

## CS 321 HW 4 – 30 points

1. (5 pts) Convert the grammar below to CNF.

$G = (V, T, S, P)$  where  
 $V = \{ S, A, B, C, D \}$   
 $T = \{ 0, 1, 2 \}$   
and  $P$  is given below.

$S \rightarrow A \mid ABD \mid 0BB$   
 $A \rightarrow 0 \mid BAA$   
 $B \rightarrow BB \mid 1 \mid 2 \mid \lambda$   
 $C \rightarrow CD \mid 0$   
 $D \rightarrow D1 \mid DD$

2. (10 pts) Consider the CNF grammar  $G = (V, T, S, P)$  where

$V = \{ S, A, B, C, D \}$ ,  $T = \{ a, b, c \}$ ,  $S = S$  and  $P$  is given below.

$S \rightarrow AB \mid AD \mid AC$   
 $A \rightarrow AA \mid a$   
 $B \rightarrow BB \mid AB \mid b$   
 $C \rightarrow AC \mid DC \mid c$   
 $D \rightarrow DD \mid b \mid c$

Use the CYK algorithm to determine if the strings  $w_1 = babbc$  and  $w_2 = aaaabb$  are in the language  $L(G)$ . Show the DP table. If the string is in  $L(G)$  construct the parse tree.

3. (15 pts) Construct npda's that accept the following languages on  $\Sigma = \{a, b\}$ . Give both a verbal explanation on how your npda works and the formal definition including the transition function and/or transition graph. **You must use JFLAP**. Submit the transition graph in the HW pdf and the JFLAP code file for each problem.

a)  $L = \{ a^n b^{2n} : n \geq 0 \}$

b)  $L = \{ w : n_a(w) = 2n_b(w) \}$

c)  $L = \{ wcw^R : w \in \{a, b\}^* \}$