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And what do we do about it?

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And what do we do about it?

- Can you think of a context where counts show less-than-Poisson variation?

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No. Deaths in corps-year	Frequencies (No. "corps-years" with y deaths)		
y	Observed	Expected ^{\$}	$y \times \text{Obs. Freq.}$
0	109	108.7	0
1	65	66.3	65
2	22	20.2	44
3	3	4.1	9
4	1	0.6	4
5	-	0.1	-
Sum:	200	200	No. Deaths: 122

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What about decade-to-decade variations in U.S. Hurricane Strikes?

Number of hurricanes by [Saffir-Simpson Category](#) to strike the mainland U.S. each decade.

Decade	Saffir-Simpson Category ¹					All 1,2,3,4,5	Major 3,4,5
	1	2	3	4	5		
1851-1860	8	5	5	1	0	19	6
1861-1870	8	6	1	0	0	15	1
1871-1880	7	6	7	0	0	20	7
1881-1890	8	9	4	1	0	22	5
1891-1900	8	5	5	3	0	21	8
1901-1910	10	4	4	0	0	18	4
1911-1920	10	4	4	3	0	21	7
1921-1930	5	3	3	2	0	13	5
1931-1940	4	7	6	1	1	19	8
1941-1950	8	6	9	1	0	24	10
1951-1960	8	1	5	3	0	17	8
1961-1970	3	5	4	1	1	14	6
1971-1980	6	2	4	0	0	12	4
1981-1990	9	1	4	1	0	15	5
1991-2000	3	6	4	0	1	14	5
2001-2004	4	2	2	1	0	9	3
1851-2004	109	72	71	18	3	273	92
Average Per Decade	7.1	4.7	4.6	1.2	0.2	17.7	6.0

¹ [Saffir-Simpson Hurricane Wind Scale](#)

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Simulate 15 decades \pm a time pattern: `summary(rpois(15, lambda= ..))`

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Source: <https://www.nhc.noaa.gov/pastdec.shtml>

Rate of *de novo* mutations and the importance of father's age to disease risk

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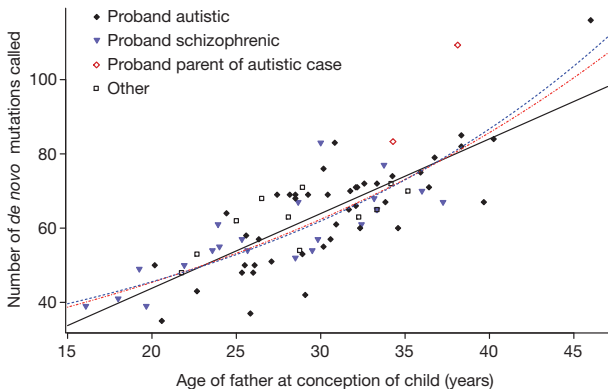


Figure 2 | Father's age and number of *de novo* mutations. The number of *de novo* mutations called is plotted against father's age at conception of child for the 78 trios. The solid black line denotes the linear fit. The dashed red curve is based on an exponential model fitted to the combined mutation counts. The dashed blue curve corresponds to a model in which maternal mutations are assumed to have a constant rate of 14.2 and paternal mutations are assumed to increase exponentially with father's age.

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<http://www.epi.mcgill.ca/hanley/bios601/FathersAgeMutations.pdf>

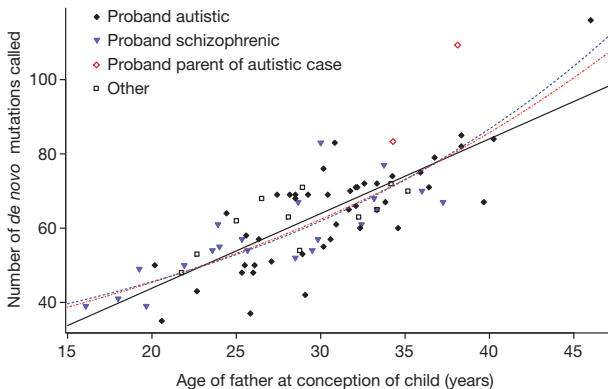


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$$\mu[y|age] \approx 2 \times age; \approx \text{Poisson variation of } y\text{'s around each } \mu[y|age]; \text{ i.e. } \sigma[y|x] \approx \sqrt{\mu[y|age]}$$

What events are these?

<http://www.epi.mcgill.ca/hanley/mysteryData/>

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2	468
3	429
4	448
5	466
6	377
7	344
8	448
9	438
10	455
11	468
12	462
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Statistics (2nd Ed) by D Freedman, R Pisani et al

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Aug.	Births	Day
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2	468	Tue
3	429	Wed
4	448	Thu
5	466	Fri
6	377	Sat
7	344	Sun
8	448	Mon
9	438	Tue
10	455	Wed
11	468	Thu
12	462	Fri
13	405	Sat
14	377	Sun
15	451	Mon
16	497	Tue
17	458	Wed
18	429	Thu
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Closer to Poisson variation if use week as unit, or if one 'conditions on' day-of-week; Over the year, some variation in weekly numbers.

Freedman cites Izenman & Zabel, "Babies and the blackout: the genesis of a misconception," Soc. Sci. Res., 1981, 282- 99. available here <http://www.epi.mcgill.ca/hanley/bios601/Intensity-Rate/GenesisOfAMisconception.pdf>

Daily (and hourly!) variations in numbers of births

<https://www.significancemagazine.com/585> and <https://rss-onlinelibrary-wiley-com.proxy3.library.mcgill.ca/doi/full/10.1111/j.1740-9713.2017.01026.x> or <http://www.epi.mcgill.ca/hanley/mysteryData/>

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2	158	187.9
3	115	143.6
4	78	82.3
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- Ignoring this variation makes for (model-based) Standard Errors (SE's) and CI's that are too narrow, and that can lead to ‘false positive’ findings
- Encoding this (not identifiable) variation in ‘random effects’ or ‘random-intercept’ regression models makes for more realistic SE's and CI's.

<http://www.epi.mcgill.ca/hanley/bios601/Intensity-Rate/AccidentsBusDrivers.pdf>

DAYLIGHT SAVINGS TIME AND TRAFFIC ACCIDENTS, NEJM 1996.04,04

DAYLIGHT SAVINGS TIME AND TRAFFIC ACCIDENTS

To the Editor: It has become increasingly clear that insufficient sleep and disrupted circadian rhythms are a major public health problem. For instance, in 1988 the cost of sleep-related accidents exceeded \$56 billion and included 24,318 deaths and 2,474,430 disabling injuries.¹ Major disasters, including the nuclear accident at Chernobyl, the *Exxon Valdez* oil spill, and the destruction of the space shuttle *Challenger*, have been linked to insufficient sleep, disrupted circadian rhythms, or both on the part of involved supervisors and staff.^{2,3} It has been suggested that as a society we are chronically sleep-deprived⁴ and that small additional losses of sleep may have consequences for public and individual safety.²

<https://www.nejm.org/doi/full/10.1056/>

NEJM199604043341416

We can use noninvasive techniques to examine the effects of minor disruptions of circadian rhythms on normal activities if we take advantage of annual shifts in time keeping. More than 25 countries shift to daylight savings time each spring and return to standard time in the fall. The spring shift results in the loss of one hour of sleep time (the equivalent in terms of jet lag of traveling one time zone to the east), whereas the fall shift permits an additional hour of sleep (the equivalent of traveling one time zone to the west). Although one hour's change may seem like a minor disruption in the cycle of sleep and wakefulness, measurable changes in sleep pattern persist for up to five days after each time shift.⁵ This leads to the prediction that the spring shift, involving a loss of an hour's sleep, might lead to an increased number of "microsleeps," or lapses of attention, during daily activities and thus might cause an increase in the probability of accidents, especially in traffic. The additional hour of sleep gained in the fall might then lead conversely to a reduction in accident rates.

We used data from a tabulation of all traffic accidents in Canada as they were reported to the Canadian Ministry of Transport for the years 1991 and 1992 by all 10 provinces. A total of 1,398,784 accidents were coded according to the date of occurrence. Data for analysis were restricted to the Monday preceding the week of the change due to daylight savings time, the Monday immediately after, and the Monday one week after the change, for both spring and fall time shifts. Data from the province of Saskatchewan were excluded because it does not observe daylight savings time. The analysis of the spring shift included 9593 accidents and that of the fall shift 12,010. The resulting data are shown in Figure 1.

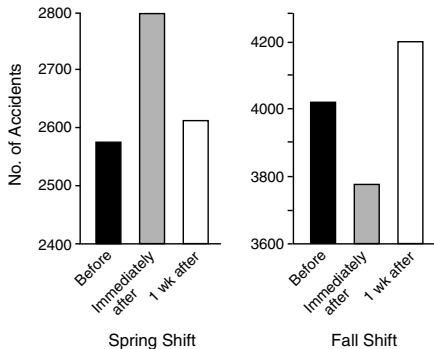


Figure 1. Numbers of Traffic Accidents on the Mondays before and after the Shifts to and from Daylight Savings Time for the Years 1991 and 1992.

There is an increase in accidents after the spring shift (when an hour of sleep is lost) and a decrease in the fall (when an hour of sleep is gained).

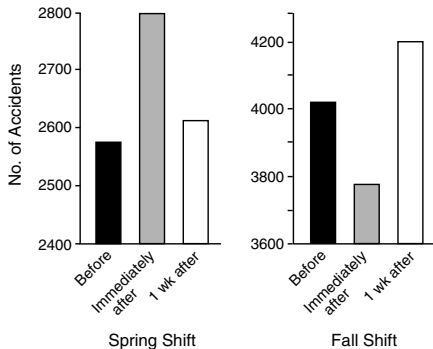


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to daylight savings time increased the risk of accidents. The Monday immediately after the shift showed a relative risk of 1.086 (95 percent confidence interval, 1.029 to 1.145; $\chi^2=9.01$, 1 df; $P<0.01$). As compared with the accident rate a week later, the relative risk for the Monday immediately after the shift was 1.070 (95 percent confidence interval, 1.015 to 1.129; $\chi^2=6.19$, 1 df; $P<0.05$). Conversely, there was a reduction in the risk of traffic accidents after the fall shift from daylight savings time when an hour of sleep was gained. In the fall, the relative risk on the Monday of the change was 0.937 (95 percent confidence interval, 0.897 to 0.980; $\chi^2=8.07$, 1 df; $P<0.01$) when compared with the preceding Monday and 0.896 (95 percent confidence interval, 0.858 to 0.937; $\chi^2=23.69$; $P<0.001$) when compared with the Monday one week later. Thus, the spring shift to daylight savings time, and the concomitant loss of one hour of sleep, resulted in an average increase in traffic accidents of approximately 8 percent, whereas the fall shift resulted in a decrease in accidents of approximately the same magnitude immediately after the time shift.

These data show that small changes in the amount of sleep that people get can have major consequences in everyday activities. The loss of merely one hour of sleep can increase the risk of traffic accidents. It is likely that the effects are due to sleep loss rather than a nonspecific disruption in circadian rhythm, since gaining an additional hour of sleep at the fall time shift seems to decrease the risk of accidents.

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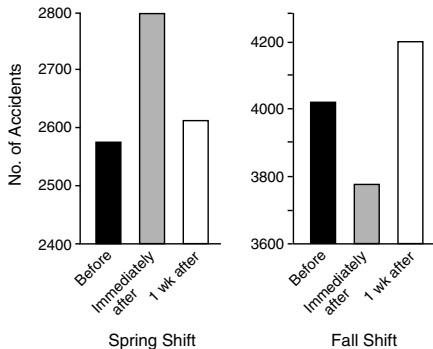


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Vincent: <http://www.epi.mcgill.ca/hanley/bios601/Intensity-Rate/Sleep-Vincent.pdf> The results of both a graphical analysis and the variability estimation of 10 years of data failed, as had an earlier study, to support Coren's hypothesis. [JH: Coren's χ^2 statistic assumes that the 2 'before' counts are like 2 Geiger counts generated by a uniform source, and ignores all outside influences.]

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- Lethality of Civilian Active Shooter Incidents With and Without Semiautomatic Rifles in the United States [The authors used a negative binomial model that allows extra-Poisson variation.] A bootstrap CI would also be appropriate.
<https://jamanetwork.com/journals/jama/fullarticle/2702134>

Is Poisson Model appropriate for?

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1. Yearly Numbers of Dengue Fever Cases
<https://www.nature.com/articles/d41586-018-05914-3> and here
<https://gatesopenresearch.org/articles/2-36/v1>
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<http://www.epi.mcgill.ca/hanley/c609/Material/LidkopingALL.pdf>
4. Yearly Accidents, Fatalities, and Rates, 1982 - 2000, U.S. Air Carriers
<http://www.epi.mcgill.ca/hanley/c626/airline-data-sas.txt>
5. Quarterly & Monthly (prevalence) rates of Spina Bifida and Anencephaly Among Births (in relation to fortification of Foods with Folic Acid)
http://www.epi.mcgill.ca/hanley/c626/folic_acid.pdf. See more data on webpage
<http://www.epi.mcgill.ca/hanley/c626/>.
6. (Yearly) fatal and nonfatal crash rates on a toll highway (following a 5-15 mph (8-24 kph) decrease in speed limits)
<https://www.ncbi.nlm.nih.gov/pubmed/1251837>
7. Daily numbers of in-hospital deaths and Daily Maximal Temperatures
http://www.epi.mcgill.ca/hanley/c626/Heatwave_death_lyon.pdf
8. The (daily) incidence of crimes reported to 3 police stations in different towns (one rural, one urban, one industrial) vis-a-vis the day of the lunar cycle
<http://www.epi.mcgill.ca/hanley/c626/fullmoon.pdf>
9. Daily no.s (Postponement of Death Until Symbolically Meaningful Occasions)
<http://www.epi.mcgill.ca/hanley/c626/holidays.pdf>
10. Rates of audience fidget. (F Galton)
http://www.epi.mcgill.ca/hanley/c626/measure_of_fidget_galton.pdf

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