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.9215 on 32 degrees of freedom
## Multiple R-squared:  0.8245, Adjusted R-squared:  0.797
## F-statistic: 30.06 on 5 and 32 DF,  p-value: 3.341e-11
```

(f) By fitting a linear model for $\text{Aroma} = \text{Region} \times \text{Body}$, we can find out the exact interaction term in (e) is of 1. (Region 1, Body, Region2:Body) and fit another model $\text{Body} = \text{Aroma} \times \text{Region}$ we can see interaction term is of 2. (Aroma, Region2, Aroma:Region2). This indicates that there are interaction terms between Region1 and Aroma, Region and Body. So we should consider put back the interaction term between Region:Aroma and Region:Body.

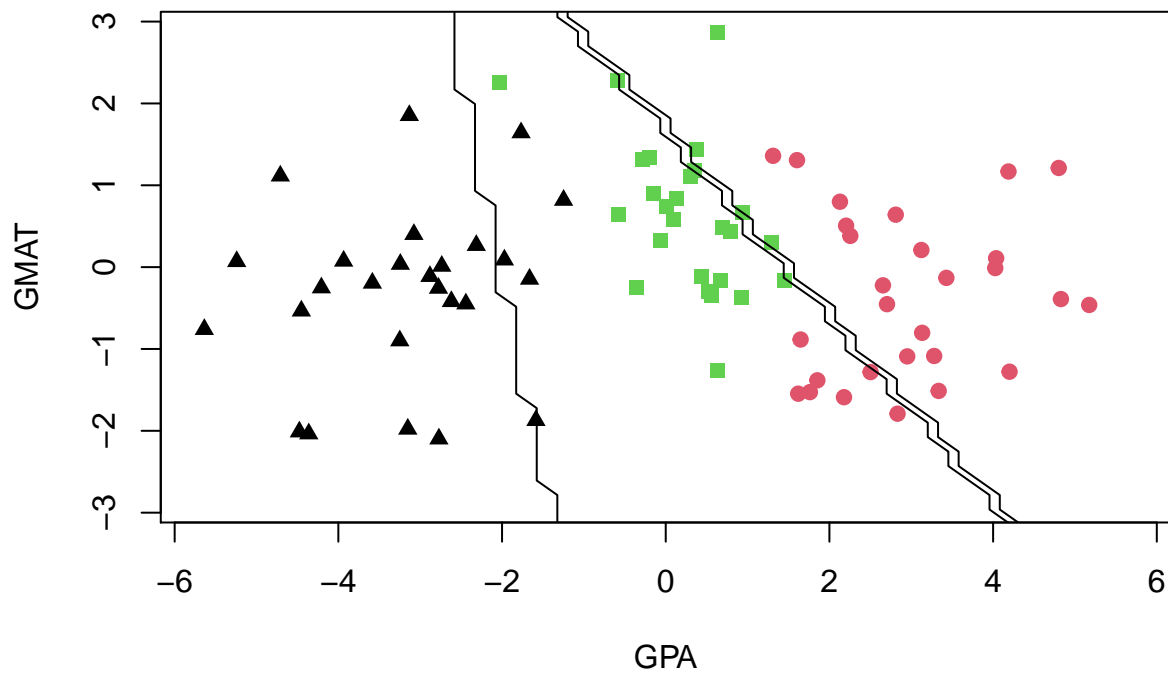
The final model: $\text{Quality} = x_0 + \text{Aroma } x_1 + \text{Body } x_2 + \text{Flavor } x_3 + \text{Region } x_4 +$



Aroma:Region x5 + Body:Region x6

2(a). It is easy to see that group is related to GPA and GMAT. Group might be an important predictor. GPA and GMAT are related to each differently in different group.

```
## Call:
## lda(Group ~ GPA + GMAT, data = adm.train)
##
## Prior probabilities of groups:
##      1      2      3
## 0.325 0.350 0.325
##
## Group means:
##      GPA      GMAT
## 1 3.431538 569.8077
## 2 2.482500 447.0714
## 3 2.992692 446.2308
##
## Coefficients of linear discriminants:
##      LD1      LD2
## GPA -5.300511724 1.91775603
## GMAT -0.009125023 -0.01438851
##
## Proportion of trace:
##      LD1      LD2
## 0.969 0.031
```



```
##
##      1  2  3
## 1 24  0  2
## 2  0 26  2
## 3  0  0 26

## [1] "confusion matrix for training data"

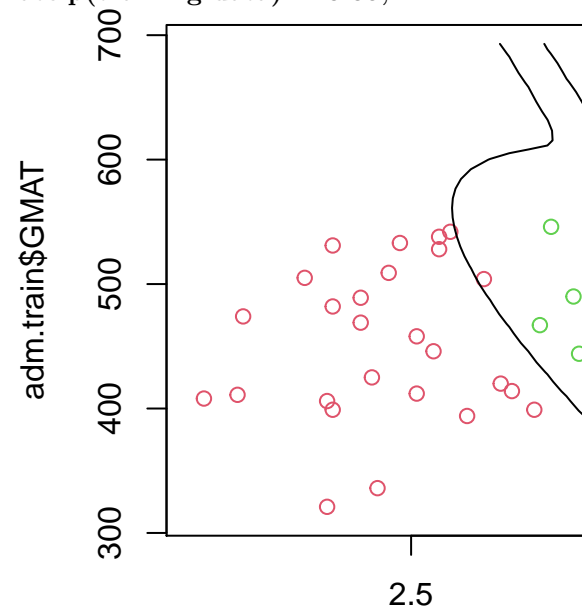
## [1] 0.05

## [1] "confusion matrix for test data"

##
##      1  2  3
## 1  2  0  3
## 2  0  0  0
## 3  0  0  0

## [1] 0.6
```

(b) The decision boundary seems sensible. The misclassification rate: $p(\text{training data}) = 0.05$,



$p(\text{test data}) = 0.6$ There is exist overfitting problem in this model.

```
##
##      1  2  3
##    1 26  0  0
##    2  0 27  1
##    3  1  0 25

## [1] "confusion matrix for training data"
## [1] 0.05

## [1] "confusion matrix for test data"

##
##      1  2  3
##    1  4  0  1
##    2  0  0  0
##    3  0  0  0

## [1] 0.2
```

(c) The decision boundary seems sensible. The misclassification rate: $p(\text{training data}) = 0.025$, $p(\text{test data}) = 0.2$ The model predicts the test data well.

(d) In general, QDA performs better than LDA in this case. So QDA is recommended.

3 It seems BloodPressure, Insulin, age, Glucose, are strongly related to Outcome.