

1--3. Solve matrix games: If you cannot find optimal strategies, give the best you can find.

1.

0	5	3	4	5	3	3
0	1	4	5	4	6	3
1	2	6	5	5	7	0
0	0	1	1	4	2	0
1	1	4	3	2	4	0
1	1	2	1	3	6	3

Use  $\Delta$  for row min and  $\nabla$  for column max

Saddle point at boxed position

Since there is a Saddle Point Value of Game = 1An optimal strategy for the row player is  $[0, 0, 0, 0, 0, 1]^T$ An optimal strategy for the column player is  $[1, 0, 0, 0, 0, 0]$ 

2.

1	2	3	1	2	4	0
3	1	4	4	2	4	0
3	3	2	0	4	3	1
4	1	4	0	2	3	2
0	1	2	4	2	1	3

3.

2	0	2	-2
2	-2	-1	2
4	2	0	1

4. Solve for  $x, y$ 

$$x + ty = 3$$

$$2x + ty = 3$$

With Given problem we have the augmented matrix

$$\begin{array}{c|c} 1 & 3 \\ 2 & 3 \end{array} \xrightarrow{-2R_1 + R_2} \begin{array}{c|c} 1 & 3 \\ 0 & -3 \end{array}$$

if  $t \neq 0$   $y = 3/t$  and  $x = 3 - yt = 3 - 3/t$   $t = 3 - 3 = 0$   
if  $t = 0$  there are no solutions
where  $t$  is a given number.

5. Find the mean, the midrange, and the central value for the following numbers:

0, -1, 3, 4, 5, -1, 7, 0, 9, 0, 0, -1, -2.

Ordering the numbers we have

 $-2, -1, -1, -1, 0, 0, 0, 0, 3, 4, 5, 7, 9$  there are 13 numbers

the mean is the sum of all values divided by the number of values thus

$$\text{Mean} = \frac{-2 + -1 + -1 + -1 + 0 + 0 + 0 + 0 + 3 + 4 + 5 + 7 + 9}{13} = \frac{23}{13}$$

$$\text{midrange} = \frac{9 + -2}{2} = \frac{7}{2}$$

this is the max value + min value divided by 2

$$\text{Central value} = 0$$

Since there are 13 numbers the central value occurs at the middle i.e. the 7<sup>th</sup> number