

### DIGITAL LOGIC

## Chapter 5 part2: Synchronous Sequential Logic

2023 Fall

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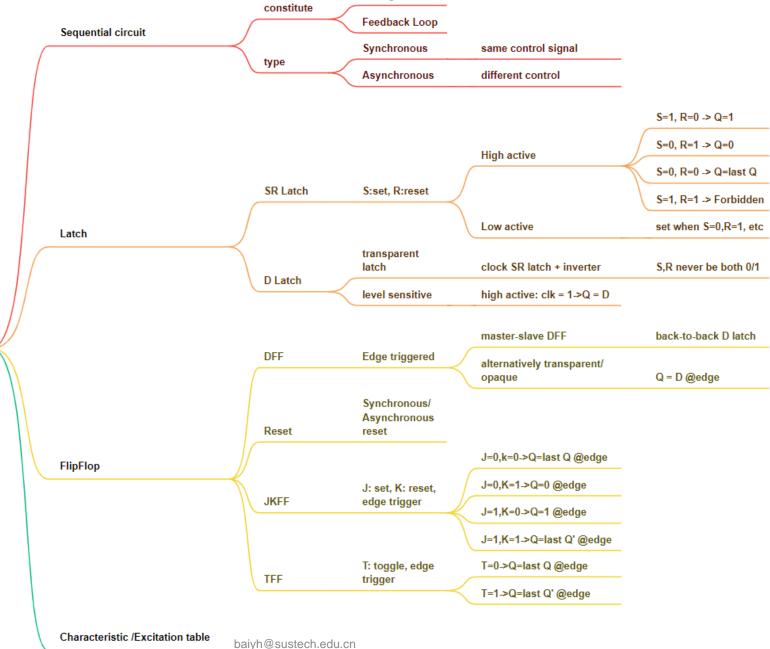
## Today's Agenda

- Recap
- Context
  - Finite State Machine
  - Analysis of Clocked Sequential Circuit
  - Designing Clocked Sequential Circuits
- Reading: Textbook, Chapter 5.5-5.8



Recap

Lec7 Latch/FF

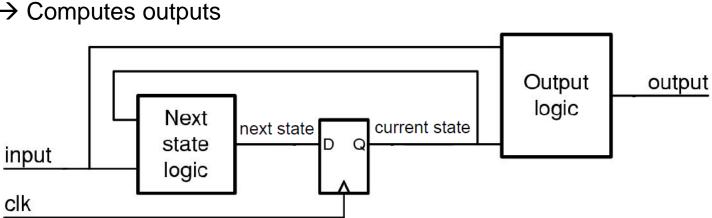


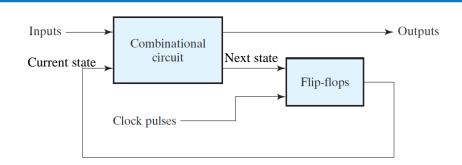
Storage Element



# Synchronous Sequential Logic

- State register
  - FlipFlop
    - Stores current state
    - Loads next state at clock edge
- Combinational circuit
  - (inputs, current state) => (outputs, next state)
  - Can be divided into two parts:
    - Next state logic → Computes next state
    - Output logic → Computes outputs







## **Outline**

- Analysis of Sequential Circuits
- Finite State Machine
- State Minimization & Encoding
- Design of Sequential Circuits



# Ways to describe a digital circuit

- logic diagram (逻辑电路图)
  - · graphical representation of a digital circuit that uses standard symbols
- K-map (卡诺图)
  - graphical representation of a logic function used to simplify Boolean expressions
- function table (功能表)
  - (truth table), list of all possible input combinations and the corresponding output values for a given logic function
- characteristic equations (特征方程)
  - Describe the behavior of a sequential logic circuit, the next state is defined as a function of the inputs and the present state
- excitation/input equation (激励方程).
  - Defines the part of the circuit that generates the inputs to sequential logic circuit
- state table (状态表)
  - tabular representation of a sequential logic circuit that shows the current state, input, next state, and output for all possible input combinations
- state equation (次态方程)
  - · defines the next state of a sequential logic circuit based on the current state and input values
- state diagram (状态图)
  - graphical representation of a sequential logic circuit that shows the states, transitions, and input-output relationships



# **Analysis Procedure of Clocked Sequential Circuits**

- 1. Derive excitation/input equations for FF inputs
- 2. Derive state and output equations
  - Substitute the excitation equations into the flip-flop characteristic equations to obtain next state equations.
  - Determine the output equations according current state and input
- 3. Generate state and output tables
- 4. Generate state diagram
- Develop timing diagram
- Simulate logic schematic

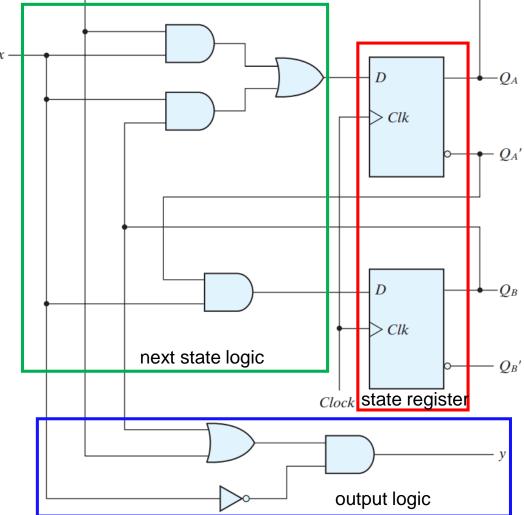
Important: FF's Characteristic equation:

- DFF Q(t+1) = D(t)
- JKFF Q(t+1) = J(t)Q(t)' + K(t)'Q(t)
- TFF Q(t+1) = T(t)'Q(t) + T(t)Q(t)'



# Analysis Example 1: A sequential circuit using DFF

- 1. Derive excitation/input equations for FF inputs
- 2. Derive state and output equations
- 3. Generate state and output tables
- 4. Generate state diagram



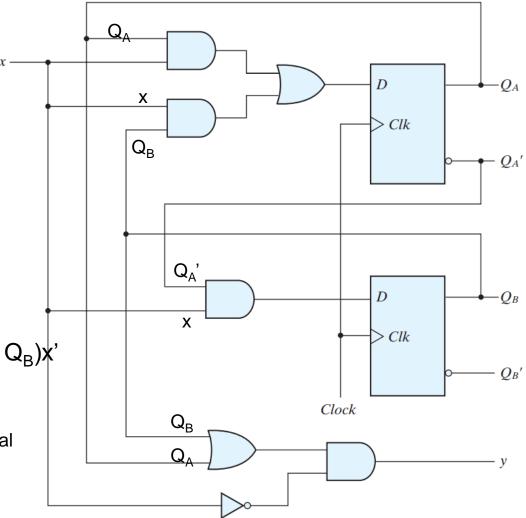


# **Example 1: A sequential circuit using DFF**

- Flip-Flop excitation/input equation
  - $D_A = Q_A x + Q_B x$
  - $D_B = Q_A'x$
- State equation
  - $Q_A(t+1) = D_A(t)$ =  $Q_A(t)x(t) + Q_B(t)x(t)$
  - $Q_B(t+1) = D_B(t) = Q_A'(t)x(t)$
  - Output equation
    - $y(t) = (Q_A(t) + Q_B(t))x'(t)$
    - all signals are labeled by t, thus y = (Q<sub>A</sub> + Q<sub>B</sub>)x<sup>3</sup>

Next state and output circuit are combinational (regardless of time)

Substituting input equation into DFF's charc. equation Q(t+1) = D(t) baiyh@sustech.edu.cn





> Clk

 $-Q_{A}'$ 

# Analysis Example 1: A sequential circuit using DFF

2 
$$Q_A(t+1) = Q_A(t)x(t) + Q_B(t)x(t)$$
  
 $Q_B(t+1) = Q_A'(t)x(t)$   
 $y = (Q_A + Q_B)x'$ 

3

Generate state and output tables

First Form of	f the State To	able		
Present State	Input	Next State	Output	
$Q_A Q_B$	x	$Q_A Q_B$	<i>y</i>	
0 0	0	0 0	0	Clk
0 0	1	0 1	0	> Clk
0 1	0	0 0	1	
0 1	1	1 1	0	Clock
1 0	0	0 0	1	
1 0	1	1 0	0	
1 1	0	0 0	1	
1 1	1	1 0	ba <b>Q</b> h@sustech.€	edu.cn



# Analysis Example 1: A sequential circuit using DFF

- Generate state and output tables
  - Two forms of state table, use the one you prefer:
    - 1st form: state table has 2m+n rows for m FFs and n inputs,
    - 2<sup>nd</sup> form has three sections, with input in the next state and output column.

First Form of the State Table

Present State		Input	Ne Sta		Output
$Q_A$	$Q_B$	X	$Q_A$	$Q_B$	y
0	0	0	0	0	0
0	0	1	0	1	0
0	1	0	0	0	1
0	1	1	1	1	0
1	0	0	0	0	1
1	0	1	1	0	0
1	1	0	0	0	1
1	1	1	1	0	0

#### Second Form of the State Table

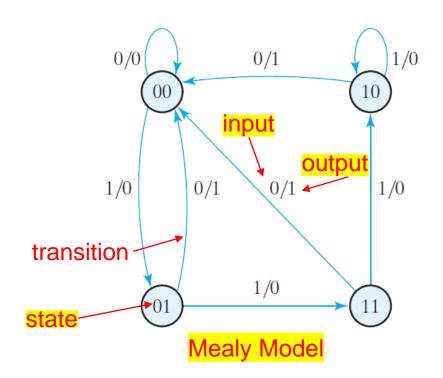
Duccont		ext	Stat	Output		
ate	<i>x</i> =	0	<b>x</b> :	= 1	x = 0	<i>x</i> = 1
$Q_{B}$	$\overline{Q_{A}}$	$Q_B$	$Q_A$	$Q_{B}$	<i>y</i>	y
0	0	0	0	1	0	0
1	0	0	1	1	1	0
0	0	0	1	0	1	0
1	0	0	1	0	1	0
	<b>Q</b> <sub>B</sub> 0 1	esent ate $x = \frac{\mathbf{Q_A}}{\mathbf{Q_A}}$ $0 \qquad 0$ $1 \qquad 0$ $0 \qquad 0$	x = 0       Q <sub>B</sub> Q <sub>A</sub> Q <sub>B</sub> 0     0       1     0       0     0	Assent ate $x = 0$ $x = 0$ $Q_B$ $Q_A$ $Q_B$ $Q_A$ 0     0     0     0       1     0     0     1       0     0     0     1       0     0     0     1	ate $x = 0$ $x = 1$ $Q_B$ $Q_A$ $Q_B$ $Q_A$ $Q_B$ 0     0     0     0     1       1     0     0     1     1       0     0     1     0	x = 0     x = 1       Q <sub>B</sub> Q <sub>A</sub> Q <sub>B</sub> Q <sub>A</sub> Q <sub>B</sub> y       0     0     0     1     0       1     0     0     1     1       0     0     0     1     0       1     0     0     1     0       0     0     0     1     0       1     0     0     1     0       0     0     0     1     0



Output

# Analysis Example 1: A sequential circuit using DFF

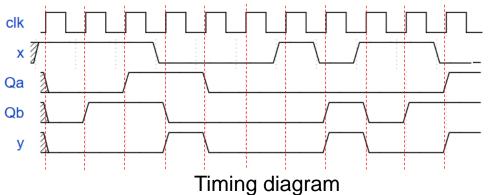
- 4 Generate state diagram
  - Each state as a circle.
  - Transitions between states are directed



#### Second Form of the State Table

Present			CAL	Jtu		Out	put
	ate	<b>x</b> =	0	<b>X</b> :	= 1	x = 0	<i>x</i> = 1
$Q_A$	$Q_B$	$Q_A$	$Q_B$	$Q_A$	Q <sub>B</sub>	y	y
0	0	0	0	0	1	0	0
0	1	0	0	1	1	1	0
1	0	0	0	1	0	1	0
1	1	0	0	1	0	1	0

**Next State** 



x and initial state of  $Q_AQ_B$  are given as an example

# Analysis Example 2: A sequential circuit using



**JKFF** 

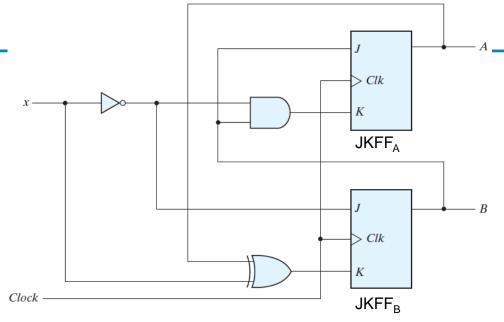
#### Excitation/Input equation

$$J_A = B,$$
  
 $K_A = Bx',$   
 $J_B = x',$   
 $K_B = A \oplus x.$ 



#### State equation

$$A(t+1) = J_A A' + K_A' A = BA' + (Bx')' A$$
  
 $B(t+1) = J_B B' + K_B' B = x' B' + (A \oplus x)' B$ 



(t) is omitted on the RHS Should be A(t+1) = B(t)A(t)'+(B(t)x(t)')'A(t)Similarly for B(t+1)

- Output equation
  - No extra output equation since output comes from the output of JKFF(state Q)

# Analysis Example 2: A sequential circuit using JKFF



2

State equation

$$A(t+1) = J_A A' + K_A' A = BA' + (Bx')' A$$
  
 $B(t+1) = J_B B' + K_B' B = x' B' + (A \oplus x)' B$ 

3

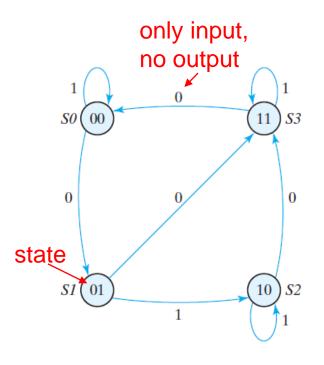
State table

State Table for Sequential Circuit with JK Flip-Flops

	sent ate	Input		ext ate	Flip-Flop Inputs			
A	В	X	A	В	J <sub>A</sub>	$K_A$	<b>J</b> <sub>B</sub>	K <sub>B</sub>
0	0	0	0	1	0	0	1	0
0	0	1	0	0	0	0	0	1
0	1	0	1	1	1	1	1	0
0	1	1	1	0	1	0	0	1
1	0	0	1	1	0	0	1	1
1	0	1	1	0	0	0	0	0
1	1	0	0	0	1	1	1	1
1	1	1	1	1	1	0	0	0

$$J_A = B,$$
  
 $K_A = Bx',$   
 $J_B = x',$   
 $K_B = A \oplus x.$ 

• Generate state diagram



Next state value can be obtained from state equation, or from corresponding FF's inputs e.g. for 1st line,  $J_A = K_A = 0 \rightarrow A(t+1) = A(t) = 0$ ;  $J_B = 1$ ,  $K_B = 0 \rightarrow B(t+1) = 1$ 



# Analysis Example 3: A sequential circuit using TFF

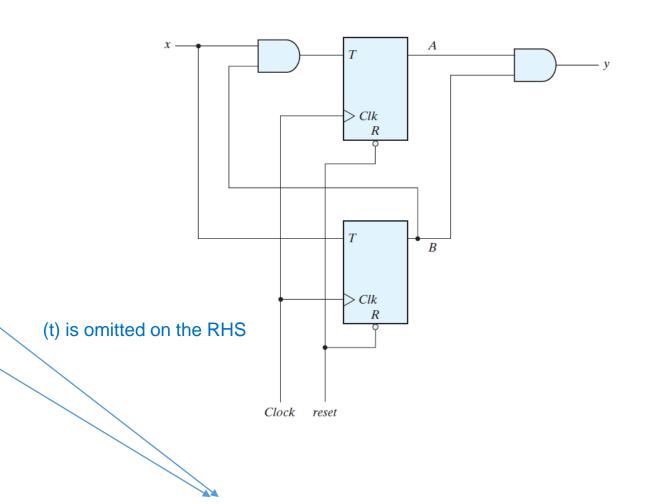
• Excitation/Input equation

$$T_A = Bx$$
  
 $T_B = x$ 

• state equation

$$A(t +1) = T_A \oplus Q_A = (Bx) \oplus A$$
  
$$B(t +1) = T_B \oplus Q_B = x \oplus B$$

Output equationy = AB



Substituting input equation into TFF's charc. Equation  $Q(t+1) = T(t) \oplus Q(t)$ 



# Analysis Example 3: A sequential circuit using TFF

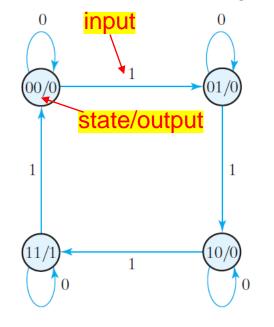
• state/output equation

$$A(t+1) = (Bx) \oplus A = (Bx)'A+(Bx)A' = AB' +Ax' +A'Bx$$
 
$$B(t+1) = x \oplus B$$
 
$$y = AB$$

3 • state table

Present State		Input		ext ate	Output	
Α	В	X	A	В	y	
0	0	0	0	0	0	
0	0	1	0	1	0	
0	1	0	0	1	0	
0	1	1	1	0	0	
1	0	0	1	0	0	
1	0	1	1	1	0	
1	1	0	1	1	1	
1	1	1	0	0	1	

Generate state diagram



**Moore Model** 



## **Outline**

- Analysis of Sequential Circuits
- Finite State Machine
- State Minimization & Encoding
- Design of Sequential Circuits

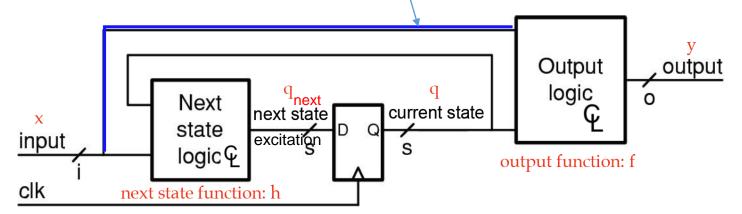


Recall: Combination

logic:  $f: x \rightarrow y$ 

# Finite State Machine (FSM)

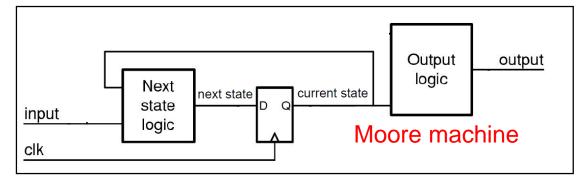
- A synchronous sequential circuit can be modeled by FSM
- State register q(t + 1) = qnext(t)
  - Stores current state
  - Loads next state at clock edge
- Combinational logic
  - Computes next state (next state logic h:  $x \times q \rightarrow qnext$ )
  - Computes outputs
    - output logic f:  $x \times q \rightarrow y$  (Mealy machine, with blue line)
    - or f:  $q \rightarrow y$  (Moore machine, without blue line)

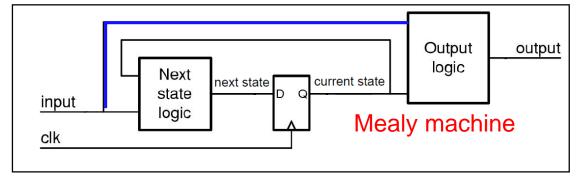




# Finite State Machine (FSM)

- A synchronous sequential circuit can be modeled by FSM (有限状态机)
  - Two types of finite state machines differ in output logic:
  - Moore FSM: outputs depend only on current state
  - Mealy FSM: outputs depend on current state and inputs

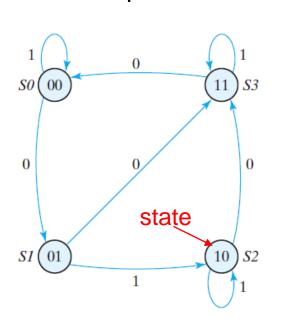




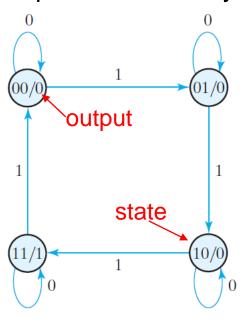


## **Models for Sequential Circuits**

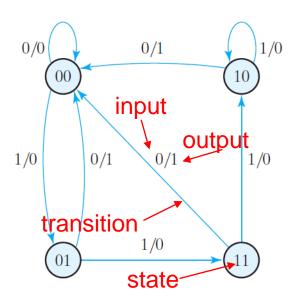
- Moore Model
- Mealy Model: To synchronize a Mealy circuit, the inputs must be synchronized with the clock and the outputs must be sampled immediately before the clock edge



Example of JKFF no output, only state



Example of TFF Moore Model



Example1
Mealy Model



## **Outline**

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# **State Minimization (Reduction)**

#### State reduction

- Reductions on the number of flip-flops (states) and the number of gates
- For an FSM with m states, we need log₂m FFs

### Definition for FSM equivalence

- (1) Given any input sequence, starting from any identical initial state, they produce the same output sequence.
- (2) Two states,  $s_j$  and  $s_k$  in an FSM are said to be equivalent  $(s_j \equiv s_k)$ , if  $\forall i \in x, h(s_j, i) = h(sk, i), \forall i \in x, f(s_j, i) = f(sk, i)$  (h is the state equation, f is the output equation)

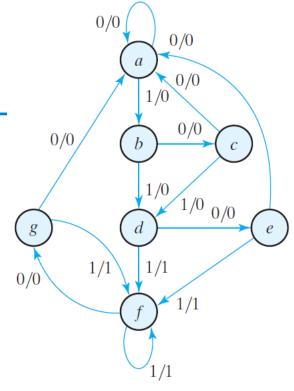
#### Reduction steps

- 1. Find rows in the state table that have identical next state and output entries. They correspond to equivalent states. If there are no equivalent states, stop.
- 2. When 2 states are equivalent, one of them can be removed. Update the entries of the remaining table to reflect the change. Go to 1.



#### State Table

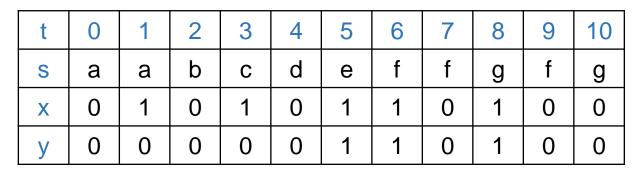
	Next	State	Output		
Present State	x = 0	x = 1	x = 0	<i>x</i> = 1	
а	а	b	0	0	
b	c	d	0	0	
С	a	d	0	0	
d	e	f	0	1	
e	a	f	0	1	
f	g	f	0	1	
g	а	f	0	1	

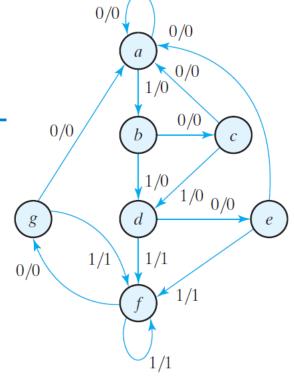


t	0	1	2	3	4	5	6	7	8	9	10
S	а	а	b	С	đ	Φ	f	f	g	f	g
X	0	1	0	1	0	1	1	0	1	0	0
У	0	0	0	0	0	1	1	0	1	0	0

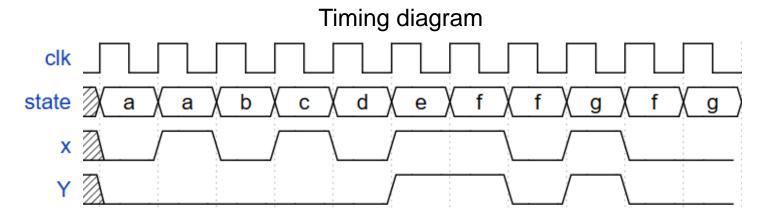
I/O sequence based on input pattern x and initial state being a







I/O sequence



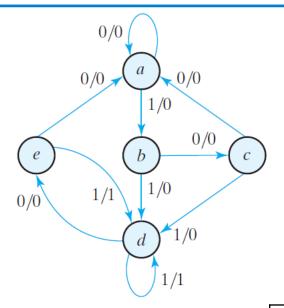


	Next	State	Output		
<b>Present State</b>	x = 0	x = 1	x = 0	<i>x</i> = 1	
а	а	b	0	0	
b	c	d	0	0	
С	a	d	0	0	
d	e	f	0	1	
==g_ e	а	f	0	1	
f	Хe	f	0	1	
	а	f	0	1	

1st turn

	Next	State	Output		
Present State	x = 0	x = 1	x = 0	x = 1	
а	а	b	0	0	
b	c	d	0	0	
c	a	d	0	0	
<b>=</b> f	е	⅓d	0	1	
e	а	⅓d	0	1	
f	е	f	0	1	





#### **Reduced State Table**

	Next	State	Output		
Present State	x = 0	x = 1	x = 0	<i>x</i> = 1	
а	а	b	0	0	
b	С	d	0	0	
c	а	d	0	0	
d	е	d	0	1	
е	a	d	0	1	

Reduced state diagram

t	0	1	2	3	4	5	6	7	8	9	10
S	а	а	b	С	d	е	d	d	е	d	е
X	0	1	0	1	0	1	1	0	1	0	0
у	0	0	0	0	0	1	1	0	1	0	0

Resulting I/O sequence with the same input pattern x and initial state being a



# State Encoding/Assignment

- Different state encodings (assignments) result in different circuits for the intended FSM.
- There is no easy state-encoding procedure that guarantees a minimal-cost or minimum-delay combinational circuits
  - Exploration of all possibilities are impossible.
  - Heuristic are often used
    - Binary counting
    - Minimum-bit change
    - One-hot encoding



# **State Encoding/Assignment**

 One-hot encoding usually leads to simpler decoding logic for the next state and output.

Three Possible Binary State Assignments

State	Assignment 1, Binary	Assignment 2, Gray Code	Assignment 3, One-Hot
a	000	000	00001
b	001	001	00010
$\boldsymbol{c}$	010	011	00100
d	011	010	01000
e	100	110	10000

#### Reduced State Table with Binary Assignment 1

	Next	State	Output		
Present State	x = 0	<i>x</i> = 1	x = 0	<i>x</i> = 1	
000	000	001	0	0	
001	010	011	0	0	
010	000	011	0	0	
011	100	011	0	1	
100	<b>0:0,0</b> @si	usteo <b>().∳</b> d[u.cn	0	1	



## **Outline**

- Analysis of Sequential Circuits
- Finite State Machine
- State Minimization & Encoding
- Design of Sequential Circuits



# **Design Procedure of Sequential Circuits**

- 1. Specification: design description or timing diagram
- 2. Formulation: develop state diagram
- 3. Generate state and output tables
- 4. Minimize States if necessary
- 5. Assign binary values to the state (encoding)
- 6. Derive state and output equations
- 7. Choose memory elements (DFFs, JKFFs, TFFs)
- 8. Derive simplified excitation/input equations and output equations
- 9. Draw logic schematic



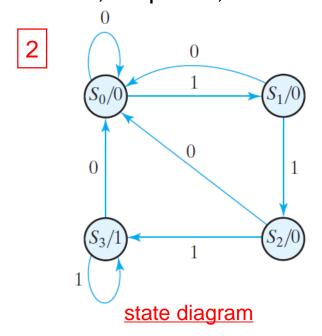
# **Choice of Memory Elements**

- Given the state transition table, we wish to find the FF input conditions that will cause the required transition.
  - A tool for such a purpose is the excitation table, which can be derived from the characteristic table/equation.
  - D FFs are good for applications requiring data transfer (shift registers).
  - T FFs are good for those involving complementation (binary counters).
  - Many digital systems are constructed entirely with JK FFs because they are the most versatile available.

# Design Example 1: Design with DFF: A Sequence Detector

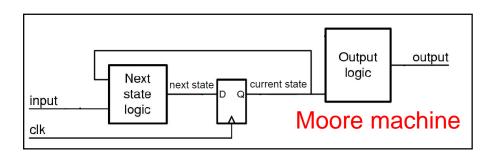


- Detect three consecutive 1's in a string of bits (using Moore machine, overlapping)
  - If detected, output=1; otherwise output=0





Overlapping: detection window can be overlapped







\* Next state and output table

4 already minimal states

Present	Next State		Output		
State	x=0	x=1	x=0	x=1	
S <sub>0</sub>	$S_0$	$S_1$	0	0	
$S_1$	$S_0$	S <sub>2</sub>	0	0	
$S_2$	$S_0$	$S_3$	0	0	
S <sub>3</sub>	$S_0$	$S_3$	1	1	

5

Reduced state table and state assignment

Reduced State table that State assignment							
Present	Next	State (AB)	Output (y)				
State (AB)	x=0		x=0	x=1			
00	00	01	0	0			
01	00	10	0	0			
10	00	11	0	0			
11	00	11	1	1			

# Design Example 1: Design with DFF: A Sequence Detector



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State equation

$$A(t + 1) = D_{A}(A(t),B(t), x)$$

$$= \sum (3, 5, 7)$$

$$B(t + 1) = D_{B}(A(t),B(t), x)$$

$$= \sum (1, 5, 7)$$

Output equation

$$y(A,B, x) = \sum (6, 7)$$

- Choose DFFs (default)
  - State encoding using 2 bits, so 2 DFFs are needed
    - $A(t+1) = D_A(t)$
    - $B(t+1) = D_B(t)$

6

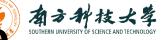
Reduced state table and state assignment

Present	Next State		Output (y)		
State (AB)	x=0		x=0	x=1	
00	00	01	0	0	
01	00	10	0	0	
10	00	11	0	0	
11	00	11	1	1	

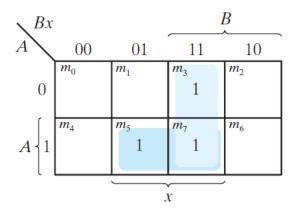
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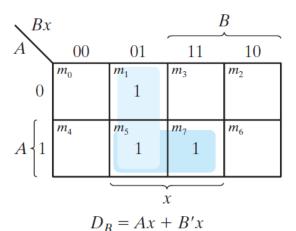
1st form	n state ta	<u>ble</u>	$D_A$	$D_B$	
A(t)	B(t)	X	A(t+1)	B(t+1)	у
0	0	0	0	0	0
0	0	1	0	1	0
0	1	0	0	0	0
0	1	1	1	0	0
1	0	0	0	0	0
1	0	1	1	1	0
1	1	0	0	0	1
1	1	1	1	1	1

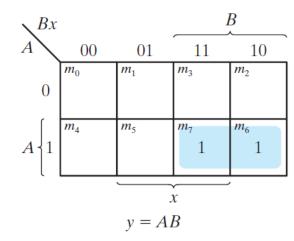
# Design Example 1: Design with DFF: A Sequence Detector



8 • Derive excitation equations and optimize logic implementation





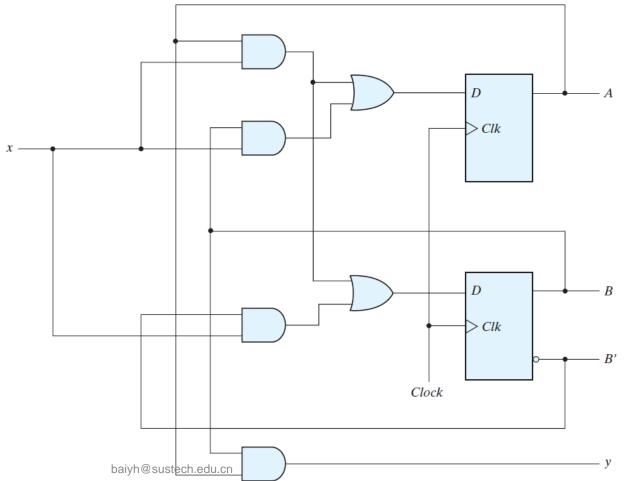


- Input/ $\vdash$ xcitation equations (minimized)
  - $D_A = Ax + Bx$
  - $D_B = Ax + B'x$
- Output equations (minimized)
  - y = AB

# **Detector**



- 9 Logic diagram
  - a **Moore-type** sequence detector
  - y depends only on A and B





#### FF's Excitation Table

• The FF's excitation table(input table) is derived from the FF's characteristic table by transposing input and output columns

Type	e Symbol Characteristic Table		ristic Table	Characteristic Equation	<b>Excitation Table</b>			ble				
0.0	-D -	Ι	)	Q(t+1)	Operation		Q	(t +1)	ı	)	Operation	
D	-> C	(	)	0	Reset	Q(t+1) = D(t)	0			)	Reset	
		]	<u> </u>	1	Set			1	1		Set	
		J	K	Q(t+1)	Operation		Q(t)	Q(t+1)	J	K	Operation	
	-J - -> C -K	-J - C - K	0	0	Q(t)	No change		0	0	0	Х	No change
JK			0	1	0	Reset	Q(t+1) = J(t) Q'(t) + K'(t) Q(t)	0	1	1	X	Set
		1	0	1	Set		1	0	X	1	Reset	
		1	1	Q'(t)	Complement		1	1	X	0	No Change	
			Т	Q(t+1)	Operation		Q(t)	Q(t +1)	7	Γ	Operation	
T	1		0	Q(t)	No change	$Q(t+1) = T(t) \oplus Q(t)$	0	0 1		0 1	No change	
	->C		1	Q'(t)	Complement		1 1	0 1		1	Complement	



#### Design Example 2: Design with JKFF

- 1
- Assume a state table as follows, design a sequential circuit with JKFF
  - Characteristics: date input x (and clock/reset of course)
  - The outputs can be the next states
- State table is directly provided, so step 2 is skipped

	sent ate	Input		ext ate
A	В	X	A	В
0	0	0	0	0
0	0	1	0	1
0	1	0	1	0
0	1	1	0	1
1	0	0	1	0
1	0	1	1	1
1	1	0	1	1
1	1	1 baiyh@sustech.edu.cn	0	0



### Design Example 2: Design with JKFF

- Design with JFKK has similar procedure as with DFF, except that we need to enhance the state table by evaluating the excitation table based on the state transition.
  - So we can then derive the input equations

3	_

4 5

State	Table a	ınd IK	Flir	2-Flo	n In	nuts
Jule	Tuble u	mu jn	гпр	<i>)-</i>	рш	puts

Present State		Input	Next State		Flip-Flop Inputs			
A	В	X	A	В	$/J_A$	$K_A$	J <sub>B</sub>	KB
0	0	0	0	0	0	X	0	Χ
0	0	1	0	1	0	X	1	X
0	1	0	1	0	1	X	X	1
0	1	1	0	1	0	X	X	0
1	0	0	1	0	X	0	0	X
1	0	1	1	1	X	0	1	X
1	1	0	1	1	X	0	X	0/
1	1	1	0	$Q_{\text{baiy}}$	h@susteeh.ec	<sub>lu.cn</sub> 1	X	1

Q(t)	Q(t + 1)	J	K
0	0	0	X
0	1	1	X
1	0	X	1
1	1	X	0

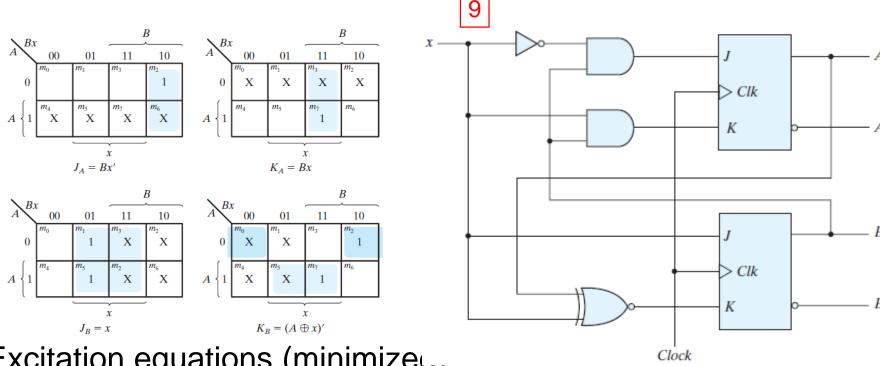
Evaluating in advance the FF inputs based on excitation table

 Input equation will be evaluated when choosing JKFFs



### Design Example 2: Design with JKFF

Derive excitation equations and optimize logic implementation



• Input/Excitation equations (minimize,

$$J_A = Bx', \quad J_B = x,$$
  
 $K_A = Bx, \quad K_B = (A \oplus x)'.$  baiyh@sustech.edu.cn

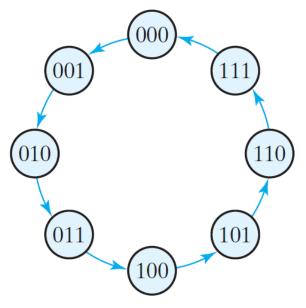
#### arv



# Design Example 3: Design with TFF: A Binary Counter

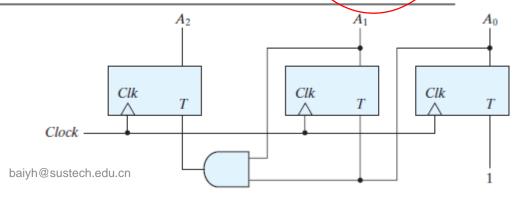
 Characteristics: No date input (except clock/reset), The outputs can be the next states

Q(t)	Q(t+1)	T
0	0	0
0	1	1
1	0	1
1	1	0



	$=A_1A_0$
	$=A_0$
$T_{A0}$	=1

Present State			<b>Next State</b>			Flip-Elop Inputs		
A <sub>2</sub>	A <sub>1</sub>	<i>A</i> <sub>0</sub>	A <sub>2</sub>	<i>A</i> <sub>1</sub>	<i>A</i> <sub>0</sub>	T <sub>A2</sub>	<i>T<sub>A1</sub></i>	TAO
0	0	0	0	0	1	0	0	1
0	0	1	0	1	0	0	1	1
0	1	0	0	1	1	0	0	1
0	1	1	1	0	0	1	1	1
1	0	0	1	0	1	0	0	1
1	0	1	1	1	0	0	1	1
1	1	0	1	1	1	\ 0	0	1 /
1	1	1	0	0	0	\1	1	1



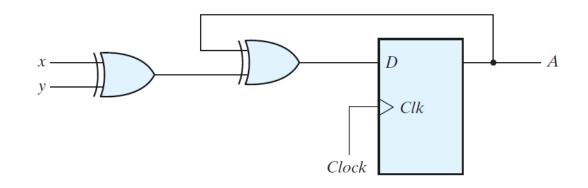


#### **Summary**

- Finite State Machine
  - Moore Machine
  - Mealy Machine
- Analysis and design of clocked sequential circuits: Recommended steps.
- Ways to describe a sequential circuit:
- Function table, state table, state diagram, next state equation, logic diagram, excitation table, K-map



#### **Exercise1: Analyze DFF base sequential circuit**



- 1. Excitation/Input equation
- 2. state equation, Output equation?
- 3. state table, Output table?
- 4. Generate state diagram



#### **Exercise1: Analyze DFF base sequential circuit**

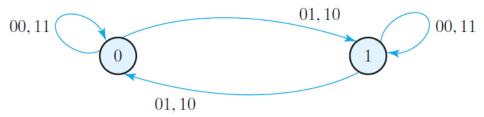
• Excitation/Input equation

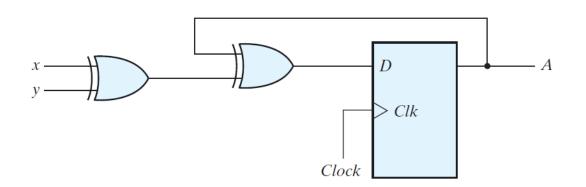
$$D_A = A \oplus x \oplus y$$

• state equation

$$A(t+1) = A(t) \oplus x(t) \oplus y(t)$$

- state table
  - No output equation since output comes from the output of DFF(state Q)
- Generate state diagram





state	Input	s state
A	x y	A
0	0 0	0
0	0 1	1
0	1 0	1
0	1 1	0
1	0 0	1
1	0 1	0
1	1 0	0
1	1 1	1

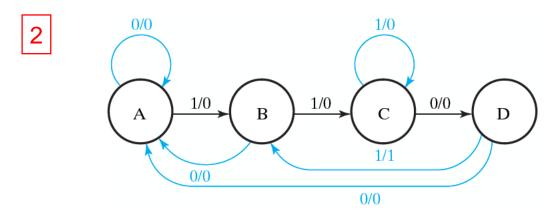
baiyh@sustech.edu.cn



 Recognize the occurrence of a particular sequence of bits (1101) (Mealy machine, overlapping, using gray code for state assignment)



 Recognize the occurrence of a particular sequence of bits (1101) (Mealy machine, overlapping, using gray code for state assignment)



3	Present	Next	State	Output Z		
4	State	X = 0	X = 1	X = 0	X = 1	
	A B C D	A A D A	B C C B	0 0 0 0	0 0 0 1	



#### state assignment with 2-bit binary Gray code

	5
ı	

Present State	Next State		Output <i>Z</i>	
AB	X = 0	X = 1	X = 0	X = 1
00	00	01	0	0
01	00	11	0	0
11	10	11	0	0
10	00	01	0	1



$$A(t+1) = D_A(A(t), B(t), X) = \sum (3, 6, 7) = AB + BX$$

$$B(t+1) = D_B(A(t), B(t), X) = \sum (1, 3, 5, 7) = X$$
  
 $Z(A, B, X) = \sum (5) = A\bar{B}X$ 

#### 1st form state table

	rent ate	Input	Next State		Output
Α	В	Х	Α	В	Z
0	0	0	0	0	0
0	0	1	0	1	0
0	1	0	0	0	0
0	1	1	1	1	0
1	0	0	0	0	0
1	0	1	0	1	1
1	1	0	1	0	0
1	1	1	1	1	0



