HPC - HW 3

Kitty Li (wl2407)

Credit: Received help from Jimmy Zhu

Processor: Intel(R) Core(TM) i9-9980HK CPU @ 2.40GHz Github repository: https://github.com/lwyhasacat/HPCHW3

Problem 1.

a) When n is an odd number, thread 0 and thread 1 would execute function f the same number of times. Thread 0 will execute f for (n-1)/2+...+1=(n+1)(n-1)/8 miliseconds, while thread 1 will execute f for (n+1)/2+...+(n-1)=(3n-1)(n-1)/8 miliseconds. The second for loop inverts the order so they will change the order and execute f again. The time they spent in waiting will be the two times the difference between the execution time of thread 0 and thread 1, which is $(n-1)^2/2$. Total time they spend is (3n-1)(n-1)/4 miliseconds.

When n is an even number, thread 0 will get one more function call than thread 1. Thread 0 will execute f for $n/2 + ... + 1 = n^2/8 + n/4$ miliseconds, while thread 1 will execute f for $(n/2 + 1) + ... + (n - 1) = 3 * n^2/8 - 3 * n/4$ miliseconds. The second for loop inverts the order so they will change the order and execute f again. Thread 0 will execute f for $(n - 1) + ... + n/2 = 3 * n^2/8 - n/4$ miliseconds, while thread 1 will execute f for $(n/2 - 1) + ... + 1 = n^2/8 - n/4$ miliseconds. The wait time is $n^2/2 - n$ miliseconds, in which thread 0 waits for $n^2/4 - n$ miliseconds and thread 1 waits for $n^2/4$ miliseconds. Total time will be $3 * n^2/4 - n$ miliseconds.

b) When we use schedule(static, 1), we are alternatively giving two threads one function call. When thread 0 executes f(1), f(3),..., thread 1 executes f(2), f(4), ... and therefore the waiting time will be shorter. Also, it doesn't matter which thread gets the function call first.

When n is odd, one of the thread will execute f for (n-1) + ... + 2 and the other one will execute f for (n-2) + ... + 1 miliseconds. For just the first for loop. the total time will be (n-1) + ... + 2 = (n-1)(n+1)/4 miliseconds, and the wait time will be (n-1)/2 miliseconds. The second for loop will be executed similarly as the first for loop, so the total time will be (n-1)(n+1)/2 miliseconds and the wait time will be n-1 miliseconds.

When n is even, the first for loop should be $(n-1)+..+1=n^2/4$ miliseconds, and the wait time should be n/2 miliseconds. The second for loop should have the same run time as the first for loop. The total time will be $n^2/2$ miliseconds and the wait time will be n miliseconds.

c) For schedule(dynamic, 1), when n is odd, the two threads will behave the same as when we use schedule(static, 1) in the first for loop, meaning that the total time will be (n-1)(n+1)/4 miliseconds and the waiting time will be (n-1)/2 miliseconds. In the second for loop, we can consider four function calls as a set. In the first set, thread 0 gets f(n-1) and f(n-4), and thread 1 gets f(n-2) and f(n-3). We can see that either one uses 2n-5 miliseconds. In the second set, thread 0 gets f(n-5) and f(n-8), and thread 1 gets f(n-6) and f(n-7). We can see that either one uses 2n-13 miliseconds. Both threads end at the same time. If we can divide the tasks into groups of four, then the wait time will be 0 milisecond, and the total time will be n(n-1)/4 miliseconds.

If we have less than four function calls at the end, there will be a remainder. When n%4 equals 3, meaning that the number of remaining tasks is 2, then we have total time (n+2)(n-3)/4+2 miliseconds, and the wait time will be 1. Therefore, when n%4 equals 1, the total time would be $n(n-1)/4+(n-1)(n+1)/4=(2n^2-n-1)/4$ miliseconds with wait time (n-1)/2 miliseconds, and when n%4 equals 3, the total time would be $((n+2)(n-3)/4+2)+(n-1)(n+1)/4=(2n^2-n+1)/4$ miliseconds with wait time (n+1)/2 miliseconds.

When n is even, the first loop will take $(n-1)+(n-3)+...+1=n^2/4$ miliseconds, and the wait time will be n/2 miliseconds. For the second loop, when n%4 equals 2, meaning that the number of remaining tasks is 1, then the total time will be (n+1)(n-2)/4+1 miliseconds with wait time 1 milisecond. When n%4 equals 0, meaning that the number of remaining tasks is 3, then the total time for the second loop will be (n-1)n/4 miliseconds with wait time 0 milisecond. Therefore if we sum the two loops, when n%4 equals 2, the total time will be $(2n^2-n+2)/4$ miliseconds with wait time n/2+1 miliseconds, and when n%4 equals 0, the total time will be $(2n^2-n)/4$ miliseconds with wait time n/2 miliseconds.

d) We can use nowait. When n odd, the two threads are given the same amount of function calls and should end together, so the total time should be (n-1)+...+1=(n-1)n/2 miliseconds, and the waiting time should be 0. When n even, thread 0 will get one more function call than thread 1, so the total time will be $((n-1)+...+n/2)+(n/2+...+1)=n^2/2$ miliseconds, and the waiting time will be $n^2/2$ miliseconds.

Problem 2.

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```
\begin{array}{l} p=2: \ sequential\text{-scan}=0.262186s\ parallel\text{-scan}=0.256076s\\ p=3: \ sequential\text{-scan}=0.254410s\ parallel\text{-scan}=0.207615s\\ p=4: \ sequential\text{-scan}=0.250087s\ parallel\text{-scan}=0.154154s\\ p=5: \ sequential\text{-scan}=0.253337s\ parallel\text{-scan}=0.137764s\\ p=6: \ sequential\text{-scan}=0.255503s\ parallel\text{-scan}=0.129882s\\ p=7: \ sequential\text{-scan}=0.251848s\ parallel\text{-scan}=0.126926s\\ p=8: \ sequential\text{-scan}=0.253870s\ parallel\text{-scan}=0.125671s\\ p=9: \ sequential\text{-scan}=0.257199s\ parallel\text{-scan}=0.128664s\\ p=10: \ sequential\text{-scan}=0.258090s\ parallel\text{-scan}=0.129190s\\ p=15: \ sequential\text{-scan}=0.266516s\ parallel\text{-scan}=0.131781s\\ p=20: \ sequential\text{-scan}=0.273825s\ parallel\text{-scan}=0.131979s\\ p=30: \ sequential\text{-scan}=0.249938s\ parallel\text{-scan}=0.133453s\\ p=50: \ sequential\text{-scan}=0.258560s\ parallel\text{-scan}=0.136586s\\ \end{array}
```

Problem 3.

Using thread = 2:

```
Jacobi Method: time = 0.008069
  Gauss-Seidel Method: time = 0.003256
    Jacobi Method: time = 0.151984
  Gauss-Seidel Method: time = 0.153242
   Jacobi Method: time = 0.159061
  Gauss-Seidel Method: time = 0.142596
  Jacobi Method: time = 0.163341
  Gauss-Seidel Method: time = 0.162014
  Jacobi Method: time = 0.211874
  Gauss-Seidel Method: time = 0.225391
  Jacobi Method: time = 0.684946
  Gauss-Seidel Method: time = 0.725793
   Jacobi Method: time = 2.8902
  Gauss-Seidel Method: time = 2.61201
Using thread = 5:
       ----- N = 10
  Jacobi Method: time = 0.010741
  Gauss-Seidel Method: time = 0.004553
      ----- N = 100 ---
  Jacobi Method: time = 0.195726
  Gauss-Seidel Method: time = 0.195393
      ----- N = 200
  Jacobi Method: time = 0.215786
  Gauss-Seidel Method: time = 0.195518
     Jacobi Method: time = 0.206891
```

Gauss-Seidel Method: time = 0.202107— N = 1000— Jacobi Method: time = 0.251678

Gauss-Seidel Method: time = 0.238038

---- N = 10

Using thread = 10:

----- N = 10Jacobi Method: time = 0.015999Gauss-Seidel Method: time = 0.007501Jacobi Method: time = 0.340212Gauss-Seidel Method: time = 0.339645----- N = 200 - -Jacobi Method: time = 0.347779Gauss-Seidel Method: time = 0.335187------ N = 400Jacobi Method: time = 0.348796Gauss-Seidel Method: time = 0.331007Jacobi Method: time = 0.367323Gauss-Seidel Method: time = 0.335686Jacobi Method: time = 0.651094Gauss-Seidel Method: time = 0.585486Jacobi Method: time = 1.77732Gauss-Seidel Method: time = 1.20809