

Question

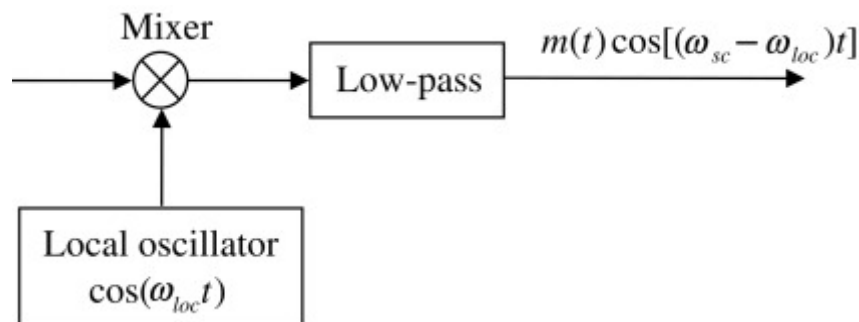
1. [why the mean value of the carrier and signal noise will be equal when in-phase and out-of-phase happens](#)
2. [why the final output signal in DSBSC is \$\frac{1}{2} f\(t\)\$, shouldn't it be \$\frac{1}{2} S_i\(t\)\$?](#)

DSBSC(Double sideband supress carrier)

- More effiecient
- Higher cost
- More complex

Coherent detection

It will be used to detect DSBSC.



DSBLC(Double sideband large carrier)

- less efficient
- lower cost

Noise in AM systems

Mean noise power in demodulator where a noise **voltage** is input into our demodulator

$$N_i = \lim_{T \rightarrow \infty} \frac{1}{T} \int_{-\frac{T}{2}}^{\frac{T}{2}} \frac{n_i^2}{R} dt$$

If the noise is in the form of a **current**, then the mean noise will be

$$N_i = \lim_{T \rightarrow \infty} \frac{1}{T} \int_{-\frac{T}{2}}^{\frac{T}{2}} n_i(t)^2 R dt$$

Ususally we will assume that the noise power will flower into $R = 1\Omega$. But it is noticable that in most cases R is matedched to 50Ω .

random noise

$$n_i(t) = n_c \cos(w_c t) - n_s(t) \sin(w_c t)$$

where the noise is defined in terms on **in-phase** and **out-of-phase**.

in-phase: If two waves coincide with peaks and troughs matching they are said to be in phase.

out-of-phase : A phrase used to characterize two or more signals whose phase relationship with each other is such that when **one is at its positive peak the other is at** (or near) its negative peak.

So the final noise will be:

$$N_i = \frac{1}{2T} \int_{-\frac{T}{2}}^{\frac{T}{2}} n_c(t)^2 + n_s(t)^2 [1 - \cos(w_c t)] - 2n_c(t)n_s(t) \sin(2w_c t) dt$$

And it basically used the trigonometry:

$$\cos^2 \alpha = \frac{1 + \cos 2\alpha}{2}$$

where the **R** is assumed to be **1Ω**.

the cos and sin terms average to zero to give,

$$N_i = \frac{1}{2T} \int_{-\frac{T}{2}}^{\frac{T}{2}} n_c^2(t) + n_s^2(t) dt = \frac{1}{2} n_c^2(t) + \frac{1}{2} n_s^2(t)$$

Which is the addition of two mean value of power.

If the noise is random, then the noise spikes will occur in-phase and out-of phase with equal frequency and so we can see

$$n_c^2(t) = n_s^2(t) = n_i^2(t)$$

Q1

☐ Why?

Signal

$$S_i = \frac{1}{T} \int_{-\frac{T}{2}}^{\frac{T}{2}} s_i(t)^2 dt$$

Amplitude demodulation

$$S_i(t) = f(t) \cos(w_c t)$$

Substitute it into the original equation:

$$S_i = \frac{1}{T} \int_{-\frac{T}{2}}^{\frac{T}{2}} f^2(t) dt$$

since the double angles was 0 during the integral.

So as shown before, according to DSBSC demodulation:

$$S_i(t) = f(t) \cos(w_c t)$$
$$S_o(t) = S_i(t) \cos(w_c t) = S_i(t) \cos^2(w_c t)$$

Since the $2w_c$ term will be filtered off. Then the obtained signal will be

$$S_o = \frac{1}{2} f(t)$$

Q2

☐ Why?

So the average power of the output signal will be

$$S_{op} = \frac{1}{T} \int_{-\frac{T}{2}}^{\frac{T}{2}} \left(\frac{1}{2} f(t)\right)^2 dt = \frac{1}{4} f(t)^2$$

No matter what is at input both noise and signal will be demodulated accordingly:

so the output noise will be $n_o(t) = n_i(t) \cos(w_c t)$ which is the same as the input signal and output signal which is:

$$n_o(t) = \frac{1}{2} n_c(t) [1 + \cos(2w_c t)] - \frac{1}{2} n_s(t) \sin(2w_c t)$$

Again, after filtered off $n_o(t) = \frac{1}{2} n_c(t)$, so the corresponding average power will be:

$$N_o = \frac{1}{T} \int_{-\frac{T}{2}}^{\frac{T}{2}} \left(\frac{1}{2} n_c(t)\right)^2 dt = \frac{1}{4} n_i^2(t)$$

Final SNR Ratio

$$\frac{S_i}{N_i} = \frac{\frac{1}{2} f(t)^2}{n_i(t)^2}$$
$$\frac{S_o}{N_o} = \frac{\frac{1}{4} f(t)^2}{\frac{1}{4} n_i(t)^2}$$

Hence $SNR_o = 2SNR_i$

Find noise performance of DSBLC through envelope detector

$$S_i = (\alpha + f(t)) \cos(w_c t) = \text{Re}\{(\alpha + f(t))e^{jw_c t}\}$$

where α is the carrier amplitude

So the input noise will be given as:

$$n_i(t) = n_c(t) \cos(w_c t) - n_s(t) \sin(w_c t)$$

So the input to envelope detector would be the addition of signal and noise:

$$s_i(t) + n_i(t) = \text{Re}\{(\alpha + f(t) + n_c(t) + jn_s(t))e^{jw_c t}\}$$

So the modulus of the input waveform can be expressed as:

$$r(t) = \sqrt{(\alpha + f(t) + n_c(t))^2 + n_s(t)^2}$$

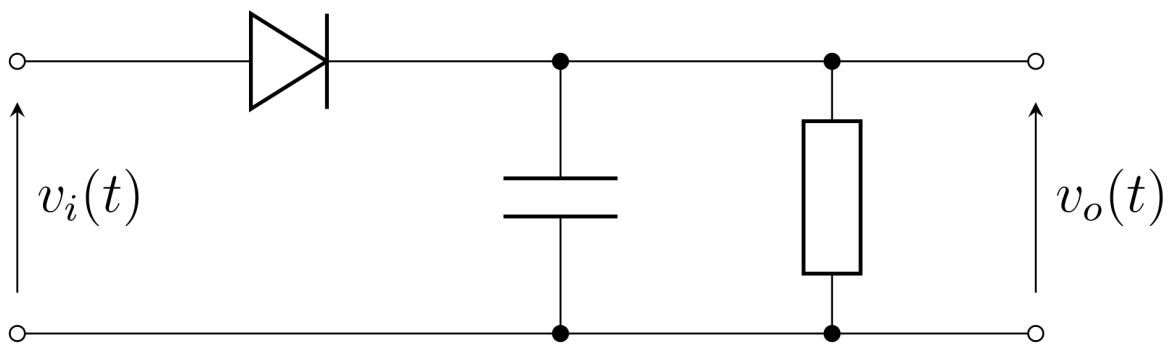
$$r(t) = (\alpha + f(t) + n_c(t))\sqrt{1 + \frac{n_s(t)^2}{\alpha + f(t) + n_c(t)^2}}$$

Since $n_s(t) \ll \alpha$ and $n_s \ll f_s(t)$. So $r(t) \approx (\alpha + f(t) + n_c(t))$. which is addition of DC term, signal term and noise term.

And $r(t)$ is the output of the envelope detector

✓ Why?

As for envelope detector:



So usually the envelope of the signal:

$$x(t) = (C + m(t))\cos(wt)$$

where C is the carrier amplitude and $m(t)$ is the message signal. And the output is the envelope. That's the reason why the $r(t)$ is the output of the envelope detector.

Since the DC term can be filtered out, so the remaining will be signal term and noise term.

which means that the output signal $S_o = f(t)$, $N_o = n_c(t)$.

which means that their corresponding mean output signal and noise power can be given as:

$$S_o = \hat{f}(t)^2$$

$$N_o = n_c(\hat{t})^2$$

Similarly, since $S_i = a + f(t)^2 \cos(w_c t)^2$ where the $2w_c t$ term will be filtered out. So the final input signal will be $\frac{1}{2}(\alpha + \hat{f}(t)^2)$

where the input noise is $n_i(\hat{t})$ which is the similar as that in DSCSC.

so

$$\frac{S_i}{N_i} = 2 \frac{S_o}{N_o} - \frac{\alpha^2}{n_i^2}$$

which means that $SNR_o < 2SNR_i$

where in DSBSC $SNR_o = 2SNR_i$, that's the reason why DSBLC is less efficient than DSBSC.

Aim of this Course

Find SNR_i and SNR_o which is SNR of input and SNR of output respectively