

# **5T3: Sinusoidal Model**

## **(3 of 3)**

***Xavier Serra***

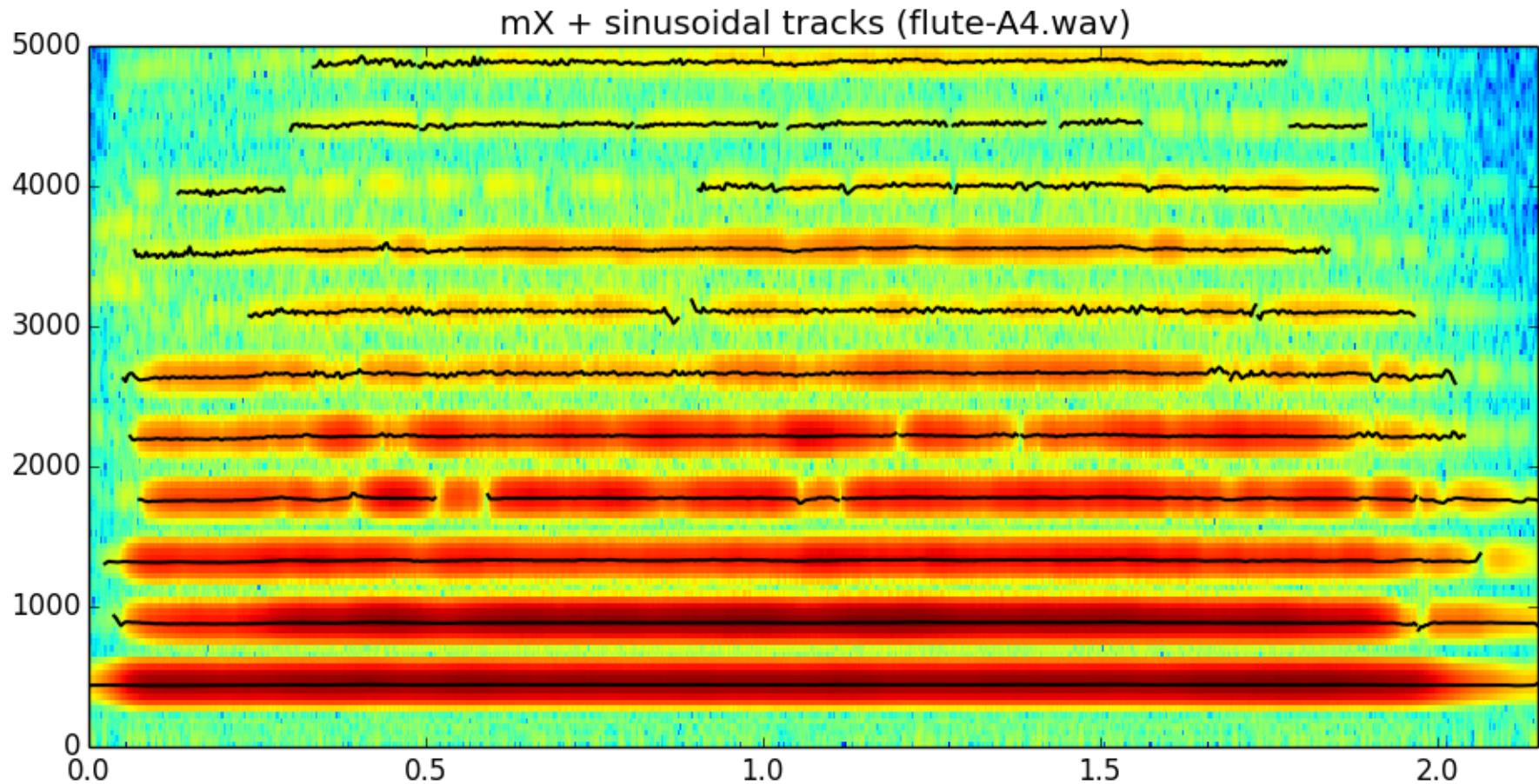
Universitat Pompeu Fabra, Barcelona

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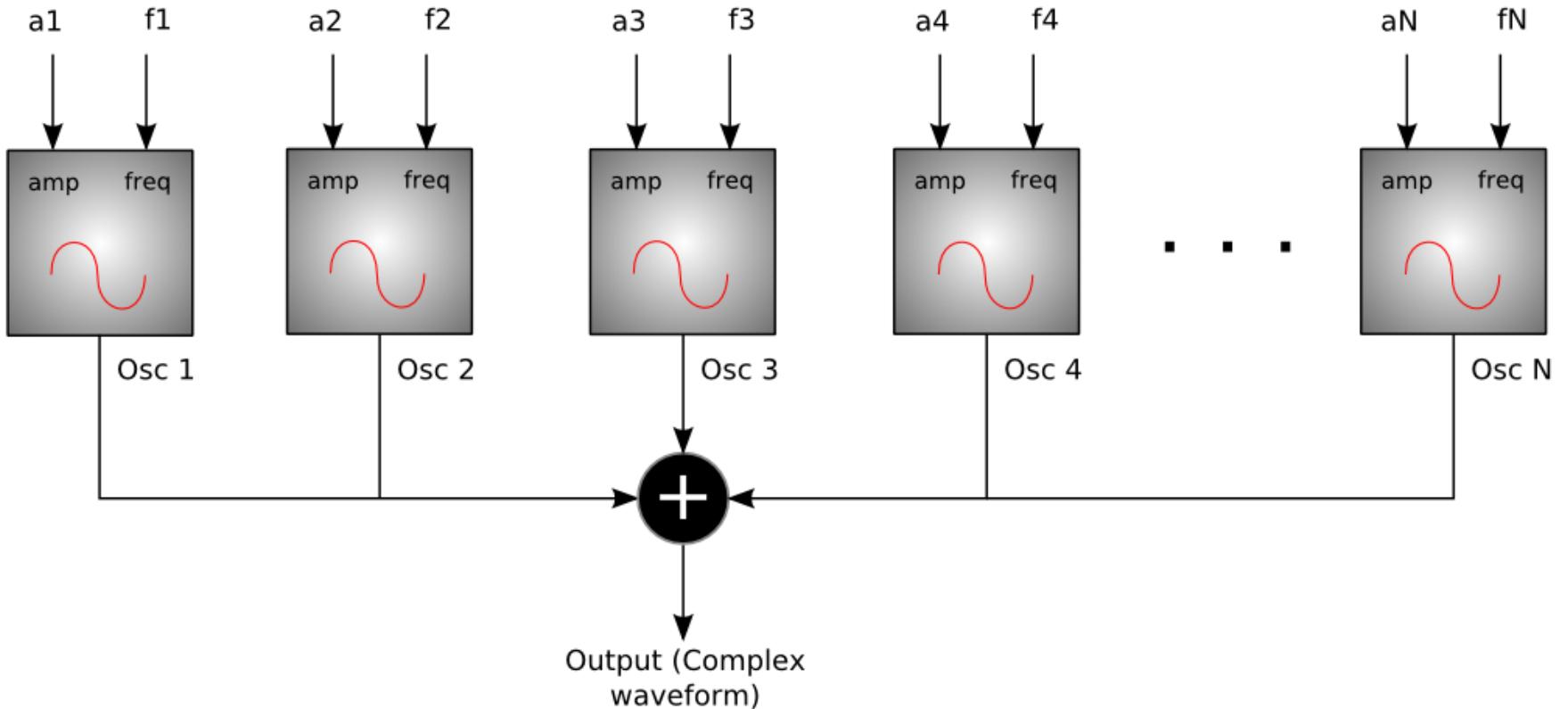
- Sinusoidal model and spectral peak tracks
- Sinusoidal (additive) synthesis
- Sinusodal model system

# Sinusoidal model

$$y[n] = \sum_{r=1}^R A_r[n] \cos(2\pi f_r[n]n)$$



# Sinusoidal (additive) synthesis

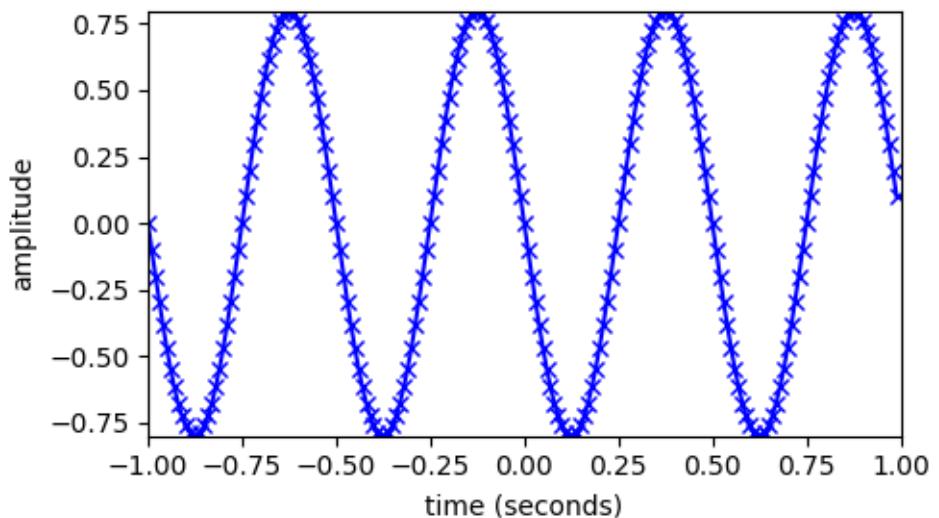


# Sinusoidal synthesis

$$y[n] = A_r[n] \cos(2\pi f_r[n]n + \phi_r)$$

$A_r[n]$ :instantaneous amplitude ;  $f_r[n]$ :instantaneous frequency  
 $\phi_r$ :initial phase

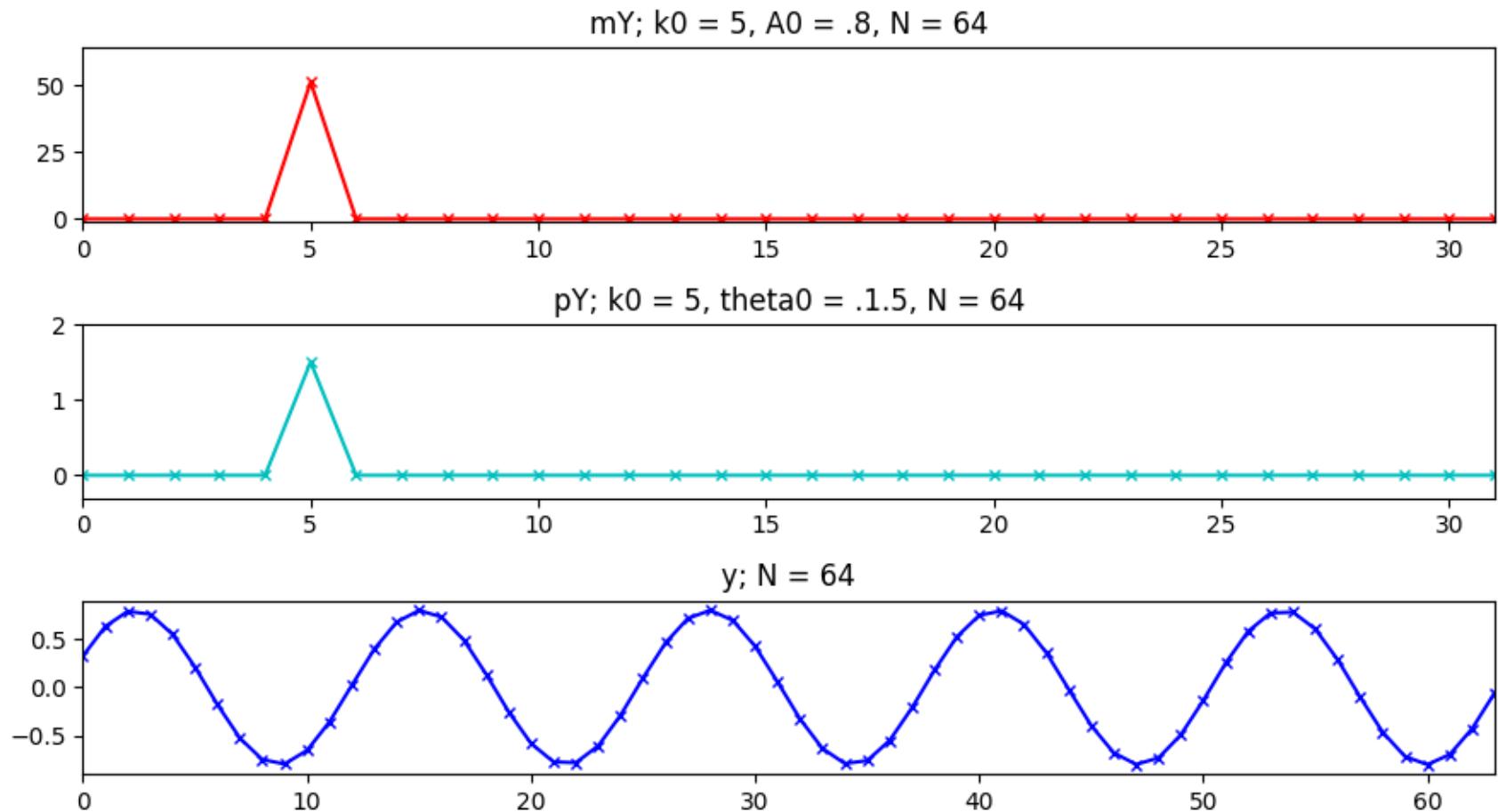
```
Ar = .8
fr = 2.0
phi = pi/2
fs = 100
t = arange(-1, 1, 1.0/fs)
x = Ar * cos(2*pi*fr*t+phi)
```



# Sinusoidal synthesis: discrete frequency

$$y[n] = IDFT(mY[k] * e^{j * pY[k]})$$

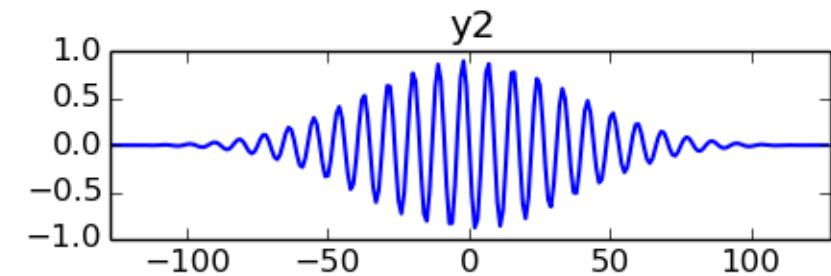
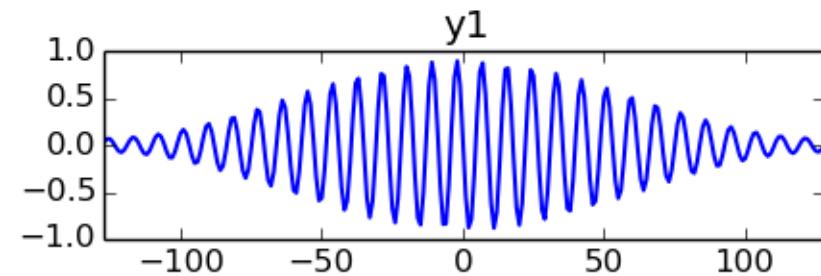
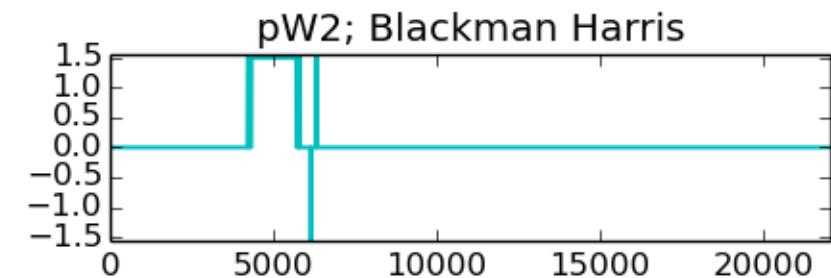
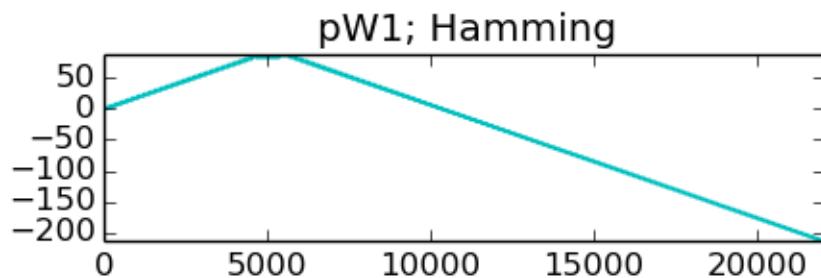
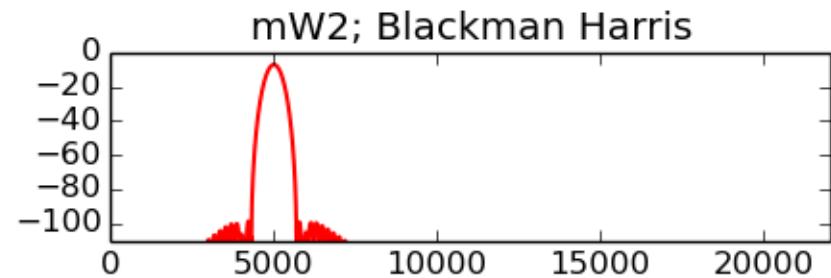
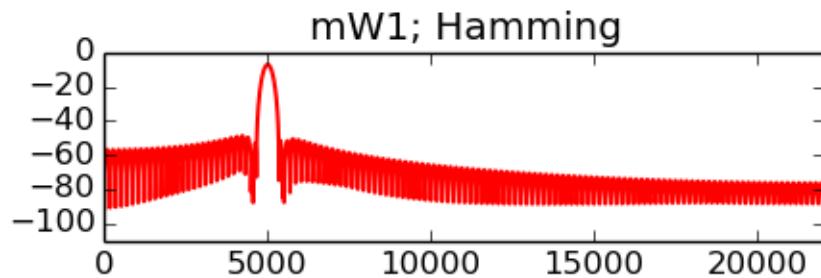
$mY[k] = A_0$  for  $k = k_0$  and 0 for  $k \neq k_0$ ;  $pY[k] = \phi_0$  for  $k = k_0$  and 0 for  $k \neq k_0$



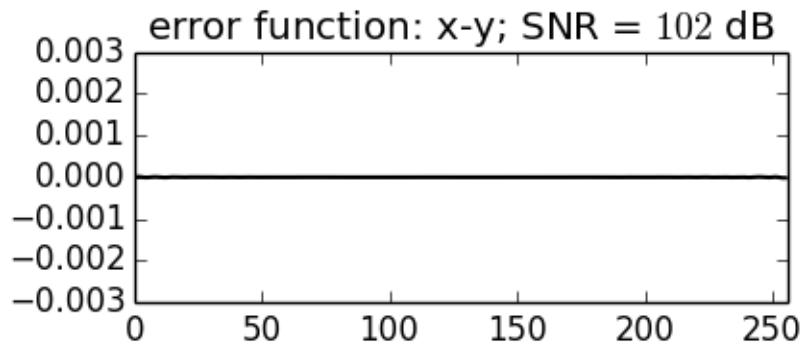
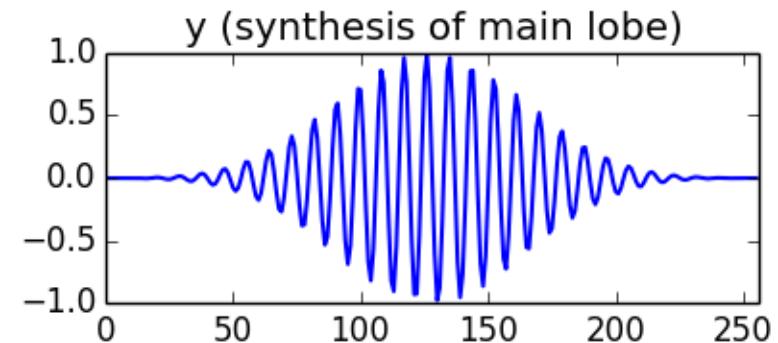
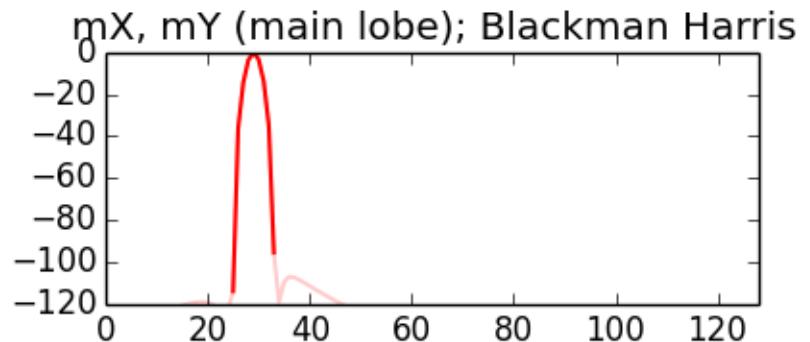
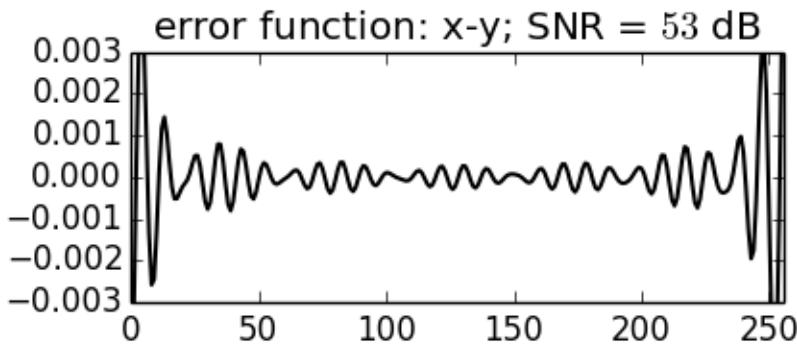
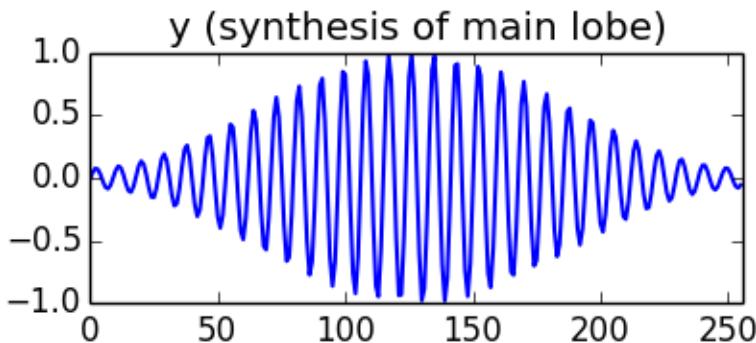
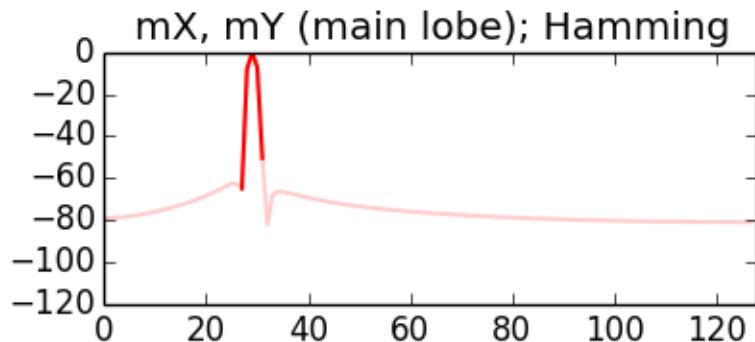
# Sinusoidal synthesis: any frequency

$$y[n] = IDFT \left( A_0 * mW[k - k_0] * e^{j*(pW[k - k_0] + \phi_0)} \right)$$

$mW[k]$ ,  $pW[k]$  magnitude and phase spectrum of window



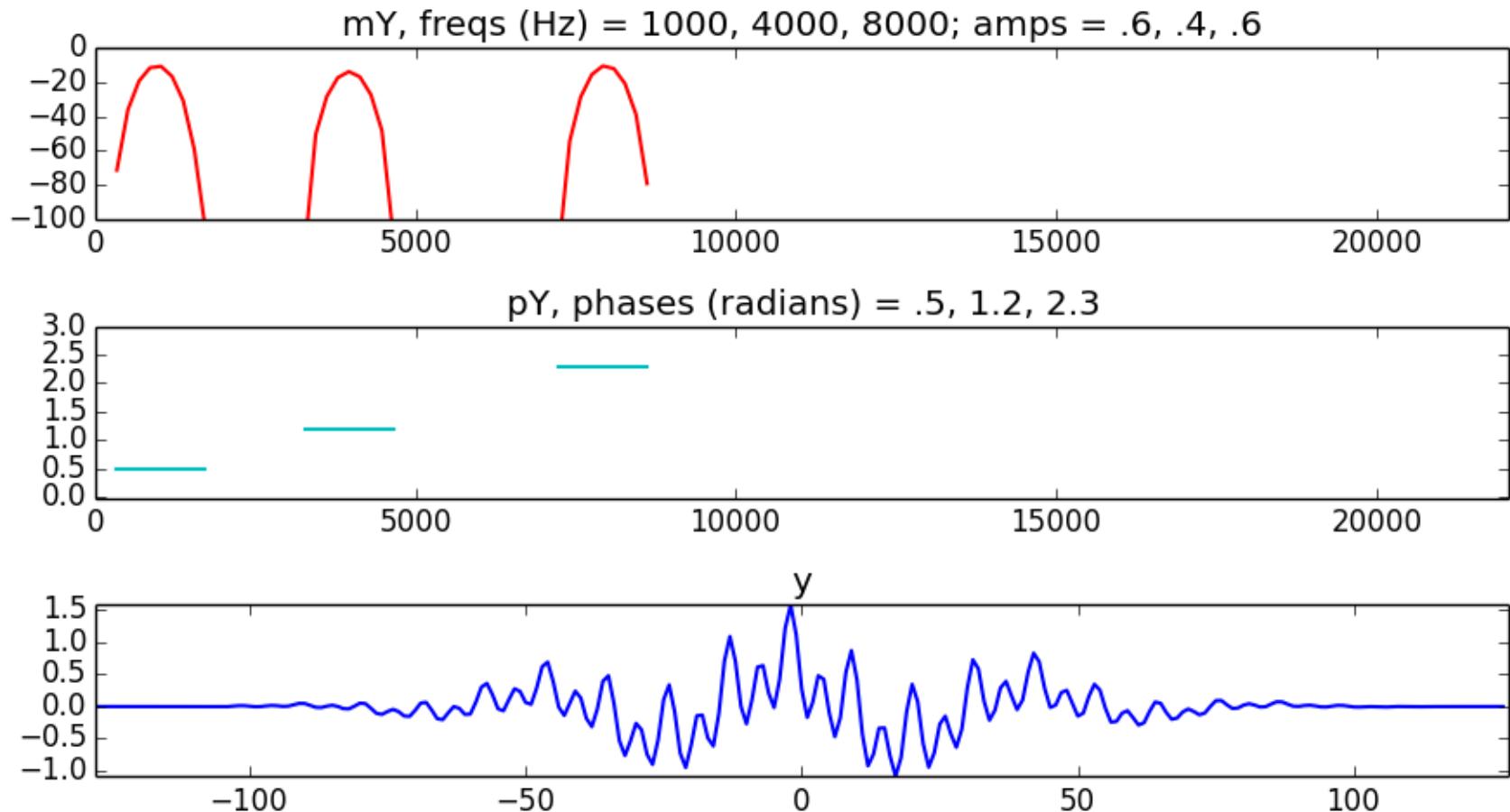
# Sinusoidal synthesis: only main lobe



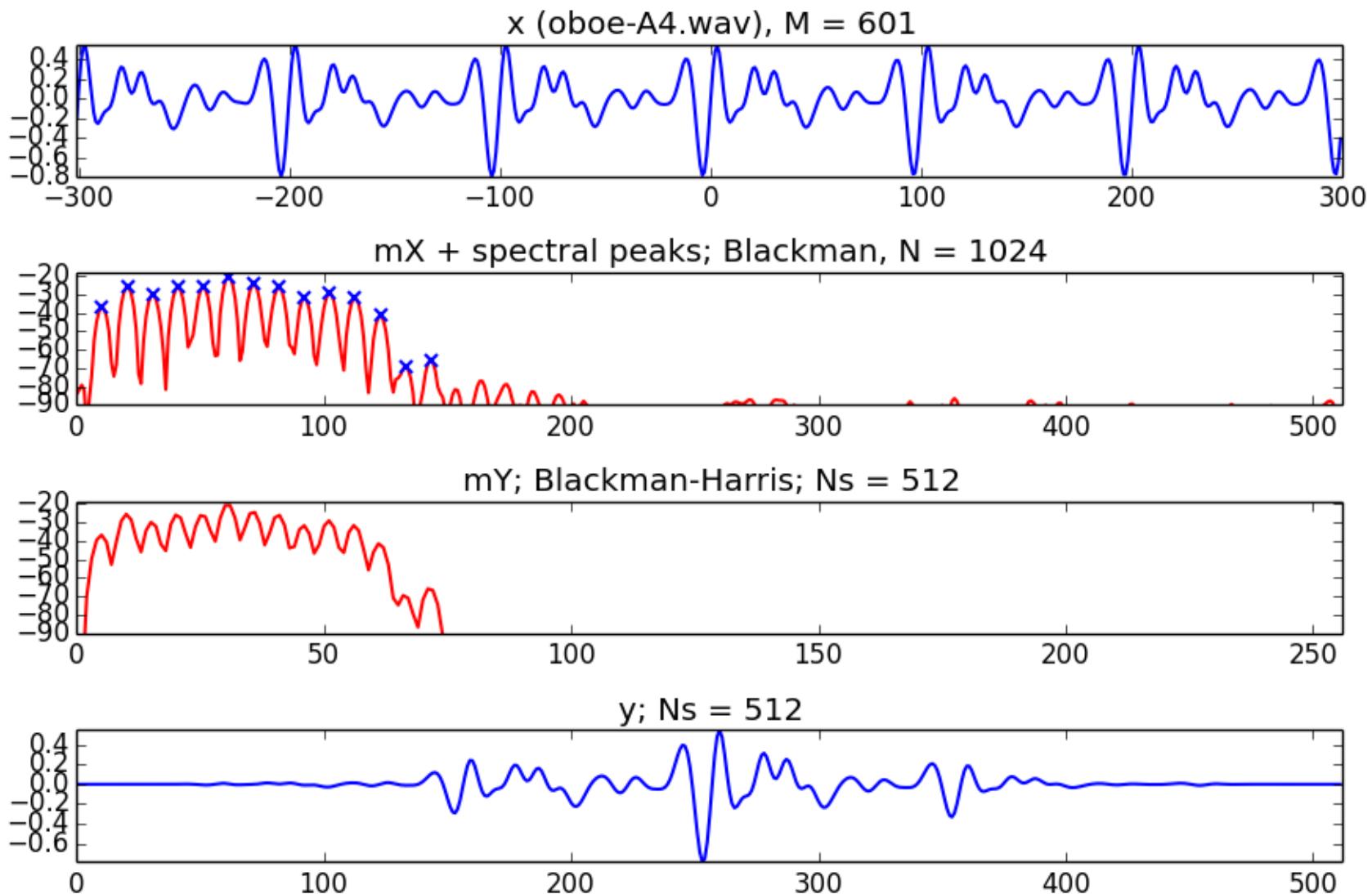
# Additive synthesis

$$y[n] = IDFT \left( \sum_{r=0}^R A_r * mWl[k - k_r] * e^{j*(pWl[k - k_r] + \phi_r)} \right)$$

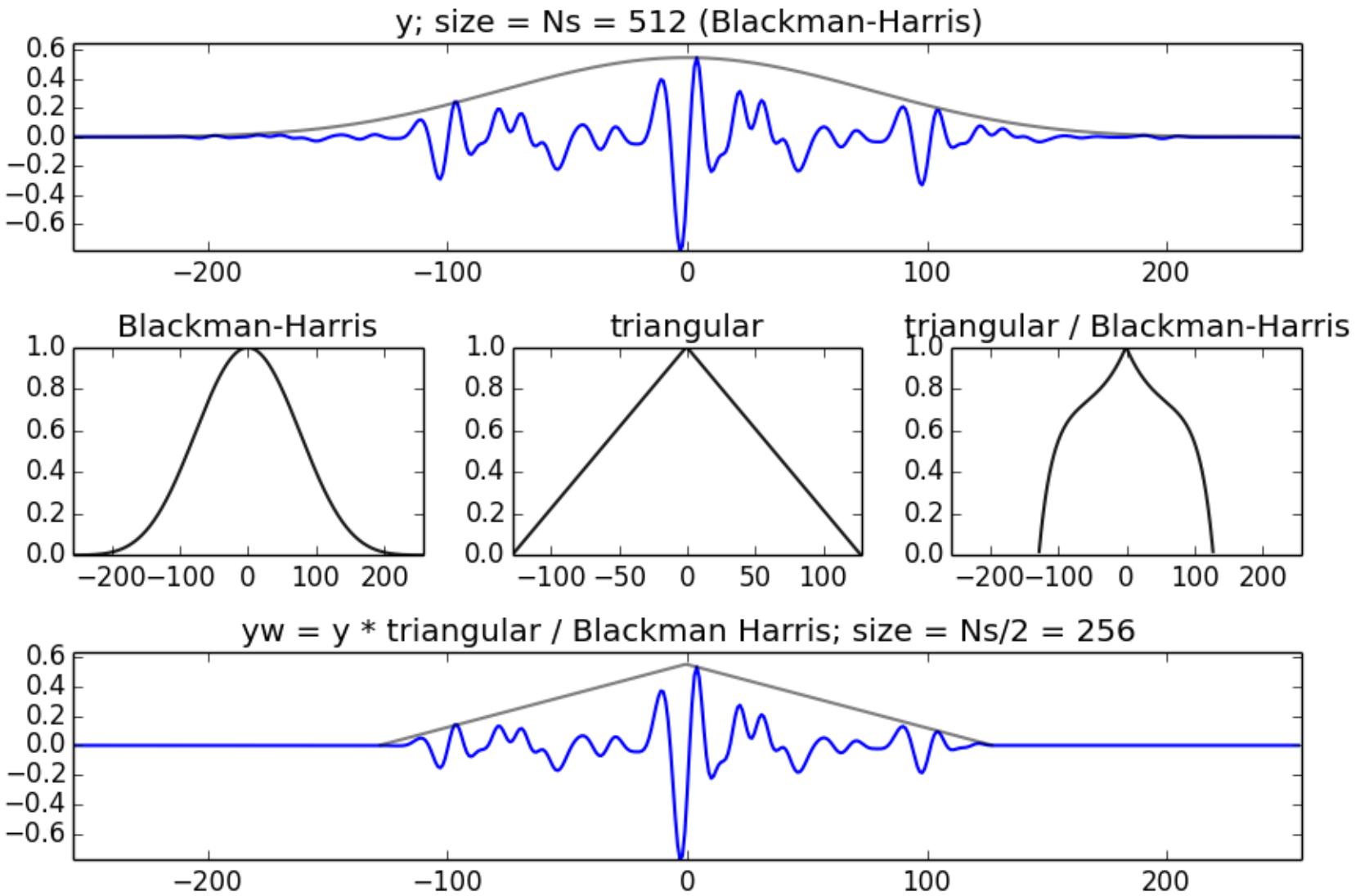
$mWl[k]$ ,  $pWl[k]$  magnitude and phase spectrum of window main lobe



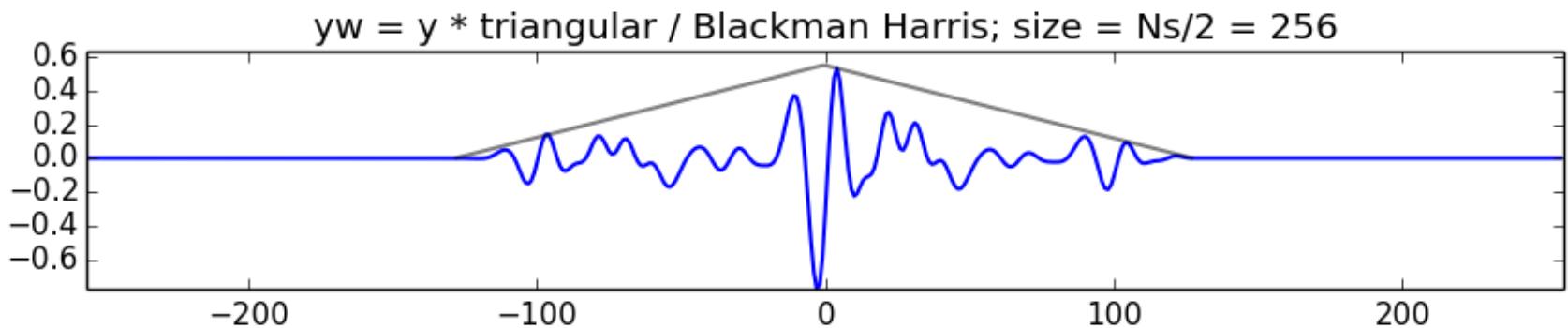
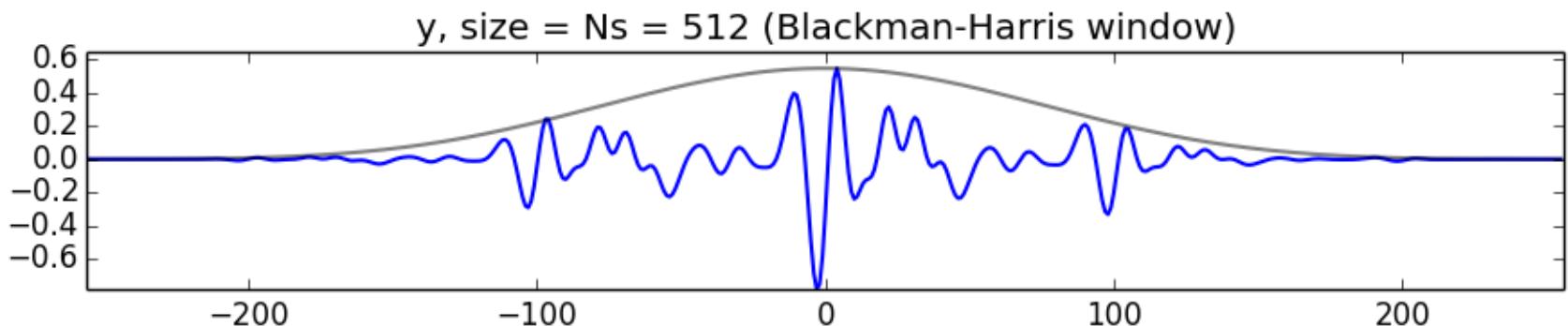
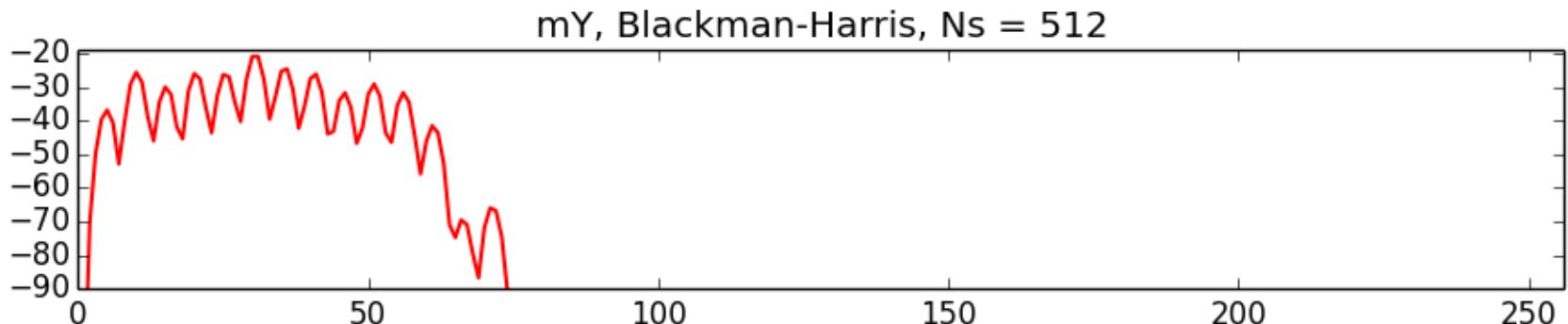
# Analysis / Synthesis



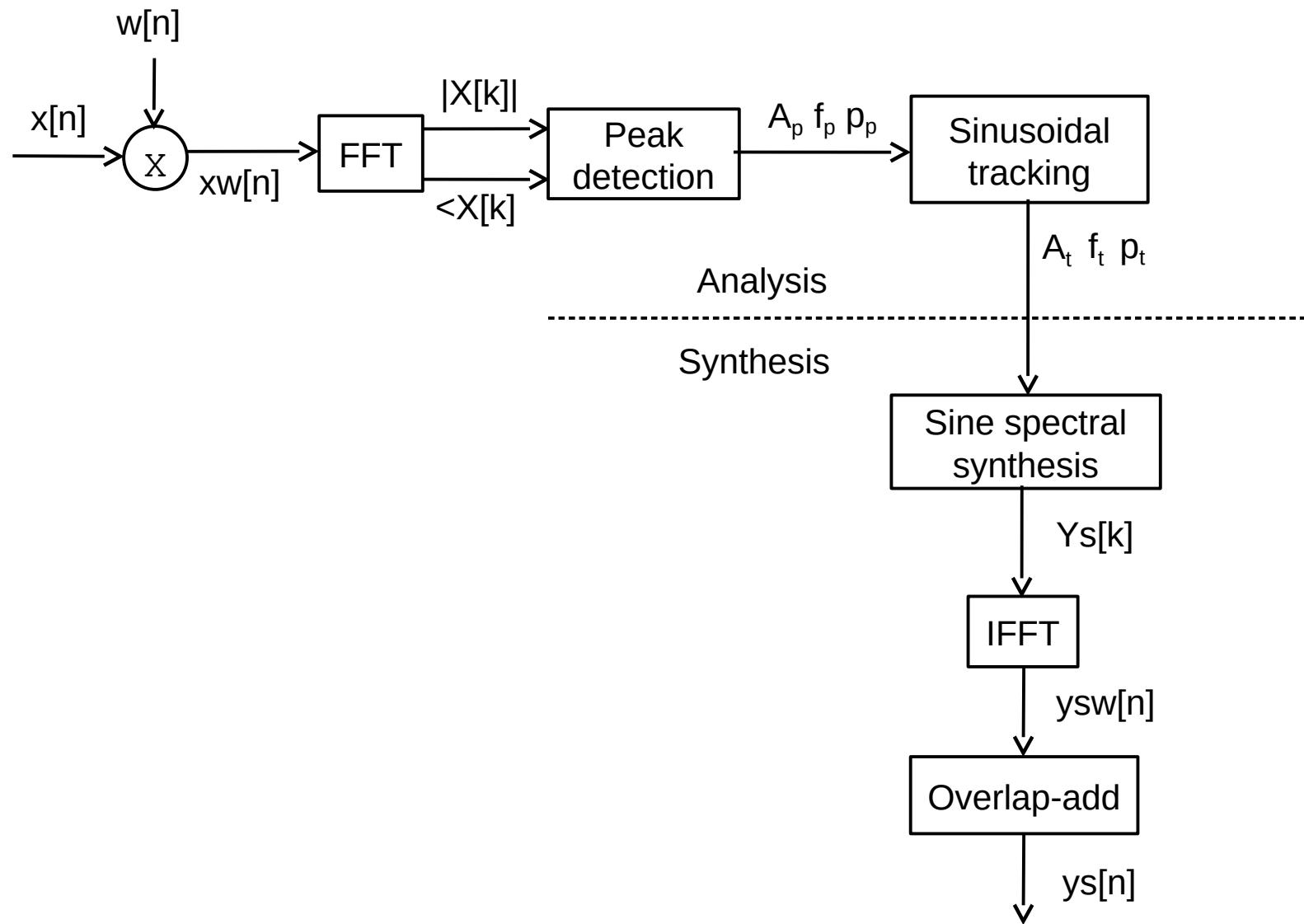
# Synthesis window



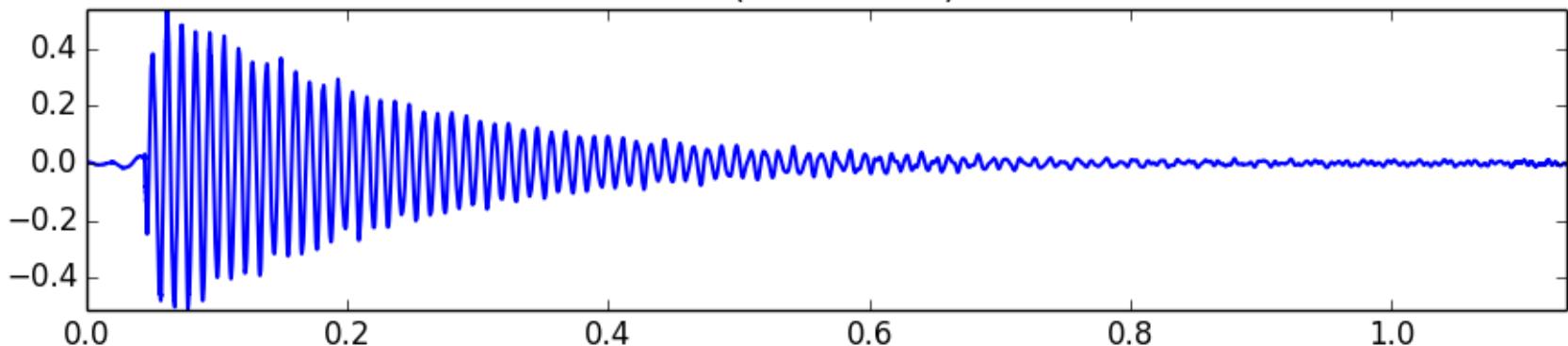
# Synthesis for overlap of 25%



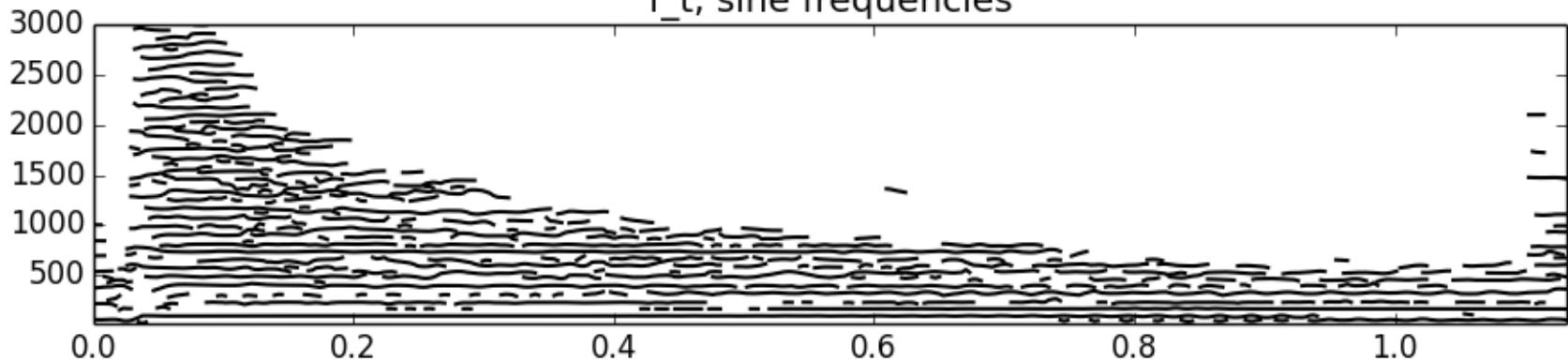
# Sinusoidal model system



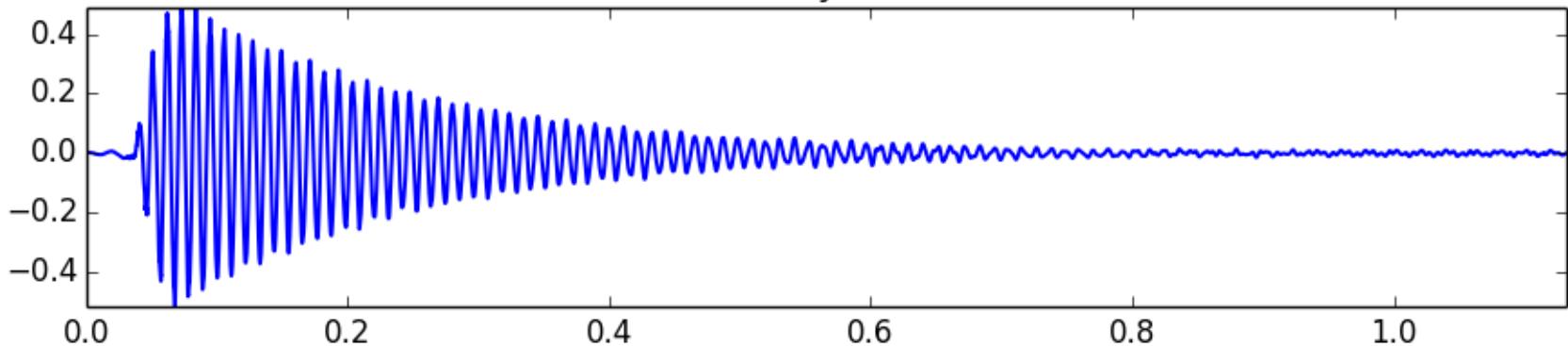
x (bendir.wav)



f\_t, sine frequencies



y



# References and credits

- More information in: [http://en.wikipedia.org/wiki/Additive\\_synthesis](http://en.wikipedia.org/wiki/Additive_synthesis) [http://en.wikipedia.org/wiki/Sinusoidal\\_model](http://en.wikipedia.org/wiki/Sinusoidal_model)
- Reference on sine modeling by Julius O. Smith: [https://ccrma.stanford.edu/~jos/sasp/Spectrum\\_Analysis\\_Sinusoids.html](https://ccrma.stanford.edu/~jos/sasp/Spectrum_Analysis_Sinusoids.html)
- Sounds from: <http://www.freesound.org/people/xserra/packs/13038/>
- Slides released under CC Attribution-Noncommercial-Share Alike license and code under the Affero GPL license; available from <https://github.com/MTG/sms-tools>

# **5T3: Sinusoidal Model**

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