

GPHY 5513

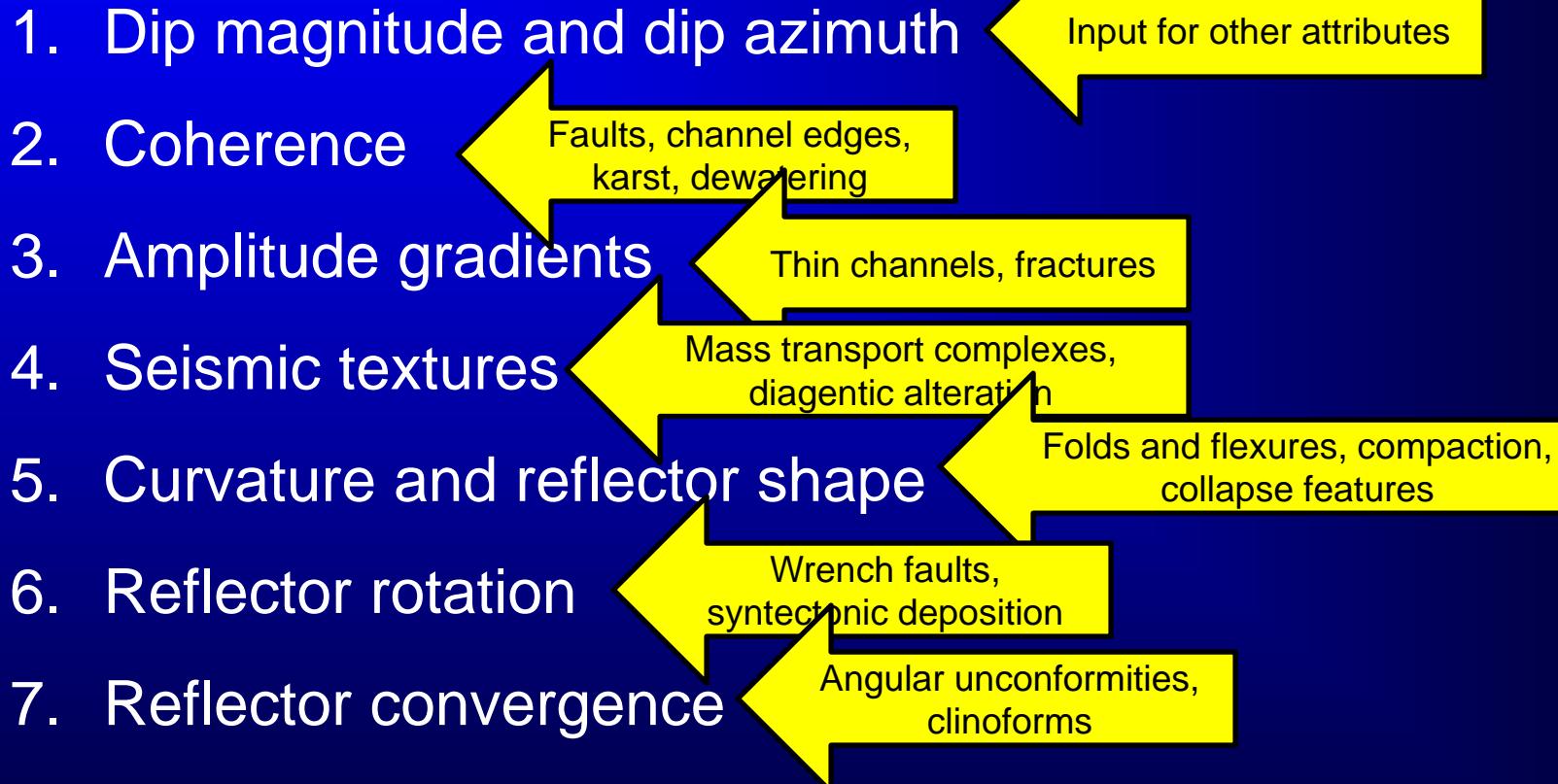
3D Seismic Interpretation

Dr. Zonghu Liao

Volumetric Dip and Azimuth



Geometric Attributes



Volumetric dip and azimuth

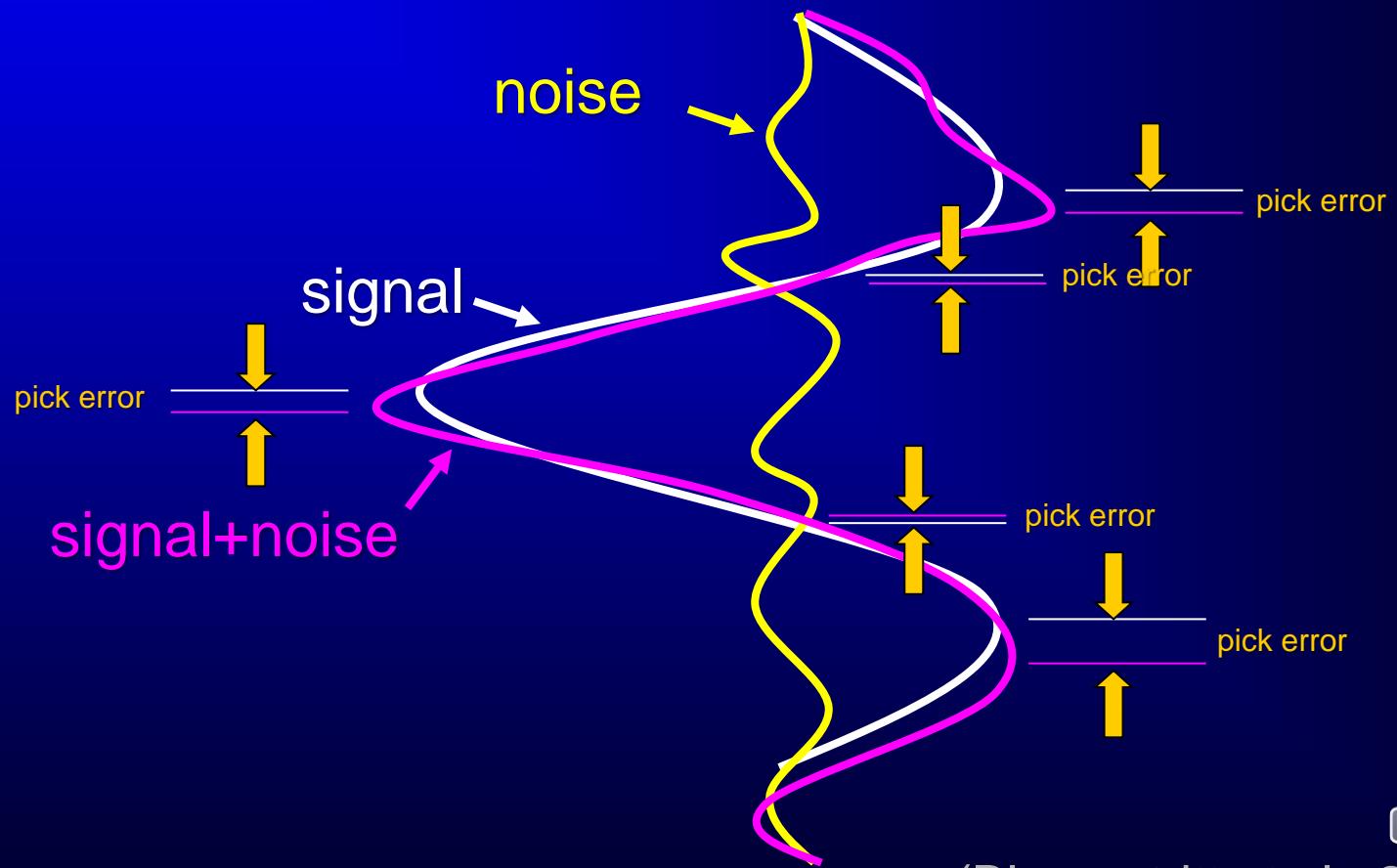
After this section you will be able to:

- Evaluate alternative algorithms to calculate volumetric dip and azimuth in terms of accuracy and lateral resolution,
- Interpret shaded relief and apparent dip images to delineate subtle structural features, and
- Apply composite dip/azimuth/seismic images to determine how a given reflector dips in and out of the plane of view.



Dip computed from picked maps:

Zero-crossing picks are less sensitive to noise than peaks or troughs

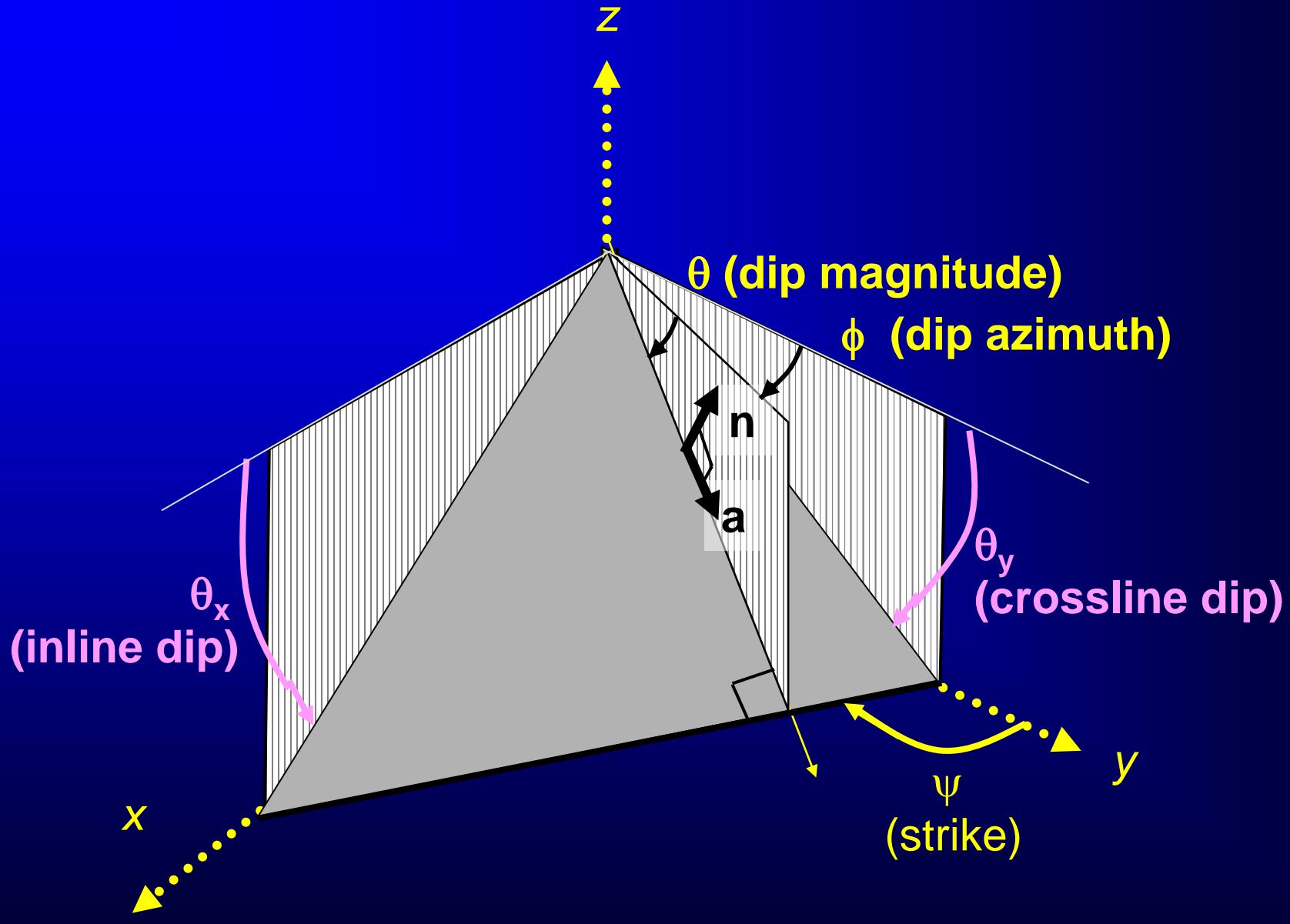


Alternative volumetric measures of reflector dip and azimuth

1. 3D Complex trace analysis
2. Gradient Structure Tensor (GST)
3. Plane-wave destructor
4. Discrete scans for dip of most coherent reflector



Definition of reflector dip



1. 3D Complex Trace Analysis (Instantaneous Dip/Azimuth)

Instantaneous phase

Hilbert transform

$$\phi = \text{ATAN2}(d^H, d)$$

Instantaneous frequency

$$\omega = 2\pi f = 2\pi \frac{\partial \phi}{\partial t} = 2\pi \frac{\frac{\partial d^H}{\partial t} d - \frac{\partial d}{\partial t} d^H}{d^2 + (d^H)^2}$$

Instantaneous
in line wavenumber

$$k_x = \frac{\partial \phi}{\partial x} = \frac{\frac{\partial d^H}{\partial x} d - \frac{\partial d}{\partial x} d^H}{d^2 + (d^H)^2}$$

Instantaneous
cross line wavenumber

$$k_y = \frac{\partial \phi}{\partial y} = \frac{\frac{\partial d^H}{\partial y} d - \frac{\partial d}{\partial y} d^H}{d^2 + (d^H)^2}$$

Instantaneous
apparent dips

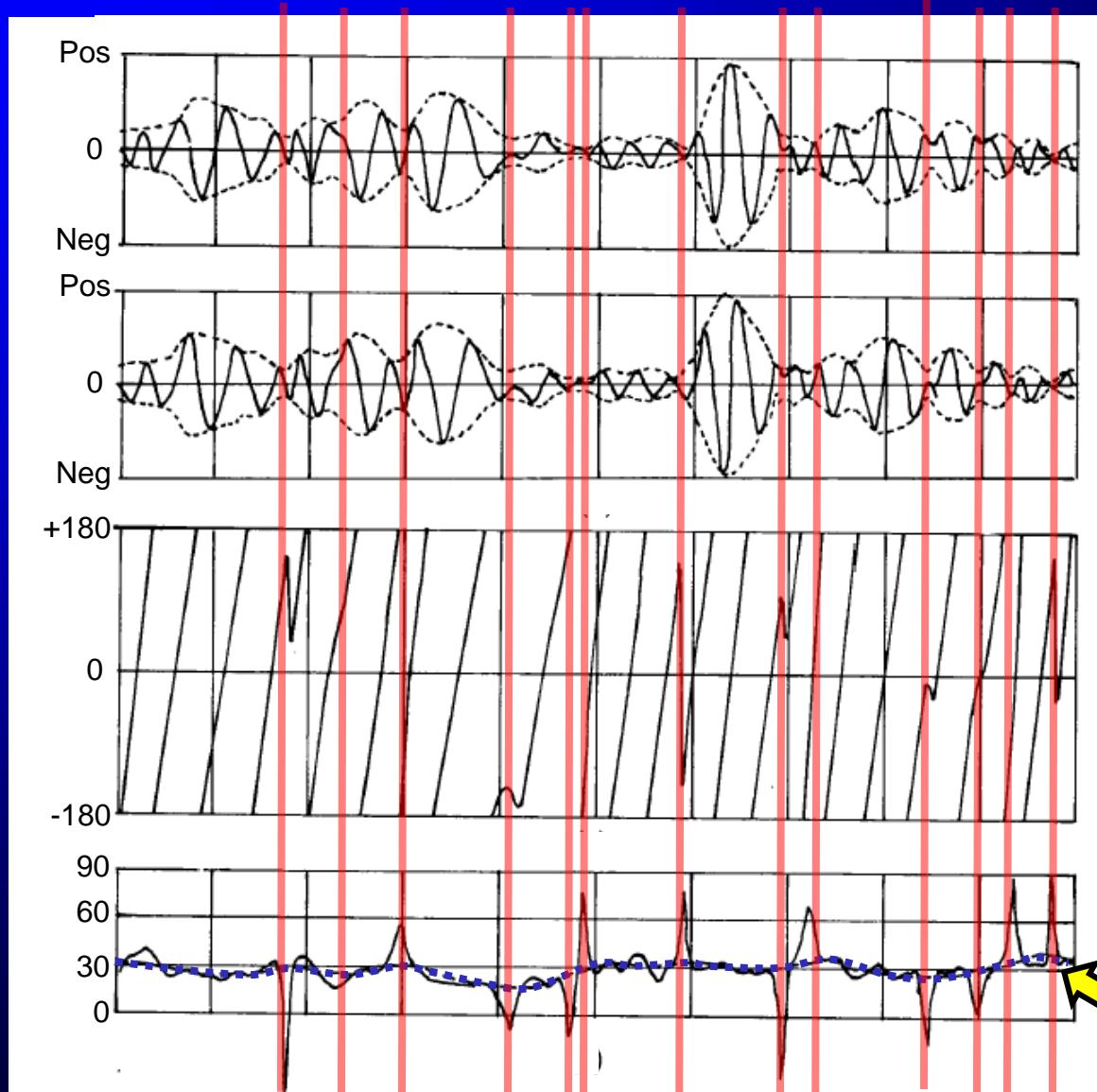
$$p = \frac{k_x}{\omega}; q = \frac{k_y}{\omega}$$

$$s = \sqrt{p^2 + q^2}$$

$$\psi = \text{ATAN2}(q, p)$$

The analytic trace

Original data (real component)
Quadrature (imaginary component)
Phase
Frequency (Hz)



$d(t)$

$d^H(t)$

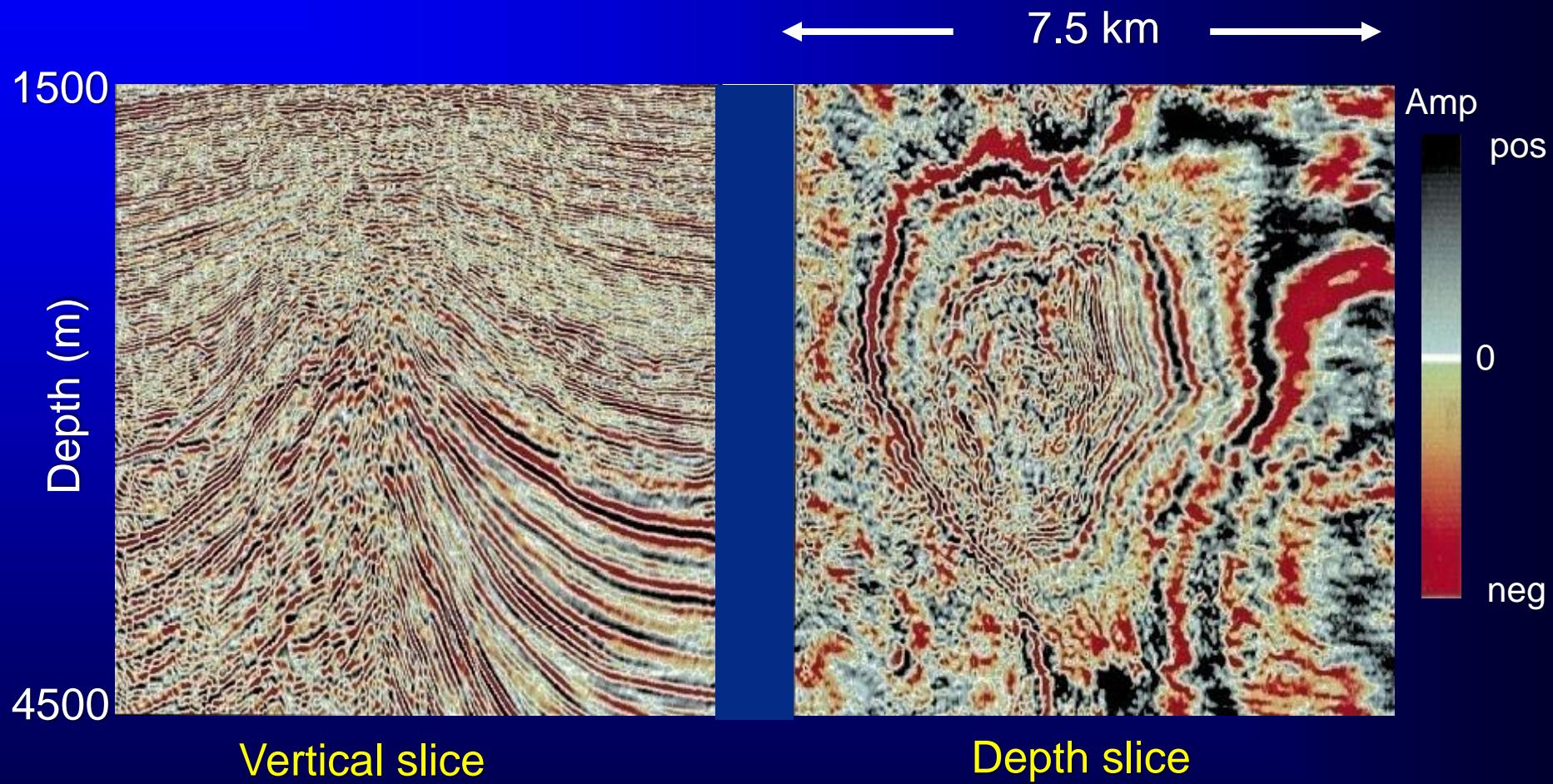
$$\phi(t) = \text{ATAN2}[d^H(t), d(t)]$$

$$\bar{f}_n \equiv \frac{\sum_{k=-K}^K e_{n+k} f_{n+k}}{\sum_{k=-K}^K e_{n+k}}$$

Weighted-average frequency



Seismic data

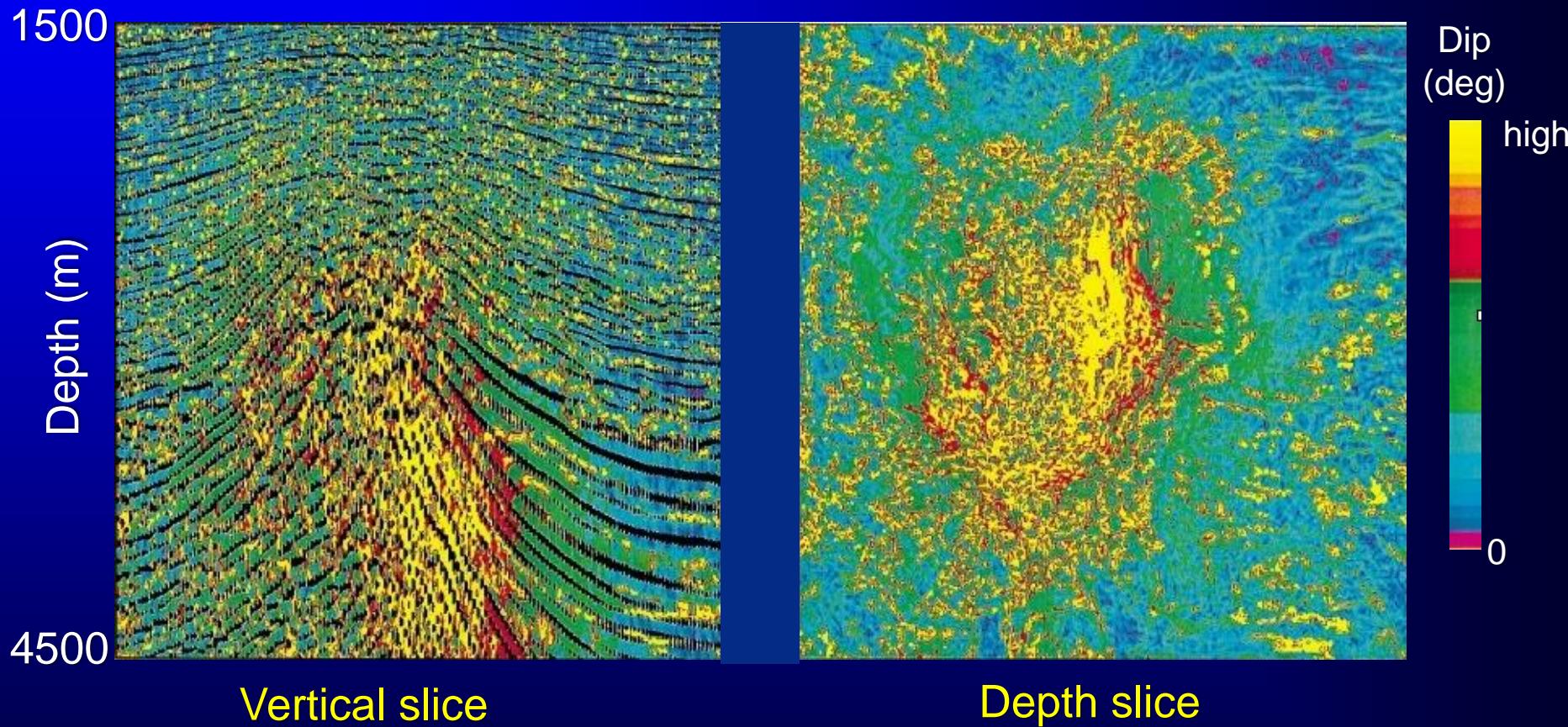


Instantaneous dip magnitude

$$s = \sqrt{p^2 + q^2}$$

(sensitive to errors in ω , k_x and k_y !)

← 7.5 km →

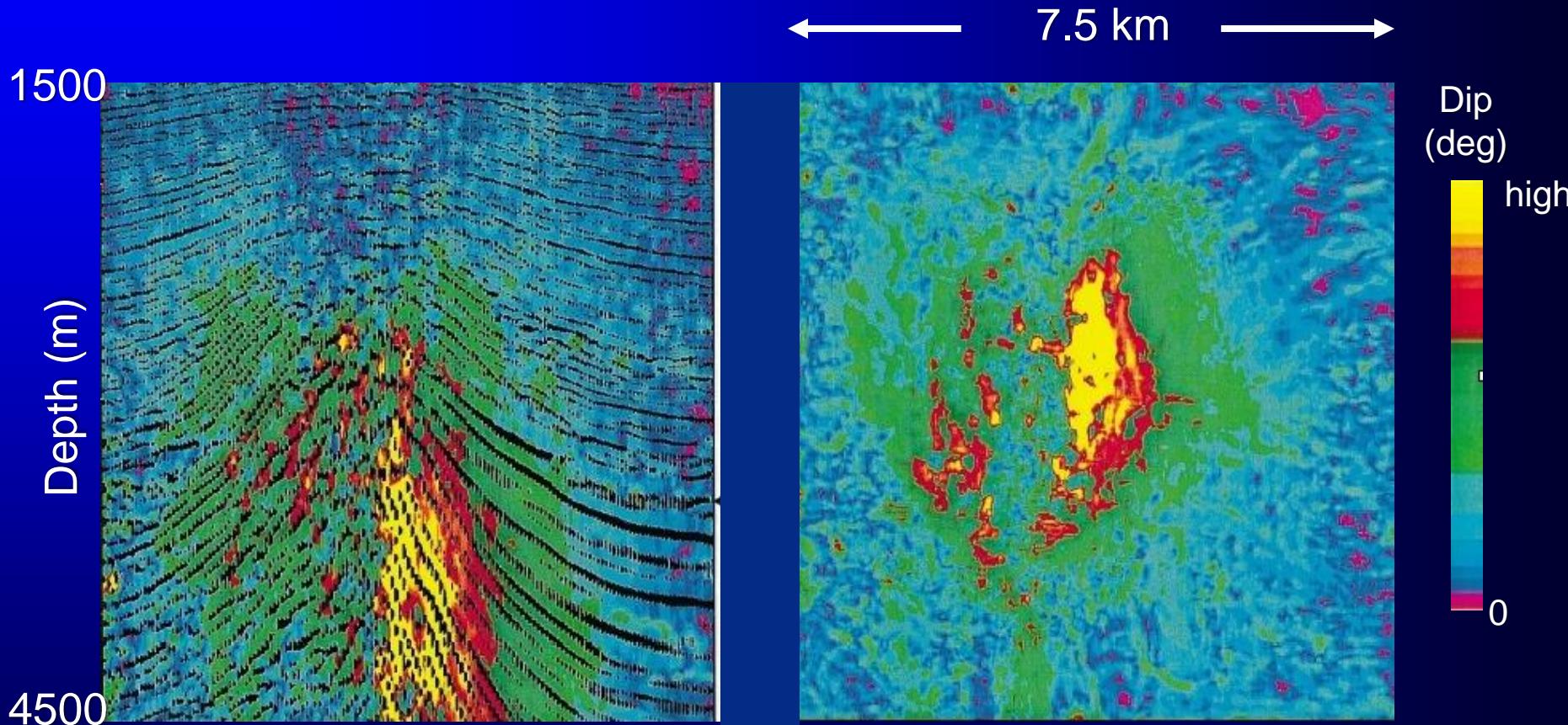


(Barnes, 2000)

Weighted average dip magnitude

(5 crossline by 5 inline by 7 sample window)

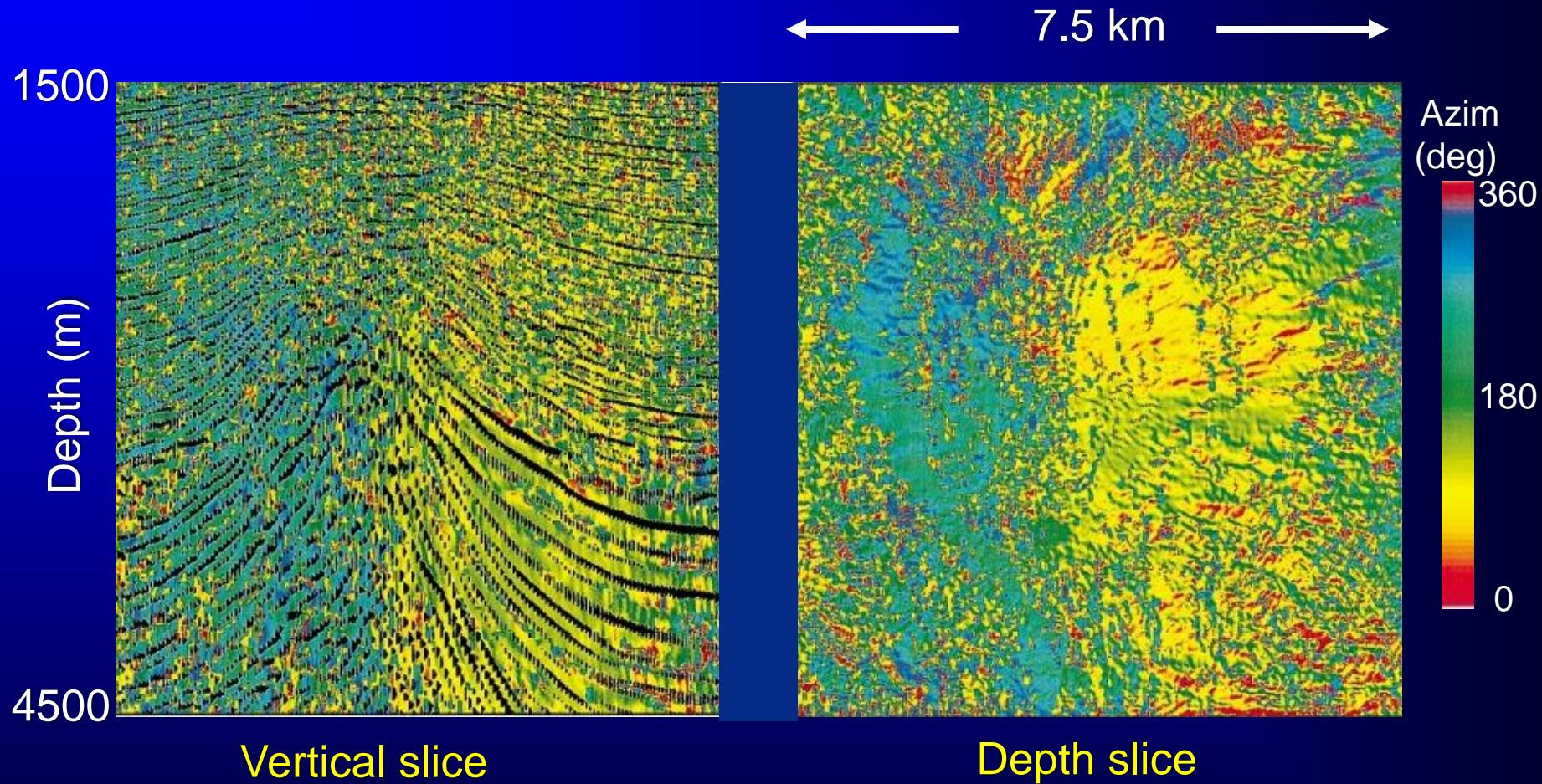
$$\bar{s} = \sqrt{\left(\frac{\bar{k}_x}{\bar{\omega}}\right)^2 + \left(\frac{\bar{k}_y}{\bar{\omega}}\right)^2}$$



$$\bar{\omega}_{rst} \equiv \frac{\sum_{l=-L}^{+L} \sum_{k=-K}^{+K} \sum_{j=-J}^{+J} e_{r+j, s+k, t+l} \bar{\omega}_{r+j, s+k, t+l}}{\sum_{l=-L}^{+L} \sum_{k=-K}^{+K} \sum_{j=-J}^{+J} e_{r+j, s+k, t+l}}$$

Instantaneous dip azimuth

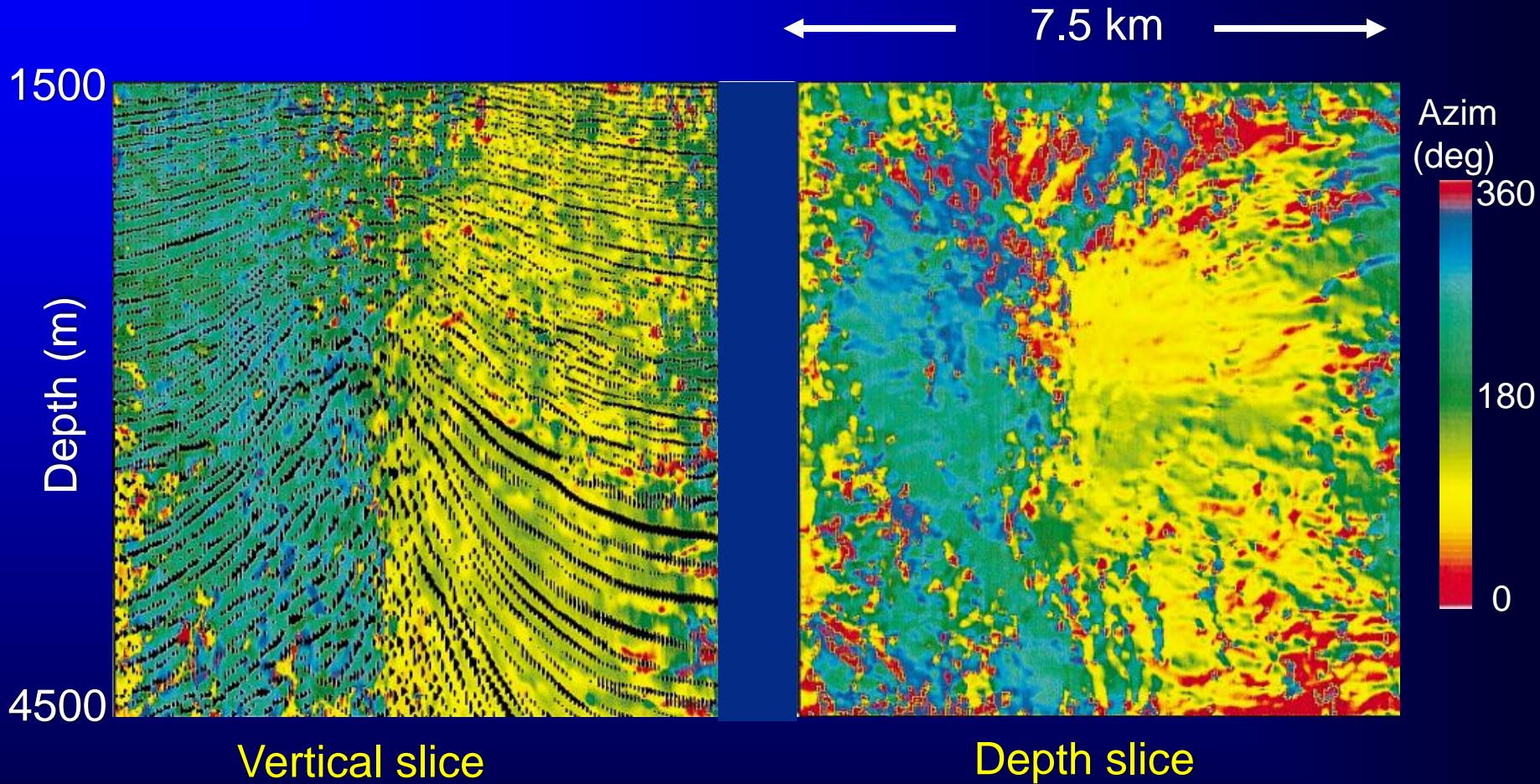
$$\psi = \text{ATAN}2(q, p)$$



Weighted average dip azimuth

(5 crossline by 5 inline by 7 sample window)

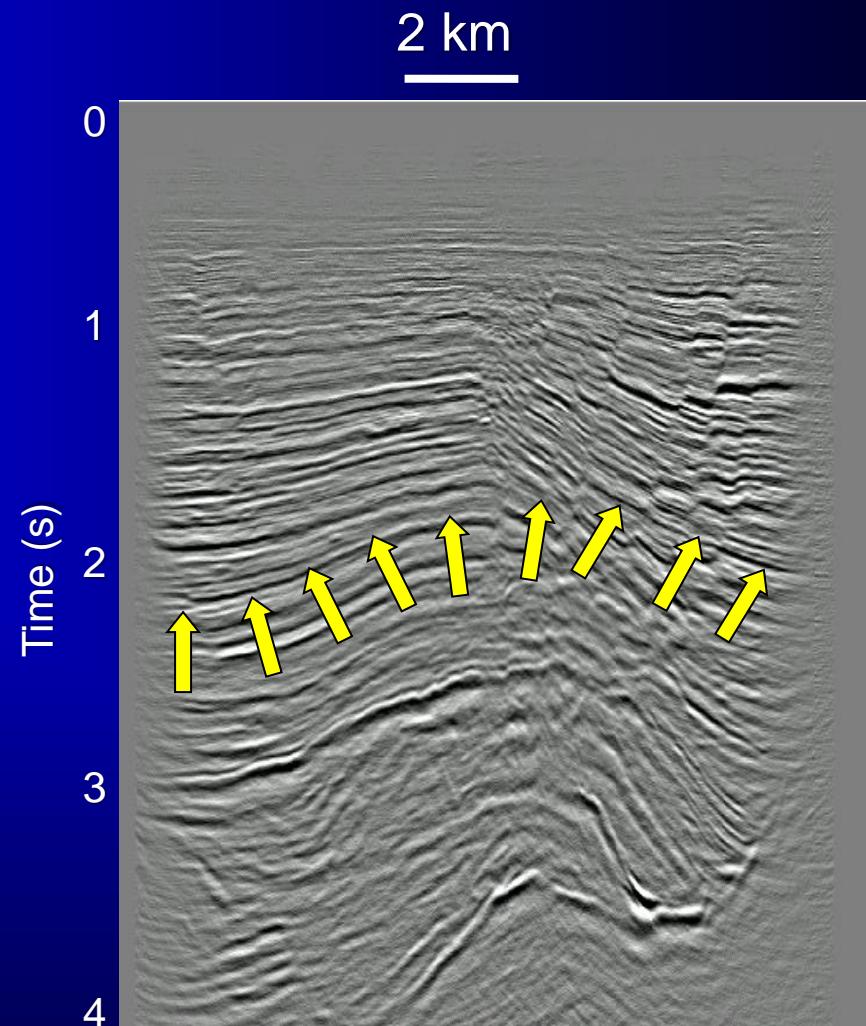
$$\bar{\psi} = \text{ATAN2}\left(\frac{\bar{k}_y}{\bar{\omega}}, \frac{\bar{k}_x}{\bar{\omega}}\right)$$



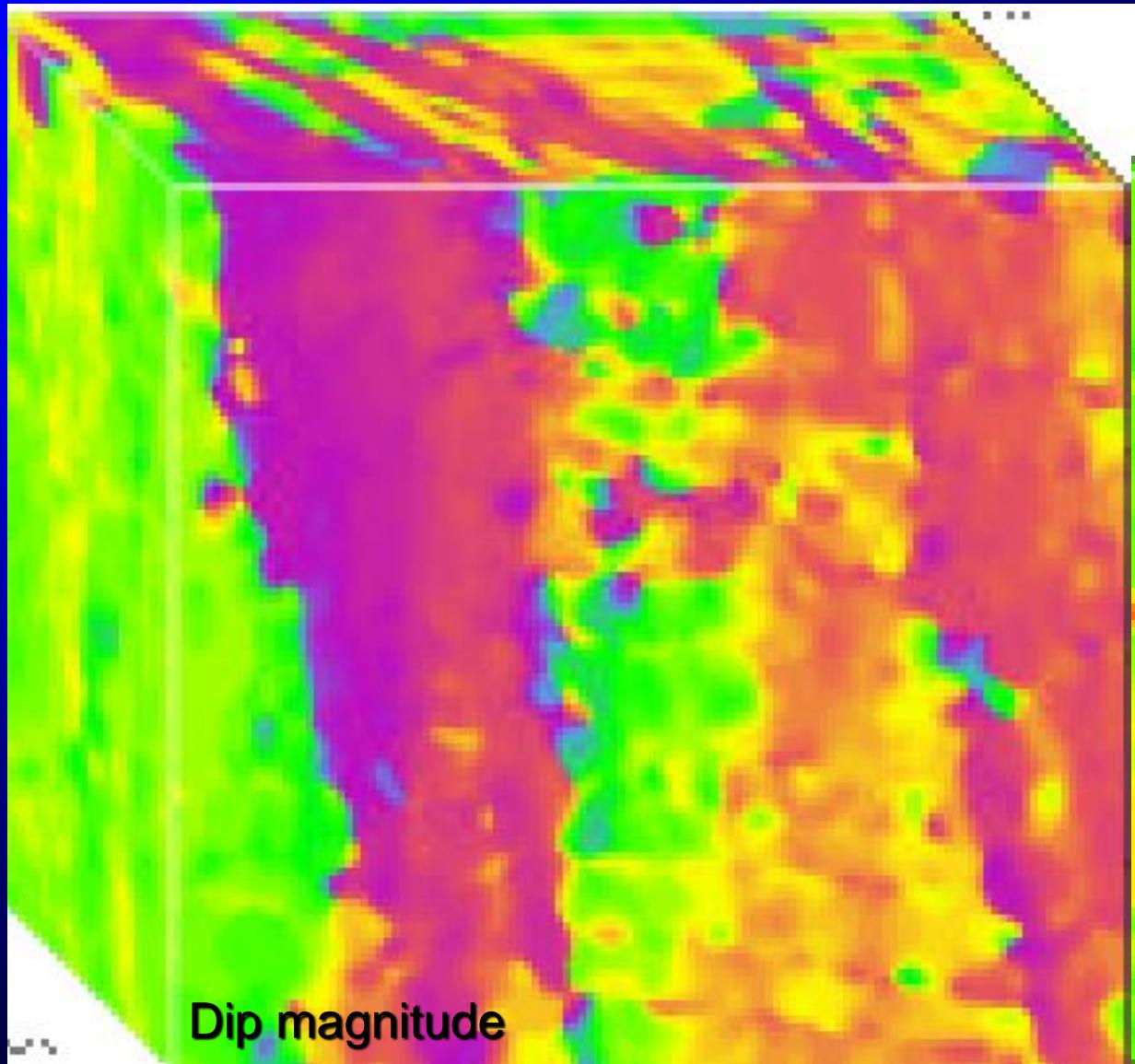
2. Gradient Structure Tensor (GST)

$$\mathbf{T}_{GS} = \begin{bmatrix} \left\langle \frac{\partial u}{\partial x}, \frac{\partial u}{\partial x} \right\rangle & \left\langle \frac{\partial u}{\partial y}, \frac{\partial u}{\partial x} \right\rangle & \left\langle \frac{\partial u}{\partial z}, \frac{\partial u}{\partial x} \right\rangle \\ \left\langle \frac{\partial u}{\partial x}, \frac{\partial u}{\partial y} \right\rangle & \left\langle \frac{\partial u}{\partial y}, \frac{\partial u}{\partial y} \right\rangle & \left\langle \frac{\partial u}{\partial z}, \frac{\partial u}{\partial y} \right\rangle \\ \left\langle \frac{\partial u}{\partial x}, \frac{\partial u}{\partial z} \right\rangle & \left\langle \frac{\partial u}{\partial y}, \frac{\partial u}{\partial z} \right\rangle & \left\langle \frac{\partial u}{\partial z}, \frac{\partial u}{\partial z} \right\rangle \end{bmatrix}$$

The eigenvector of the \mathbf{T}_{GS} matrix points in the direction of the maximum amplitude gradient



2. Gradient Structure Tensor (GST)



(Randen et al., 2008)



3. Plane-wave destructor

Predict a trace s_j , from a neighboring trace along an unknown inline dip, p :

$$s_j(t) \approx s_{j-1}(t + px) \equiv P_{j,j-1}^{(x)}(p)s_{j-1}(t)$$

Minimize the squared error, ε^2 , along the inline dip direction, p :

$$\|\boldsymbol{\varepsilon}\|^2 \equiv \sum_{j=2}^J \|s_j - s_{j-1}(t + px)\|^2 = \|\mathbf{D}\mathbf{s}\|^2$$

$$\mathbf{D} = \begin{bmatrix} \mathbf{I} & 0 & 0 & \dots & 0 \\ -\mathbf{P}_{1,2} & \mathbf{I} & 0 & \dots & 0 \\ 0 & -\mathbf{P}_{2,3} & \mathbf{I} & \dots & 0 \\ \dots & \dots & \dots & \dots & \dots \\ 0 & 0 & \dots & -\mathbf{P}_{N-1,N} & \mathbf{I} \end{bmatrix}$$



3. Plane-wave destructor (using Marfurt's inelegant math)

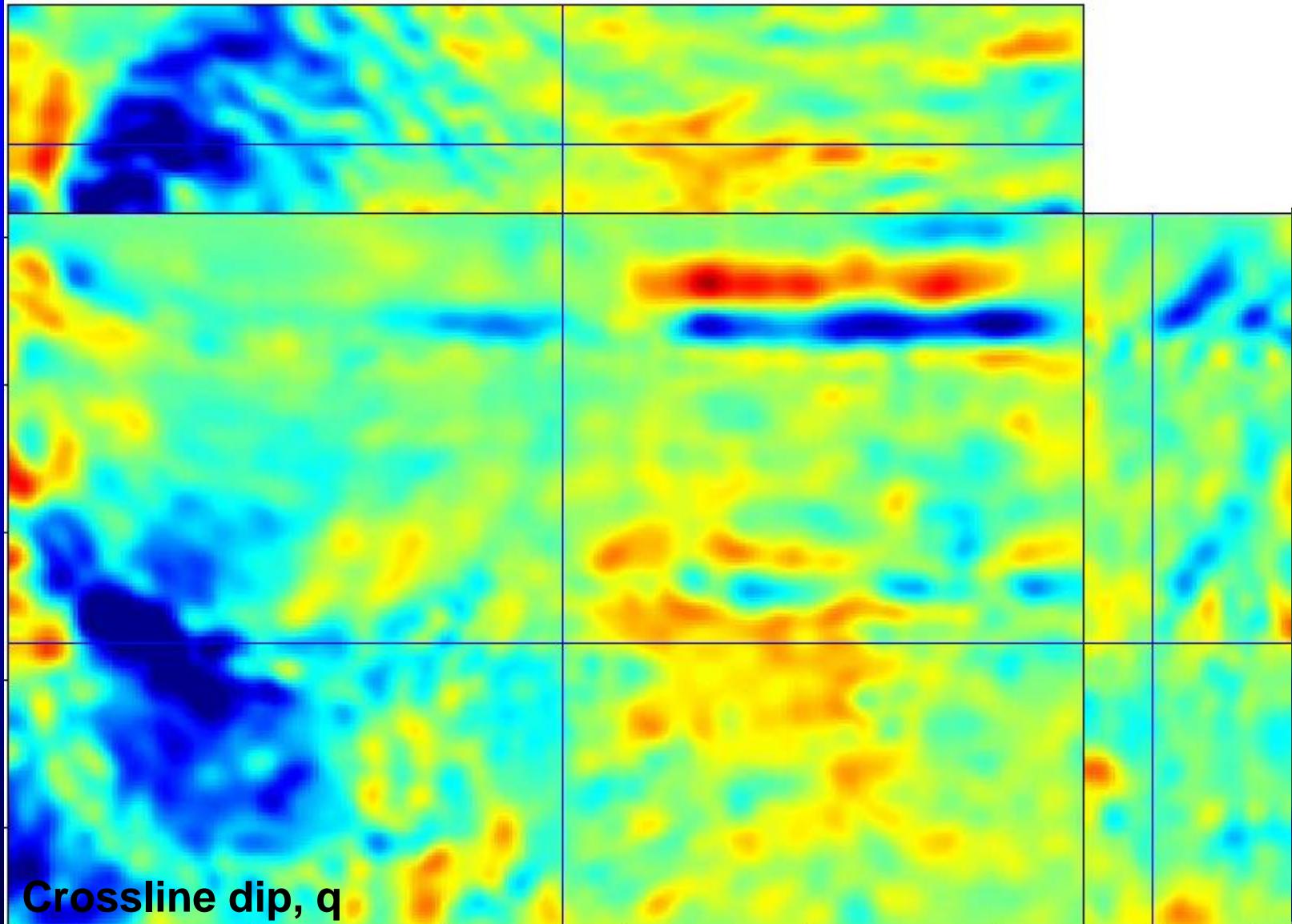
1. Predict (interpolate) the adjacent trace at unknown sample $t+px$ using a simple 3-point parabola

$$\begin{aligned}s_j(t + px) &\approx s_{j-1}(t) \\ &+ \frac{s_{j-1}(t + \Delta t) - s_{j-1}(t - \Delta t)}{2\Delta t} (px) \\ &+ \frac{s_{j-1}(t + \Delta t) - 2s_{j-1}(t) + s_{j-1}(t - \Delta t)}{(\Delta t)^2} (px)^2\end{aligned}$$

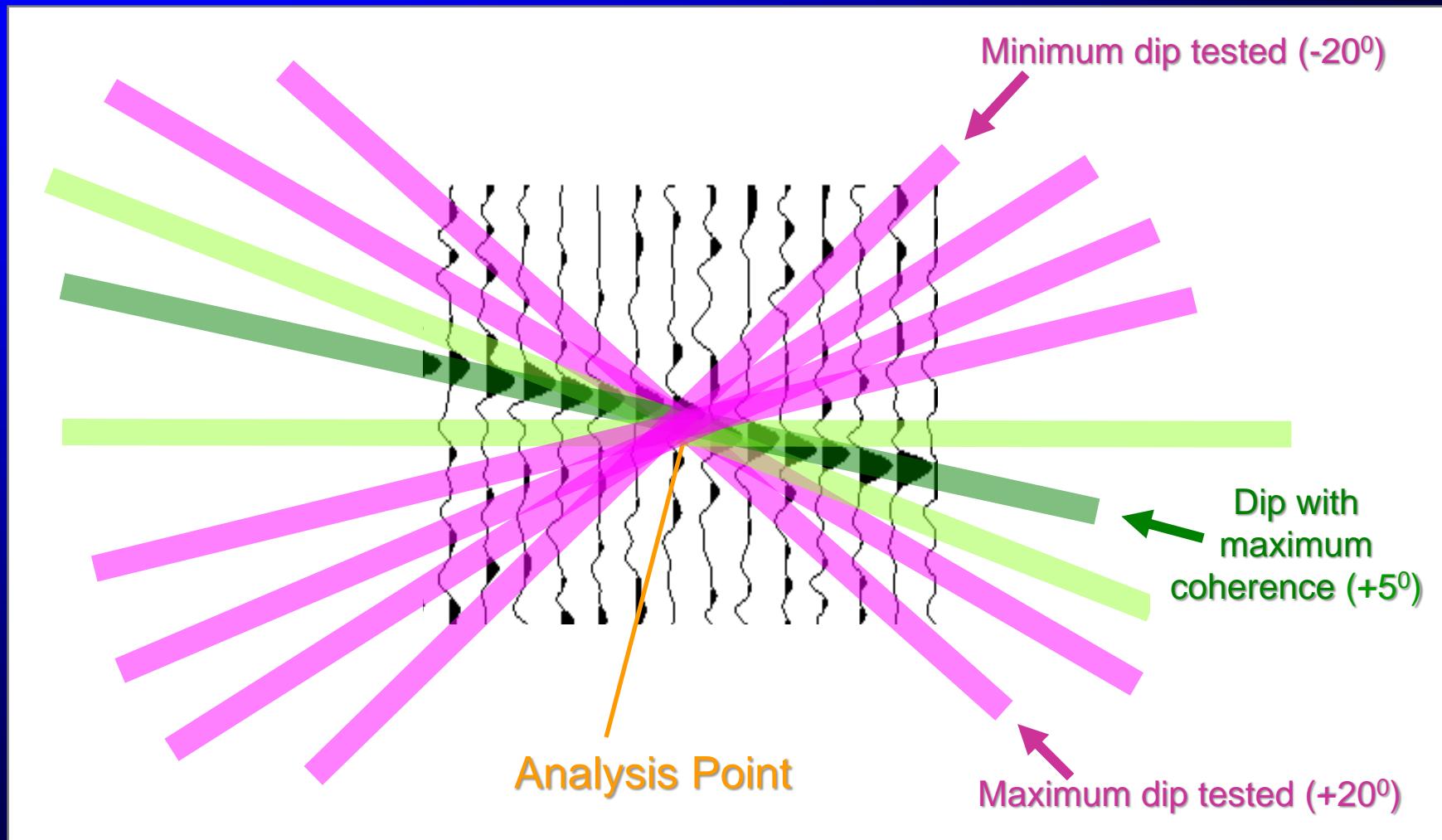
2. Minimize the predicted error by minimizing the objective function with respect to p .



3. Plane-wave destructor



4. Discrete scans for dip of most coherent reflector

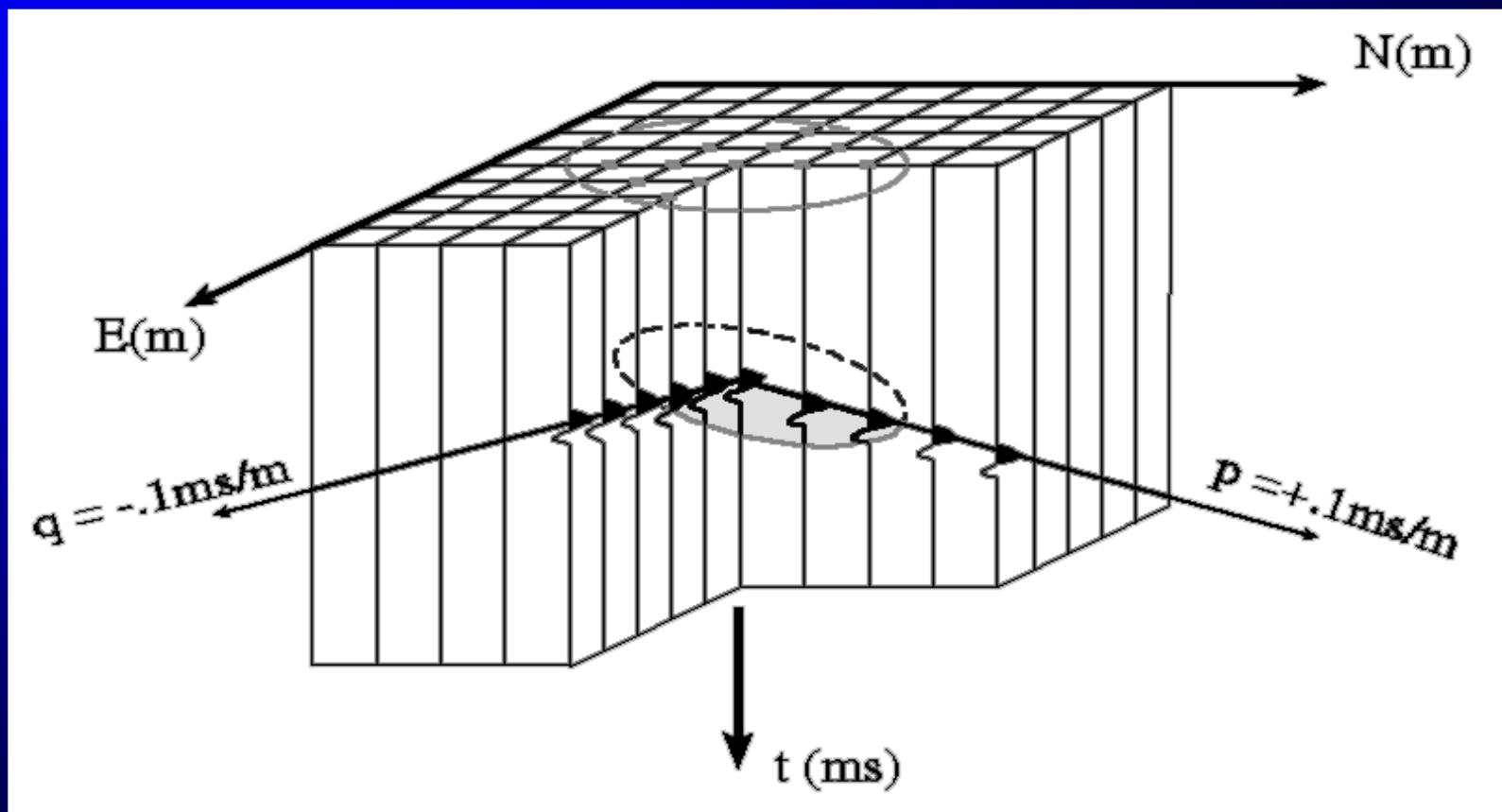


Instantaneous dip = dip with highest coherence

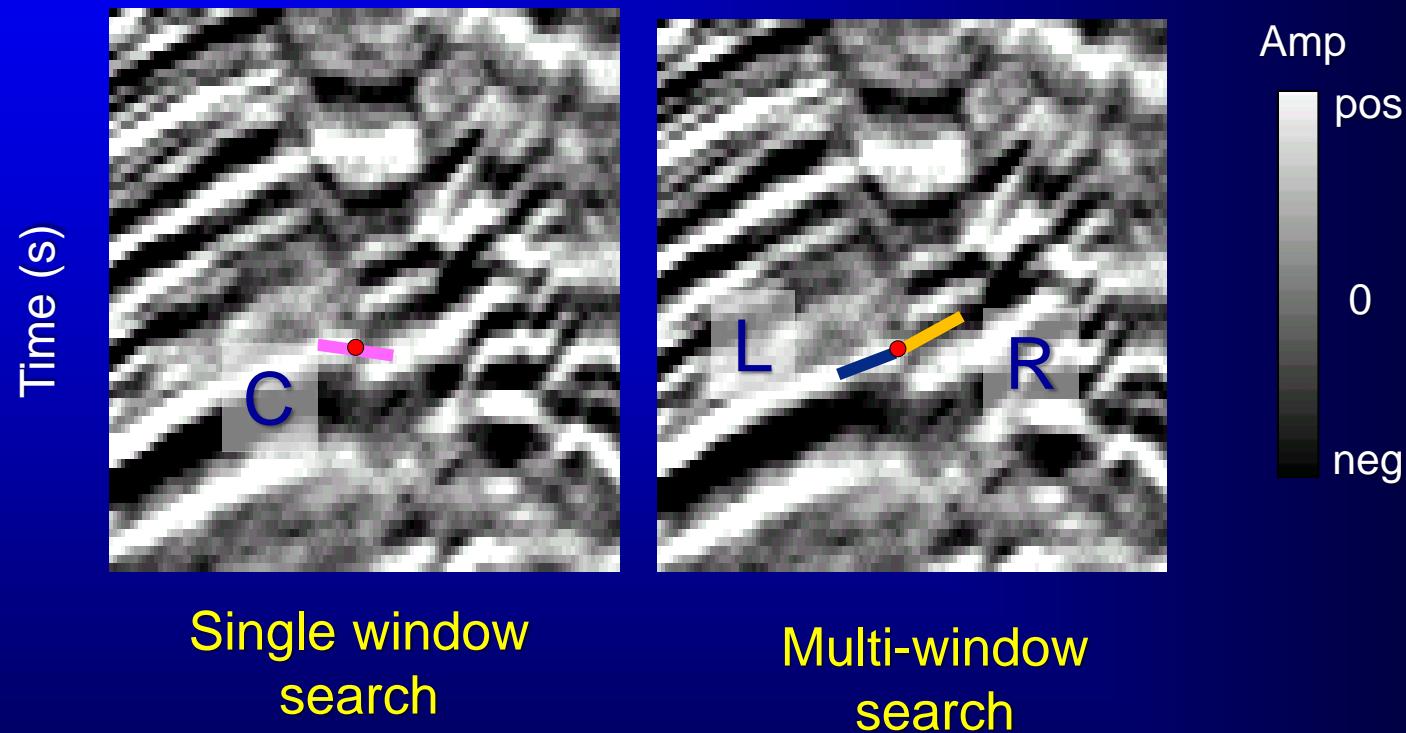


(Marfurt et al, 1998)

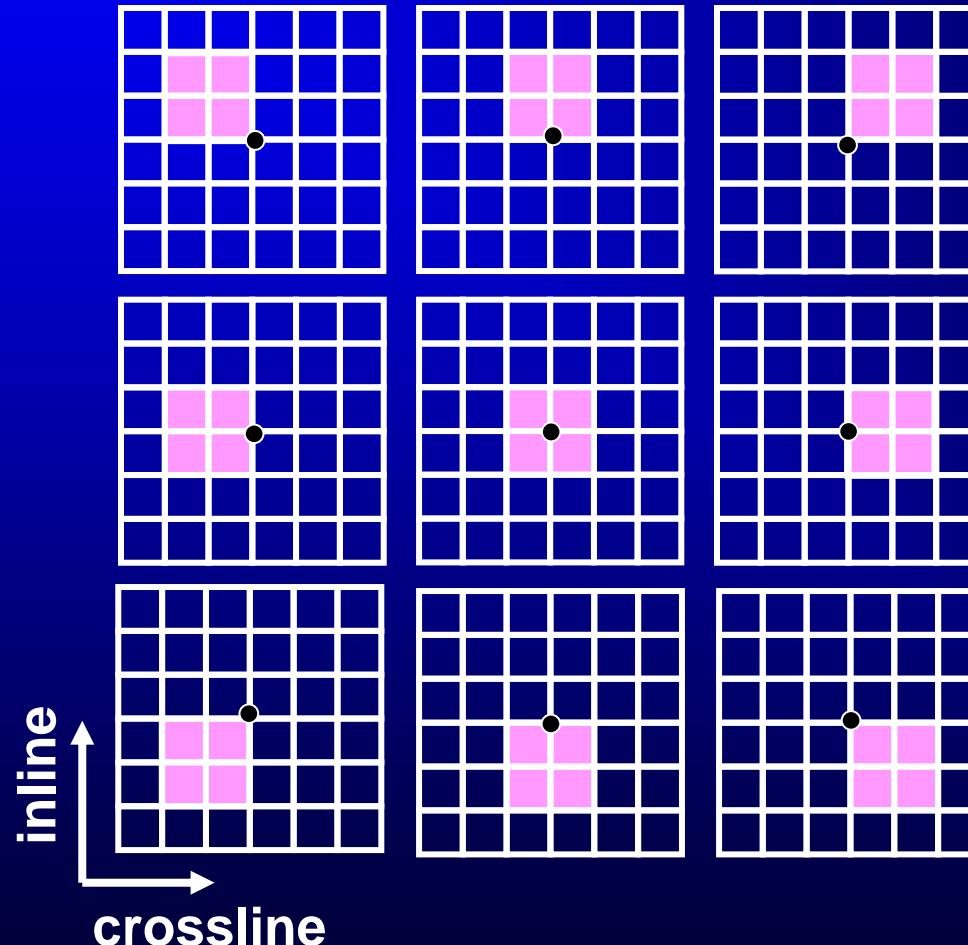
3D estimate of coherence and dip/azimuth



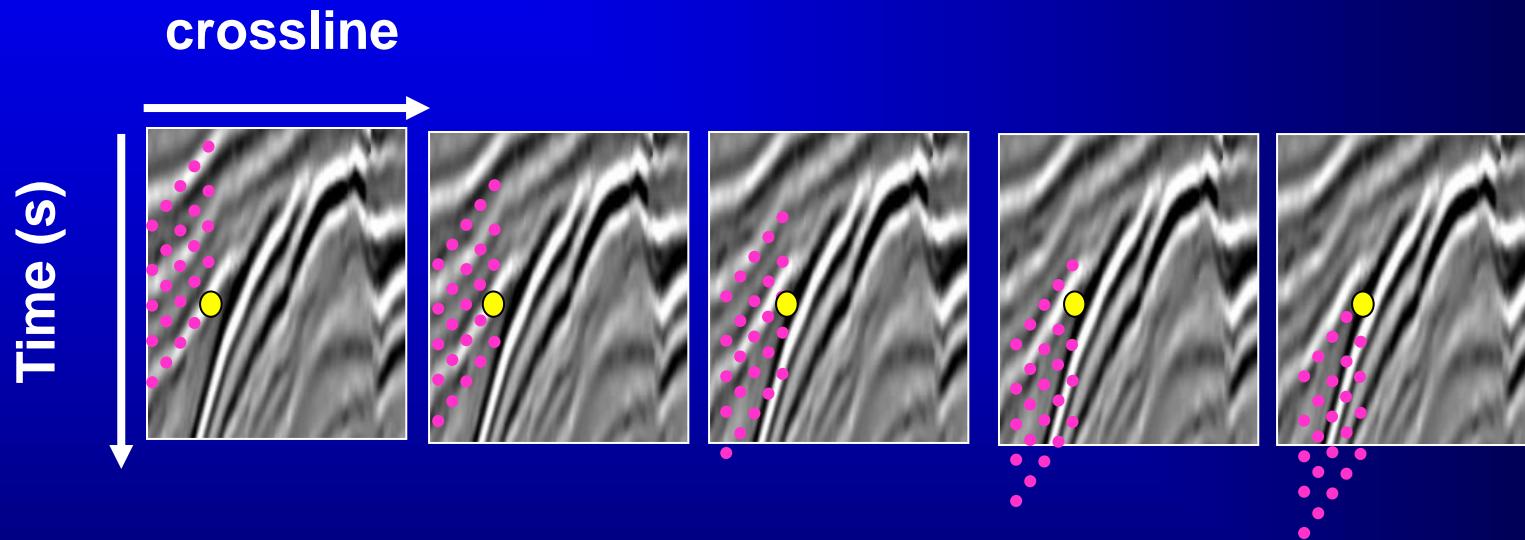
Searching for dip in the presence of faults



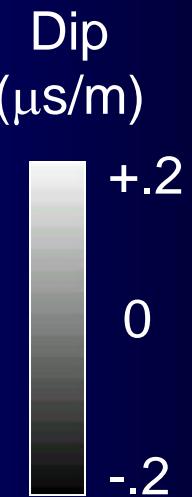
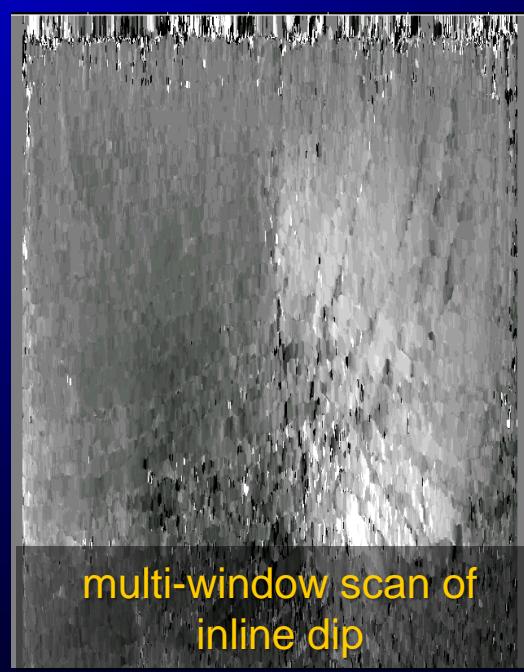
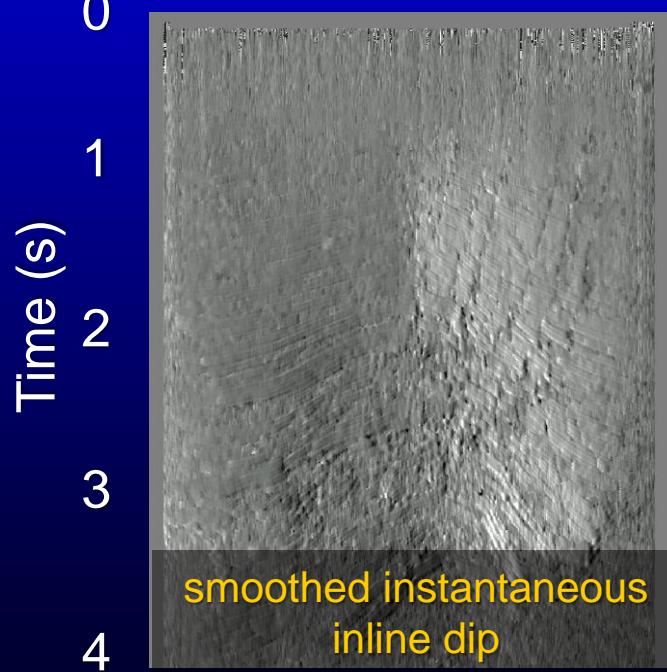
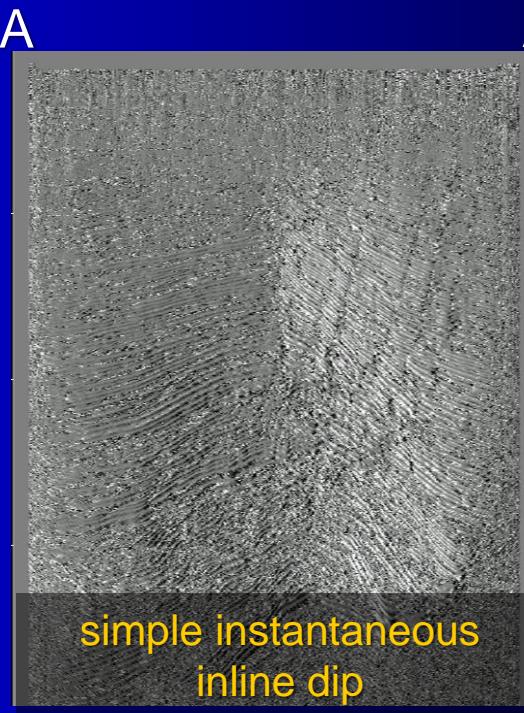
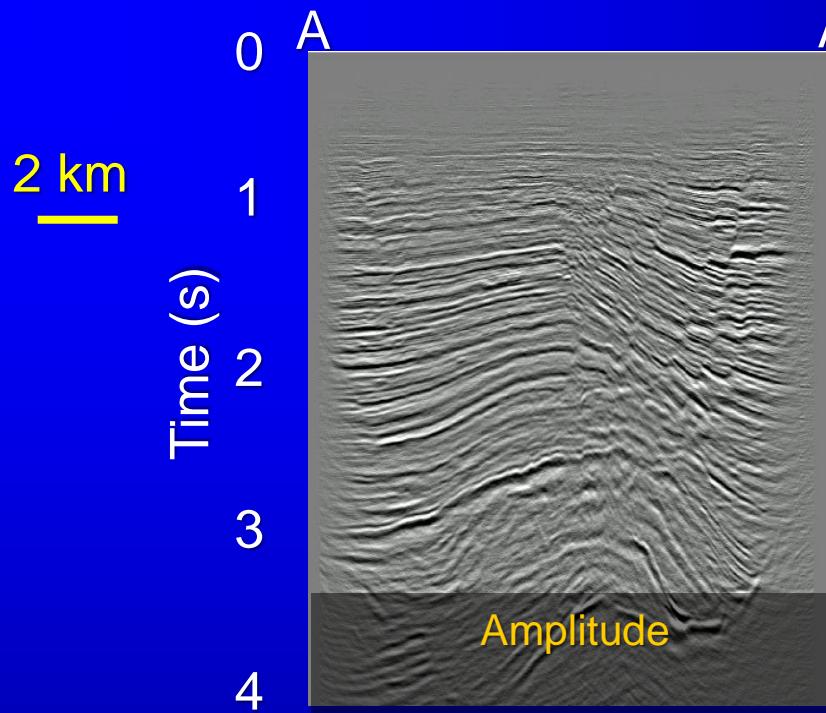
Search for the most coherent window containing the analysis point



Search for the most coherent window containing the analysis point

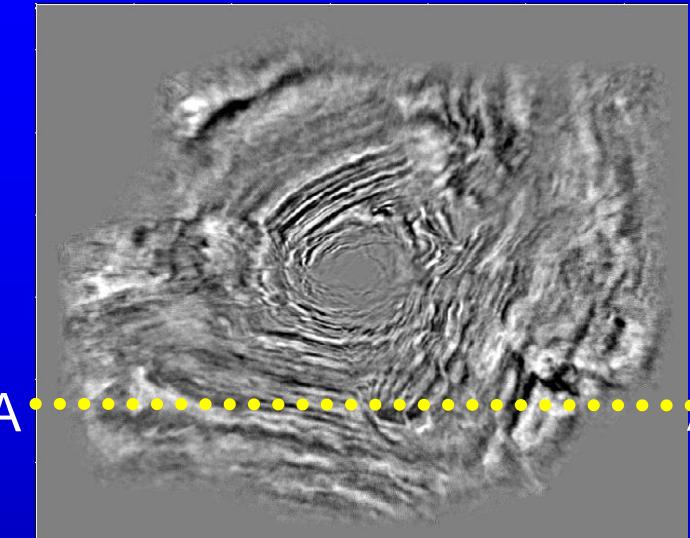


Comparison
of dip
estimates on
vertical slice

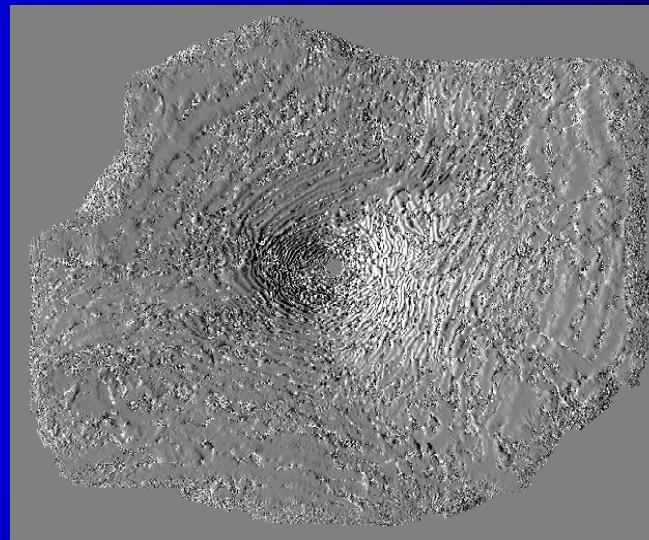


(Marfurt, 2006)

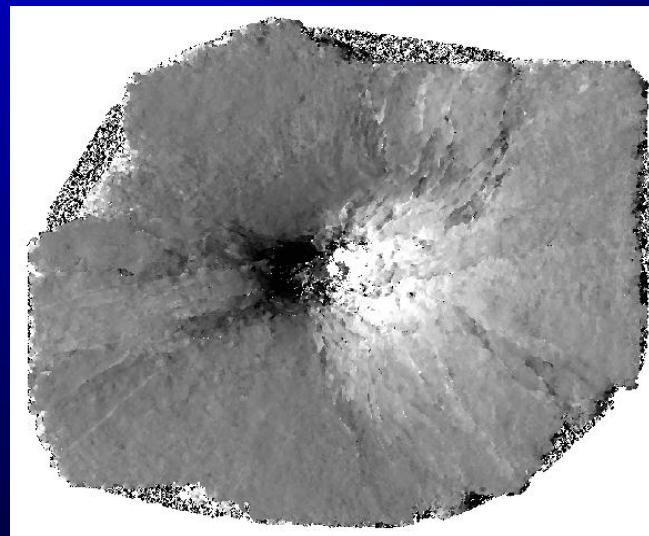
2 km



Amplitude



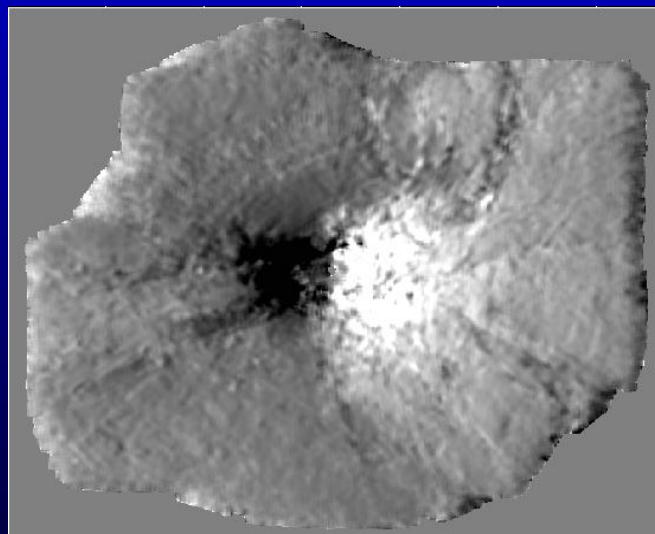
simple instantaneous
inline dip



multi-window scan of
inline dip

Comparison
of dip
estimates on
time slice
($t=1.0$ s)

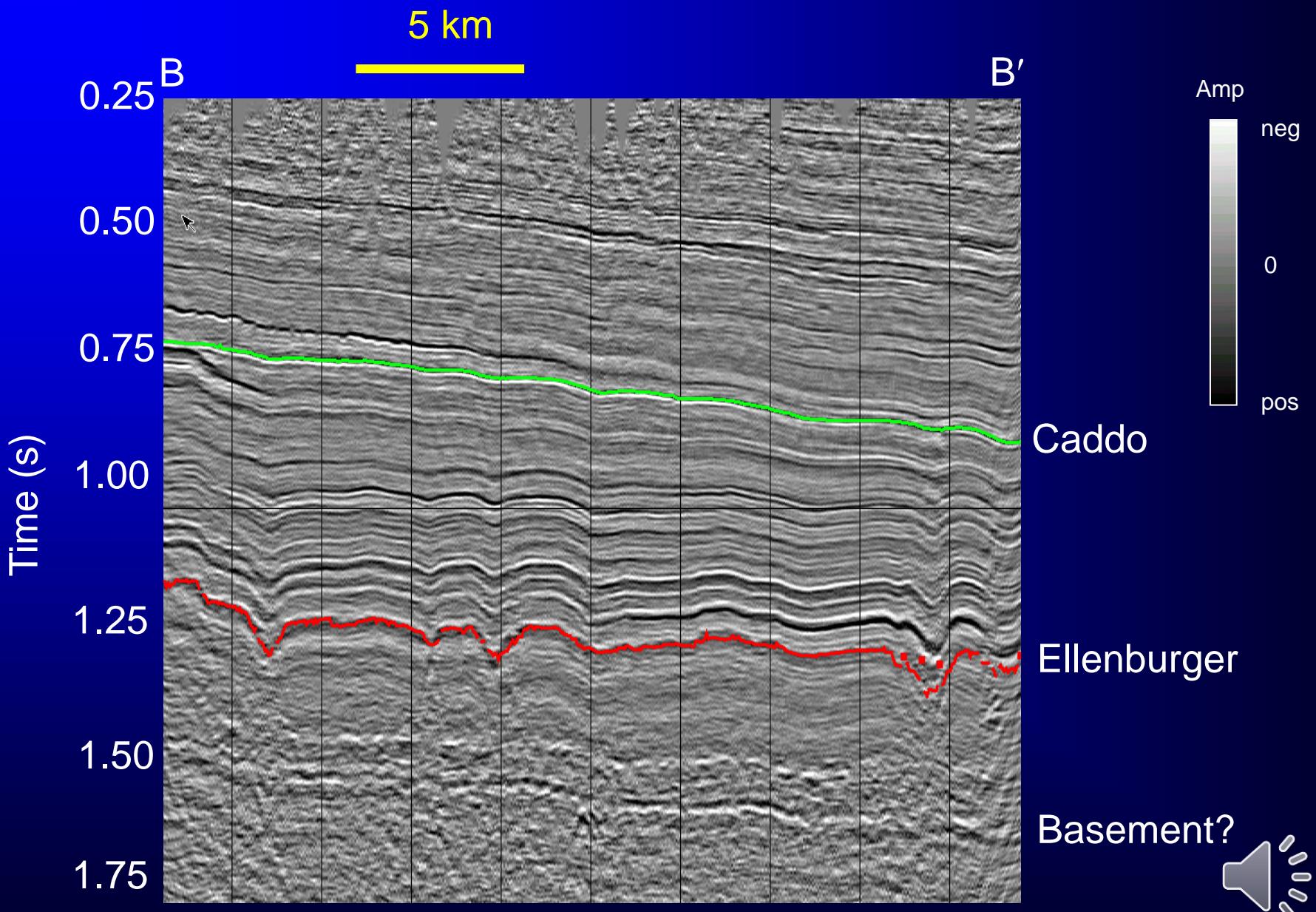
Dip
($\mu\text{s}/\text{m}$)



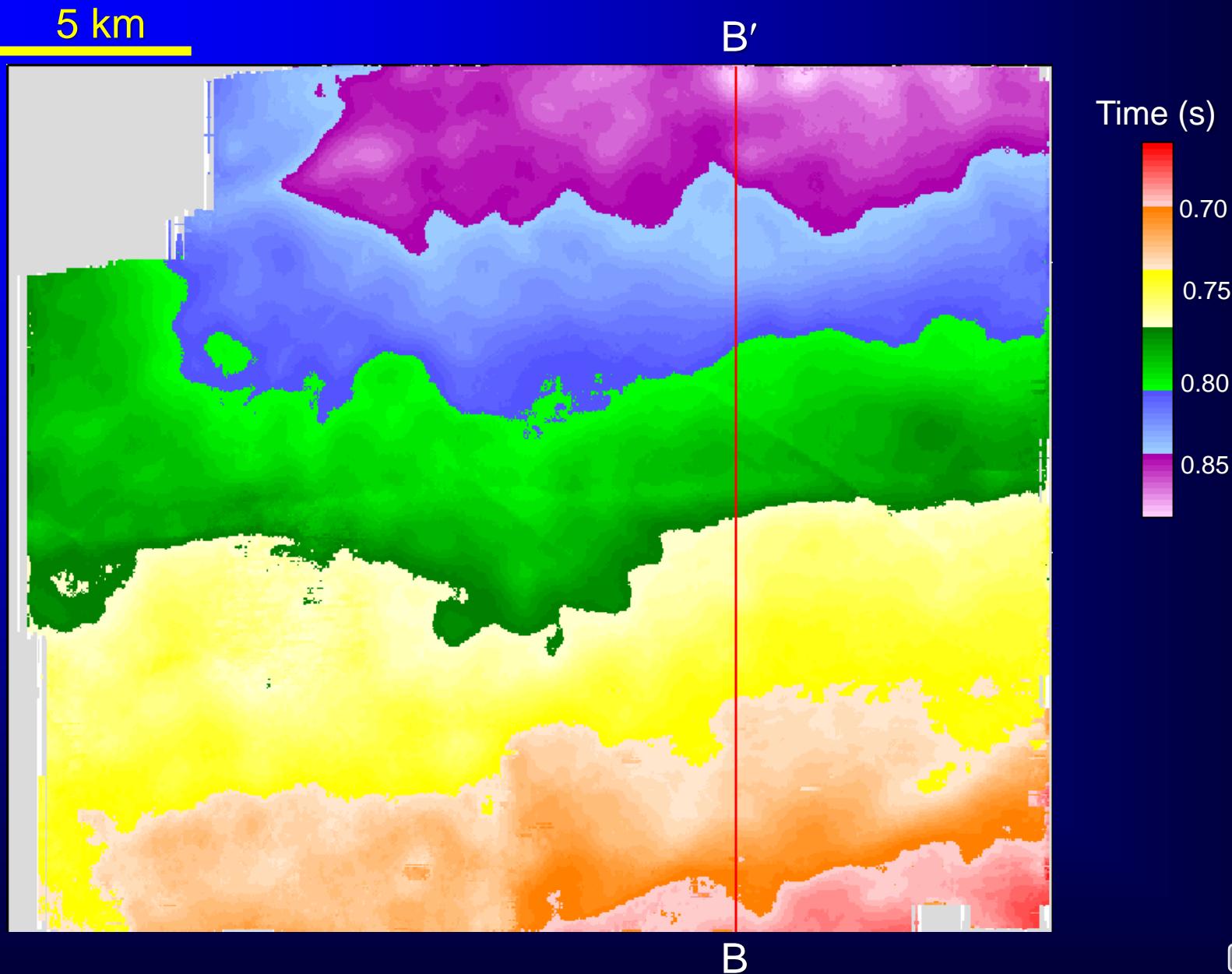
smoothed instantaneous
inline dip



Vertical Slice through Seismic



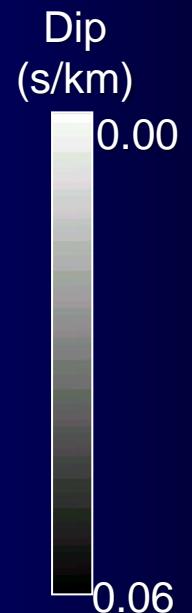
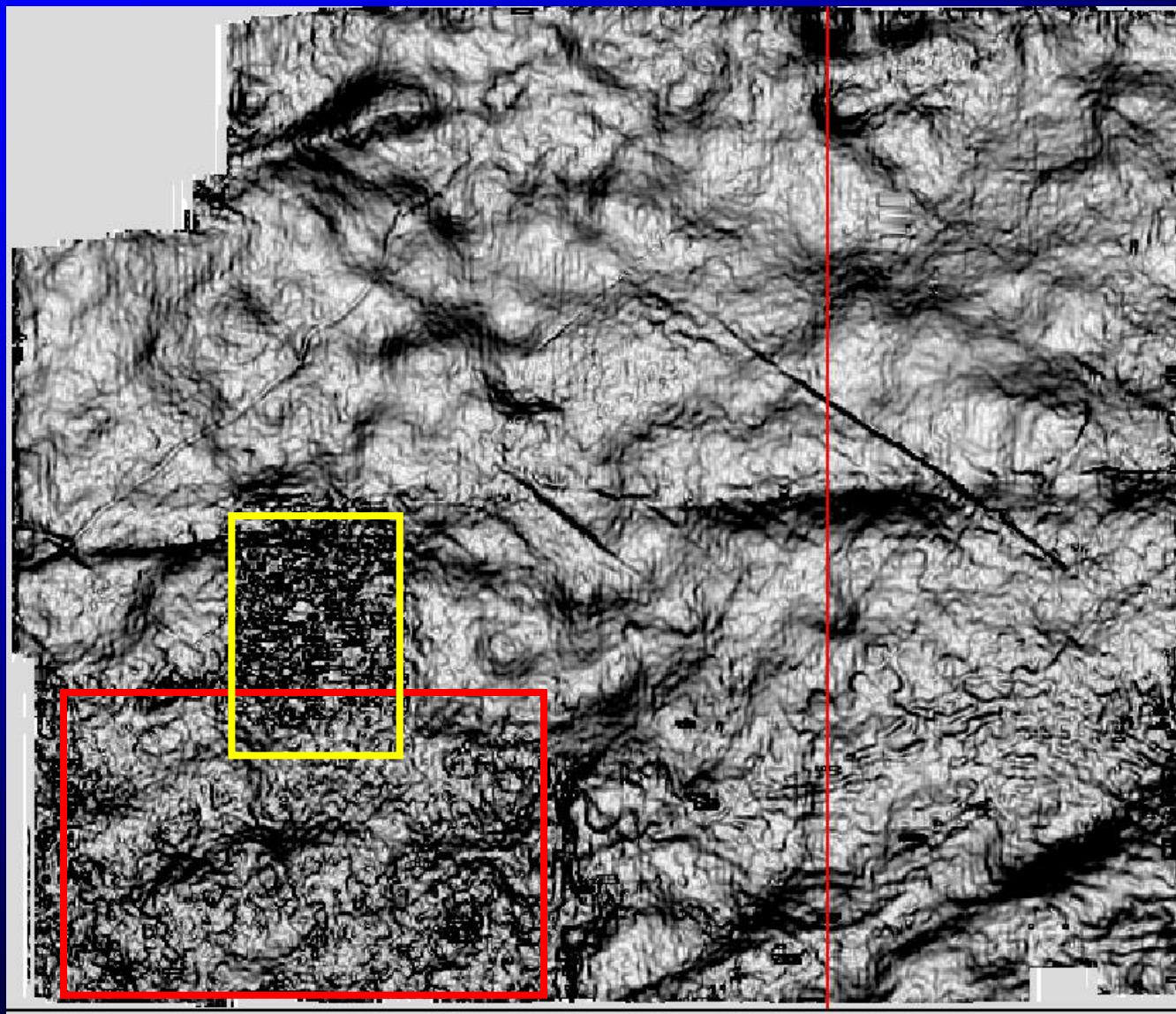
Time/structure of Caddo horizon



Dip magnitude from picked Caddo horizon

5 km

B'



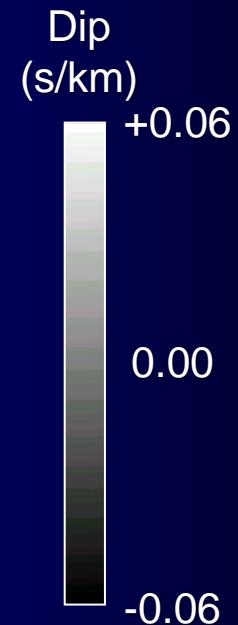
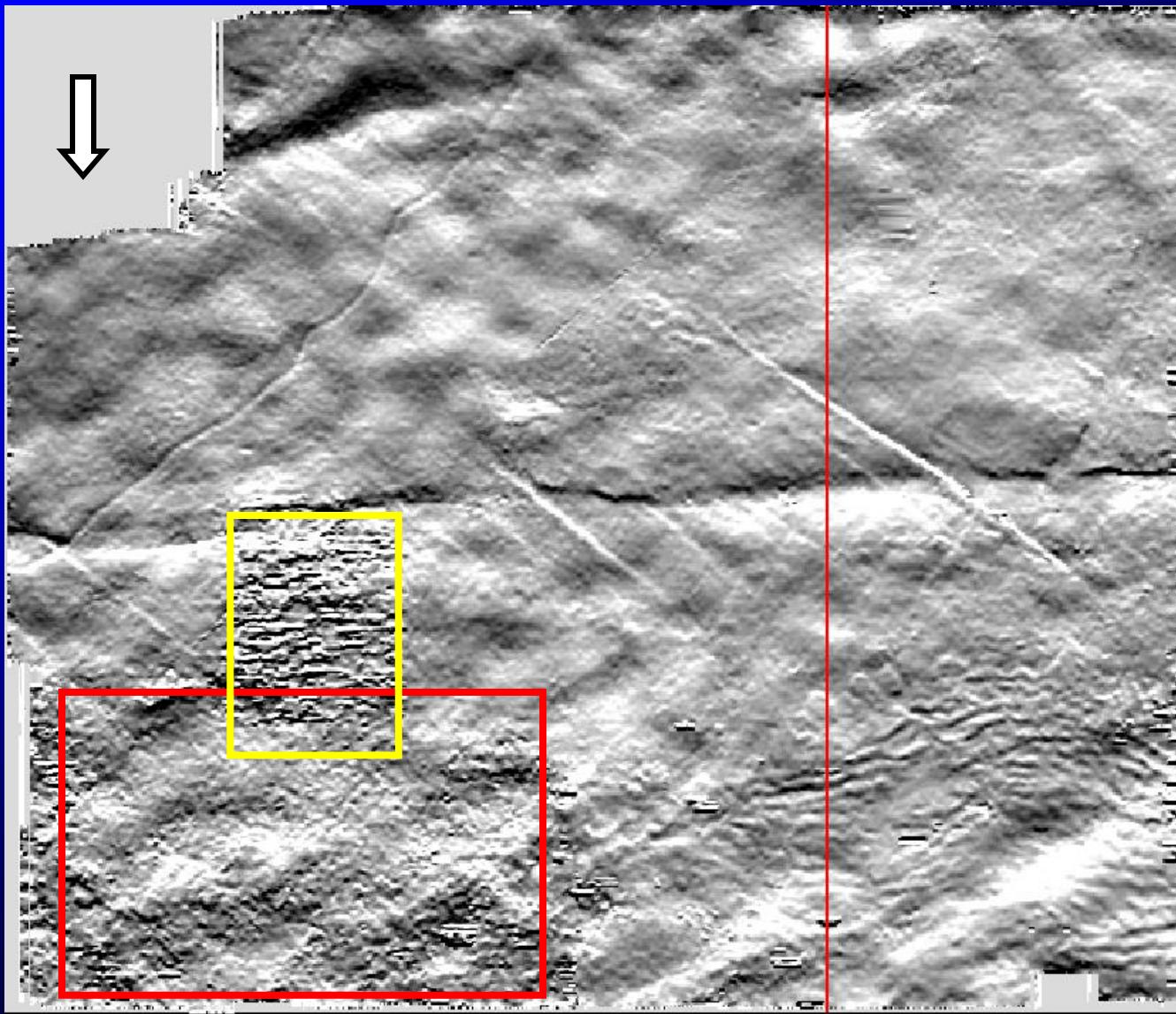
B



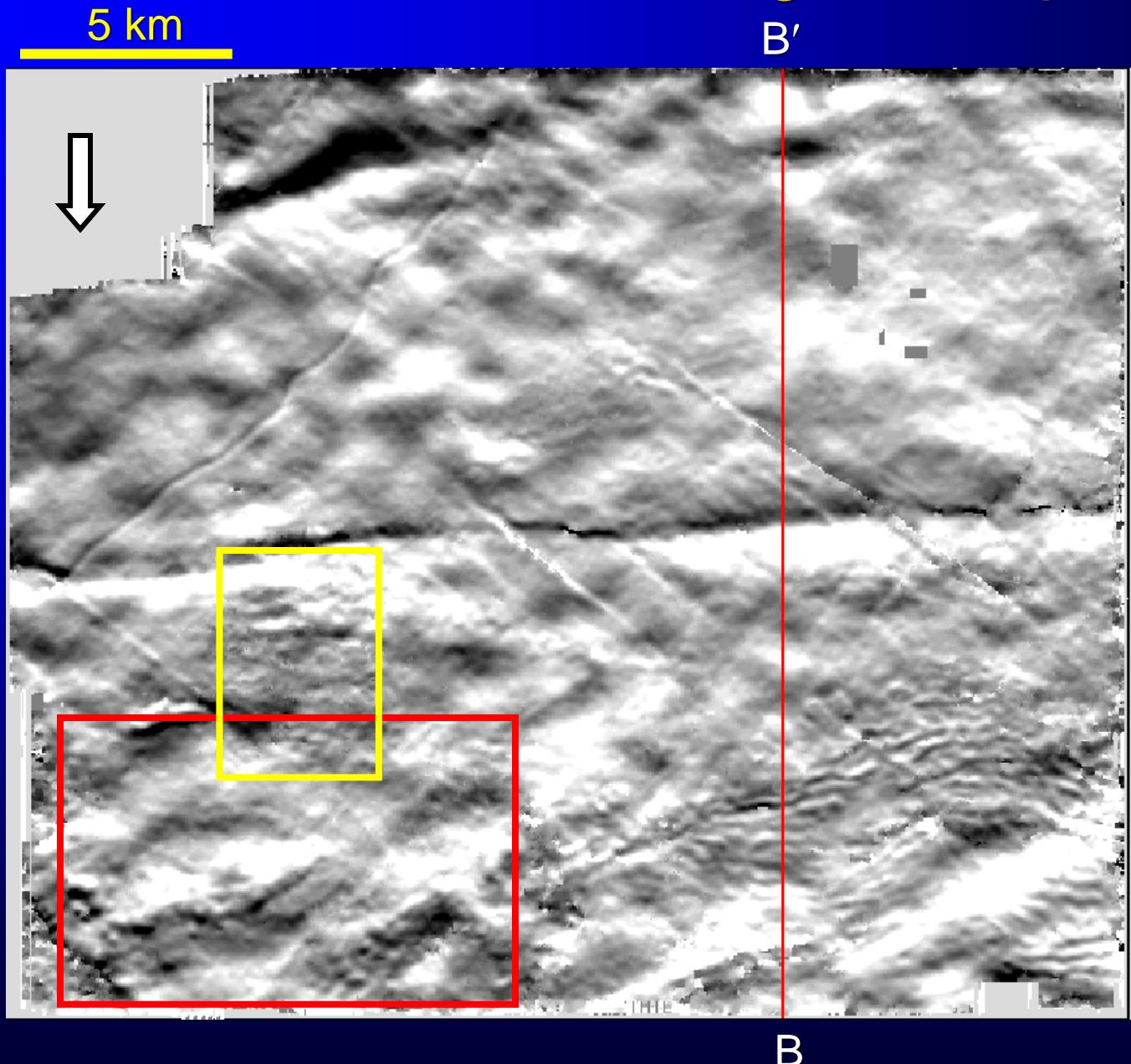
NS dip from picked Caddo horizon

5 km

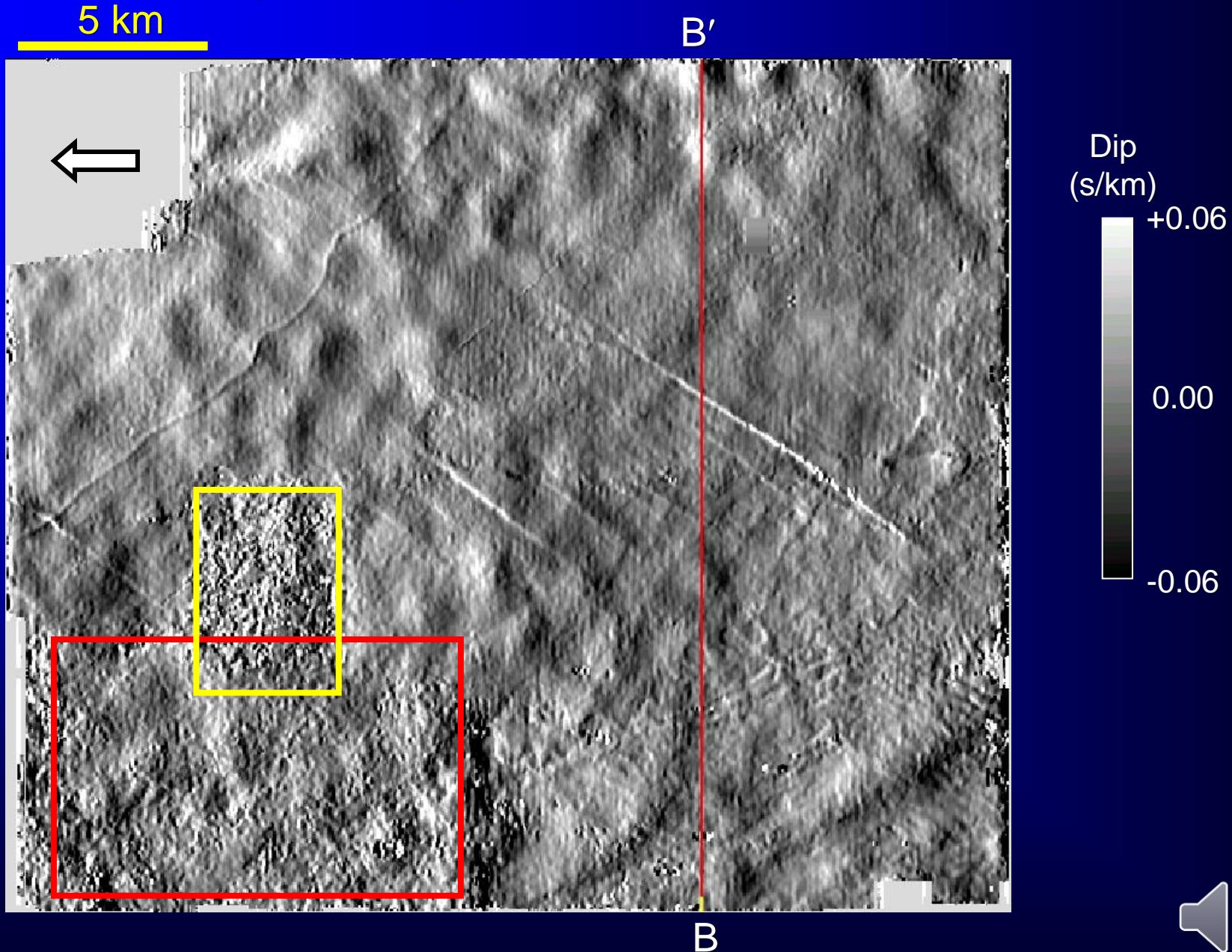
B'



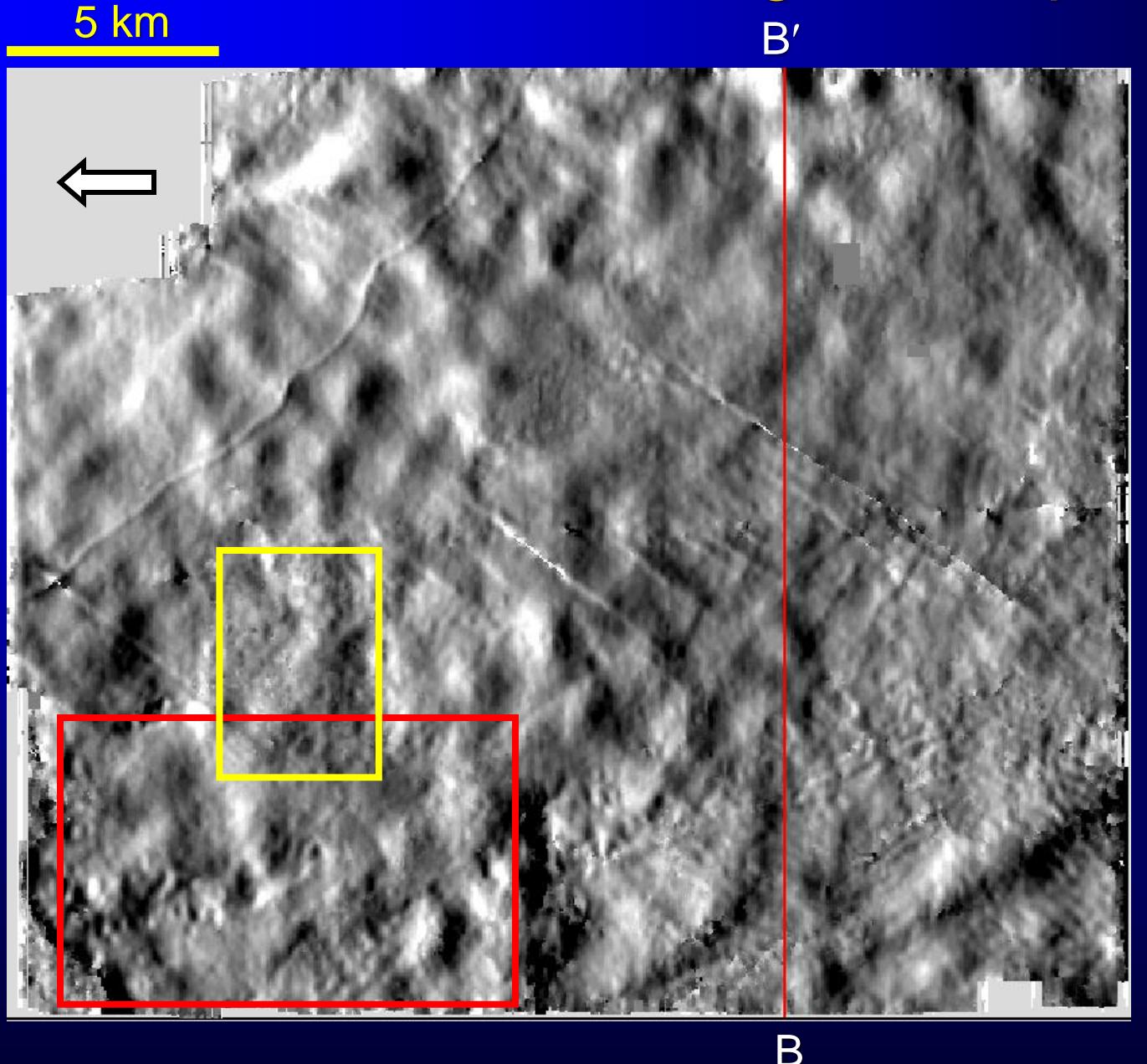
Caddo horizon slice through NS dip volume



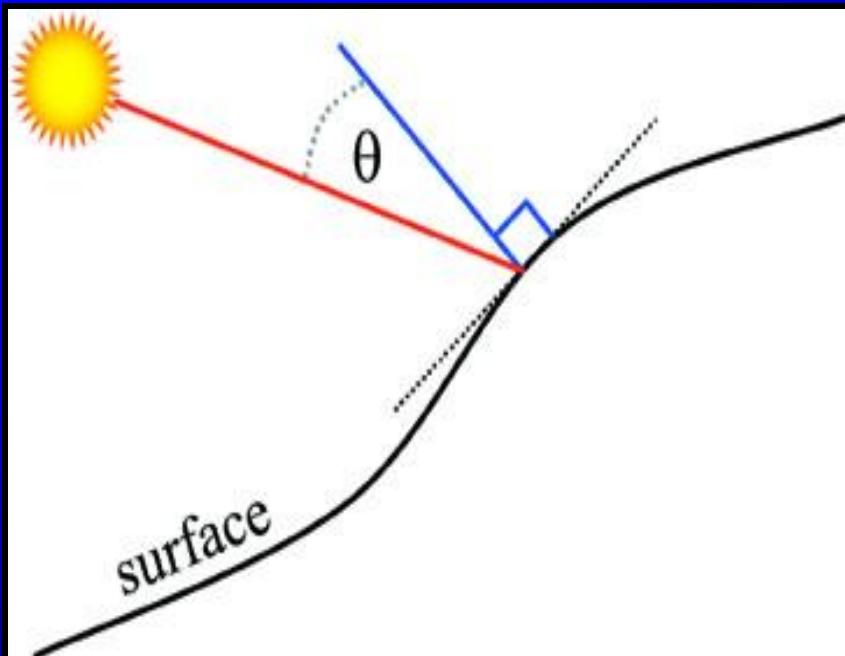
EW dip from picked Caddo horizon



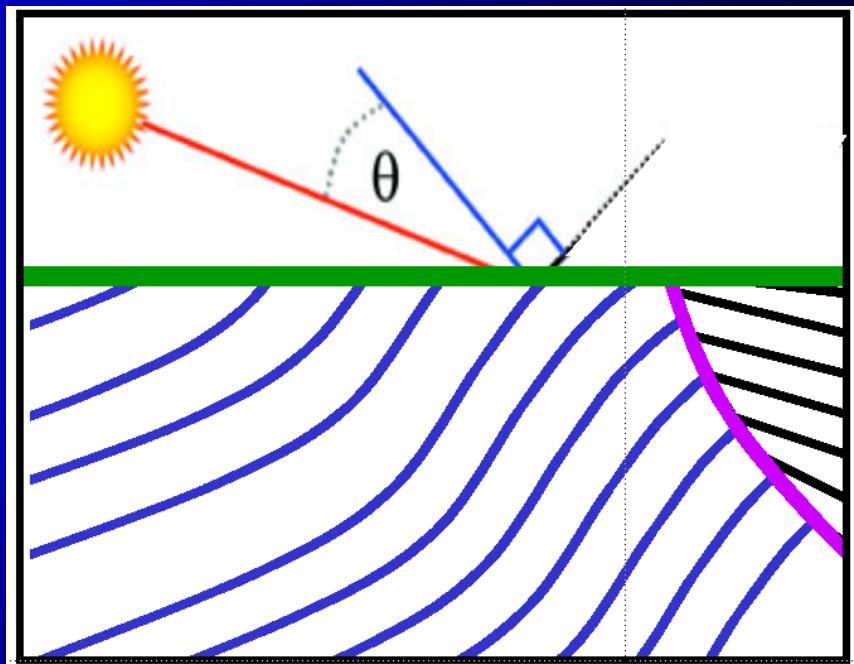
Caddo horizon slice through EW dip volume



Shaded illumination



on a surface

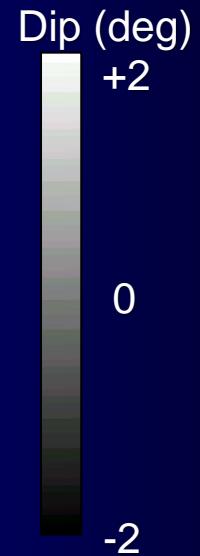
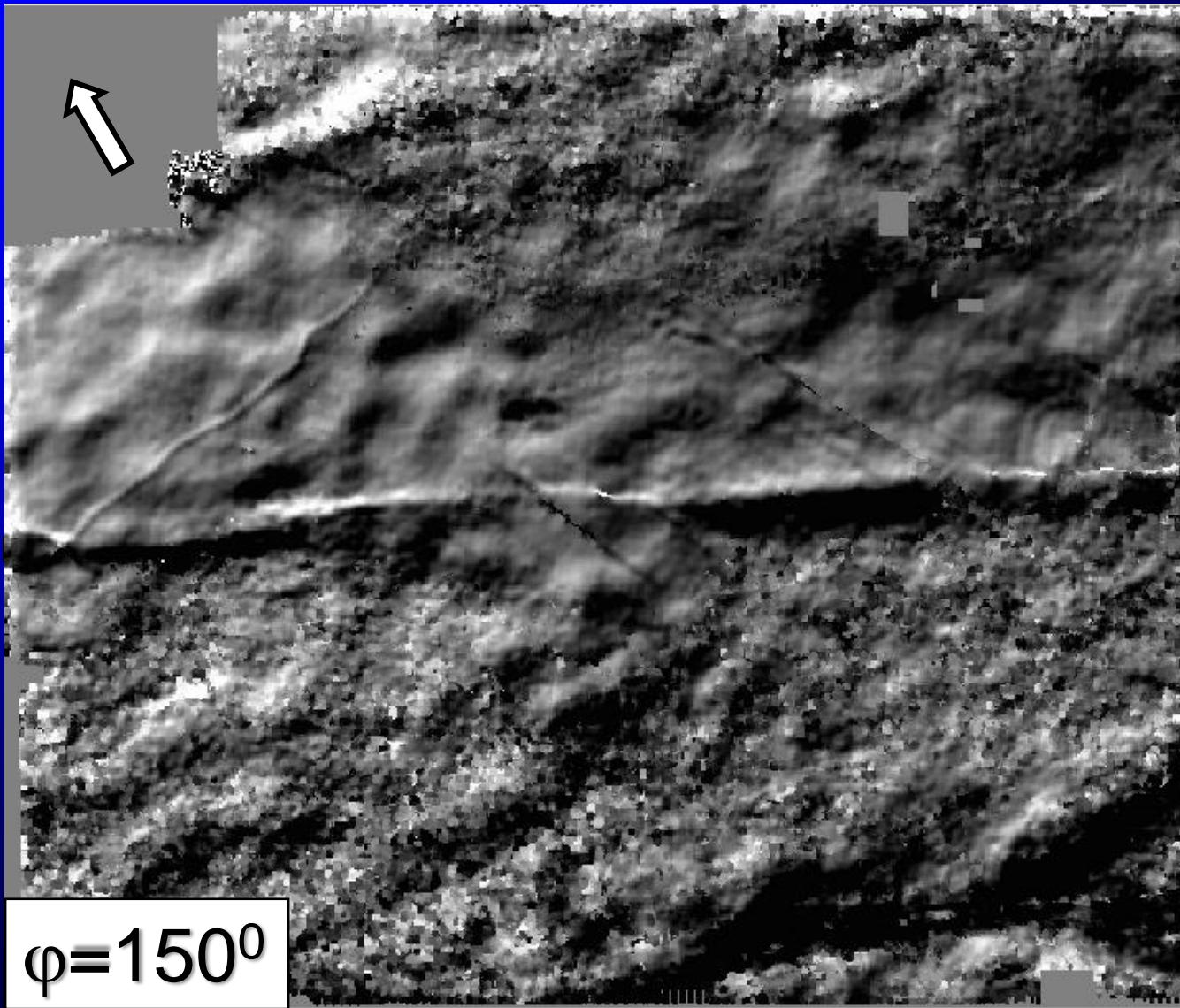


on a time slice through
dip and azimuth volumes



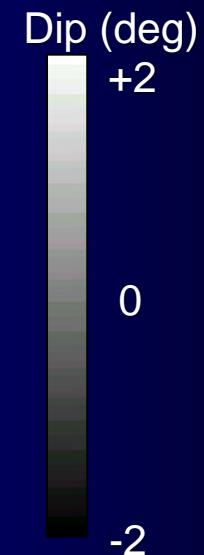
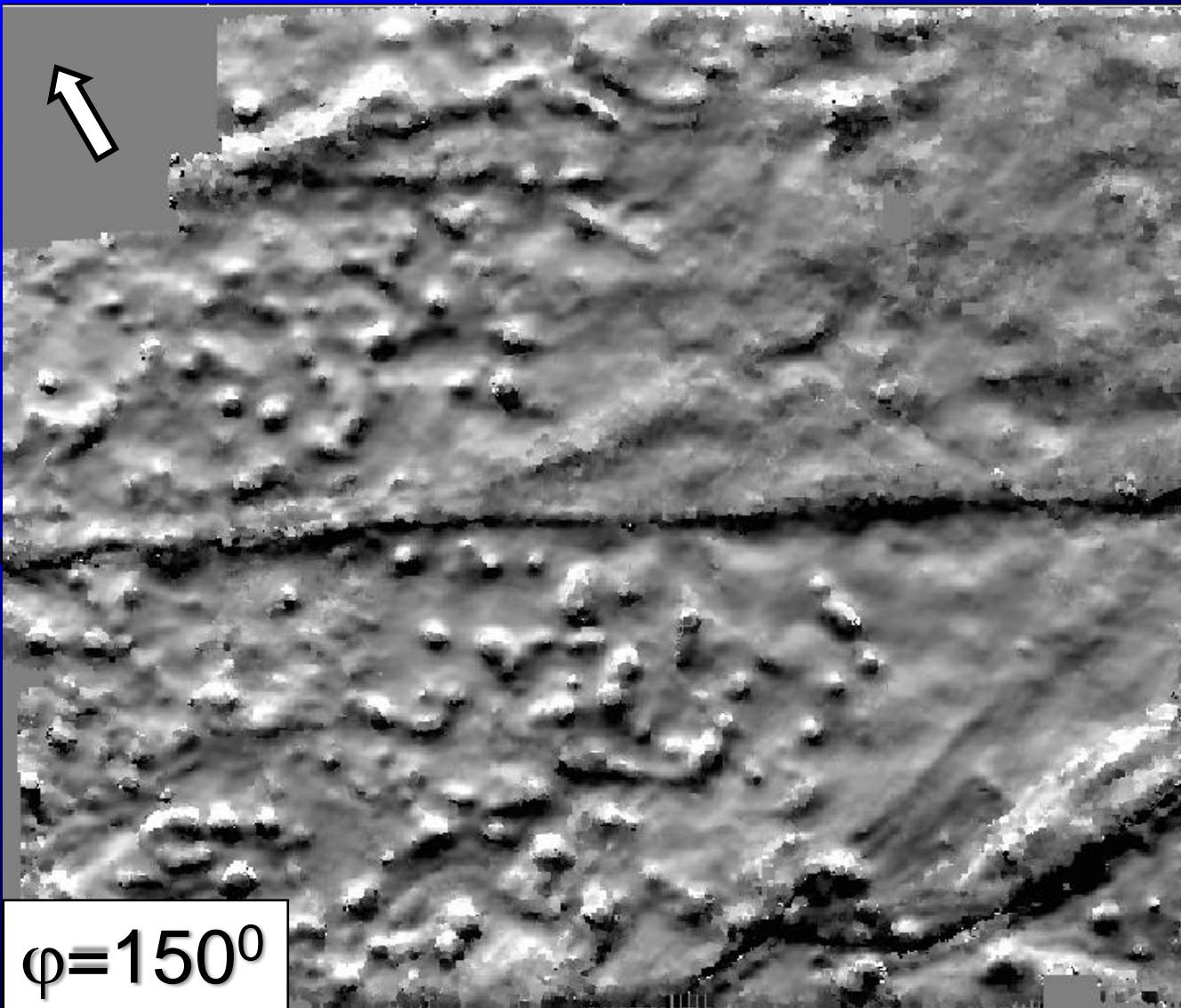
Time slices through apparent dip ($t=0.8$ s)

5 km

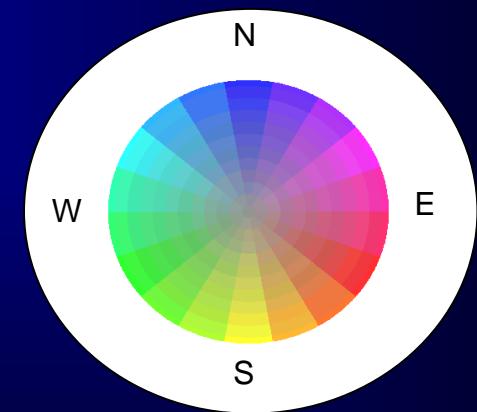
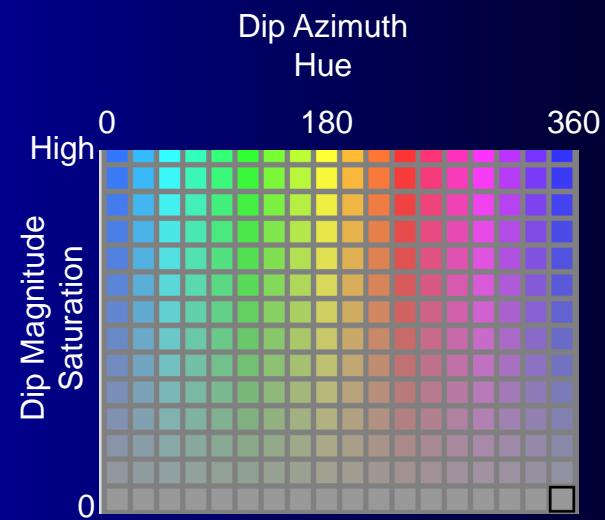
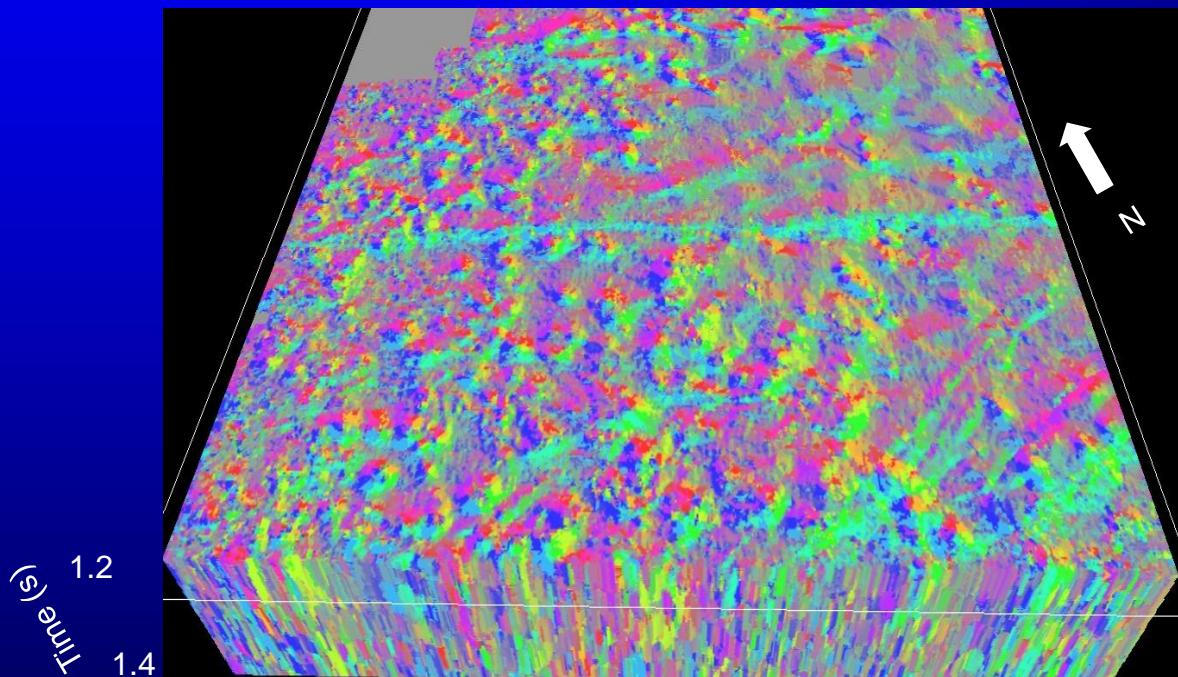


Time slices through apparent dip ($t = 1.2$ s)

5 km



Volumetric visualization of reflector dip and azimuth

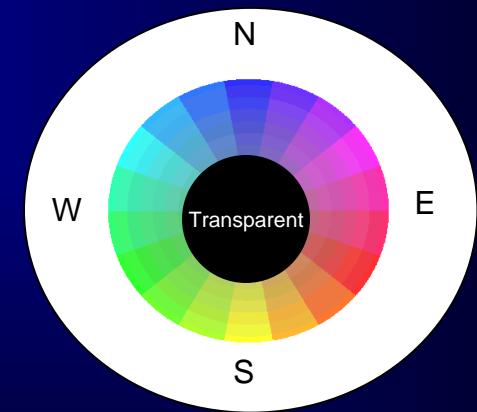
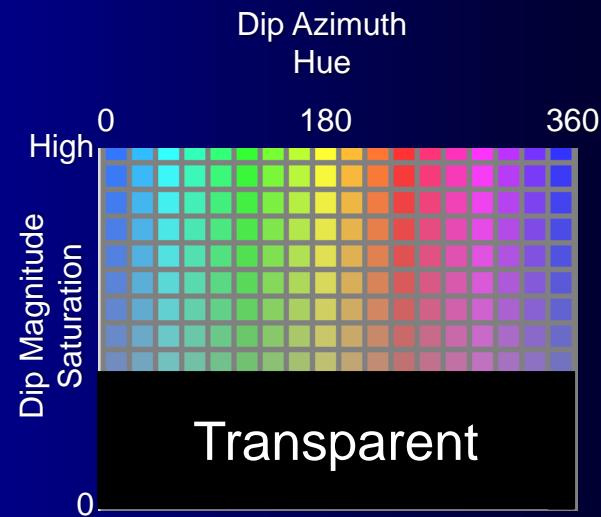
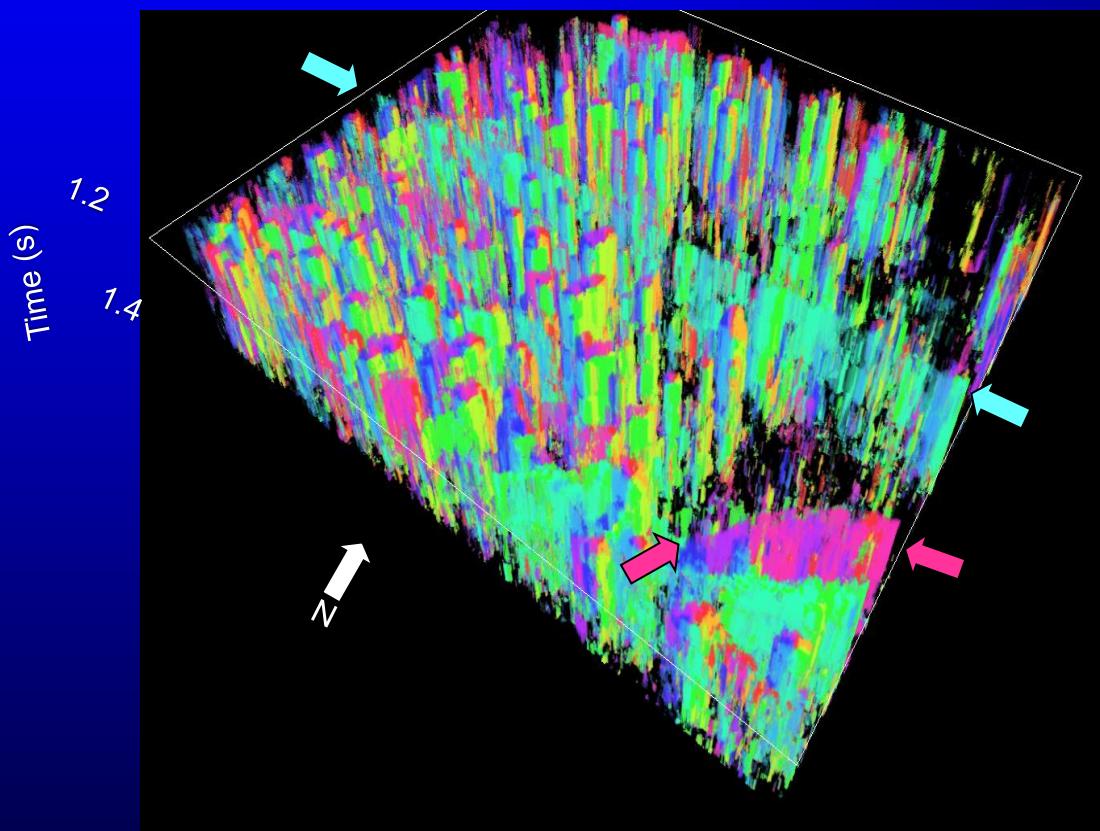


(c)



(Guo et al., 2008)

Volumetric visualization of reflector dip and azimuth



(c)



(Guo et al., 2008)

Volumetric Dip and Azimuth

In Summary:

- Dip and azimuth estimated using a vertical window in general provide more robust estimates than those based on picked horizons
- Dip and azimuth volumes form the basis for volumetric curvature, coherence, amplitude gradients, seismic textures, and structurally-oriented filtering
- Dip and azimuth are the key components for computer-aided 3D seismic stratigraphy
- Dip and azimuth will suffer from fault shadow and other velocity pull-up and push-down artifacts

