CS208 Lab1 Practice

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DDL: Mar.2 23:59

Practice 1

Description

Trace the computation for the tower of Hanoi when n = 3.

Analysis

Firstly, when n=1 , move the disk from A to C directly. When n>=2 , we consider the smaller n-1 disks as a whole , thus we just need to:

- 1. move them from A to B
- 2. move the largest disk from A to C
- 3. move the n-1 disks from B to C.

And when we consider the way to move n-1 disks, the problem is degraded to move the smaller n-2 disks, where recursion occurs.

C++ code:

```
#include <iostream>
using namespace std;

void hanoi(int n, char from_rod, char to_rod, char aux_rod) {
    if (n == 1) {
        cout << "Move disk 1 from " << from_rod << " to " << to_rod << endl;
        return;
    }
    hanoi(n - 1, from_rod, aux_rod, to_rod);
    cout << "Move disk " << n << " from " << from_rod << " to " << to_rod << endl;
        hanoi(n - 1, aux_rod, to_rod, from_rod);
}

int main()
{
    int main()
}</pre>
```

```
hanoi(n, 'A', 'C', 'B');
return 0;
}
```

Output:

```
Move disk 1 from A to C
Move disk 2 from A to B
Move disk 1 from C to B
Move disk 3 from A to C
Move disk 1 from B to A
Move disk 2 from B to C
Move disk 1 from A to C
```

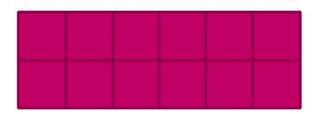
Practice 2

Description

Find the number of ways a 2 * n rectangle can be tiled with rectangular tiles of size 2 * 1.



2*1



2*6

Analysis

Firstly, when n=1, we only have one way to tile the 2*1 rectangle, so count(1)=1. When n=2, we have two ways which are horizontal and vertical, so count(2)=2. Now we consider the ways to fill when n>=3. We have two options:

- 1. fill the 2 * (n 2) rectangle then tile two horizontal 2 * 1 rectangle
- 2. fill the 2 * (n 1) rectangle then tile a vertical 2 * 1 rectangle

So the number of ways to fill the 2 * n rectangle will be:

```
count(n) = egin{cases} 1, & n=1 \ 2, & n=2 \ count(n-1) + count(n-2), & n>=3 \end{cases}
```

and it is smiliar with the Fibonacci sequence.

C++ code:

```
#include <iostream>
using namespace std;

int count(int n) {
    if (n <= 2) return n;
    return count(n - 1) + count (n - 2);
}

int main() {
    int n;
    cin >> n;

    if (n < 1) cout << "Invalid input!";
    else {
        int cnt = count(n);
        cout << cnt;
    }

    return 0;
}</pre>
```

Input:

6

Output:

13

Practice 3 (optional)

Description

Enter a string and print out all permutations of the characters in the string.

```
Example:
Input: abc
Output: abc, acb, bac, bca, cab, cba
```

Analysis

We use **backtrack method**. Suppose nums is the original array, path is the arrangement being built, used is a boolean array of which elements have been used.

We call the recursive function and iterate over each element in nums: If it has not been used (used[i] == false), add it to path and let used[i] = true , then keep iterating until the length of path equals to the length of nums, thus we have a complete permutation path. After that, we return the recursive function, undo the selection (remove the element from path, and used[i] = false), and back to the last situation.

No code needed

Practice 4 (optional)

Description

Enter a string and print out all combinations of the characters in the string.

```
Example:
Input: abc
Output: a, b, c, ab, bc, ac, abc
```

Analysis

Suppose the length of the string is n. For each character of the string, a binary 0 is used to indicate no selection and a 1 is used to indicate selection, so that **each binary number whose number of bits does not exceed** n **represents a different combination**.

Therefore, all combinations can be obtained by looping from 1 to $2^n - 1$ and performing a bitwise operation on each number to determine whether the character is selected or not.

No code needed