



# *Module 6*

# Advanced Data Structures

## Part 1: Heap Structure



Definition



Operations



Applications

## Part 2: Tries Structure



Definition



Terminologies



Types

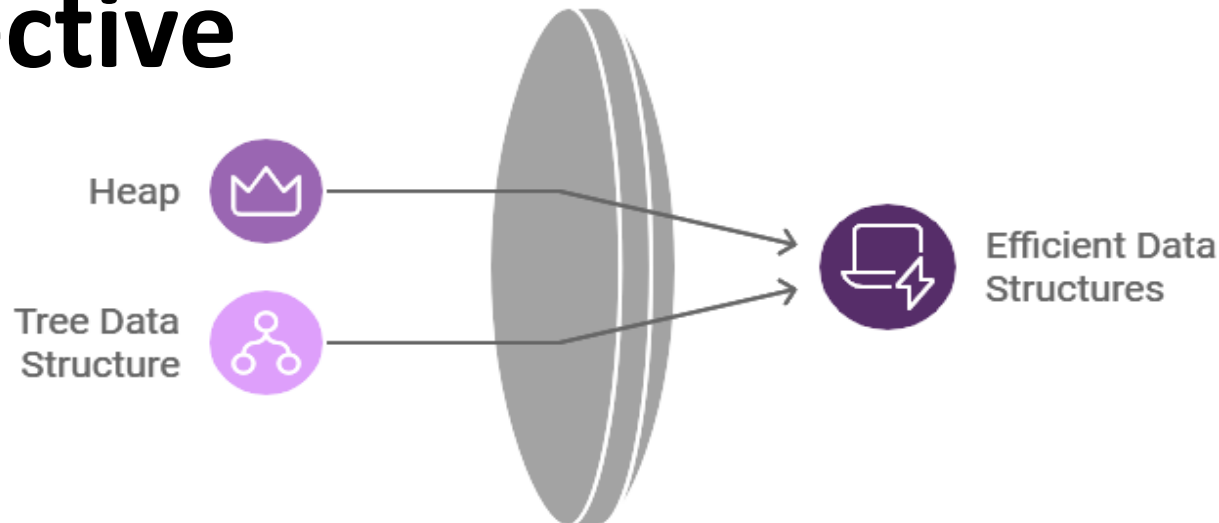


Operations



Applications

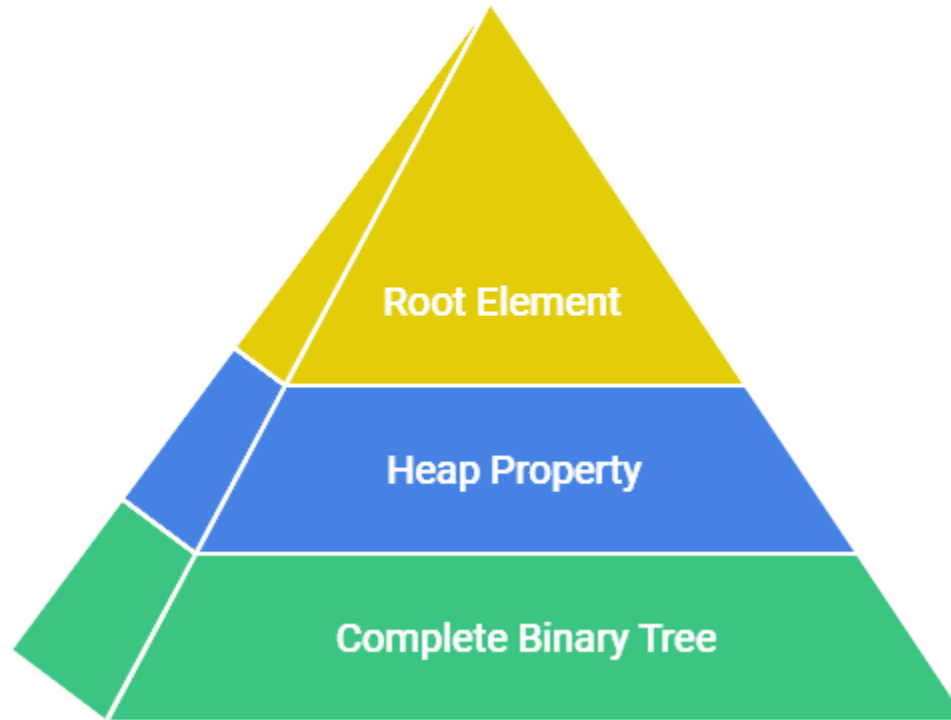
# Objective



# Part 1: Heap Structure

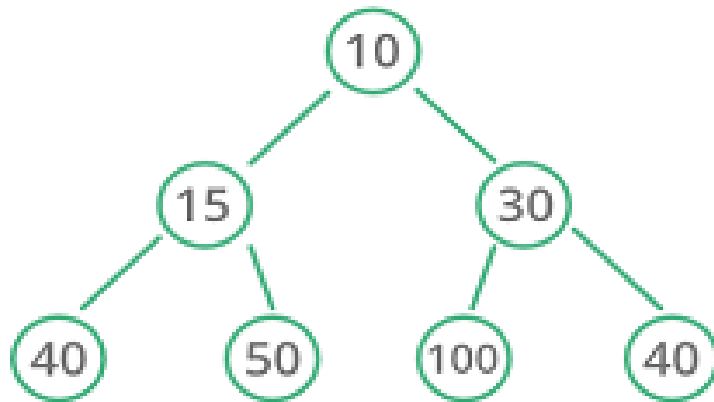
# I. Definition and operations

Heap Structure

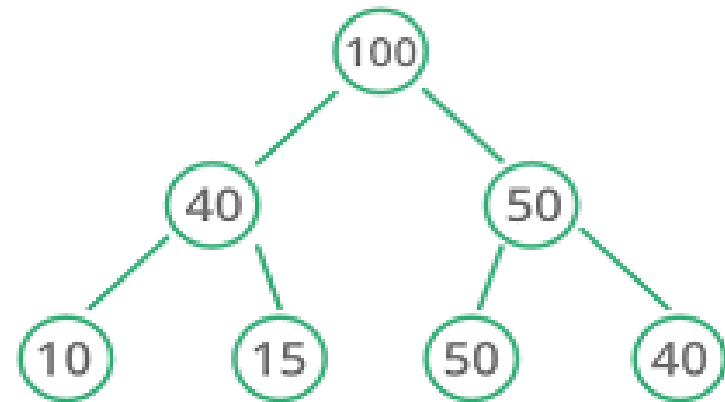


# I. Definition and operations

## Heap Data Structure



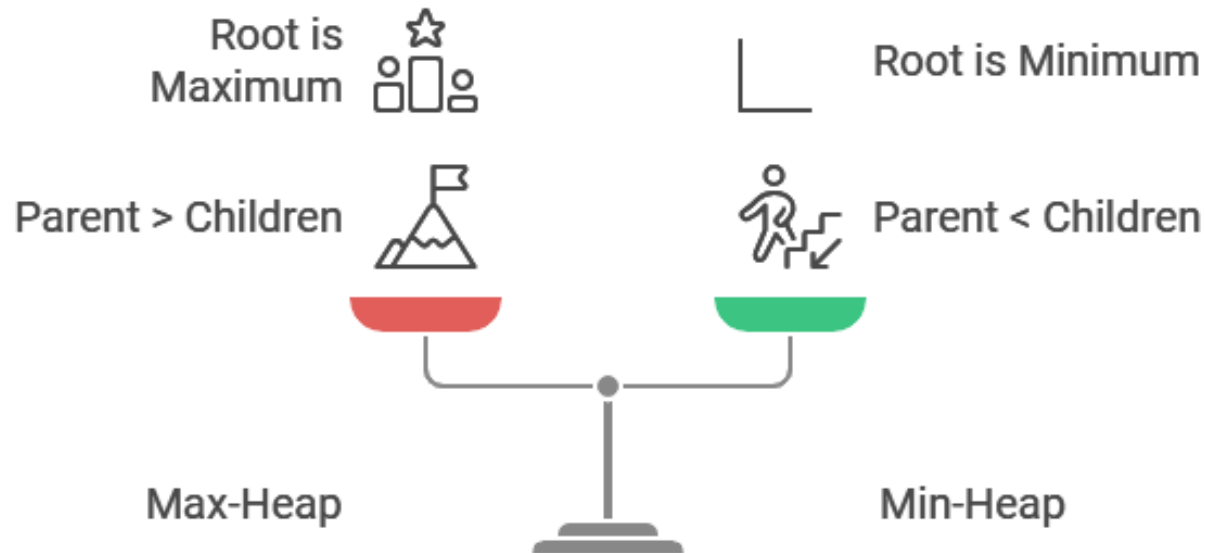
Min Heap



Max Heap

# I. Definition and operations

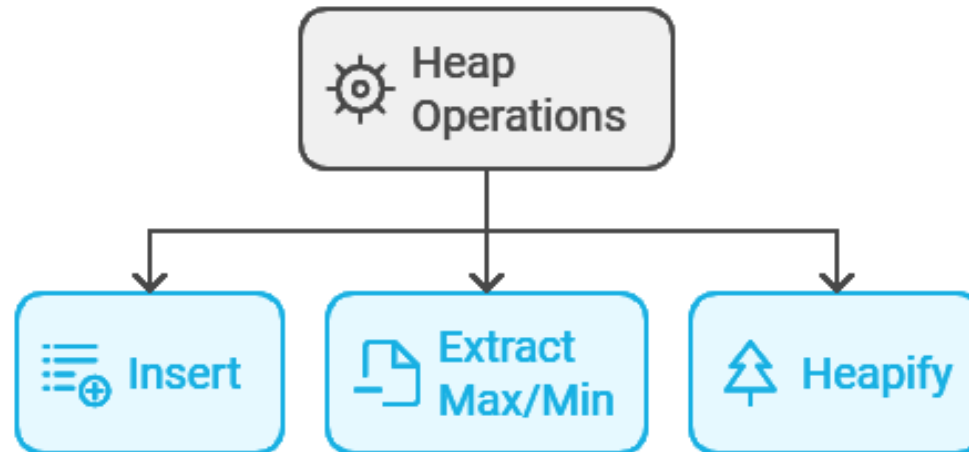
## a) What is Heap Data Structure?



Understanding Max-Heap vs. Min-Heap

# I. Definition and operations

## b) Heap Operations





# II. Applications of heaps

Example 1:

Input:  $N = 5$

$\text{arr}[] = \{4, 1, 3, 9, 7\}$

Output: 1 3 4 7 9

Explanation:

After sorting elements

- using heap sort, elements will be
- in order as 1, 3, 4, 7, 9.



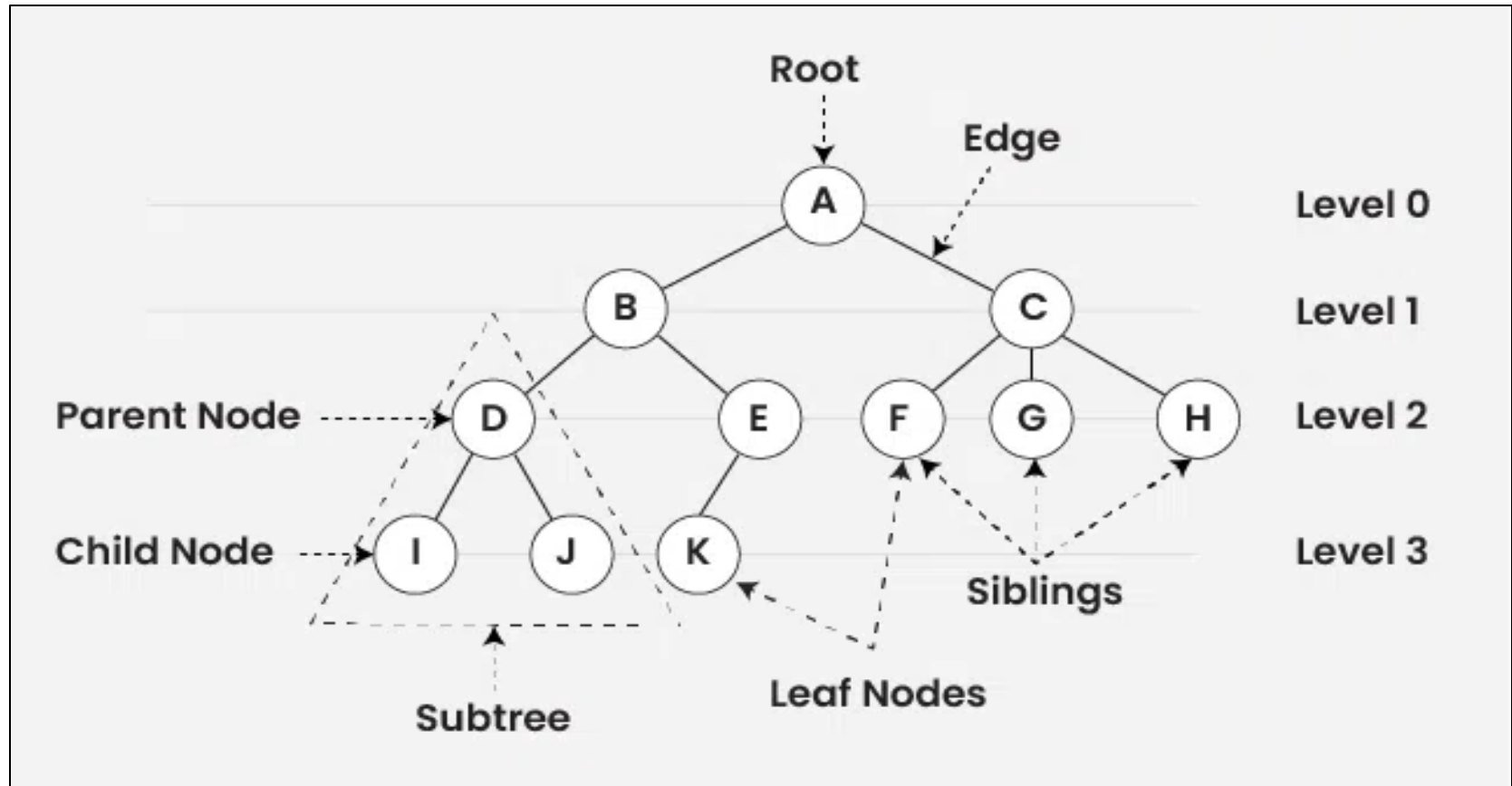
# II. Applications of heaps

```
using System; class HeapSort
{ public void Sort(int[] array)
{ int n = array.Length; //(rearrange array)
  for (int i = n / 2 - 1; i >= 0; i--)
    Heapify(array, n, i); // One 2 one extract ele.
  for (int i = n - 1; i >= 0; i--)
  { int temp = array[0]; // Move current to end
    array[0] = array[i]; array[i] = temp;
    Heapify(array, i, 0); }
} // Call max heapify on the reduced heap
void Heapify(int[] array, int n, int i)
{ int largest = i; // Initialize largest as root
  int left = 2 * i + 1; // left = 2*i + 1
  int right = 2 * i + 2; // right = 2*i + 2
  if (left < n && array[left] > array[largest])
```

```
    largest = left; // If right child > largest
  if (right < n && array[right] > array[largest])
    largest = right;
  if (largest != i) // If largest is not root
  { int swap = array[i]; array[i] = array[largest];
    array[largest] = swap; Heapify(array, n,
largest); } // heapify the affected sub-tree
  static void PrintArray(int[] array)
  { int n = array.Length; //fun to print array of size n
    for (int i = 0; i < n; ++i) Console.Write(array[i] + " ");
    Console.WriteLine(); }
  public static void Main() // Driver program
  { int[] array = { 12, 11, 13, 5, 6, 7 };
    HeapSort heapSort = new HeapSort();
    heapSort.Sort(array); Console.WriteLine("Sorted
array is"); PrintArray(array); } }
```

# Part 2: Tries Structure

# I. Definition and Operations



# I. Definition and Operations



Central Node



Structural  
Nodes



Sub-Nodes



Roots



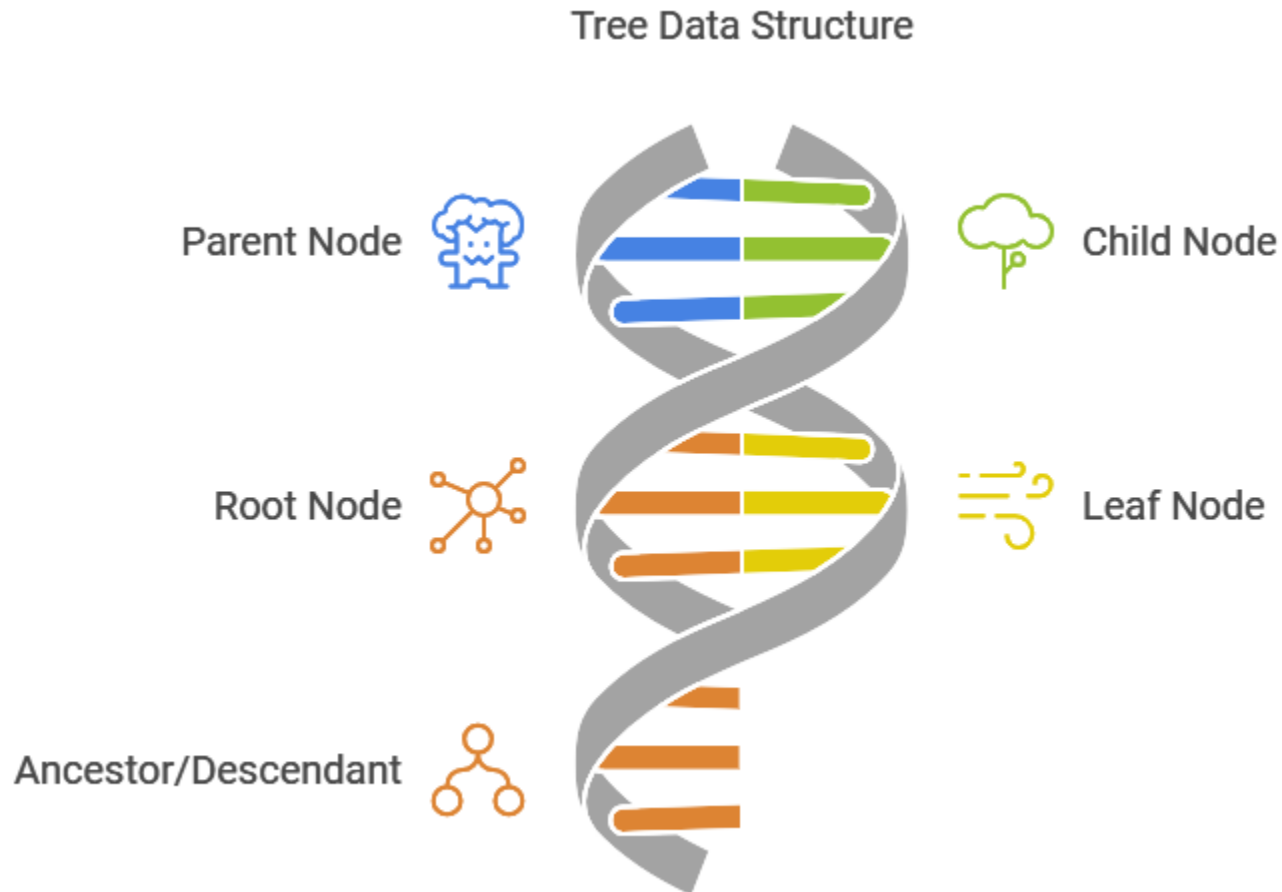
Branches



Leaves

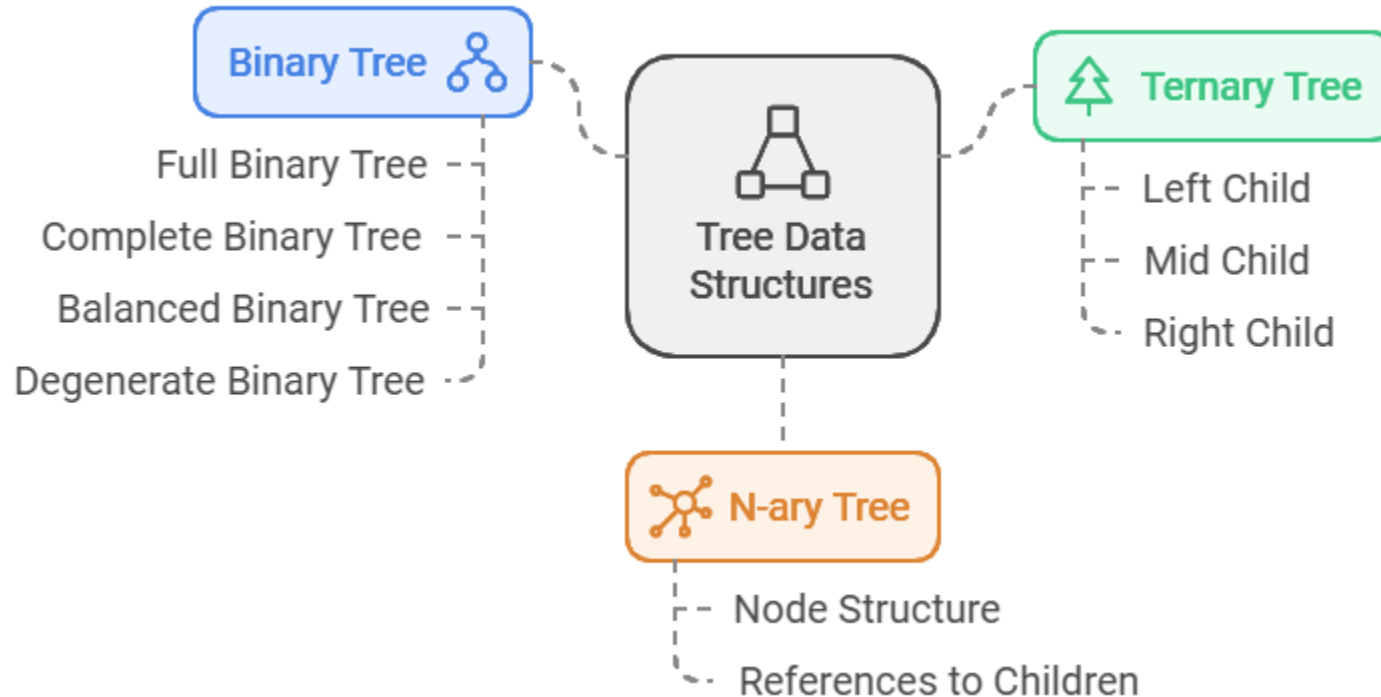
# I. Definition and Operations

## a) Basic Terminologies in Tree:



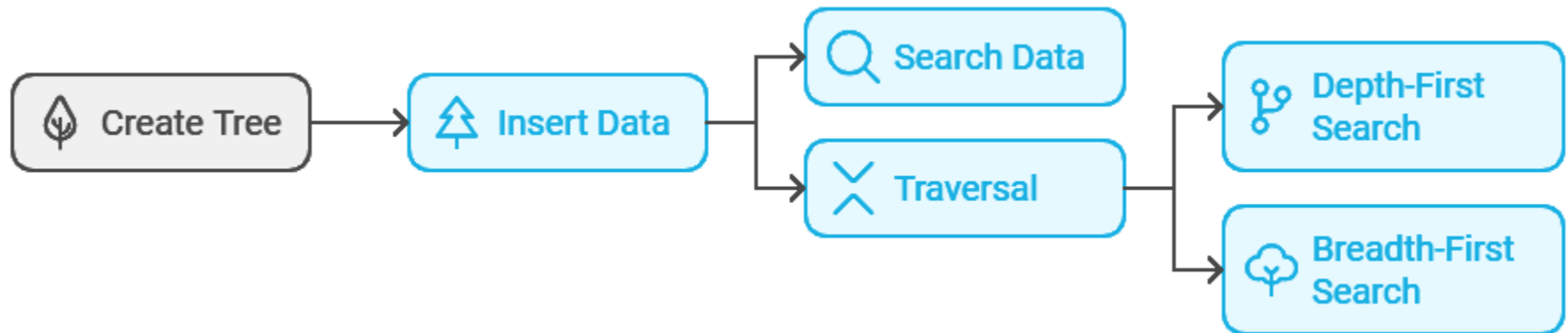
# I. Definition and Operations

## b) Types of Tree data structures:



# I. Definition and Operations

## c) Basic Operations of Tree Data Structure:





# II. Applications of Tries

```
using System;

using System.Collections.Generic;

class Program
{
    static void PrintParents(int node, List<List<int>>
adj, int parent)
    {
        if (parent == 0)
        {
            Console.WriteLine($"{node} -> Root");
        }
        else
        {
            Console.WriteLine($"{node} -> {parent}");
        }
        foreach (int cur in adj[node])
        {
            if (cur != parent)
            {
                PrintParents(cur, adj, node);
            }
        }
    }

    static void PrintChildren(int Root, List<List<int>> adj)
    {
        Queue<int> q = new Queue<int>();
        q.Enqueue(Root);
```

```
bool[] vis = new bool[adj.Count];

while (q.Count > 0)
{
    int node = q.Dequeue(); vis[node] = true;
    Console.WriteLine($"{node} -> ");
    foreach (int cur in adj[node])
    {
        if (!vis[cur])
        {
            Console.WriteLine($"{cur} ");
            q.Enqueue(cur);
        }
        Console.WriteLine();
    }
}

static void PrintLeafNodes(int Root, List<List<int>>
adj)
{
    for (int i = 0; i < adj.Count; i++)
    {
        if (adj[i].Count == 1 && i != Root)
        {
            Console.WriteLine($"{i} ");
        }
        Console.WriteLine();
    }
}
```

# II. Applications of Tries

```
static void PrintDegrees(int Root, List<List<int>> adj)
{   for (int i = 1; i < adj.Count; i++)
    {   Console.WriteLine($"{i}: ");
        if (i == Root)
        {   Console.WriteLine(adj[i].Count);           }
        else
        {   Console.WriteLine(adj[i].Count - 1); } }
}

static void Main(string[] args)
{   int N = 7;
    int Root = 1;
    List<List<int>> adj = new List<List<int>>();
    for (int i = 0; i <= N; i++)
    {   adj.Add(new List<int>());   }
    adj[1].AddRange(new int[] { 2, 3, 4 });
    adj[2].AddRange(new int[] { 1, 5, 6 });
    adj[4].Add(7);
```

```
    Console.WriteLine("The parents of each node are:");
        PrintParents(Root, adj, 0);

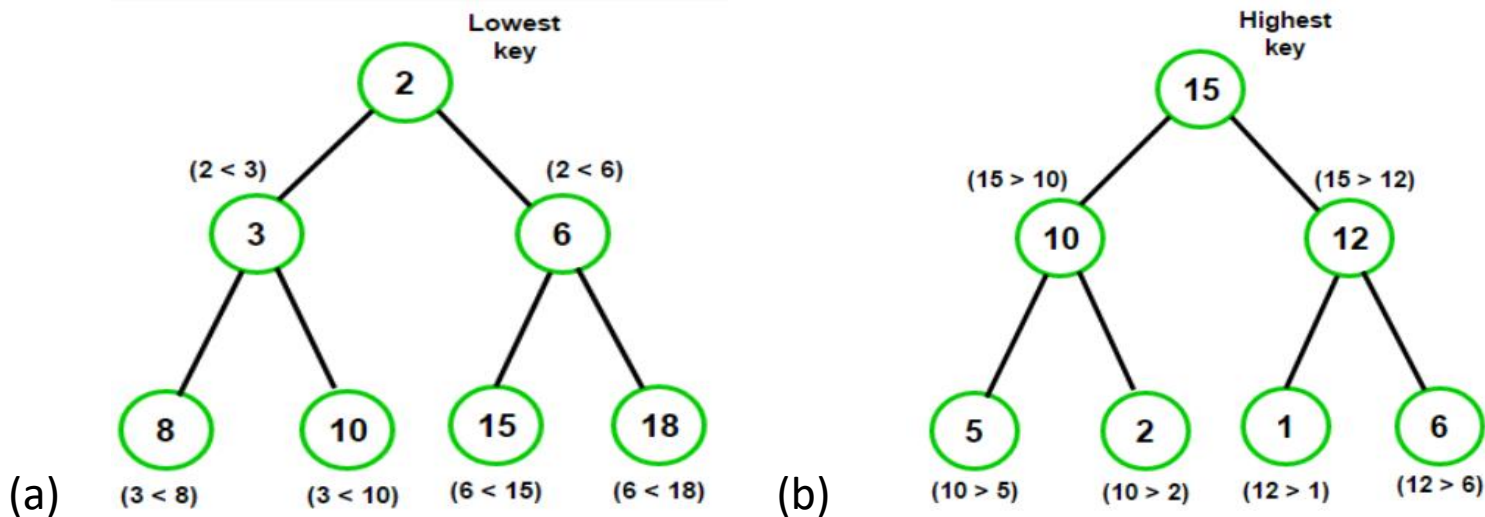
    Console.WriteLine("The children of each node are:");
    PrintChildren(Root, adj);

    Console.WriteLine("The leaf nodes of the tree are:");
    PrintLeafNodes(Root, adj);

    Console.WriteLine("The degrees of each node are:");
    PrintDegrees(Root, adj);   }
}
```

# Quizzes

1. What is Heap Data Structure?
2. What is the Heap Sort?
3. What are the basic Heap Operations?
4. What type of the following heap a, b:



5. What is the difference between Min Heap and Max heap?
6. Explain Heapify and where it is used in heap operations.

7. What is a tree data structure?
8. For the expression  $(7-(4*5))+(9/3)$  which of the following is the post-order tree traversal?
9. For the expression  $(7-(4*5))+(9/3)$  which of the following is the pre-order tree traversal?
10. For the expression  $(7-(4*5))+(9/3)$  which of the following is the In-order tree traversal?
11. Construct a binary tree by using post-order and in-order sequences given below.  
In-order: N, M, P, O, Q; Post-order: N, P, Q, O, M
12. Which (Pre, In, Post Order) traversal's pseudo code is written here?  

order(node)	print current_node.value
Q $\rightarrow$ Queue()	if current_node.left is not NULL:
Q.push(node)	Q.push(current_node.left)
while !Q.empty():	if current_node.right is not NULL:
current_node = Q.pop()	Q.push(current_node.right)

