

12.1 PLANES IN 3D

- Eq. for a plane by Point (P_0) and normal (\vec{n}), and (P)
 $P = (x, y, z)$ $P_0 = (x_0, y_0, z_0)$ $n = \langle a, b, c \rangle$
 $\rightarrow ax + by + cz = ax_0 + by_0 + cz_0$
- Eq for a plane with two vectors \vec{v}_1, \vec{v}_2
 $\rightarrow \vec{n} = \vec{v}_1 \times \vec{v}_2$
- Eq for a plane with three points P, Q, X
 $\rightarrow \vec{v}_1 = \vec{PQ}$ $\vec{v}_2 = \vec{PX}$ $P = "P_0"$, $\vec{n} = \vec{PQ} \times \vec{PX}$
- Axis Intersections: x axis: $y=0, z=0$ y axis: $x=0, z=0$
z axis: $x=0, y=0$
- Plane Intersection $XY: z=0, XZ: y=0, YZ: x=0$
- Parallel Planes: have \vec{n} that is a scalar factor of \vec{n}_1
- Perpendicular Planes: $\vec{n}_1 \cdot \vec{n}_2 = 0$
- Line of intersection of two planes: substitute $z=0$ and solve sim eq's. $P_0 = (x, y, 0)$. Find cross product of normals for direction.
- Norm (\vec{n}) from $n_1x + n_2y + n_3z = \dots$ $\vec{n} = \langle n_1, n_2, n_3 \rangle$

12.2 3D FUNCTIONS AND LEVEL CURVES

- Graphing: Make shadows in applicable planes, substituting z where applicable (Planes XY, XZ, YZ , see above)
- Level Curves: $z = \overset{n \text{ for any value}}{c}$, solve for y and graph in xy
- Domain: all values of x and y that make eq valid, Range: Output (z)