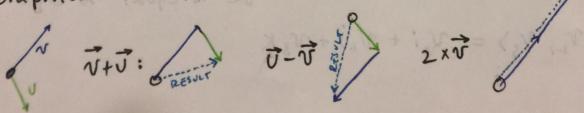
#### CHAPTER 11. \* 10/4/2018 REVIEW

- 11.1 VECTORS IN THE PLANE THESE ARE CHALLENGES · Vector is any segment that has both magnifide (171) and direction (0). Denoted as  $\vec{v} = \langle ..., ..., ... \rangle$ 
  - · Displacement vectors: A displacement rector from P to Q is indicated by PQ
  - · Position Vector: Any vector that has 0 (0,0,0) as It's tall end ("starts at 0")
- · Unit Vector: vector vi with magnitude |vi = 1 -> can be calculated by \(\frac{N}{|V|} = Unit Vector in dir. of \(\vec{N}\)
- · Vector Magnitude: |v| = \v; + v2 + v3 assuming v = (v, N2, N2)
- · R: R': Number line. R2: Plane (typically xy). R3: 3D space
- · Vector properties:

Define Nectors  $\vec{v} = \langle v_1, v_2, v_3 \rangle$   $\vec{v} = \langle v_1, v_2, v_3 \rangle$ n\*v = (nv,, nv2, nv3) N+V= (V,+V,, N2+U2, V3+U3)  $\vec{\nabla} - \vec{U} = \vec{\nabla} + (-\vec{U})$ - = (-V, + -V2, -V3)

· Graphical Manipulation:



## 11.2 VELTORS IN THREE DIMENSIONS

- · 3 prinupal unit vectors: i(1,0,0), j(0,1,0), k(0,0,1)
- · Equation for a circle, centered at (a,b) with radius r: → r2 = (x-a)2 + (y-b)2
- · Equation for a sphere centeredat (0,6,C) with radius r
- · Ball: all the points on, or inside of a sphere. Equation for a ball centered at (a,b,c) with radius r:  $\rightarrow (x-a)^2 + (y-b)^2 + (z-c)^2 \leq r^2$
- sets and "construct"
- · sets and "constraints":

$$\mathbb{R}^{2} \begin{cases} (x,y): x=a \} = \text{line } x=a \\ \{(x,y): x=a, y=b \} = \text{point } (a,b) \end{cases} \begin{cases} (x,y): x=a \text{ or } y=b \} = \text{lines} \\ \text{at } (a,b) \end{cases}$$

$$\begin{cases} (x,y, \pm): x=a \end{cases} = \text{plane } x=a \\ \{(x,y, \pm): x=a, \pm 2 \}: \text{point} \end{cases}$$

$$\begin{cases} (x,y, \pm): x=a, y=b \end{cases} = \text{plane } x=a \\ \{(x,y, \pm): x=a, y=b \}: \text{point} \end{cases}$$

$$\begin{cases} (x,y, \pm): x=a, y=b \end{cases} = \text{plane } x=a \\ \{(x,y, \pm): x=a, y=b \}: \text{point} \end{cases}$$

$$\begin{cases} (x,y, \pm): x=a, y=b \end{cases} = \text{plane } x=a \\ \{(x,y, \pm): x=a, y=b \}: \text{point} \end{cases}$$

- · "Circle Magic": for a wick with r=1, center at 0: -> all points on will are (x=rwso, y=rsino) [ =1] -> arc length from (1,0) to an angle is equal to 0[s=10]
- · v= (v, v2, v3) = v, i + v2) + v3 K

Lyell ( Read CHs 11.3, 11.9, 11.5 Review 10/2/2018 FOR QUIZ ON 10/3/2018

#### 11.3 DOT PRODUCTS

- · U dot v = | U | V | COSO | 0 = between J, J
- · U dot v = U, V, + U2U2 + V3U3 If U= (U, U2, U3), V= (V, V2, V3)
- · LOS O = Udot v / WIVI
- · Projection: projet = |V| wso (U) = U·V (U) = (U·V) U
- · Scalar: Scalov = |V| cost = U.V · dot product of  $\perp$  vectors is always o cos(90) = 0!
- · I and // components to a borce (grav). ver sin 0 = 11 Vec ws 0 = 1

MIN &

### 11.4 CROSS PRODUCTS

- · Matrix Determinants: | ab ( = ad bc for 2x2
- · Matrix 3x3 Determinant: 12

$$\begin{vmatrix} a-b & c \\ -d & ef \end{vmatrix} = a \begin{vmatrix} ef \\ -b \end{vmatrix} gil + c \begin{vmatrix} de \\ gh \end{vmatrix} mense above$$

$$\begin{vmatrix} g-h & i \end{vmatrix} = a \begin{vmatrix} ef \\ h & i \end{vmatrix} - b \begin{vmatrix} gil \\ gil + c \end{vmatrix} gh \end{vmatrix}$$

- · cross Product: UX v = |u||v| sin & between u, v - perpendicular to both u, v . Use Right Hand Rule.
- · Area of a parallelogram = |u||v|sint
- · Area of a parallel operpet war. w
- · Torque T = | F| | 4 SINO = | F x L|

- · Area of b = |UXV| = = |U||V|sint or use Matricies

# 11.5 LECTUR DEFINED FUNCTIONS

- · line through point, in direction (t) = point + + dir.
- · Une through v, v v-v = dir r(t) = v + t dir
- · line for from eq (remove everything but what is mult by t)

| a - b | = a | c | - b | gil + c | g | panse above

eapendwia to both u, a use Right Hand Rule.

· Wass Product: UX 4 = |u| [v| sin & behiven u, 4

· Her of a paralleloperpet it fing uxu. w

· Lovane I = 16/1/20ma = 16 x FI

· Mayrix 3X3

· Area of a paralelogram

# 11.6 CALWLUS ON VECTOR DEFINED FUNCTIONS

- · Derivative of r(+) = < X(+), y(+), Z(+) > = r'(+) = < x'(+), Y'(+),
- Integrals of  $r(t) = \langle \chi(t), \gamma(t), \xi(t) \rangle =$   $\rightarrow \int r(t) dt = \langle \int \chi(t), \int \gamma(t), \int \xi(t) \rangle dt + \langle C_1, C_2, C_3 \rangle$
- and without C. Remember:  $\int_{a}^{b} \frac{d^{2}}{dt} = \frac{1}{R(b)} \frac{dt}{dt}$
- · Tangent vector at apoint is the derivative evaluated at that point.
- · Unit Tangent Vector r'(+) = UT+
- r(t) from v'(t): calc ANTIDERWATIVE then make sure that the point given works (and ± A for any valves [(valve..., ..., ...)] that med dijusting).
- -> Tangent line Equation: for r(t) at point a

  -> T(t) = tangent line = r(a) + t\*(r'(a)) "Direction"
- Points where r(t) and r'(t) are orthogonal:

  -> where  $r(t) \cdot r'(t) = 0$  ...  $r_1(t)r_1'(t) + r_2(t)r_2'(t) ... = 0$