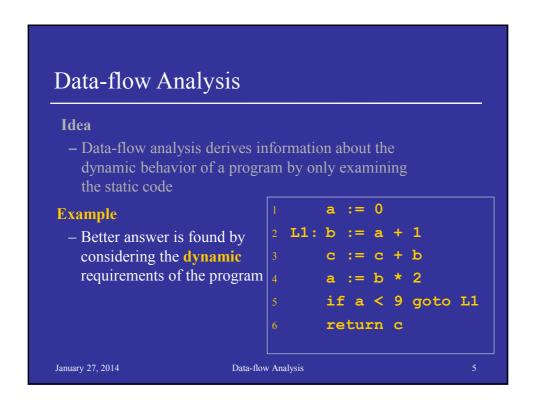


```
Data-flow Analysis
 Idea
  - Data-flow analysis derives information about the
    dynamic behavior of a program by only examining
    the static code
                                       a := 0
Example
 – How many registers do we
    need for the program on the
    right?
  - Easy bound: the number of
                                       if a < 9 goto L1
    variables used (3)
                                       return c
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                          Data-flow Analysis
```



```
Liveness Analysis
Definition
 - A variable is live at a particular point in the program if its
    value at that point will be used in the future (dead, otherwise).
    :. To compute liveness at a given point, we need to look into
    the future
                                        a := 0
                                  L1: b := a + 1
Example
                                        c := c + b
 - Is c live on line 3?
                                        a := b * 2
                                        if a < 9 goto L1
                                        return c
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```

Motivation for Liveness Analysis

Register Allocation

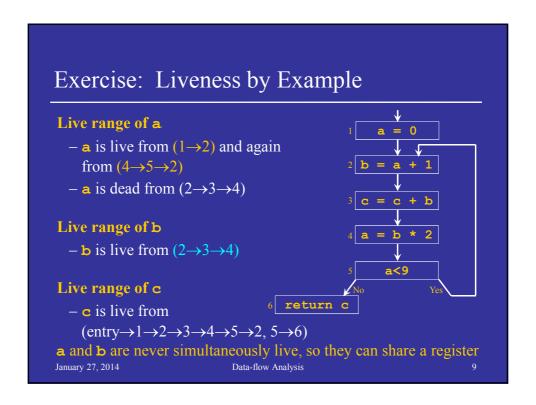
- A program contains an unbounded number of variables
- Must execute on a machine with a bounded number of registers
- Two variables can use the same register if they are never in use at the same time (*i.e.*, never simultaneously live).
 - :. Register allocation uses liveness information

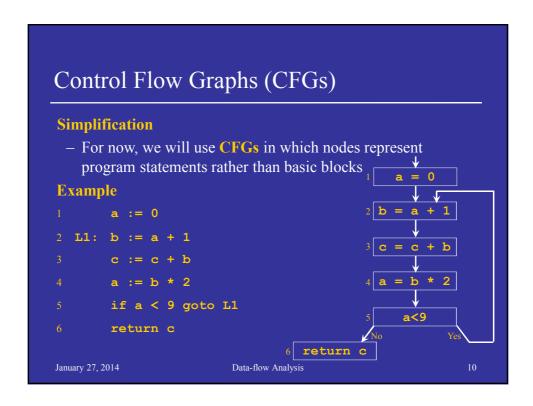
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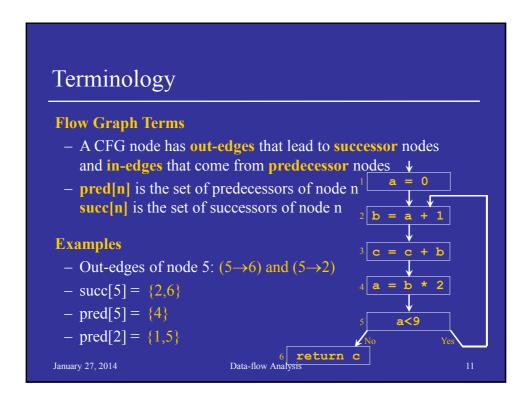
Data-flow Analysis

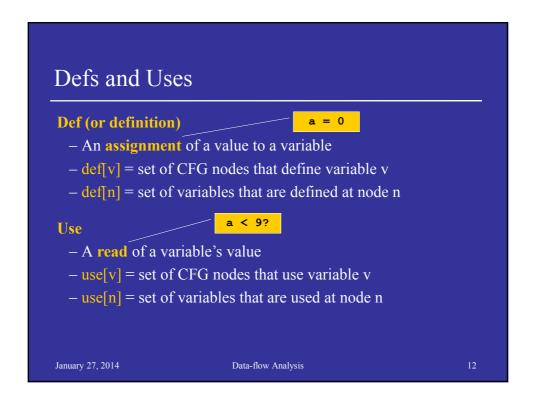
7

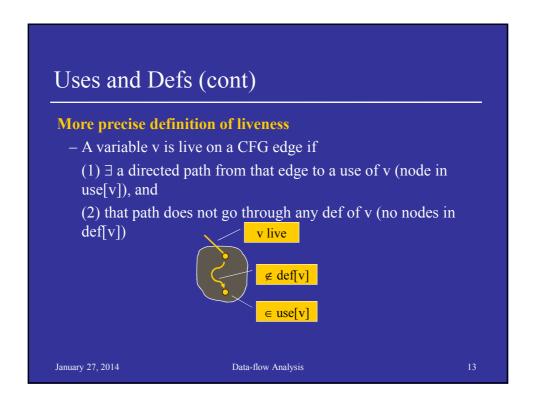
Liveness by Example What is the live range of b? - Variable **b** is read in statement 4, so **b** is live on the $(3 \rightarrow 4)$ edge 2 b = a + 1- Since statement 3 does not assign into **b**, **b** is also live on the $(2\rightarrow 3)$ = b * 2edge a<9 – Statement 2 assigns **b**, so any value of **b** on the return c $(1\rightarrow 2)$ and $(5\rightarrow 2)$ edges are not needed, so **b** is dead **b's** live range is $(2 \rightarrow 3 \rightarrow 4)$ along these edges January 27, 2014 Data-flow Analysis

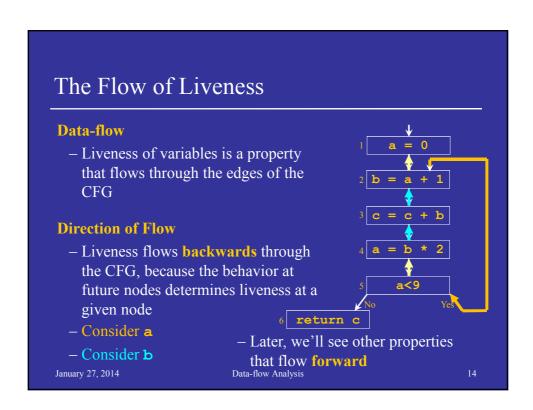


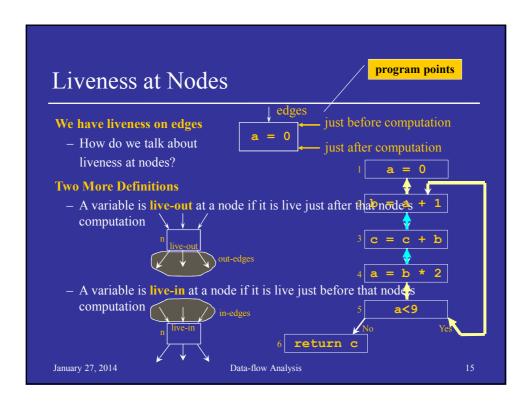


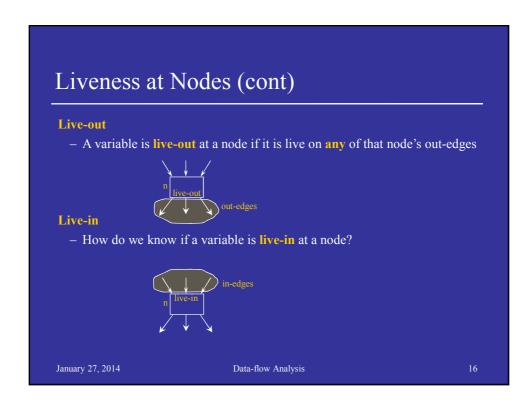


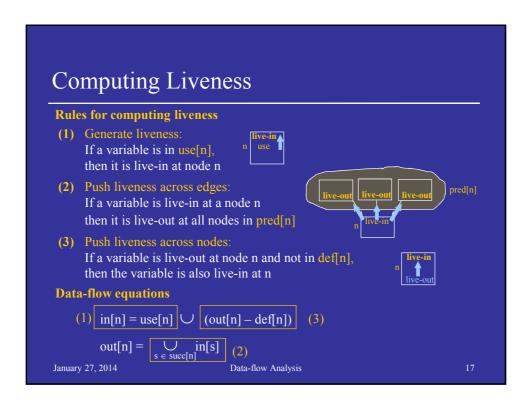












```
Solving the Data-flow Equations

Algorithm

for each node n in CFG

in[n] = \emptyset; out[n] = \emptyset

repeat

for each node n in CFG

in'[n] = in[n]

out'[n] = out[n]

in[n] = use[n] \cup (out[n] - def[n])

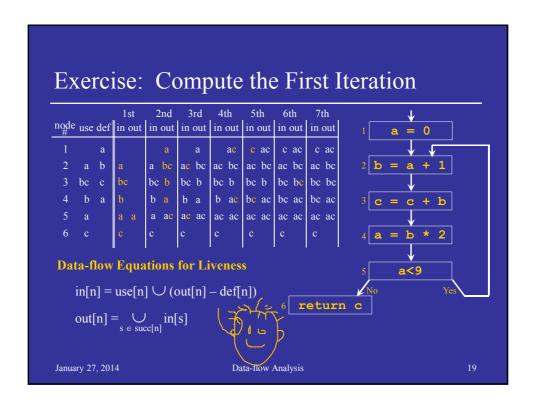
out[n] = \bigcup_{s \in succ[n]} in[s]

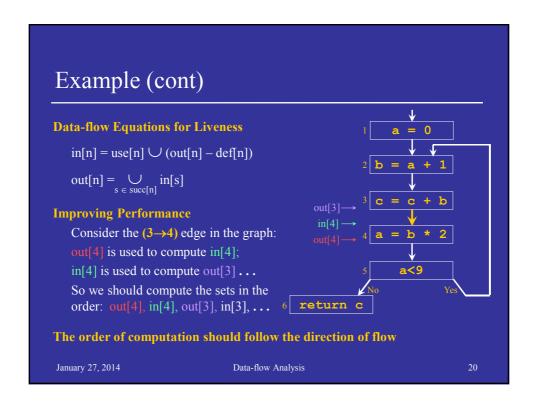
until in'[n] = in[n] and out'[n] = out[n] for all n } test for convergence

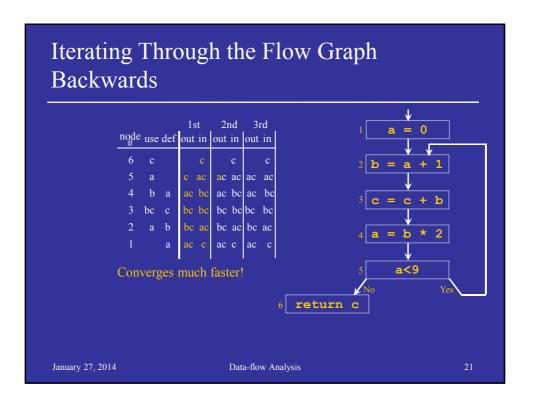
This is iterative data-flow analysis (for liveness analysis)

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Data-flow Analysis
```







```
Solving the Data-flow Equations (reprise)

Algorithm

for each node n in CFG

in[n] = \emptyset; out[n] = \emptyset

repeat

for each node n in CFG in reverse topsort order

in'[n] = in[n]

out'[n] = out[n]

out[n] = \emptyset

save current results

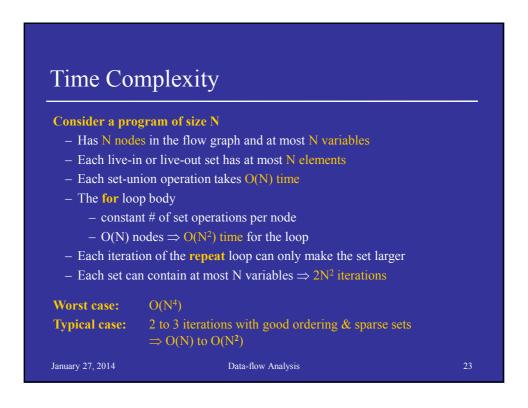
out[n] = use[n] \emptyset (out[n] - def[n])

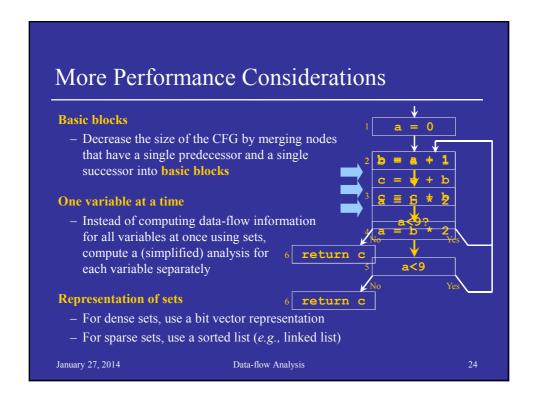
and out'[n] = out[n] for all n

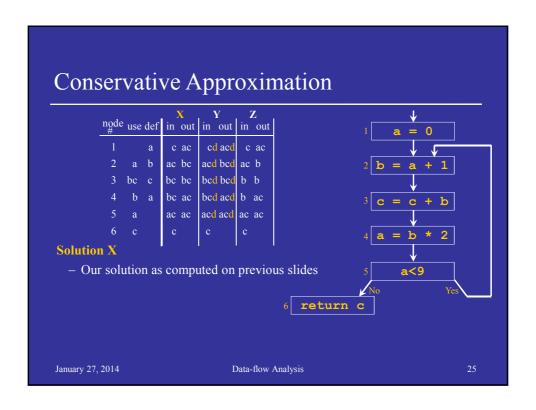
test for convergence

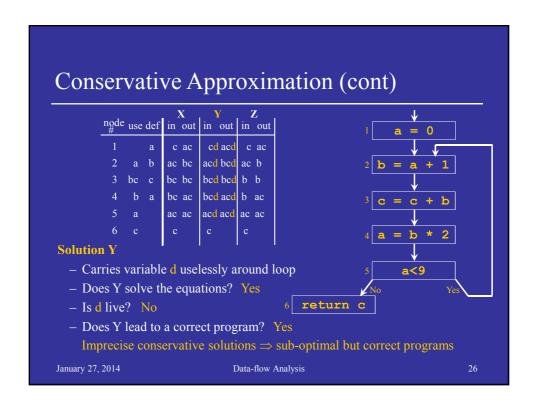
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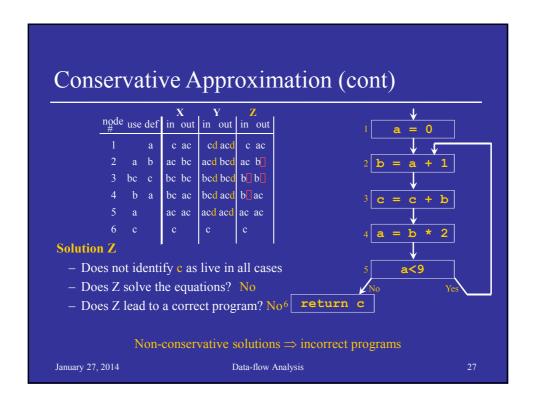
Data-flow Analysis 22
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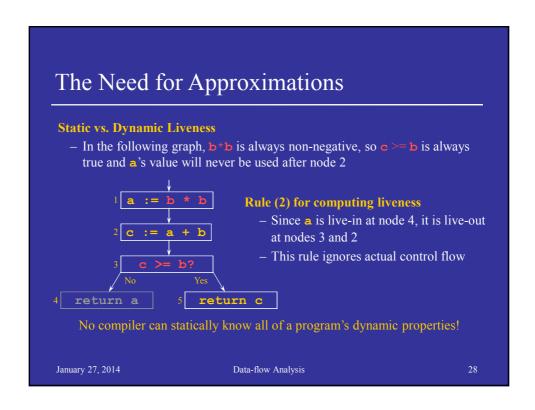












Concepts

Liveness

- Use in register allocation
- Generating liveness
- Flow and direction
- Data-flow equations and analysis
- Complexity
- Improving performance (basic blocks, single variable, bit sets)

Control flow graphs

Predecessors and successors

Defs and uses

Conservative approximation

- Static versus dynamic liveness

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Data-flow Analysis

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Next Time

Lecture

- Generalizing data-flow analysis

Reading

- Response for Smith paper due Tuesday at 5:00pm

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Data-flow Analysis

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