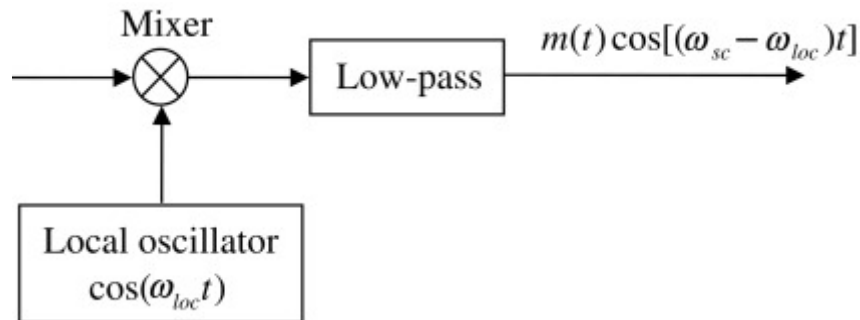


DSBSC

- More efficient
- Higher cost
- More complex

Coherent detection

It will be used to detect DSBSC.



DSBLC

- less efficient
- lower cost

Noise in AM systems

Mean noise power in demodulator where a noise **voltage** is input into our demodulator

$$N_i = \lim_{T \rightarrow \infty} \frac{1}{T} \int_{-\frac{T}{2}}^{\frac{T}{2}} \frac{n_i^2}{R} dt$$

If the noise is in the form of a **current**, then the mean noise will be

$$N_i = \lim_{T \rightarrow \infty} \frac{1}{T} \int_{-\frac{T}{2}}^{\frac{T}{2}} n_i(t)^2 R dt$$

Usually we will assume that the noise power will flow into $R = 1\Omega$. But it is noticeable that in most cases R is matched to 50Ω .

random noise

$$n_i(t) = n_c \cos(w_c t) - n_s(t) \sin(w_c t)$$

where the noise is defined in terms on **in-phase** and **out-of-phase**.

in-phase: If **two waves coincide with peaks and troughs matching they are** said to be in phase.

out-of-phase: A phrase used to characterize two or more signals whose phase relationship with each other is such that when **one is at its positive peak the other is at** (or near) its negative peak.

So the final noise will be:

$$N_i = \frac{1}{2T} \int_{-\frac{T}{2}}^{\frac{T}{2}} n_c(t)^2 + n_s(t)^2 [1 - \cos(w_c t)] - 2n_c(t)n_s(t) \sin(2w_c t) dt$$

And it basically used the trigonometry:

$$\cos^2 \alpha = \frac{1 + \cos 2\alpha}{2}$$

where the **R** is assumed to be **1Ω**.

the cos and sin terms average to zero to give,

$$N_i = \frac{1}{2T} \int_{-\frac{T}{2}}^{\frac{T}{2}} n_c^2(t) + n_s^2(t) dt = \frac{1}{2} n_c^2(t) + \frac{1}{2} n_s^2(t)$$

Which is the addition of two mean value of power.

If the noise is random, then the noise spikes will occur in-phase and out-of phase with equal frequency and so we can see

$$n_c^2(t) = n_s^2(t) = n_i^2(t)$$

☐ Why?

Signal

$$S_i = \frac{1}{T} \int_{-\frac{T}{2}}^{\frac{T}{2}} s_i(t)^2 dt$$

Amplitude demodulation

$$S_i(t) = f(t) \cos(w_c t)$$

Substitute it into the original equation:

$$S_i = \frac{1}{T} \int_{-\frac{T}{2}}^{\frac{T}{2}} f^2(t) dt$$

since the double angles was 0 during the integral.

So as shown before, according to DSBSC demodulation:

$$S_i(t) = f(t) \cos(w_c t)$$

$$S_o(t) = si(t) \cos(w_c t) = Si_t \cos^2(w_c t)$$

Since the $2w_c$ term will be filtered off. Then the obtained signal will be

$$S_o = \frac{1}{2} f(t)$$

□ **Why?**

So the average power of the output signal will be

$$S_{op} = \frac{1}{T} \int_{-\frac{T}{2}}^{\frac{T}{2}} \left(\frac{1}{2} f(t)\right)^2 dt = \frac{1}{4} f(t)^2$$

No matter what is at input both noise and signal will be demodulated accordingly:

so the output noise will be $n_o(t) = ni(t) \cos(w_c t)$ which is the same as the input signal and output signal which is:

$$n_o(t) = \frac{1}{2} n_c(t) [1 + \cos(2w_c t)] - \frac{1}{2} n_s(t) \sin(2w_c t)$$

Again, after filtered off $n_o(t) = \frac{1}{2} n_c(t)$, so the corresponding average power will be:

$$N_o = \frac{1}{T} \int_{-\frac{T}{2}}^{\frac{T}{2}} \left(\frac{1}{2} n_c(t)\right)^2 dt = \frac{1}{4} n_i^2(t)$$

Final SNR Ratio

$$\frac{S_i}{N_i} = \frac{\frac{1}{2} f(t)^2}{n_i(t)^2}$$

$$\frac{S_o}{N_o} = \frac{\frac{1}{4} f(t)^2}{\frac{1}{4} n_i(t)^2}$$

Hence $SNR_o = 2SNR_i$

Aim of this Course

Find SNR_i and SNR_o which is SNR of input and SNR of output respectively