Evaluating a model graphically

SUPERVISED LEARNING IN R: REGRESSION

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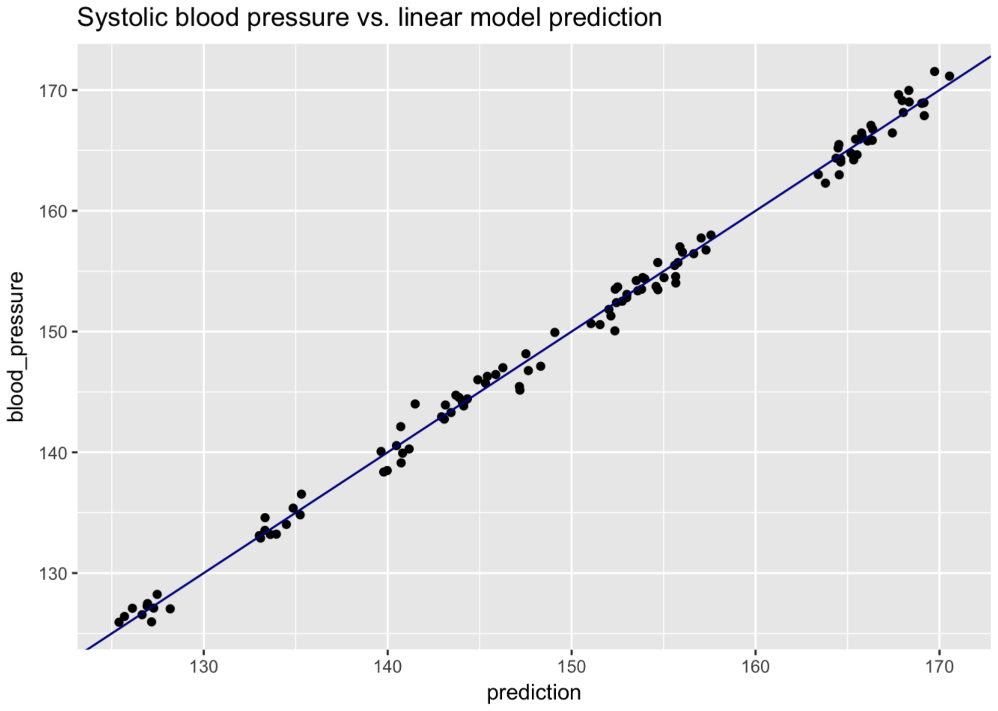
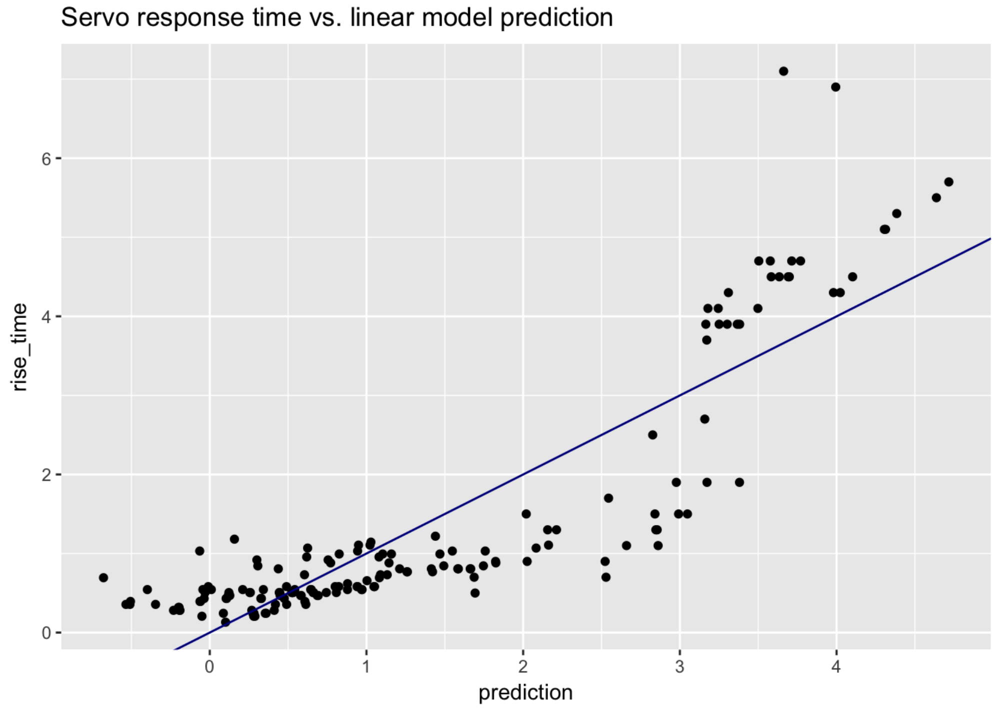
Plotting Ground Truth vs. Predictions

A well fitting model



- $x = y$ line runs through center of points
- "line of perfect prediction"

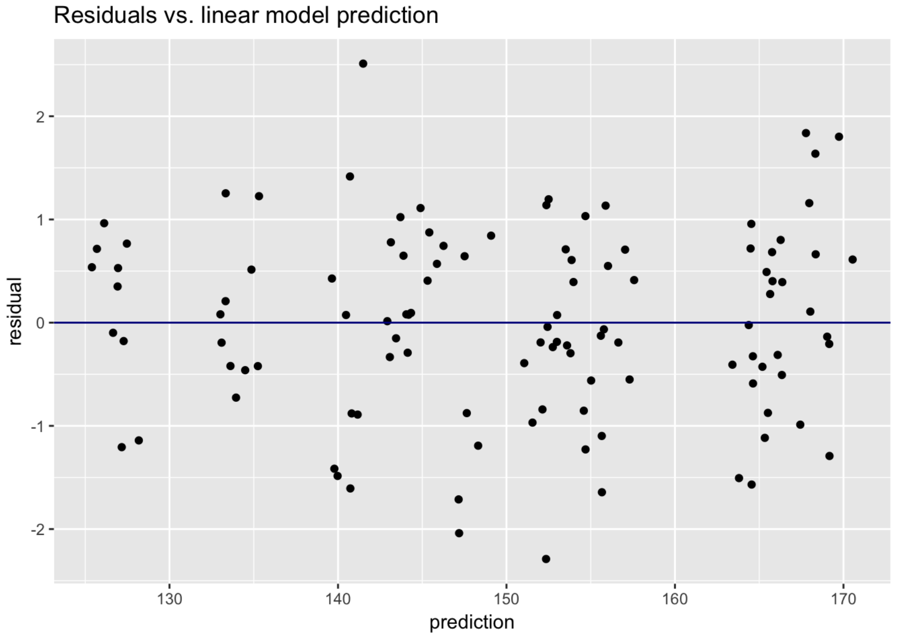
A poorly fitting model



- Points are all on one side of $x = y$ line
- Systematic errors

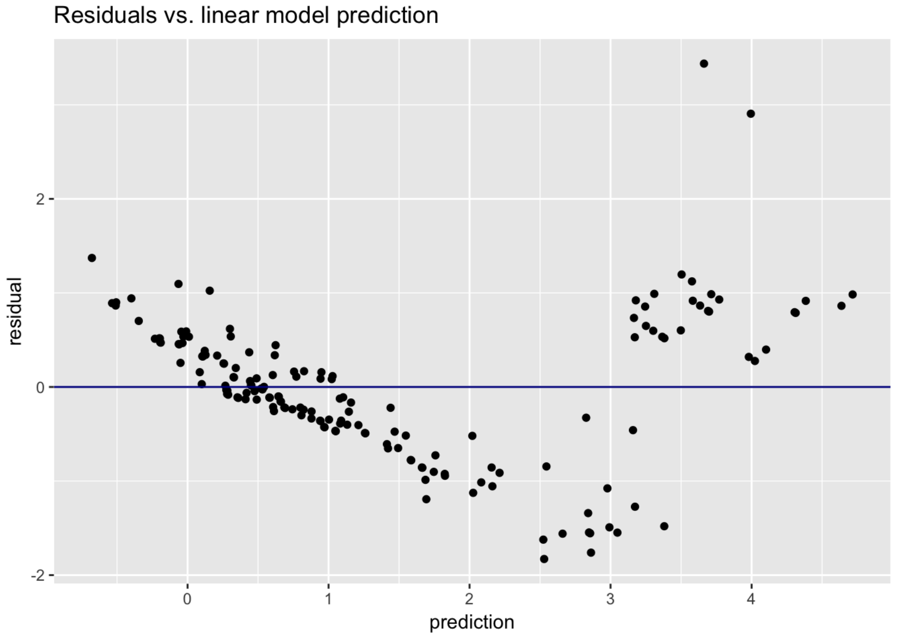
The Residual Plot

A well fitting model



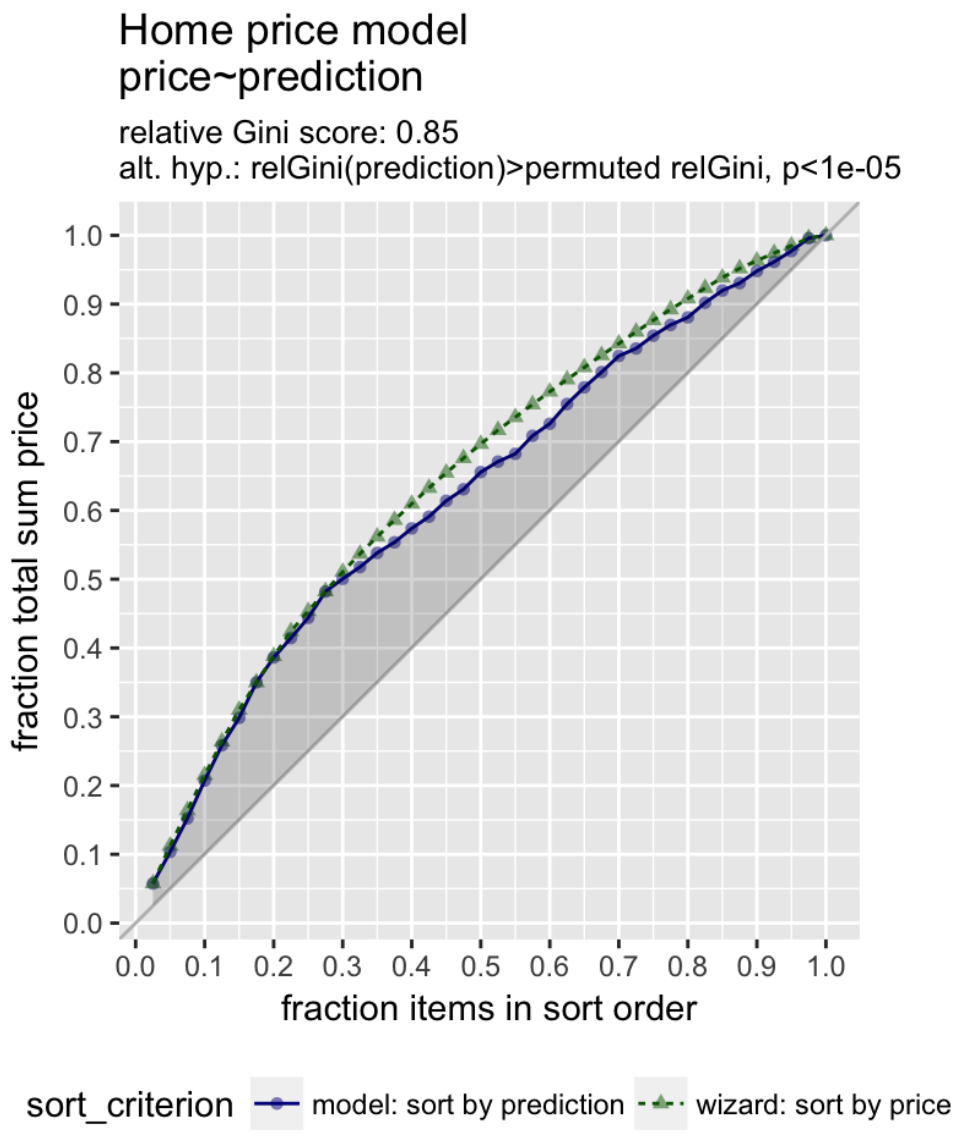
- Residual: actual outcome - prediction
- Good fit: no systematic errors

A poorly fitting model



- Systematic errors

The Gain Curve

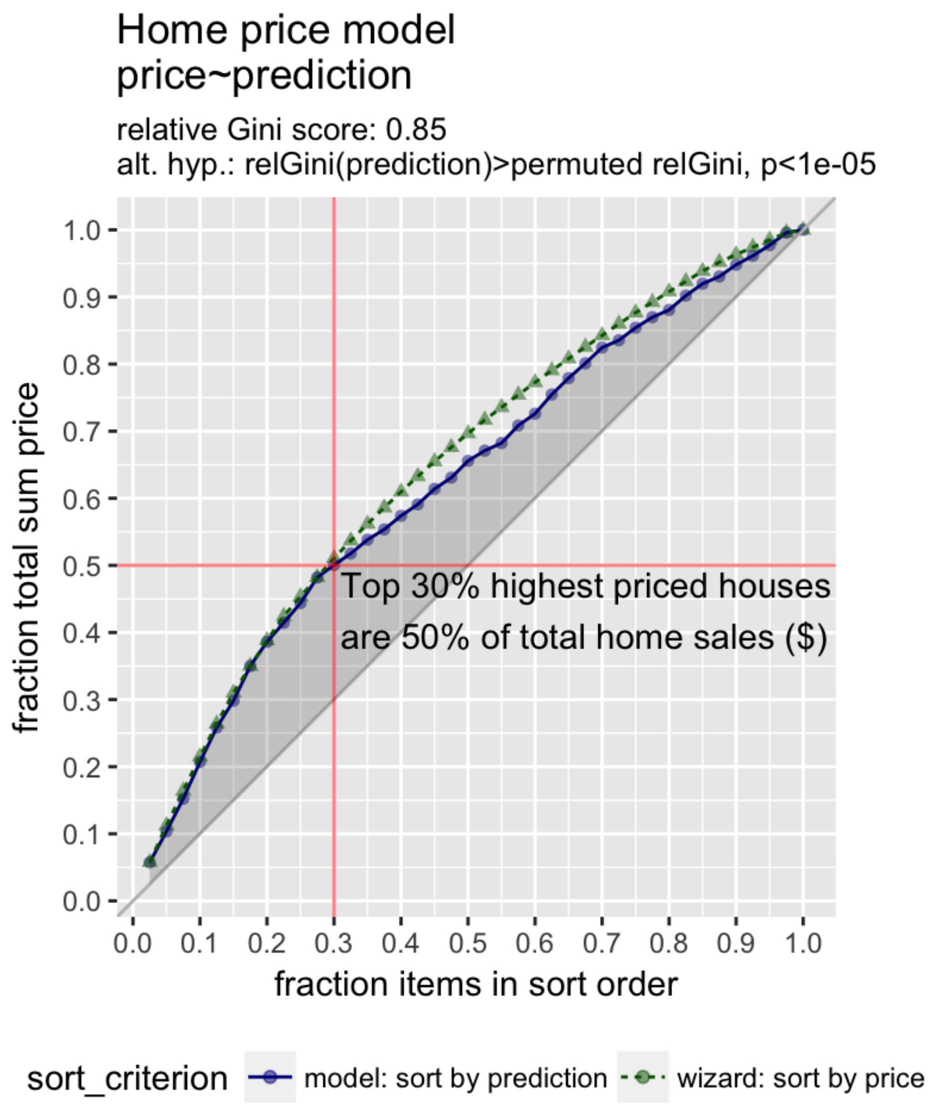


Measures how well model sorts the outcome

- **x-axis**: houses in model-sorted order (decreasing)
- **y-axis**: fraction of total accumulated home sales

Wizard curve: perfect model

Reading the Gain Curve




```
GainCurvePlot(houseprices, "prediction", "price", "Home price model")
```

Let's practice!

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Root Mean Squared Error (RMSE)

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What is Root Mean Squared Error (RMSE)?

$$RMSE = \sqrt{\overline{(pred - y)^2}}$$

where

- $pred - y$: the error, or residuals vector
- $\overline{(pred - y)^2}$: mean value of $(pred - y)^2$

RMSE of the Home Sales Price Model

```
# Calculate error
err <- houseprices$prediction - houseprices$price
```

- `price` : column of actual sale prices (in thousands)
- `prediction` : column of predicted sale prices (in thousands)

RMSE of the Home Sales Price Model

```
# Calculate error
err <- houseprices$prediction - houseprices$price

# Square the error vector
err2 <- err^2
```

RMSE of the Home Sales Price Model

```
# Calculate error
err <- houseprices$prediction - houseprices$price

# Square the error vector
err2 <- err^2

# Take the mean, and sqrt it
(rmse <- sqrt(mean(err2)))
```

```
58.33908
```

- $RMSE \approx 58.3$

Is the RMSE Large or Small?

```
# Take the mean, and sqrt it
(rmse <- sqrt(mean(err2)))
```

```
58.33908
```

```
# The standard deviation of the outcome
(sdtemp <- sd(houseprices$price))
```

```
135.2694
```

- $RMSE \approx 58.3$
- $sd(price) \approx 135$

Let's practice!

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R-Squared (R^2)

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What is R^2?

A measure of how well the model fits or explains the data

- A value between 0-1
  - near 1: model fits well
  - near 0: no better than guessing the average value

Calculating R^2

R^2 is the *variance explained by the model*.

$$R^2 = 1 - \frac{RSS}{SS_{Tot}}$$

where

- $RSS = \sum (y - prediction)^2$
  - Residual sum of squares (variance from model)
- $SS_{Tot} = \sum (y - \overline{y})^2$
  - Total sum of squares (variance of data)

Calculate R^2 of the House Price Model: RSS

- Calculate error

```
err <- houseprices$prediction - houseprices$price
```

- Square it and take the sum

```
rss <- sum(err^2)
```

- `price` : column of actual sale prices (in thousands)
- `pred` : column of predicted sale prices (in thousands)
- $RSS \approx 136138$

Calculate R^2 of the House Price Model: SS_{Tot}

- Take the difference of prices from the mean price

```
toterr <- houseprices$price - mean(houseprices$price)
```

- Square it and take the sum

```
sstot <- sum(toterr^2)
```

- $RSS \approx 136138$
- $SS_{Tot} \approx 713615$

Calculate R^2 of the House Price Model

```
(r_squared <- 1 - (rss/sstot) )
```

```
0.8092278
```

- $RSS \approx 136138$
- $SS_{Tot} \approx 713615$
- $R^2 \approx 0.809$

Reading R^2 from the lm() model

```
# From summary()
summary(hmodel)
```

```
...
Residual standard error: 60.66 on 37 degrees of freedom
Multiple R-squared:  0.8092, Adjusted R-squared:  0.7989
F-statistic: 78.47 on 2 and 37 DF,  p-value: 4.893e-14
```

```
summary(hmodel)$r.squared
```

```
0.8092278
```

```
# From glance()
glance(hmodel)$r.squared
```

```
0.8092278
```

Correlation and R^2

```r
rho <- cor(houseprices$prediction, houseprices$price)
```

```
0.8995709
```

```r
rho^2
```

```
0.8092278
```

- $\rho =$ `cor(prediction, price)` $= 0.8995709$
- $\rho^2 = 0.8092278 = R^2$

Correlation and R^2

- True for models that minimize squared error:
  - Linear regression
  - GAM regression
  - Tree-based algorithms that minimize squared error
- True for training data; **NOT** true for future application data

Let's practice!

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Properly Training a Model

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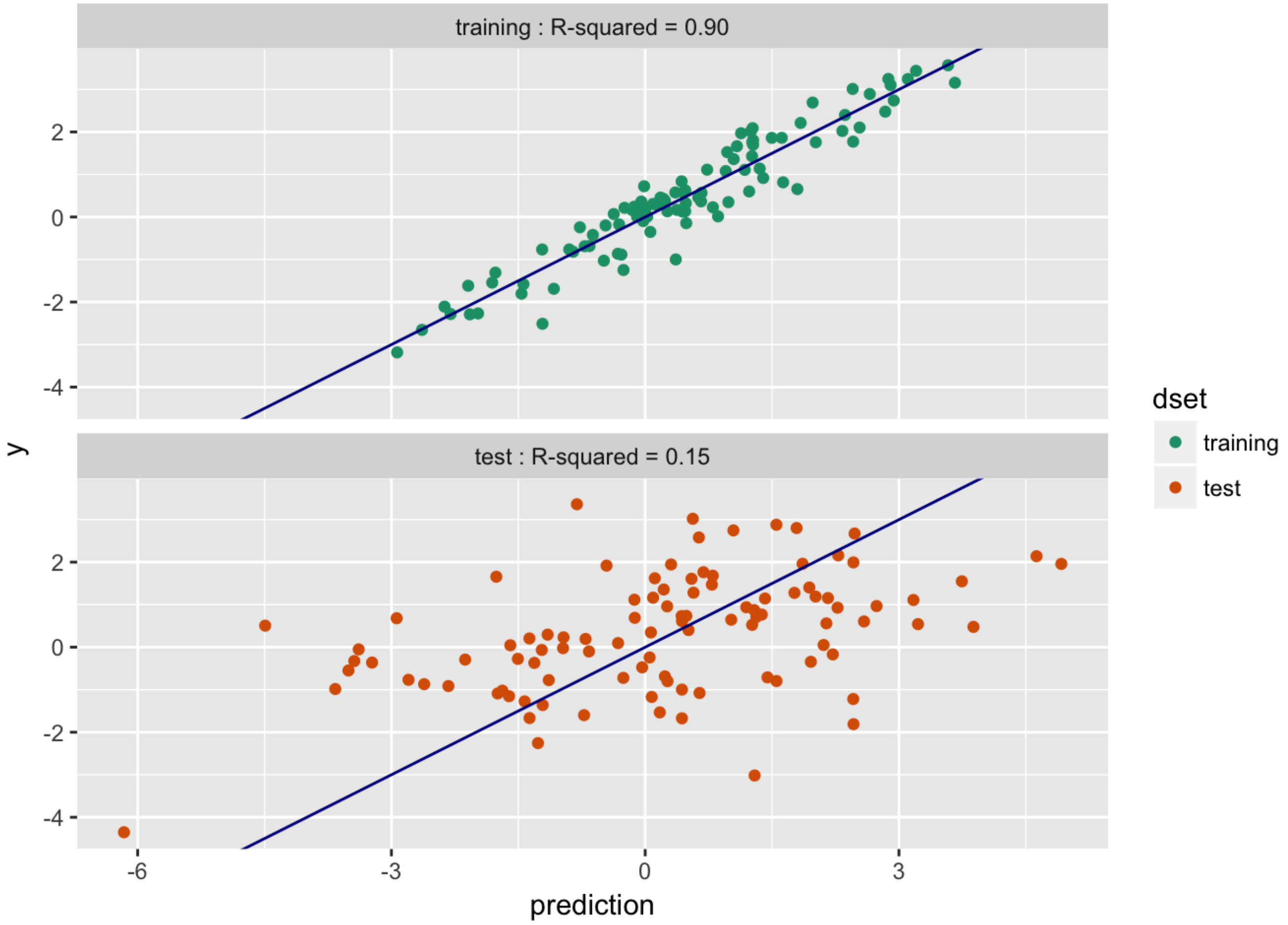
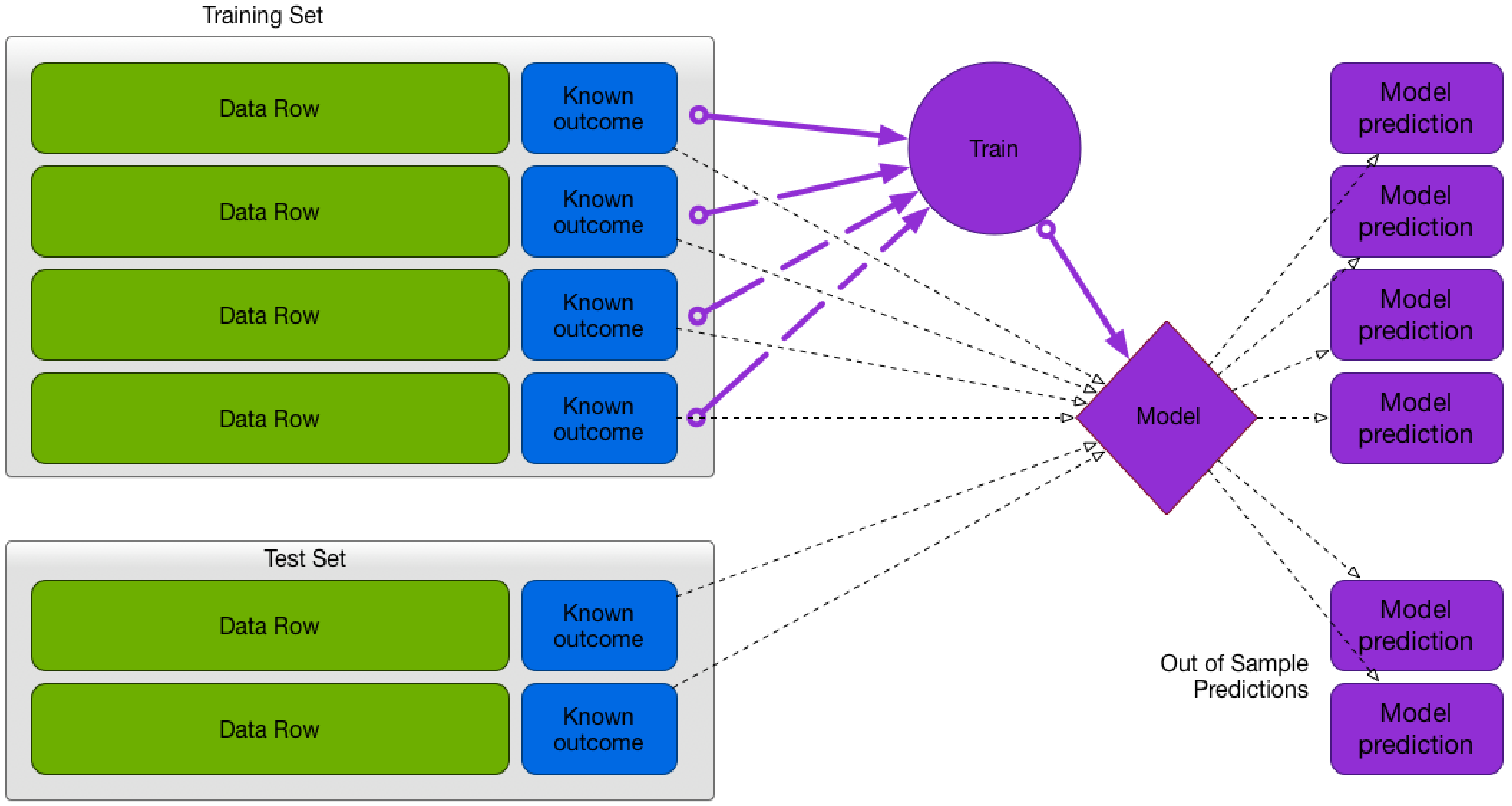
Models can perform much better on training than they do on future data.



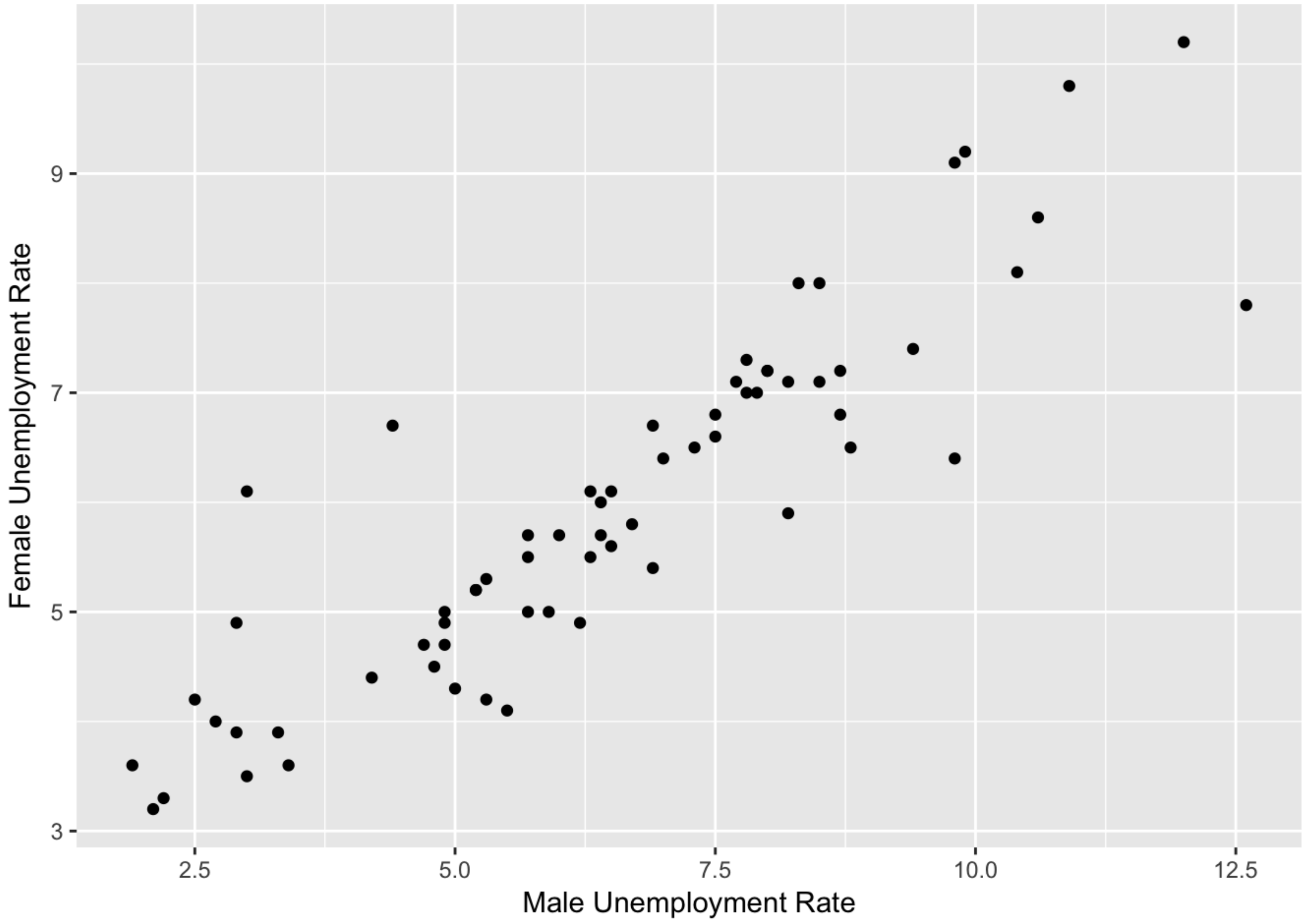
- Training R^2: 0.9; Test R^2: 0.15 -- **Overfit**

Test/Train Split



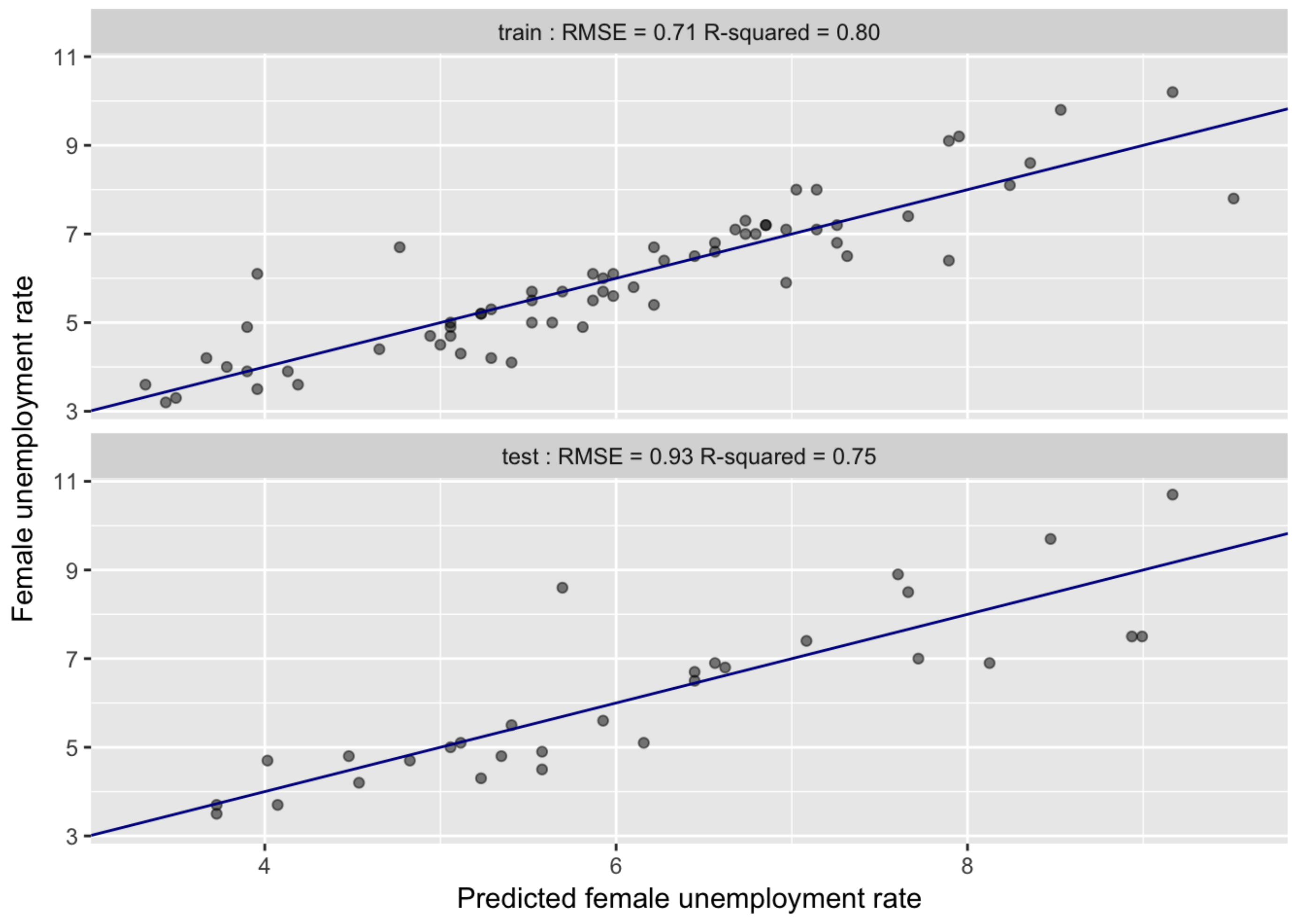
Recommended method when data is plentiful

Example: Model Female Unemployment



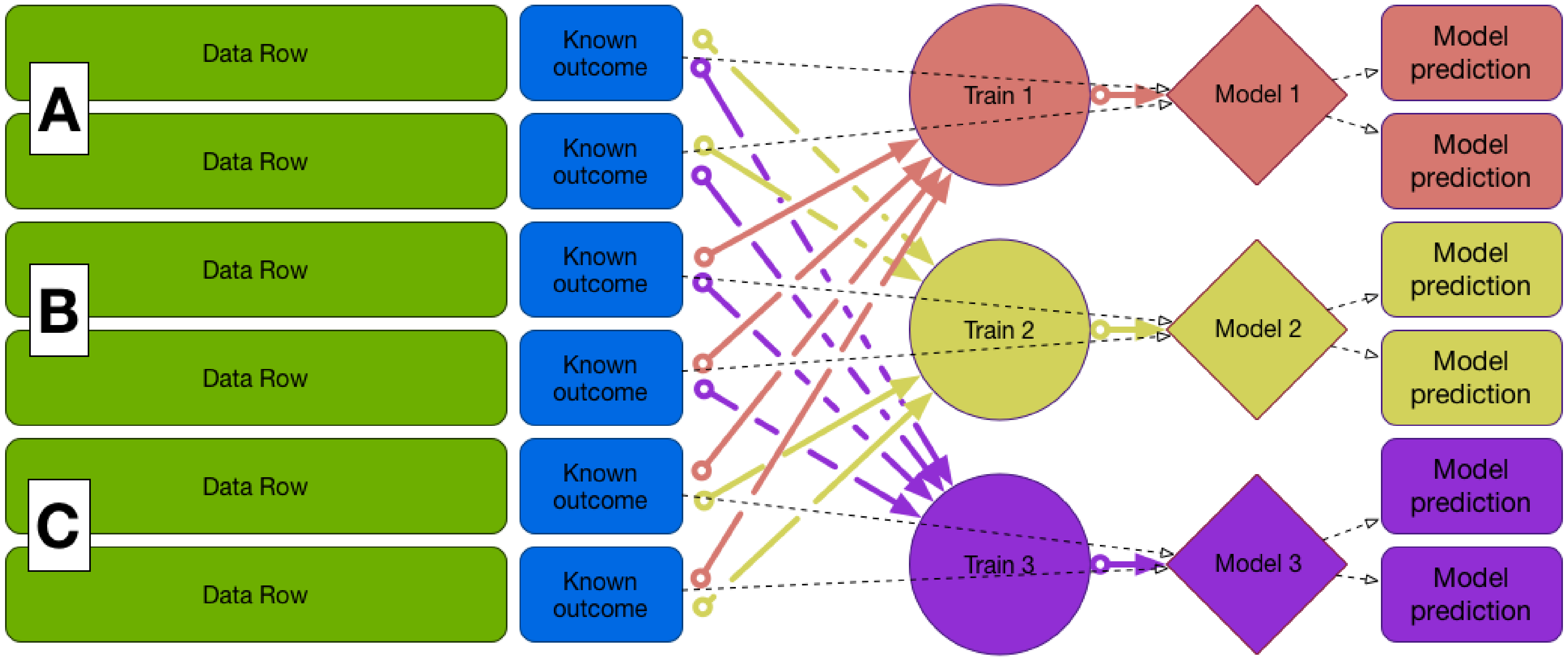
- Train on 66 rows, test on 30 rows

Model Performance: Train vs. Test



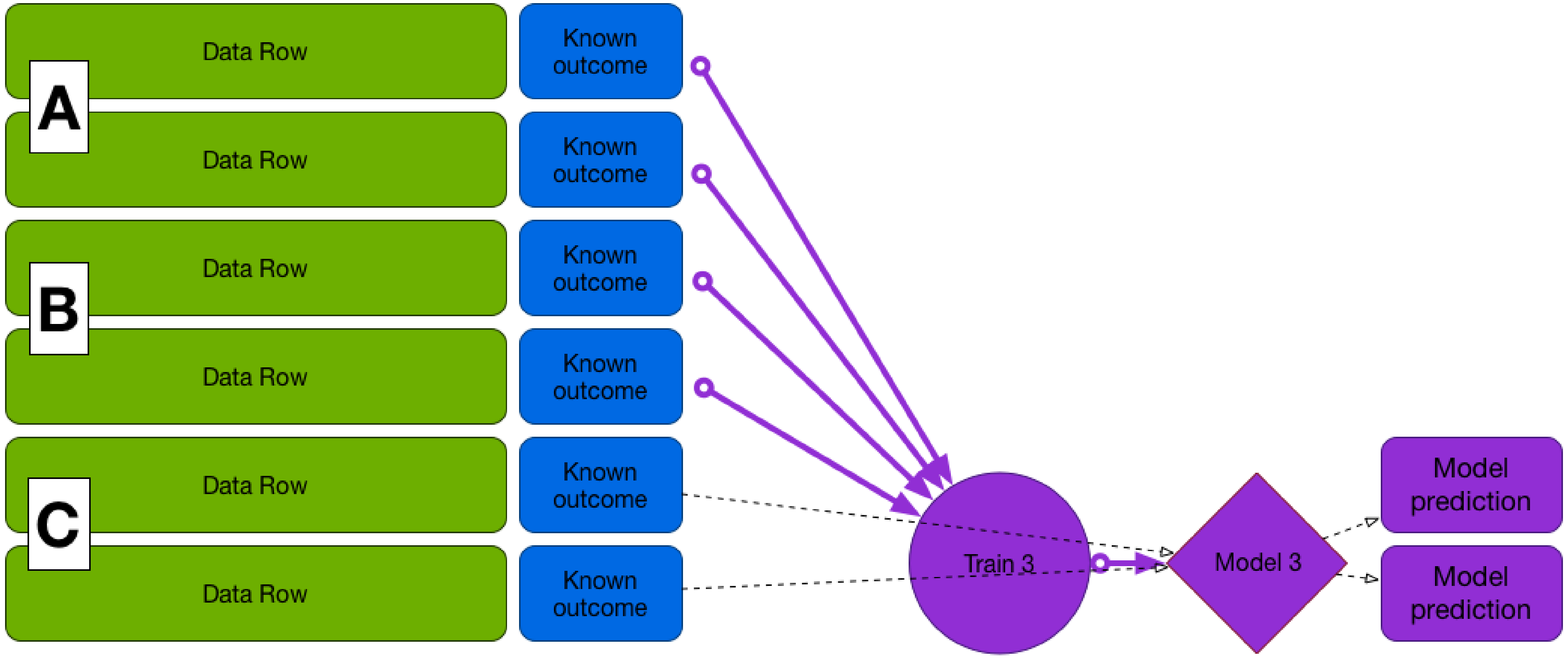
- Training: RMSE 0.71, R^2 0.8
- Test: RMSE 0.93, R^2 0.75

Cross-Validation

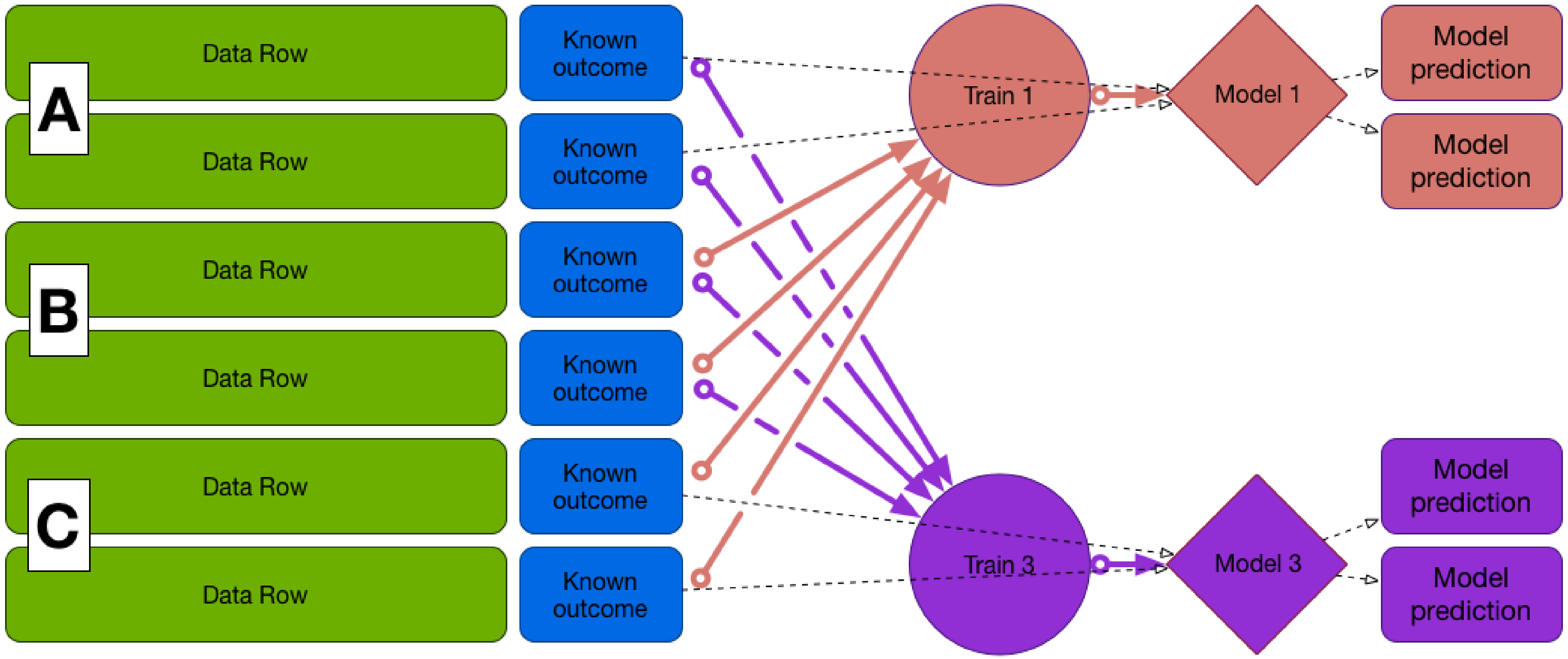


Preferred when data is not large enough to split off a test set

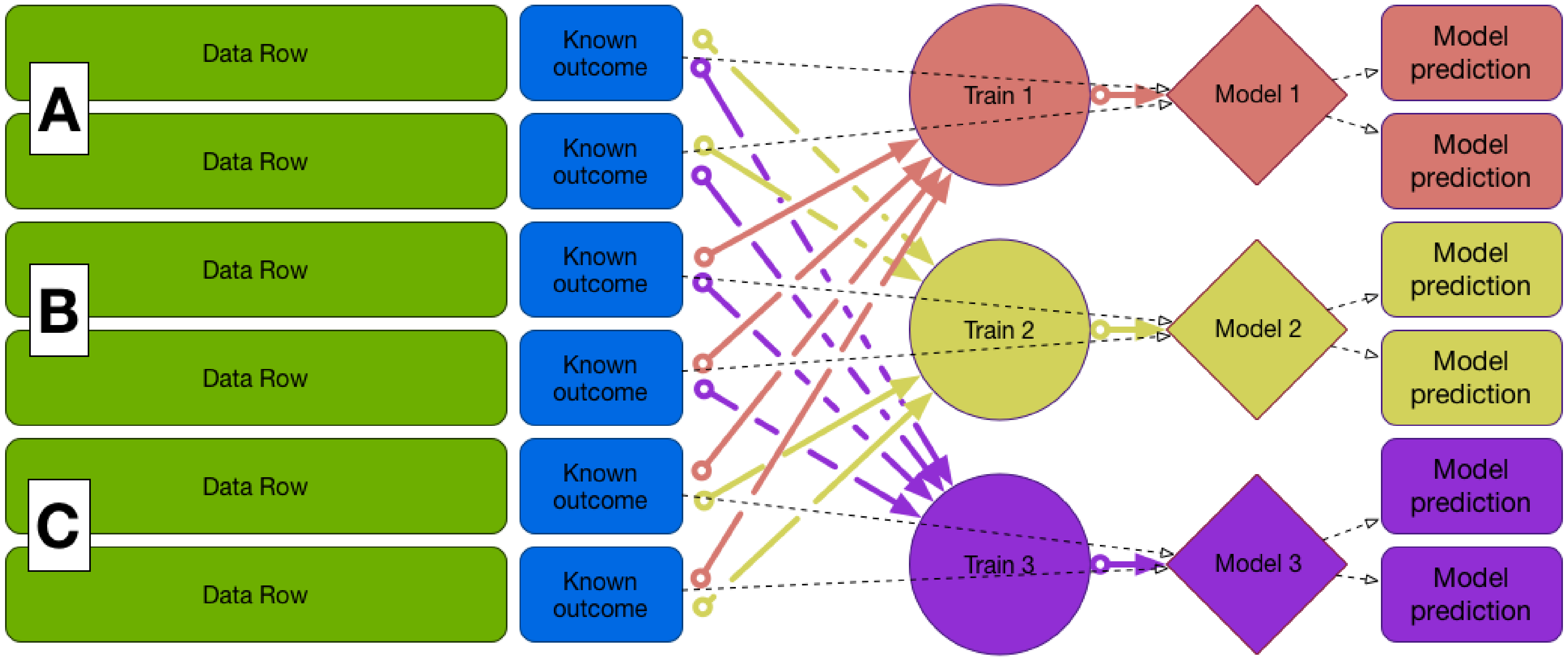
Cross-Validation



Cross-Validation



Cross-Validation



Create a cross-validation plan

```
library(vtreat)
splitPlan <- kWayCrossValidation(nRows, nSplits, NULL, NULL)
```

- `nRows` : number of rows in the training data
- `nSplits` : number folds (partitions) in the cross-validation
  - e.g, nfolds = 3 for 3-way cross-validation
- remaining 2 arguments not needed here

Create a cross-validation plan

```
library(vtreat)
splitPlan <- kWayCrossValidation(10, 3, NULL, NULL)
```

First fold (A and B to train, C to test)

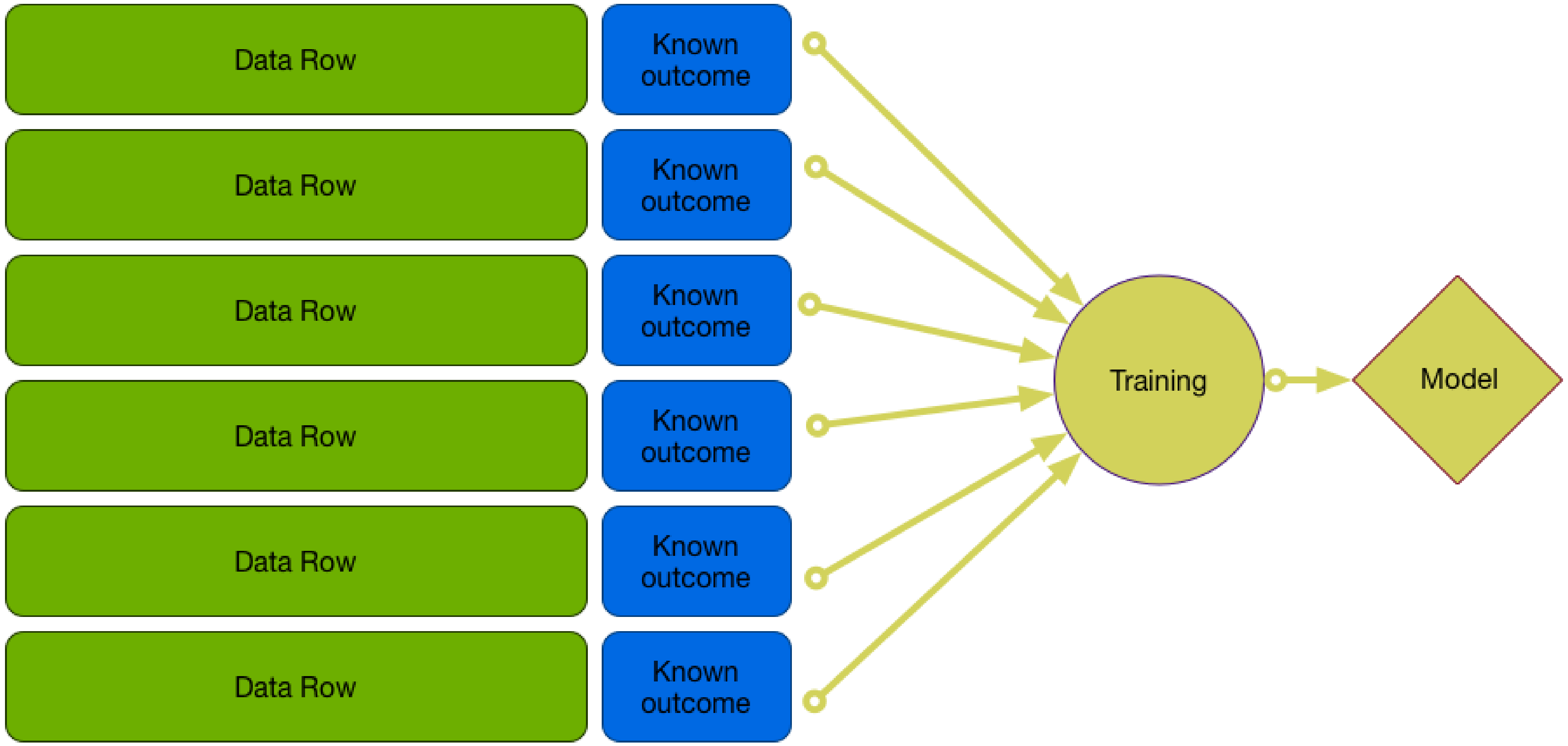
```
splitPlan[[1]]
```

```
$train
1  2  4  5  7  9 10
$app
3 6 8
```

Train on A and B, test on C, etc...

```
split <- splitPlan[[1]]
model <- lm(fmla, data = df[split$train,])
df$pred.cv[split$app] <- predict(model, newdata = df[split$app,])
```

Final Model



Data Row
Known outcome
Data Row
Known outcome
Data Row
Known outcome
Data Row
Known outcome
Data Row
Known outcome
Data Row
Known outcome
Training
Model

Example: Unemployment Model

Measure type	RMSE	R^2
train	0.7082675	0.8029275
test	0.9349416	0.7451896
cross-validation	0.8175714	0.7635331

Let's practice!

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