

Lydia Teinfalt, 3/25/2025, HW6: Low-level Noise Added to Edgeworth Box Code simulating the real-world unpredictability of bilateral exchange between two agents and 2 goods
specs: Python 3x on Google Collab and Spyder

Background from Homework 5

Consumer (agents) class instantiated with Cobb-Douglas preferences with α, β randomly chosen from the list of values = 0.25, 0.33, 0.5. Consumer's initial endowment x_1 is randomly initialized with possible values from 1 to K and x_2 with possible values 1 to L. The parameters, K and L, are global variables representing the dimensions of the Edgeworth box and maximum amounts of goods 1 and goods 2 that can be traded between consumer 1 and consumer 2.

The Population class is instantiated with N agents. The model selects two consumers randomly and determines if a trade is possible. Trade is possible if given the two selected consumers do not have the equal marginal rates of substitutions (MRS) (Foundations of ABM, p. 67)

Cobb-Douglas preferences (see appendix G), i.e.,

$$U^i(x_1^i, x_2^i) = (x_1^i)^{\alpha^i} (x_2^i)^{1-\alpha^i}$$

From this we can compute the marginal rates of substitution:

$$MRS_{12}^i(x^i) = \frac{\frac{\partial U^i(x^i)}{\partial x_1^i}}{\frac{\partial U^i(x^i)}{\partial x_2^i}} = \frac{\alpha^i x_2^i}{(1-\alpha^i)x_1^i}.$$

If exchange is possible, the trade is executed by randomly selected a new x_1 between consumer 1's x_1 initial endowment and consumer 2's x_1 initial endowment. A new x_2 is derived from a contract curve between the two consumers based on the following formula (1) (Foundations of ABM, p. 76)

Solving this for x_2^i as a function of x_1^i gives

$$x_2^i = \frac{\alpha^j (1 - \alpha^i) x_1^i x_2^T}{\alpha^i x_1^T (1 - \alpha^j) - x_1^i (\alpha^i - \alpha^j)} \quad (1)$$

Code Introducing Low-Level Noise HW6

```
# Function to execute trade between two consumers by picking a value from the contract curve
# Low level noise added to simulate real-world unpredictability controlled by noise_level
# If the randomly generated value is above or equal to the noise level which is set by default to 0.5,
# then randomly select a y_new value between consumer 1 and 2's endowment2 values instead of a
# value on the contract curve
```

```
def execute_trade(self, consumer1, consumer2, noise_level=0.5):
```

```
    # Pick a random value of x within the range of their endowments
```

```
    x_new = random.uniform(consumer1.endowment1, consumer2.endowment1)
```

```
    #total endowments of consumers 1 and 2
```

```
    x_total = consumer1.endowment1 + consumer2.endowment1
```

```
    y_total = consumer1.endowment2 + consumer2.endowment2
```

```
    # generate random x between 0 and 1
```

```
    # introducing low level of noise into the process
```

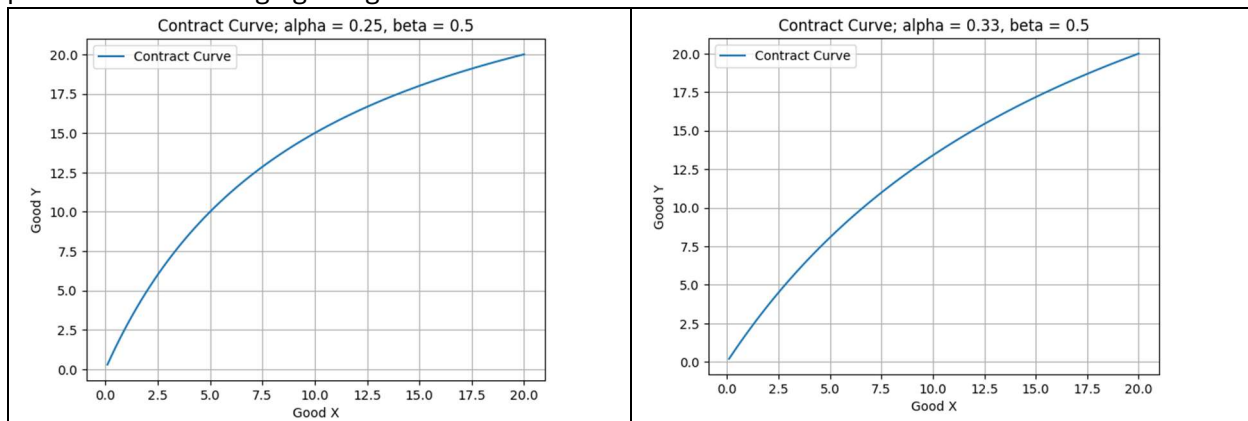
```
# to simulate real-world unpredictability in trades
randx = random.rand()
if randx >= noise_level:
    #print("Random 'noise' variable meets criteria, execute trades",randx)
    y_new= random.uniform(consumer1.endowment2, consumer2.endowment2)
else:
    # Calculate the corresponding y value on the contract curve
    y_new = (consumer1.beta*(1-
consumer1.alpha)*x_new*y_total)/(consumer1.alpha*x_total*(1-consumer1.beta)-
(x_new*(consumer1.alpha - consumer1.beta)))
```

Results HW 6

Simulation creates a population of N consumers trading two goods and have agents trade until the population reaches Pareto Optimality or the maximum number 1000 trades. Simulation re-run for 45 runs. Columns D and F display the new results of the run with low-level noise code introduced. With 10 agents, the new code shows a higher percentage of experiment runs (out of 45) where Pareto Optimality solution is found and at a lower number of trades required. At 20 agents, the new code resulted in more runs reaching pareto optimality than without the noise but at a cost of a greater average number of trades. For 50 agents, pareto optimality declines dramatically and rise in cost for number of trades. At 70 and 100 agents, pareto optimality is never reached before the 1000 maximum number of trades is reached first.

A	B	C	D	E	F
Number of Agents	Number of Runs	% Runs with Pareto Optimal Solution	With Noise % Run Pareto Optimal Solution	Avg Number of Trades	With Noise Avg Number of Trades
10	45	31%	42.22%	691.02	652.04
20	45	27%	37.78%	737.18	789.09
50	45	29%	2.22%	721.55	999.16
70	45	24%	0.00%	768.0	1000.00
100	45	40%	0.00%	629.36	1000.00

Sample contract curves between two agents with different alpha and beta levels Cobb-Douglas preferences exchanging two goods: X & Y



Code repository

<https://github.com/lydiateinfalt/CSS610-AgentBasedModelingSimulation-Spring2025/blob/main/EdgeworthBoxNoise.py>