Principles of Database Systems (CS307)

Lecture 16: Advanced / Miscellaneous Topics

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- Most contents are from slides made by Stéphane Faroult and the authors of Database System Concepts (7th Edition).
- Their original slides have been modified to adapt to the schedule of CS307 at SUSTech.
- The slides are largely based on the slides provided by Dr. Yuxin Ma

Announcements

- We will have one final assignment coming out very soon
 - Please pay attention to the notifications in the QQ group and emails from blackboard
- Final exam will be on Jan 8, 2025 (Wed), 14:00-16:00, 三教105/106
- Student Course Evaluation (评教)
 - Help instructors optimize course design,
 - Improve teaching quality
 - Enhance students' learning experience and sense of accomplishment
 - Evaluation Period
 - From 9:00 on Dec 13, 2024, to 24:00 on Dec 27, 2024

Outline

Part 1: Relational Language

Basic SQL

- Create Tables and Insert Data
- Basic Queries

Intermediate SQL

- Advanced Join
- Subquery
- Window Function
- Transactions

Advanced SQL

- Function
- Procedure
- Trigger
- View



Lab

Only

Part 2: DB Design and Application

Relational DB Design

- The Entity-Relationship Model
- E-R Diagram Design

Relational Algebra

Normalization

- Functional Dependency
- Normal Forms
- FD Theory
- Decomposition w/ FD

Application Design

- Use Databases in Programs
- Complex Data Types (JSON, XML, etc.)

Part 3: Internal Mechanism Of Relational DB Systems

Storage Management

- Physical and Logical Storage Structure
- Indexing

Query Management

- Query Processing
- Query Optimization

Transaction Management

- Transaction
- Concurrency

Part 4: Miscellaneous Topics

Big Data

- Big Data Storage
- Query and Process Big Data

Advanced Topics

- Beyond Relational DB
- Data Analytics

Beyond Tables: More Data Types

Semi-Structured Data

- Many applications require storage of complex data, whose schema changes often
 - In these applications, the constraints on data types imposed by the relational model could cause more problems than they solve
- The relational model's requirement of atomic data types may be an overkill
 - E.g., storing set of interests as a set-valued attribute of a user profile may be simpler than normalizing it
- Data exchange can benefit greatly from semi-structured data
 - Exchange can be between applications, or between back-end and front-end of an application
 - Web-services are widely used today, with complex data fetched to the front-end and displayed using a mobile app or JavaScript
- JSON and XML are widely used semi-structured data models

Features of Semi-Structured Data Models

- Flexible schema
 - Wide column representation: allow each tuple to have a different set of attributes, can add new attributes at any time
 - Sparse column representation: schema has a fixed but large set of attributes, by each tuple may store only a subset

Features of Semi-Structured Data Models

- Multivalued data types
 - Sets, multisets
 - E.g.,: set of interests: {"basketball", "cooking", "anime", "jazz"}
 - Key-value map (or just map for short)
 - Store a set of key-value pairs
 - E.g.,
 - {(brand, Apple), (ID, MacBook Air), (size, 13), (color, silver)}
 - Operations on maps
 - put(key, value)
 - get(key)
 - delete(key)

Features of Semi-Structured Data Models

- Arrays
 - Widely used for scientific and monitoring applications
 - E.g., readings taken at regular intervals can be represented as array of values instead of (time, value) pairs
 - [5, 8, 9, 11] instead of {(1,5), (2, 8), (3, 9), (4, 11)}
- Array database: a database that provides specialized support for arrays
 - E.g., compressed storage, query language extensions, etc.
 - Oracle GeoRaster, PostGIS, SciDB, etc

Nested Data Types

- Hierarchical data is common in many applications
- JSON (JavaScript Object Notation)
 - Widely used today
- XML (eXtensible Markup Language)
 - Earlier generation notation, still used extensively

```
"contentLink": {
   "id": 6,
   "workId": 0,
   "guidValue": "ca287bcd-6790-4ac1-9132-cc
   "providerName": null,
   "url": "/en/alloy-plan/",
   "expanded": null
"name": "Alloy Plan",
"language": {
   "link": "/en/alloy-plan/",
   "displayName": "English",
   "name": "en"
"existingLanguages": [
        "link": "/en/alloy-plan/",
       "displayName": "English",
        "name": "en"
```

```
xmlns:xsi="http://www.w3.org/2001/XMLSchema-instance"
        xsi:schemaLocation="http://maven.apache.org/POM/4.0.0
        http://maven.apache.org/xsd/maven-4.0.0.xsd">
   <modelVersion>4.0.0</modelVersion>
   <groupId>com.spring.aspect</groupId>
   <artifactId>SpringAspect</artifactId>
   <version>0.0.1-SNAPSHOT</version>
   <url>http://maven.apache.org</url>
   <dependencies>
       <dependency>
           <groupId>junit</groupId>
           <artifactId>junit</artifactId>
           <version>4.0.1</version>
           <scope>test</scope>
      </dependency>
   </dependencies>
```

JSON

- Textual representation widely used for data exchange
- Types: integer, real, string, and
 - Objects: key-value maps, i.e. sets of (attribute name, value) pairs
 - Objects do not have to adhere to any fixed schema
 - Arrays: also key-value maps (from offset to value)
 - Shown in square brackets

```
"ID": "22222",
    "name": {
        "firstname: "Albert",
        "lastname: "Einstein"
},
    "deptname": "Physics",
    "children": [
        {"firstname": "Hans", "lastname": "Einstein" },
        {"firstname": "Eduard", "lastname": "Einstein" }
}
```

JSON

- JSON is ubiquitous in data exchange today
 - Widely used for web services
 - primary data representation used for communication between applications and web services.
- PostgreSQL supports JSON format columns

```
create table json_test (
   id serial not null primary key,
    student json not null
);

insert into json_test (student) values ('{"name": "aaa", "age": 20, "major": {"primary": "cs", "minor":
   "math"}}');
insert into json_test (student) values ('{"name": "bbb", "major": {"primary": "math", "minor": "physics"}}');
insert into json_test (student) values ('{"name": "ccc", "age": 19, "major": {"primary": "biology"}}');
```

JSON

- JSON is ubiquitous in data exchange today
 - Widely used for web services
 - primary data representation used for communication between applications and web services.
- PostgreSQL supports JSON format columns

XML

- XML uses tags to mark up text
 - Tags make the data self-documenting
 - Humans can understand the meanings based on the names
 - Tags can be hierarchical
 - Important in many business applications

Textual Data

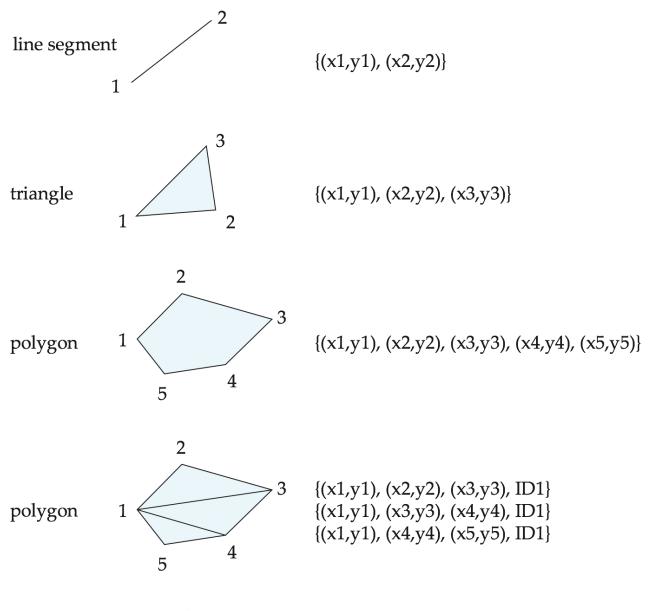
- Information retrieval: querying of unstructured textual data
 - Simple model of keyword-based queries
 - Each document is associated with several key words
 - Given query keywords, retrieve documents containing all the keywords
 - More advanced models rank relevance of documents
 - Today, keyword queries return many types of information as answers
 - E.g., a query "cricket" typically returns information about ongoing cricket matches
- Relevance ranking
 - Essential since there are usually many documents matching keywords

Spatial Data

- Spatial databases store information related to <u>spatial locations</u>, and support <u>efficient storage</u>, indexing and querying of spatial data.
 - Geographic data: road maps, land-usage maps, topographic elevation maps, political maps showing boundaries, land-ownership maps, and so on.
 - Geographic information systems (GIS) are special-purpose databases tailored for storing geographic data.
 - Round-earth coordinate system may be used
 - (Latitude, longitude, elevation)
 - Geometric data: design information about how objects are constructed
 - E.g., designs of buildings, aircraft, layouts of integrated-circuits.
 - 2 or 3 dimensional Euclidean space with (X, Y, Z) coordinates

Representation of Geometric Information

 Various geometric constructs can be represented in a database in a normalized fashion



NoSQL Database (Key-Value Storage Systems)

- "Not Only SQL"
 - Useful when working with a huge quantity of data when nature of data does not require a relational model
 - Many web applications need to store very large numbers of relatively small records
 - Records are stored and retrieved based on a key, and may additionally provide limited query facilities
 - Usually not built on tables and queried by SQL

Examples

- Document store MongoDB
- Graph structure Neo4j
- Key-value storage Redis, LevelDB
- Tabular Apache Hbase (Hadoop-based)







Beyond PostgreSQL: More DBMS

Commercial & Open-Source Solutions

Commercial Relational DBMS:

- Oracle Database
- Microsoft SQL Server
- IBM DB2
- •

Open-Source Counterparts:

- MySQL (MariaDB)
- PostgreSQL
- •

Commercial & Open-Source Solutions

- Factors to consider open-source databases
 - Cost
 - Open-source databases are generally free
 - Customizability
 - Add your own features in the source code
 - Community support
 - Documentations, bug fixes, discussions

Commercial & Open-Source Solutions

- Factors to consider commercial databases
 - Technical support
 - Guaranteed professional services
 - Usability
 - Generally easier to deploy and use
 - Can be seamlessly integrated into other commercial products
 - Feature support
 - Enterprise-level feature extension (More functions, useful SQL syntax, etc.)

openGauss

- Relational DBMS from Huawei
 - Enterprise-grade open-source relational database
 - Client-server architecture
 - High-performance, highreliability, high-security
 - Community support
 - * Compatible to PostgreSQL clients



https://www.opengauss.org/en/

Key Differences between openGauss and PostgreSQL

- originated from PostgreSQL-XC (eXtensible Cluster)
- Fundamental differences in the architecture and key technologies, especially in the storage engine and query optimizer

关键差异化因素		openGauss	PostgreSQL
运行时模型	执行模型	线程池模型,高并发连接切换代价小、内存损耗小, 执行效率高,一万并发连接比最优性能损耗<5%。	进程模型,数据库进通过共享内存实现通讯和 数据共享。每个进程对应一个并发连接,存在 切换性能损耗,导致多核扩展性问题。
事务处理	并发控制	64位事务ID,使用CSN解决动态快照膨胀问题; NUMA-Aware引擎优化改造解决"五把大锁。	事务ID回卷,长期运行性能因为ID回收周期大幅波动;存在"五把大锁"的问题,导致事务执行效率和多处理器多核扩展性存在瓶颈。
	日志和检查点	增量Checkpoint机制,实现性能波动<5%。	全量checkpoint,性能短期波动>15%。
	鲲鹏NUMA	NUMA改造、cache-line padding、原生spin- lock。	NUMA多核能力弱,单机两路性能TPMC <60w。
数据组织	多引擎	行存、列存、内存引擎,在研DFV存储和原位更新。	仅支持行存 。
SQL引擎	优化器	支持SQL Bypass, CBO吸收工行等企业场景优化能力。	支持CBO,复杂场景优化能力一般。
	SQL解析	ANSI/ISO标准SQL92、SQL99和SQL2003 和企业扩展包。	ANSI/ISO标准SQL92、SQL99和SQL2003。

Key Differences between openGauss and PostgreSQL

- originated from PostgreSQL-XC (eXtensible Cluster)
- Fundamental differences in the architecture and key technologies, especially in the storage engine and query optimizer

	openGauss	PostgreSQL
Execution Model	Thread pool-based (higher concurrency performance)	Process-based
Data Organization	Multiple engines: Row-oriented, column-oriented, in-memory storage	Only row-oriented
SQL Optimization	More complex enterprise-level optimization	Cost-based optimization
SQL Parsing	ANSI/ISO SQL92, SQL99, SQL2003 w/ enterprise-level extensions	ANSI/ISO SQL92, SQL99, SQL2003

Beyond Storage: Big Data Processing and Analytics

What is Data (Revisited)

data noun, plural in form but singular or plural in construction, often attributive



da·ta | \'dā-tə ♠, 'da- ♠ also 'dä- ♠ \

Definition of data

- 1 : factual information (such as measurements or statistics) used as a basis for reasoning, discussion, or calculation
 - // the data is plentiful and easily available
 - H. A. Gleason, Jr.
 - // comprehensive data on economic growth have been published
 - N. H. Jacoby
- 2 : information in digital form that can be transmitted or processed
- 3 : information output by a sensing device or organ that includes both useful and irrelevant or redundant information and must be processed to be meaningful

factual information (such as measurements or statistics) used as <u>a basis</u> for reasoning, discussion, or calculation

Basic Statistical Descriptions

- Overall picture of your data
- Basis of exploratory data analysis

$$\bar{x} = \frac{\sum_{i=1}^{N} x_i}{N} = \frac{x_1 + x_2 + \dots + x_N}{N}.$$

$$Q_{\frac{1}{2}}(x) = \begin{cases} x'_{\frac{n+1}{2}}, & \text{if } n \text{ is odd.} \\ \frac{1}{2}(x'_{\frac{n}{2}} + x'_{\frac{n}{2}+1}), & \text{if } n \text{ is even.} \end{cases}$$

Variance
$$\sigma^2 = \frac{1}{N} \sum_{i=1}^{N} (x_i - \bar{x})^2 = \left(\frac{1}{N} \sum_{i=1}^{N} x_i^2\right) - \bar{x}^2,$$

Relationship between Data Objects: Data (Dis)Similarity

- Measurement of relationships
 - Commonly used in many statistical methods and data mining algorithms
- Dissimilarity Matrix & Distance Measures

$$\begin{bmatrix} 0 \\ d(2,1) & 0 \\ d(3,1) & d(3,2) & 0 \\ \vdots & \vdots & \vdots \\ d(n,1) & d(n,2) & \cdots & \cdots & 0 \end{bmatrix}$$

Euclidean	$d(x, y) = \sqrt{\sum (x_i - y_i)^2}$
Squared Euclidean	$d(x, y) = \sum_{i} (x_i - y_i)^2$
Manhattan	$d(x, y) = \sum_{i} (x_i - y_i)$
Canberra	$d(x,y) = \sum \frac{ x_i - y_i }{ x_i + y_i }$
Chebychev	$d(x, y) = \max(x_i - y_i)$
Bray Curtis	$d(x, y) = \frac{\sum x_i - y_i }{\sum x_i + y_i}$
Cosine Correlation	$d(x,y) = \frac{\sum_{i} (x_{i}y_{i})}{\sqrt{\sum_{i} (x_{i})^{2} \sum_{i} (y_{i})^{2}}}$
Pearson Correlation	$d(x,y) = \frac{\sum (x_i - \overline{x})(y_i - \overline{y})}{\sqrt{\sum (y_i - \overline{y})^2} \sqrt{\sum (y_i - \overline{y})^2}}$
Uncentered Peason Correlation	$d(x,y) = \frac{\sum_{i} x_{i} y_{i}}{\sqrt{\sum_{i} (y_{i} - \overline{y})^{2}} \sqrt{\sum_{i} (y_{i} - \overline{y})^{2}}}$
Euclidean Nullweighted	Same as Euclidean, but only the indexes where both x and y have a value (not NULL) are used, and the result is weighted by the number of values calculated. Nulls must be replaced by the missing value calculator (in dataloader).

What is Big Data?

- Modern data management applications often need to deal with data that are not necessarily in relational form
 - Such applications also need to deal with volumes of data that are far larger than what a single enterprise would generate
- A collection of data sets so large and complex



Three Dimensions of Big Data

Volume

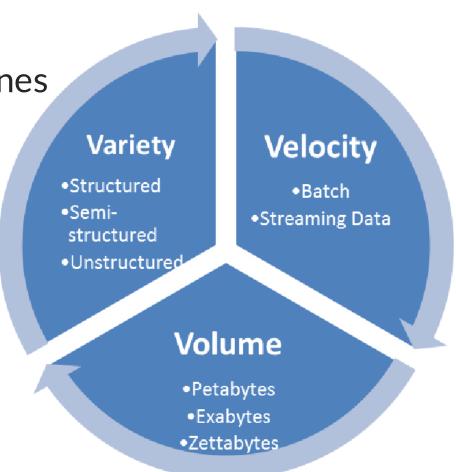
• From GB to TB, PB, or higher; requires many machines

Velocity

Processing speed, online streaming data systems

Variety

- Text, sensor data, multimedia, ...
- Not all data are relational
- Other (new) aspects:
 - Veracity: Trustworthiness
 - Value: Worth of data



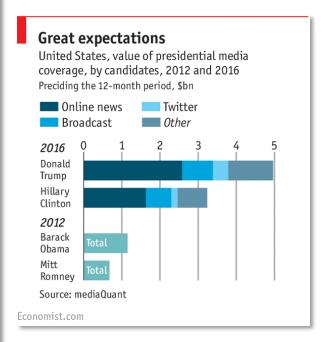
The Emergence of Data Science

 Using data about the past to predict the future and using the predictions to make decisions

2016: "Trump vs. Clinton: How Big Data and scientists helped Trump win the election"

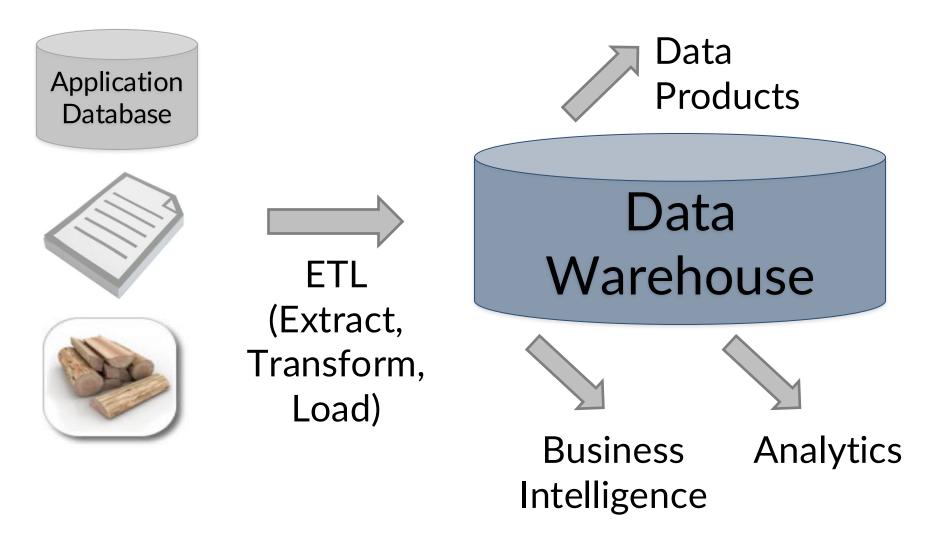






Standard Architecture

 Collecting data from multiple sources, cleaning/deduplicating the data, and loading the data into a warehouse



Instantiations(1) - Businesspersons

- Data Sources
 - Web pages
 - Excel
- Extract-Transform-Load (ETL)
 - Copy & paste
- Data Warehouse
 - Excel

- Bl and Analytics
 - Excel functions
 - Excel charts
 - VB scripts?
 - Visualization tools: Power BI, Tableau

Instantiations(2) - Programmers

- Data Sources
 - Web scraping, web services API
 - CSV files
 - Database queries
- ETL
 - wget, curl, Beautiful Soup, lxml, ...

- Data Warehouse
 - Files
- Analytics
 - Numpy, pandas, Matplotlib, R,
 Octave, ...

Instantiations(3) - Enterprises

- Data Sources
 - Application databases(Oracle, IBM, ...)
 - Intranet files
 - Application log files
- ETL
 - Infomatica, IBM DataStage, ...

- Data Warehouse
 - Teradata, Oracle, IBM DB2, ...
- Business Intelligence & Analytics
 - SAS, SPSS, R, ...
 - Power BI, Tableau, Spotfire, ...

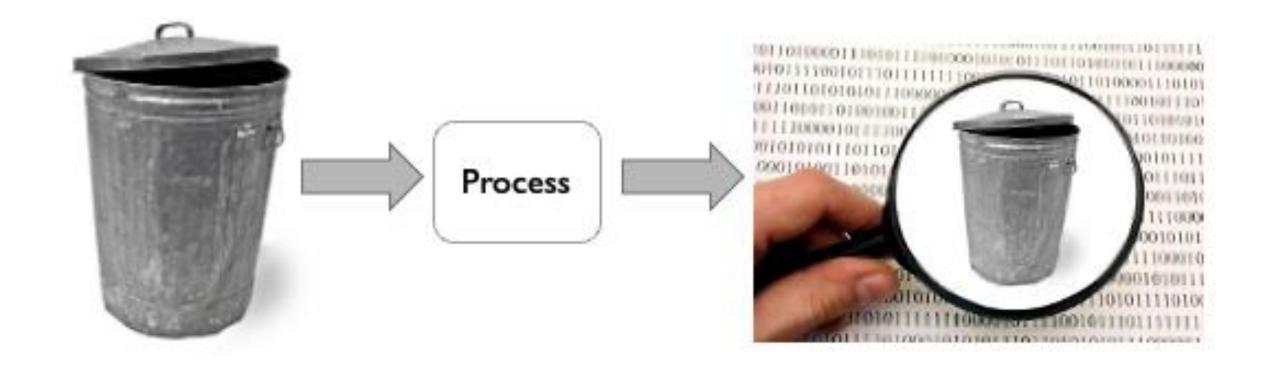
Instantiations(4) – Web Companies

- Data Sources
 - Application databases
 - Logs
 - Web crawl data
- ETL
 - Apache Flume, Apache Sqoop, ...

- Data Warehouse
 - Hadoop-based: Hive, Hbase
 - Microsoft Azure, Amazon Redshift
- Business Intelligence & Analytics
 - Argus, R, ...

"Garbage in, garbage out."

• Raw data can always be **DIRTY**!

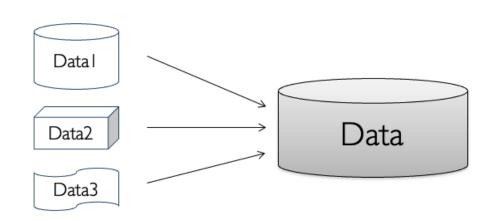


Data Quality

- Data quality: data has quality if it satisfies the requirements of its intended use
 - Accuracy
 - Completeness
 - Consistency
 - Timeliness
 - Believability
 - Interpretability

Data Integration

- Data integration involves combining data residing in different sources and providing users with a unified view of these data.
 - Remember "views" in DBMS?
- Management of data from multiple sources



Customer (source 1)

CID	Name	Street	City	Sex
11	Kristen Smith	2 Hurley Pl	South Fork, MN 48503	0
24	Christian Smith	Hurley St 2	S Fork MN	1

Client (source 2)

Cno	LastName	FirstName	Gender	Address	Phone/Fax
24	Smith	Christoph	М	23 Harley St, Chicago IL, 60633-2394	333-222-6542 / 333-222-6599
493	Smith	Kris L.	F	2 Hurley Place, South Fork MN, 48503-5998	444-555-6666

Customers (integrated target with cleaned data)

	b was on the Chine Branch and Bot William Chine Chine										
No	LName	FName	Gender	Street	City	State	ZIP	Phone	Fax	CID	Cno
1	Smith	Kristen L.	F	2 Hurley Place	South Fork	MN	48503- 5998	444-555- 6666		11	493
2	Smith	Christian	M	2 Hurley Place	South Fork	MN	48503- 5998			24	
3	Smith	Christoph	M	23 Harley Street	Chicago	IL	60633- 2394	333-222- 6542	333-222- 6599		24

Typical Data Cleaning and Integration Workflow

- Data analysis
 - Detailed inspection before operations
- Conflicts resolution
 - Resolve data confliction between data sources to be integrated
- Definition of transformation workflow and mapping rules
 - Workflow methods for schema adaption and transformation
- Verification of Workflow
 - Verify each steps
- Transformation
 - start the process

Load and Store Data

- File-based Storage
 - Simplest way & easy to manage
 - Scalability is low
- Database & DBMS
 - What we have learned for 10+ weeks
- Data Warehouse

Data Warehouse

A data warehouse is a **subject-oriented**, **integrated**, **time-varient**, and **nonvolatile** collection of data in support of management's decision making process.

-- W. H. Inmon, "Building the Data Warehouse". 1996.

Loosely Speaking, a data warehouse refers to a data repository that is **maintained** separately from an organization's operational databases.

-- J. Han and M. Kamber, "Data Mining: Concepts and Techniques", 3rd ed., 2011.

Differences between Databases and Data Warehouses

	DB	DW
Characteristics	operational processing	informational processing
Orientation	transaction	analysis
User	terminal users: clerk, database administrator(DBA)	knowledge workers: manager, analyst, executive
Function	everyday operations	long-term informational requirements decision support
Data	current, up-to-date	historic, accuracy maintained over time
Access	read/write	mostly read
Focus	data in	information/knowledge out
Size	GB to high-order GB	>=TB

Large-Scale Data Storage and Processing

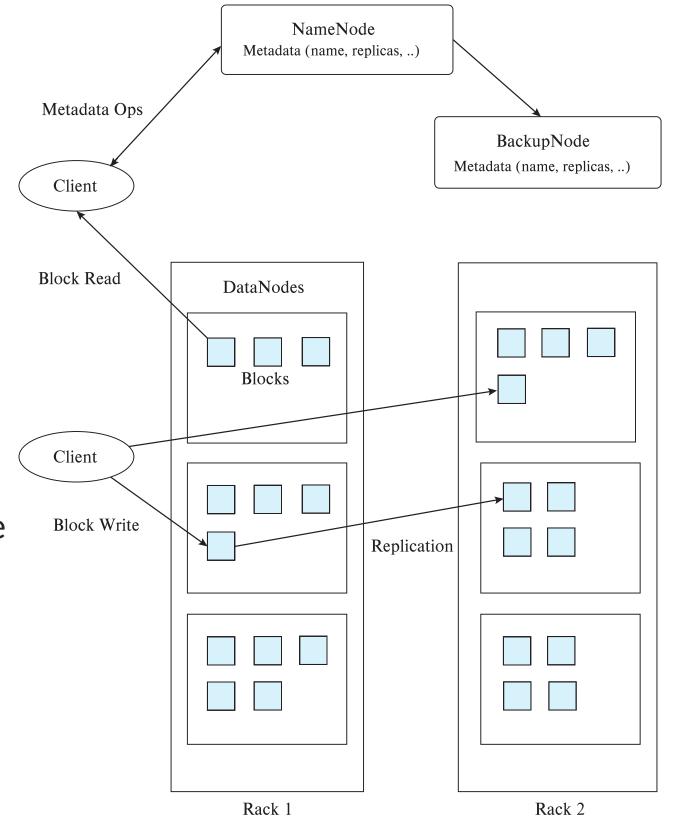
- Distributed file systems
- MapReduce

Distributed File System

- A distributed file system stores data across a large collection of machines, but provides <u>single file-system view</u>
- Highly scalable distributed file system for large data-intensive applications
 - E.g., 10K nodes, 100 million files, 10 PB
- Provides <u>redundant storage</u> of massive amounts of data on cheap and unreliable computers
 - Files are replicated to handle hardware failure
 - Detect failures and recovers from them
- Examples:
 - Google File System (GFS)
 - Hadoop File System (HDFS)

Hadoop File System Architecture

- Single Namespace for entire cluster
- Files are broken up into blocks
 - Typically 64 MB block size
 - Each block replicated on multiple DataNodes
- Client
 - Finds location of blocks from NameNode
 - Accesses data directly from DataNode



Hadoop Distributed File System (HDFS)

NameNode

- Maps a filename to list of Block IDs
- Maps each Block ID to DataNodes containing a replica of the block

DataNode

- Maps a Block ID to a physical location on disk
- Data Coherency
 - Write-once-read-many access model
 - Client can only append to existing files
- Distributed file systems good for millions of large files
 - But have very high overheads and poor performance with billions of smaller tuples

The MapReduce Computation Paradigm

- Platform for reliable, scalable parallel computing
 - map() is applied to each of a large number of input records
 - reduce(): some form of aggregation is applied to the result of the map() function
- Abstracts issues of distributed and parallel environment from programmer
 - Programmer provides core logic (via map() and reduce() functions)
 - System takes care of parallelization of computation, coordination, etc.
- Paradigm dates back many decades
 - But very large scale implementations running on clusters with 10³ to 10⁴ machines are more recent
 - Google Map Reduce, Hadoop, ...
- Data storage/access typically done using distributed file systems or key-value stores

MapReduce: Word Count Example

- Consider the problem of counting the number of occurrences of each word in a large collection of documents
 - Think about it: how do you write a program to handle it on your own machine?
- How would you do it in parallel?

MapReduce: Word Count Example

- Solution
 - Divide documents among workers
 - Each worker parses document to find all words, map function outputs (word, count) pairs
 - Partition (word, count) pairs across workers based on word
 - For each word at a worker, reduce function locally add up counts
- Given input: "One a penny, two a penny, hot cross buns."
 - Records output by the map() function would be
 - ("One", 1), ("a", 1), ("penny", 1), ("two", 1), ("a", 1), ("penny", 1), ("hot", 1), ("cross", 1), ("buns", 1)
 - Records output by the reduce() function would be
 - ("One", 1), ("a", [1,1]), ("penny", [1,1]), ("two", 1), ("hot", 1), ("cross", 1), ("buns", 1)
 - ("One", 1), ("a", 2), ("penny", 2), ("two", 1), ("hot", 1), ("cross", 1), ("buns", 1)

MapReduce: Word Count Example (Pseudocode)

for each value in value_list:

count = count + value

Output(word, count);

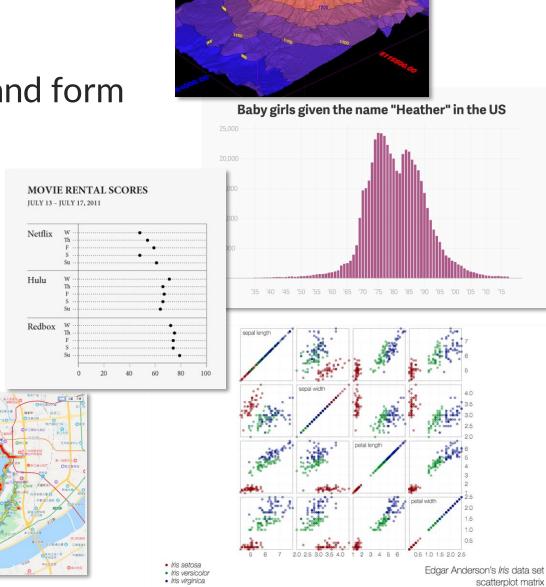
```
map(String record):
  for each word in record
   emit(word, 1);
// First attribute of "emit" above is called reduce key
// In effect, "group by" is performed on reduce key to create a list of values (all
 1's in above code). This requires shuffle step across machines.
// The "reduce" function is called on list of values in each group
reduce(String key, List value list):
  String word = key
  int count = 0;
```

Data Analysis

- Exploratory Data Analysis
- Data Mining

Exploratory Data Analysis (EDA)

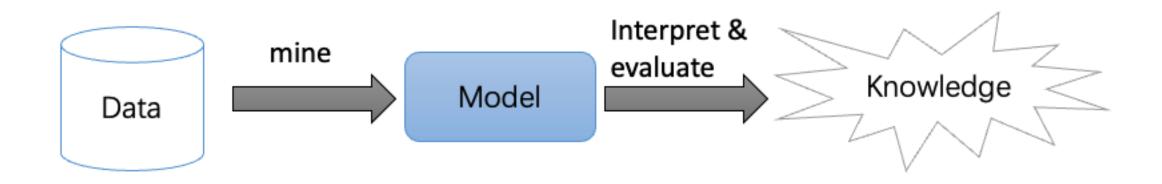
- Based on statistics
 - Data visualization-driven method
 - Summary of main characteristics in easy-to-understand form
- Types of data visualization methods in EDA:
 - Plotting of raw data
 - Plotting of statistical values
 - Multiple coordinated views (Dashboard)



Data Mining

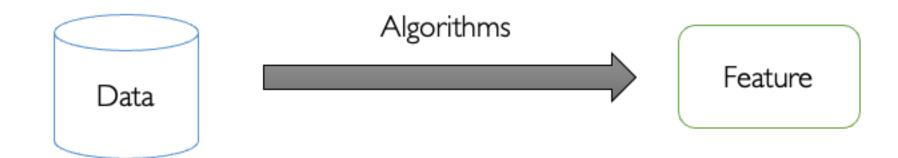
"Data Mining, also popularly referred to as knowledge discovery from data (KDD), is the automated or convenient extraction of patterns representing knowledge implicitly stored or captured in large databases, data warehouses, the Web, other massive repositories, or data streams."

-- H. Jiawei and M. Kamber, "Data Mining: Concepts and Techniques", 3rd ed., 2011.

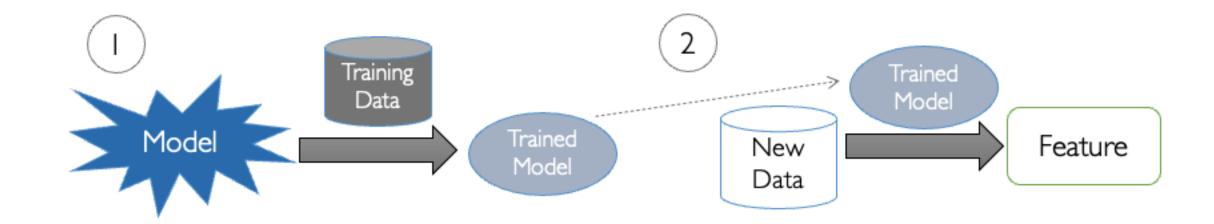


Tasks in Data Mining

Descriptive Tasks



Predictive Tasks



Descriptive Tasks

- Concept Description
 - Describe features of data directly
- Association Analysis
 - Analyze "feature-value" pairs that occur frequently in data
- Clustering
 - Group data on the principle of maximizing the intra-class similarity and minimizing the inter-class similarity
- Outlier Detection
 - Analyze objects that do not comply with the general behavior or model of the data

Predictive Tasks

- Regression
 - Model the relationship between a scalar response and a number of variables
- Classification
 - Find a model/function that describes and distinguish data classes or concepts based on analysis of a set of training data
- Evolution Analysis
 - Analyze temporal and spatial patterns in dataset, model these patterns and predict data in unknown spatio-temporal positions

Data Visualization

 Visualization is the creation and study of the visual representation of data

Input: data

Output: visual form

Goal: insight



Why Do We Need Visualization?

Sometimes, statistics may not work

Set A		Set B		ł C	Set	Set D	
Υ	Х	Υ	X	Υ	X	Υ	
8.04	10	9.14	10	7.46	8	6.58	
6.95	8	8.14	8	6.77	8	5.76	
7.58	13	8.74	13	12.74	8	7.71	
8.81	9	8.77	9	7.11	8	8.84	
8.33	11	9.26	11	7.81	8	8.47	
9.96	14	8.1	14	8.84	8	7.04	
7.24	6	6.13	6	6.08	8	5.25	
4.26	4	3.1	4	5.39	19	12.5	
10.84	12	9.11	12	8.15	8	5.56	
4.82	7	7.26	7	6.42	8	7.91	
5.68	5	4.74	5	5.73	8	6.89	
Summary Statistics $u_X = 9.0 G_X = 3.317$ $u_Y = 7.5 G_Y = 2.03$		Y = 3 + 0.5 X			[Anscom	be 73]	
	γ 8.04 6.95 7.58 8.81 8.33 9.96 7.24 4.26 10.84 4.82 5.68 ry Statistics σ _X = 3.317	Y X 8.04 10 6.95 8 7.58 13 8.81 9 8.33 11 9.96 14 7.24 6 4.26 4 10.84 12 4.82 7 5.68 5	Y X Y 8.04 10 9.14 6.95 8 8.14 7.58 13 8.74 8.81 9 8.77 8.33 11 9.26 9.96 14 8.1 7.24 6 6.13 4.26 4 3.1 10.84 12 9.11 4.82 7 7.26 5.68 5 4.74	Y X Y X 8.04 10 9.14 10 6.95 8 8.14 8 7.58 13 8.74 13 8.81 9 8.77 9 8.33 11 9.26 11 9.96 14 8.1 14 7.24 6 6.13 6 4.26 4 3.1 4 10.84 12 9.11 12 4.82 7 7.26 7 5.68 5 4.74 5	YXYXY8.04109.14107.466.9588.1486.777.58138.741312.748.8198.7797.118.33119.26117.819.96148.1148.847.2466.1366.084.2643.145.3910.84129.11128.154.8277.2676.425.6854.7455.73 ry Statistics Cy Statistics Linear Regression Y = 3 + 0.5 X	Y X Y X Y X 8.04 10 9.14 10 7.46 8 6.95 8 8.14 8 6.77 8 7.58 13 8.74 13 12.74 8 8.81 9 8.77 9 7.11 8 8.33 11 9.26 11 7.81 8 9.96 14 8.1 14 8.84 8 7.24 6 6.13 6 6.08 8 4.26 4 3.1 4 5.39 19 10.84 12 9.11 12 8.15 8 4.82 7 7.26 7 6.42 8 5.68 5 4.74 5 5.73 8 Ty Statistics Linear Regression Y = 3 + 0.5 X	

