

Python DPDA Executor

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High Level Idea

- Represent the components of a DPDA using simple data structures that are already present in Python
- Execute the acceptance or denial of a string in a provided DPDA
- Create DPDA Complement
- Execute the acceptance or denial of a string in the complement of the provided DPDA
- Neat debug printout for user understanding.

Data Structures?

- **DPDA Requires a Pushdown Stack.**
 - Use a list in python:
 - Pop: `list.pop()`
 - Push: `list.append()`
 - Intricacy: Must push things in proper order, i.e. 'aZ' must be pushed as 'Z', 'a'.
- **DPDA Requires a set of transitions**
 - Nested lists
 - `[[q0, x, y, q1, z], [...], ...]`
- **How to represent the whole DPDA for input?**
 - JSON
- **How to represent the whole DPDA internally?**
 - Dictionary, easily parsed by `json.loads()`

JSON DPDA Representation

```
{  
  "states": [  K = finite state set  
    "q0",  
    ...,  
    "qn"  
  ],  
  "alphabet": [   $\Sigma$  = finite input alphabet  
    "a",  
    ...,  
    "n"  
  ],  
  "stack_alphabet": [   $\Gamma$  = finite stack alphabet  
    "b",  
    ...,  
    "m",  
    "Z"  
  ],  
  "start_state": "q0",   $s \in K$ : start state  
  "final_states": [   $F \subseteq K$ : final states  
    "q1",  
    ...,  
    "qn"  
  ],  
  "transition_functions": [   $\Delta$ , a finite subset of  $(K \times (\Sigma \cup \{\epsilon\})^* \times \Gamma^*) \times (K \times \Gamma^*)$   
    ["q0", "b", "a", "q0", "ba"],  
    ...,  
    ["q0", "c", "Z", "q2", "Z"]  
  ],  
}
```

How the program works

1. Parse the JSON, sanity check the start and end states.
2. Loop:
 - a. Filter the list of all transitions by which one(s) we can take given
 - i. Current state
 - ii. Current character
 - iii. Stack top character
 - b. Take the move, provided there is only one transition
 - i. If there are no possible transitions, we are at a trap / 'end' state
 - ii. If there are multiple transitions, this signals nondeterminism.
3. Repeat for language / DPDA Complement

DPDA Complement?

To get the complement of a DPDA, make all non-final states final states, and make all final states non-final states.

For a DPDA represented as a dictionary, this is a matter of simple set manipulation.

```
accepting_states = dpda_dict["final_states"]
nonaccepting_states = (
    set(dpda_dict["states"])
    - set(dpda_dict["final_states"])
    - {dpda_dict["start_state"]}
)

complement_dict = dpda_dict
complement_dict["final_states"] = list(nonaccepting_states)

return complement_dict
```

Demonstration