ST314 Final Exam
Fall 2020

Take a deep breath. Read every question. Follow directions.
Be confident. Relax. You've got this!

Student Name: <Write your name here>

Student ID: <Write your ID number here>

Directions:

- This exam is open book and open note. You may use any materials posted on Canvas but please refrain from using any other resources.
- Please do not discuss the exam with anyone else in the class or outside of the class. Also, please do not post questions to online forums for help.
    - Do not share solutions, code, answers, etc. Answers which appear "too similar" will be forwarded to the *Office of Student Life* for investigation.
- Write you solutions where indicated in the exam document itself. Please don't make any other alterations to the exam.
    - I've tried to include a purple font color to make your solutions "stand out". If possible, keep the purple color for your solutions.
- When asked, please show your work and write explanations, justifications, etc. using complete sentences.
    - This is really helpful for assigning partial credit in case you do something incorrectly in the short answer section.
    - Do not show your work for the multiple choice questions.
    - If you need to include math, write it out in plain text or using Word's equation editor.
- Submit your completed exam as a PDF file to Gradescope prior to the deadline shown on Canvas.
    - Indicate where the solutions are in the uploaded document. Not doing this slows the grading process down considerably and will result in a points deduction for each instance the questions are not properly indicated in Gradescope.
- **Read each question slowly and carefully**. If you don't understand a question, write a post on the Midterm Exam Question Clarification discussion board on Canvas (But do not include solutions/partial solutions in your post).

Questions 1 – 2 (3 points each): **Choose the appropriate statistical procedure for the scenario. That is, which test is most appropriate for answering the question of interest?**

1. The width of a piston in an internal combustion engine can be measured using an analog caliper or with a digital laser. A piston manufacturer wants to decide if the added expense of purchasing digital lasers is worth the cost. They decide to compare both instruments by measuring each piston in a set of thirty with both instruments. They then compare the average measurements for each instrument.

   A. One sample z-test for the mean
   B. One sample t-test for the mean
   C. Two sample t-test for the difference in the means
   D. Matched pairs t-test
   E. Single-factor ANOVA
   F. Simple linear regression

   Answer: <Write just the letter of your answer here>

2. A car manufacturer produces a certain automobile at four different plants located throughout the United States. The manufacturer is interested in comparing the average number of cars produced per hour at each factory to see if they are similar or if there's evidence that one or more factories is producing more, or fewer, automobiles per hour. To accomplish this task, the manufacturer asks each factory to record the number of cars produced in five randomly chosen hours over the course of a week.

   A. One sample z-test for the mean
   B. One sample t-test for the mean
   C. Two sample t-test for the difference in the means
   D. Matched pairs t-test
   E. Single-factor ANOVA
   F. Simple linear regression

   Answer: <Write just the letter of your answer here>

Questions 3 – 5 (3 points each): **For each set of hypotheses, indicate the matching distribution needed to compute the *p*-value of the test**

3. Assume σ is **known**

$$H_0: \mu_1 = \mu_2$$
$$H_A: \mu_1 \neq \mu_2$$

A. z-distribution
B. t-distribution
C. Chi-square distribution
D. F distribution

Answer: <Write just the letter of your answer here>

4. Assume σ is **unknown**

$$H_0: \mu_1 = \mu_2$$
$$H_A: \mu_1 \neq \mu_2$$

A. z-distribution
B. t-distribution
C. Chi-square distribution
D. F distribution

Answer: <Write just the letter of your answer here>

5. Assume $\sigma_1 = \sigma_2 = \sigma_3$

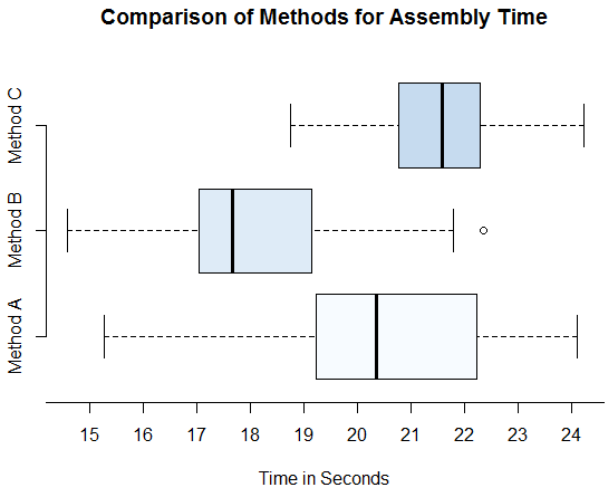
$$H_0: \mu_1 = \mu_2 = \mu_3$$
H_A: *At least two population means are different.*

A. z-distribution
B. t-distribution
C. Chi-square distribution
D. F distribution

Answer: <Write just the letter of your answer here>

Questions 6-10 (3 points each): Use the following scenario to answer the questions.

A manufacturer of videogame cartridges performs an experiment to compare the average time of three assembly methods. The goal of this analysis is to see whether these methods differ in average time to assemble the cartridge. Use the output provided to answer the following questions.



	Df	Sum Sq	Mean Sq	F value	Pr(>F)
Method	2	121.1	60.53	16.4	2.37e-06
Residuals	57	210.4	3.69		

	diff	lwr	upr	p adj
MethodB-MethodA	-2.221779	-3.683946	-0.7596126	0.0015977
MethodC-MethodA	1.208065	-0.254102	2.6702318	0.1243524
MethodC-MethodB	3.429844	1.967677	4.8920113	0.0000016

6. Based on the side-by-side boxplot, which statement is a **FALSE** description of the data?

   A. Method B is typically the fastest.
   B. Method C is typically the slowest.
   C. Method A the most variability of the methods.
   D. No method took longer than 17 seconds to produce a single cartridge.

   Answer: <Write just the letter of your answer here>

7. From the Single-Factor ANOVA table, which value represents the **average** *between* group variation?

   A. 2.37e-06
   B. 3.69
   C. 16.4
   D. 60.53

   Answer: <Write just the letter of your answer here>

8. The F statistic and p-value from the Single-Factor ANOVA table represent a null hypothesis of:

A. $H_o: \beta_1 = \beta_2 = \beta_3 = 0$
B. $H_o: \bar{x}_1 = \bar{x}_2 = \bar{x}_3$
C. $H_o: \mu_1 = \mu_2 = \mu_3$
D. $H_o: \mu_1 = \mu_2 = \mu_3 = 0$

Answer: <Write just the letter of your answer here>

9. Based on the F test statistic and p-value from the Single-Factor ANOVA table, what can we conclude?

A. There is convincing evidence the average assembly times of at least two methods are different.
B. There is no evidence which suggests the average assembly times for the different methods are different.
C. The F test statistic comes from an F distribution of 3 and 60 degrees of freedom.
D. The test is not valid since Method B contains an outlier.

Answer: <Write just the letter of your answer here>

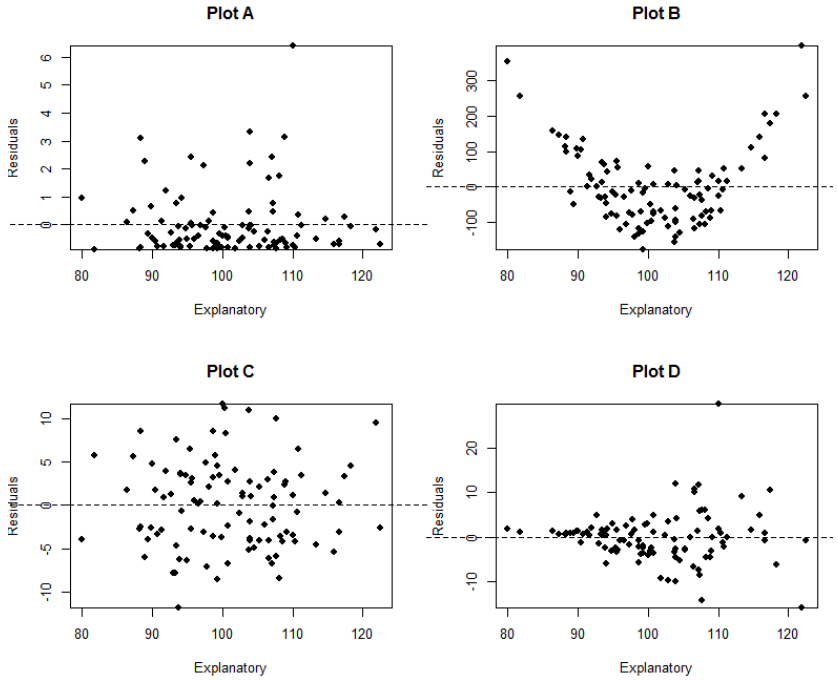
10. Based on the output from the multiple comparisons procedure, which statement is **FALSE** (Assume $\alpha = 0.05$)?

A. There is a significant difference between methods A and B.
B. Method A has smaller mean than Method B.
C. The 95% F-W confidence interval estimates Method B is approximately 1.97 to 4.89 seconds faster than Method C.
D. Method B has the fastest average assembly time in comparison to the other groups.

Answer: <Write just the letter of your answer here>

Questions 11 – 12 (3 points each): **Use the following scenario to answer the questions**.

Consider the residual plots below. What do they tell you about the relationship of the variables in a simple linear regression analysis? Each residual plot matches a specific violation or no violations.



11. Which plot provides evidence the variance is not the same for all values of the explanatory variable?

A. Plot A
B. Plot B
C. Plot C
D. Plot D

Answer: <Write just the letter of your answer here>

12. Which plot provides evidence the relationship between the response and predictors is not linear?

A. Plot A
B. Plot B
C. Plot C
D. Plot D

Answer: <Write just the letter of your answer here>

Questions 13 – 15 (3 points each): **Answer the following questions**.

13. The 90% confidence interval for μ is (1.8, 3.2). Assuming $n = 13$ and that σ is unknown, what is the 95% confidence interval?

    A. (1.646, 3.384)
    B. (1.644, 3.356)
    C. (1.926, 3.074)
    D. (1.928, 3.072)

    Answer: <Write just the letter of your answer here>

14. Fill in the blank cells (indicated with a "?") of the ANOVA table below (Each correct answer is worth 3 points):

Source	Degrees of Freedom	Sum of Squares	Mean Squares	F
Treatments	**5**	**?**	**?**	**7.8**
Error	**?**	**7640.0**	**95.5**	
Total	**85**	**?**		

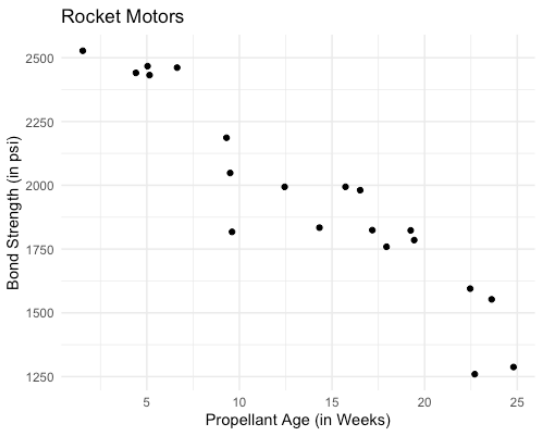
15. In a hypothesis test, if we fail to reject a true null hypothesis, we make…

    A. the correct choice.
    B. a type I error.
    C. a type II error.
    D. All of the above

    Answer: <Write just the letter of your answer here>

Questions 16 – 20: **Use the following scenario to answer the questions**.

A rocket motor is manufactured by bonding together two types of propellants, an igniter and a sustainer. A random sample of 20 specimens is used to investigate the relationship between the shear strength of the bond (in psi) and the age of the propellant (in weeks). **Use the R software output to answer the following questions.**




```
Coefficients:
            Estimate Std. Error t-value  Pr(>|t|)
(Intercept) 2641.185     68.901   38.33   < 2e-16
age          -49.550      4.436  -11.17  1.59e-09
---

Residual standard error: 138.3 on 18 degrees of freedom
Multiple R-squared: 0.8739, Adjusted R-squared:  0.8669
F-statistic: 124.8 on 1 and 18 DF,  p-value: 1.586e-09
```

16. (8 points) Based on the scatterplot, describe the relationship between the two variables **using context**

    Strength: <Write your answer here using complete sentences>

    Direction: <Write your answer here using complete sentences>

    Form: <Write your answer here using complete sentences>

    Outliers: <Write your answer here using complete sentences>

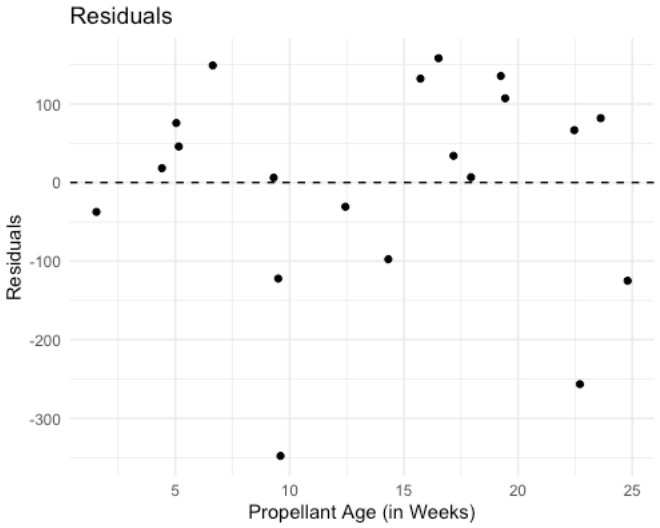
17. (4 points) Write down the least squares regression equation.

$$\hat{y} =$$

18. (4 points) Calculate the residual for the observation that is 12.4 weeks old with bond strength of 1993.8 psi. Write your answer in the blank and **show your work.**

<Write your answer here>

19. (4 points) Based on the residual plot in part below, state all of the conditions for the least squared regression model to be valid, whether or not they are satisfied, and why.



<Write your answer here>

20. (4 points) Interpret the estimated slope of the linear model:

<Write your answer here>

21.

STANDARD NORMAL DISTRIBUTION: Table Values Represent AREA to the LEFT of the Z score.

Z	.00	.01	.02	.03	.04	.05	.06	.07	.08	.09
-3.9	.00005	.00005	.00004	.00004	.00004	.00004	.00004	.00004	.00003	.00003
-3.8	.00007	.00007	.00007	.00006	.00006	.00006	.00006	.00005	.00005	.00005
-3.7	.00011	.00010	.00010	.00010	.00009	.00009	.00008	.00008	.00008	.00008
-3.6	.00016	.00015	.00015	.00014	.00014	.00013	.00013	.00012	.00012	.00011
-3.5	.00023	.00022	.00022	.00021	.00020	.00019	.00019	.00018	.00017	.00017
-3.4	.00034	.00032	.00031	.00030	.00029	.00028	.00027	.00026	.00025	.00024
-3.3	.00048	.00047	.00045	.00043	.00042	.00040	.00039	.00038	.00036	.00035
-3.2	.00069	.00066	.00064	.00062	.00060	.00058	.00056	.00054	.00052	.00050
-3.1	.00097	.00094	.00090	.00087	.00084	.00082	.00079	.00076	.00074	.00071
-3.0	.00135	.00131	.00126	.00122	.00118	.00114	.00111	.00107	.00104	.00100
-2.9	.00187	.00181	.00175	.00169	.00164	.00159	.00154	.00149	.00144	.00139
-2.8	.00256	.00248	.00240	.00233	.00226	.00219	.00212	.00205	.00199	.00193
-2.7	.00347	.00336	.00326	.00317	.00307	.00298	.00289	.00280	.00272	.00264
-2.6	.00466	.00453	.00440	.00427	.00415	.00402	.00391	.00379	.00368	.00357
-2.5	.00621	.00604	.00587	.00570	.00554	.00539	.00523	.00508	.00494	.00480
-2.4	.00820	.00798	.00776	.00755	.00734	.00714	.00695	.00676	.00657	.00639
-2.3	.01072	.01044	.01017	.00990	.00964	.00939	.00914	.00889	.00866	.00842
-2.2	.01390	.01355	.01321	.01287	.01255	.01222	.01191	.01160	.01130	.01101
-2.1	.01786	.01743	.01700	.01659	.01618	.01578	.01539	.01500	.01463	.01426
-2.0	.02275	.02222	.02169	.02118	.02068	.02018	.01970	.01923	.01876	.01831
-1.9	.02872	.02807	.02743	.02680	.02619	.02559	.02500	.02442	.02385	.02330
-1.8	.03593	.03515	.03438	.03362	.03288	.03216	.03144	.03074	.03005	.02938
-1.7	.04457	.04363	.04272	.04182	.04093	.04006	.03920	.03836	.03754	.03673
-1.6	.05480	.05370	.05262	.05155	.05050	.04947	.04846	.04746	.04648	.04551
-1.5	.06681	.06552	.06426	.06301	.06178	.06057	.05938	.05821	.05705	.05592
-1.4	.08076	.07927	.07780	.07636	.07493	.07353	.07215	.07078	.06944	.06811
-1.3	.09680	.09510	.09342	.09176	.09012	.08851	.08691	.08534	.08379	.08226
-1.2	.11507	.11314	.11123	.10935	.10749	.10565	.10383	.10204	.10027	.09853
-1.1	.13567	.13350	.13136	.12924	.12714	.12507	.12302	.12100	.11900	.11702
-1.0	.15866	.15625	.15386	.15151	.14917	.14686	.14457	.14231	.14007	.13786
-0.9	.18406	.18141	.17879	.17619	.17361	.17106	.16853	.16602	.16354	.16109
-0.8	.21186	.20897	.20611	.20327	.20045	.19766	.19489	.19215	.18943	.18673
-0.7	.24196	.23885	.23576	.23270	.22965	.22663	.22363	.22065	.21770	.21476
-0.6	.27425	.27093	.26763	.26435	.26109	.25785	.25463	.25143	.24825	.24510
-0.5	.30854	.30503	.30153	.29806	.29460	.29116	.28774	.28434	.28096	.27760
-0.4	.34458	.34090	.33724	.33360	.32997	.32636	.32276	.31918	.31561	.31207
-0.3	.38209	.37828	.37448	.37070	.36693	.36317	.35942	.35569	.35197	.34827
-0.2	.42074	.41683	.41294	.40905	.40517	.40129	.39743	.39358	.38974	.38591
-0.1	.46017	.45620	.45224	.44828	.44433	.44038	.43644	.43251	.42858	.42465
-0.0	.50000	.49601	.49202	.48803	.48405	.48006	.47608	.47210	.46812	.46414

STANDARD NORMAL DISTRIBUTION: Table Values Represent AREA to the LEFT of the Z score.

Z	.00	.01	.02	.03	.04	.05	.06	.07	.08	.09
0.0	.50000	.50399	.50798	.51197	.51595	.51994	.52392	.52790	.53188	.53586
0.1	.53983	.54380	.54776	.55172	.55567	.55962	.56356	.56749	.57142	.57535
0.2	.57926	.58317	.58706	.59095	.59483	.59871	.60257	.60642	.61026	.61409
0.3	.61791	.62172	.62552	.62930	.63307	.63683	.64058	.64431	.64803	.65173
0.4	.65542	.65910	.66276	.66640	.67003	.67364	.67724	.68082	.68439	.68793
0.5	.69146	.69497	.69847	.70194	.70540	.70884	.71226	.71566	.71904	.72240
0.6	.72575	.72907	.73237	.73565	.73891	.74215	.74537	.74857	.75175	.75490
0.7	.75804	.76115	.76424	.76730	.77035	.77337	.77637	.77935	.78230	.78524
0.8	.78814	.79103	.79389	.79673	.79955	.80234	.80511	.80785	.81057	.81327
0.9	.81594	.81859	.82121	.82381	.82639	.82894	.83147	.83398	.83646	.83891
1.0	.84134	.84375	.84614	.84849	.85083	.85314	.85543	.85769	.85993	.86214
1.1	.86433	.86650	.86864	.87076	.87286	.87493	.87698	.87900	.88100	.88298
1.2	.88493	.88686	.88877	.89065	.89251	.89435	.89617	.89796	.89973	.90147
1.3	.90320	.90490	.90658	.90824	.90988	.91149	.91309	.91466	.91621	.91774
1.4	.91924	.92073	.92220	.92364	.92507	.92647	.92785	.92922	.93056	.93189
1.5	.93319	.93448	.93574	.93699	.93822	.93943	.94062	.94179	.94295	.94408
1.6	.94520	.94630	.94738	.94845	.94950	.95053	.95154	.95254	.95352	.95449
1.7	.95543	.95637	.95728	.95818	.95907	.95994	.96080	.96164	.96246	.96327
1.8	.96407	.96485	.96562	.96638	.96712	.96784	.96856	.96926	.96995	.97062
1.9	.97128	.97193	.97257	.97320	.97381	.97441	.97500	.97558	.97615	.97670
2.0	.97725	.97778	.97831	.97882	.97932	.97982	.98030	.98077	.98124	.98169
2.1	.98214	.98257	.98300	.98341	.98382	.98422	.98461	.98500	.98537	.98574
2.2	.98610	.98645	.98679	.98713	.98745	.98778	.98809	.98840	.98870	.98899
2.3	.98928	.98956	.98983	.99010	.99036	.99061	.99086	.99111	.99134	.99158
2.4	.99180	.99202	.99224	.99245	.99266	.99286	.99305	.99324	.99343	.99361
2.5	.99379	.99396	.99413	.99430	.99446	.99461	.99477	.99492	.99506	.99520
2.6	.99534	.99547	.99560	.99573	.99585	.99598	.99609	.99621	.99632	.99643
2.7	.99653	.99664	.99674	.99683	.99693	.99702	.99711	.99720	.99728	.99736
2.8	.99744	.99752	.99760	.99767	.99774	.99781	.99788	.99795	.99801	.99807
2.9	.99813	.99819	.99825	.99831	.99836	.99841	.99846	.99851	.99856	.99861
3.0	.99865	.99869	.99874	.99878	.99882	.99886	.99889	.99893	.99896	.99900
3.1	.99903	.99906	.99910	.99913	.99916	.99918	.99921	.99924	.99926	.99929
3.2	.99931	.99934	.99936	.99938	.99940	.99942	.99944	.99946	.99948	.99950
3.3	.99952	.99953	.99955	.99957	.99958	.99960	.99961	.99962	.99964	.99965
3.4	.99966	.99968	.99969	.99970	.99971	.99972	.99973	.99974	.99975	.99976
3.5	.99977	.99978	.99978	.99979	.99980	.99981	.99981	.99982	.99983	.99983
3.6	.99984	.99985	.99985	.99986	.99986	.99987	.99987	.99988	.99988	.99989
3.7	.99989	.99990	.99990	.99990	.99991	.99991	.99992	.99992	.99992	.99992
3.8	.99993	.99993	.99993	.99994	.99994	.99994	.99994	.99995	.99995	.99995
3.9	.99995	.99995	.99996	.99996	.99996	.99996	.99996	.99996	.99997	.99997

t Table

cum. prob	$t_{.50}$	$t_{.75}$	$t_{.80}$	$t_{.85}$	$t_{.90}$	$t_{.95}$	$t_{.975}$	$t_{.99}$	$t_{.995}$	$t_{.999}$	$t_{.9995}$
one-tail	**0.50**	**0.25**	**0.20**	**0.15**	**0.10**	**0.05**	**0.025**	**0.01**	**0.005**	**0.001**	**0.0005**
two-tails	**1.00**	**0.50**	**0.40**	**0.30**	**0.20**	**0.10**	**0.05**	**0.02**	**0.01**	**0.002**	**0.001**
df											
1	0.000	1.000	1.376	1.963	3.078	6.314	12.71	31.82	63.66	318.31	636.62
2	0.000	0.816	1.061	1.386	1.886	2.920	4.303	6.965	9.925	22.327	31.599
3	0.000	0.765	0.978	1.250	1.638	2.353	3.182	4.541	5.841	10.215	12.924
4	0.000	0.741	0.941	1.190	1.533	2.132	2.776	3.747	4.604	7.173	8.610
5	0.000	0.727	0.920	1.156	1.476	2.015	2.571	3.365	4.032	5.893	6.869
6	0.000	0.718	0.906	1.134	1.440	1.943	2.447	3.143	3.707	5.208	5.959
7	0.000	0.711	0.896	1.119	1.415	1.895	2.365	2.998	3.499	4.785	5.408
8	0.000	0.706	0.889	1.108	1.397	1.860	2.306	2.896	3.355	4.501	5.041
9	0.000	0.703	0.883	1.100	1.383	1.833	2.262	2.821	3.250	4.297	4.781
10	0.000	0.700	0.879	1.093	1.372	1.812	2.228	2.764	3.169	4.144	4.587
11	0.000	0.697	0.876	1.088	1.363	1.796	2.201	2.718	3.106	4.025	4.437
12	0.000	0.695	0.873	1.083	1.356	1.782	2.179	2.681	3.055	3.930	4.318
13	0.000	0.694	0.870	1.079	1.350	1.771	2.160	2.650	3.012	3.852	4.221
14	0.000	0.692	0.868	1.076	1.345	1.761	2.145	2.624	2.977	3.787	4.140
15	0.000	0.691	0.866	1.074	1.341	1.753	2.131	2.602	2.947	3.733	4.073
16	0.000	0.690	0.865	1.071	1.337	1.746	2.120	2.583	2.921	3.686	4.015
17	0.000	0.689	0.863	1.069	1.333	1.740	2.110	2.567	2.898	3.646	3.965
18	0.000	0.688	0.862	1.067	1.330	1.734	2.101	2.552	2.878	3.610	3.922
19	0.000	0.688	0.861	1.066	1.328	1.729	2.093	2.539	2.861	3.579	3.883
20	0.000	0.687	0.860	1.064	1.325	1.725	2.086	2.528	2.845	3.552	3.850
21	0.000	0.686	0.859	1.063	1.323	1.721	2.080	2.518	2.831	3.527	3.819
22	0.000	0.686	0.858	1.061	1.321	1.717	2.074	2.508	2.819	3.505	3.792
23	0.000	0.685	0.858	1.060	1.319	1.714	2.069	2.500	2.807	3.485	3.768
24	0.000	0.685	0.857	1.059	1.318	1.711	2.064	2.492	2.797	3.467	3.745
25	0.000	0.684	0.856	1.058	1.316	1.708	2.060	2.485	2.787	3.450	3.725
26	0.000	0.684	0.856	1.058	1.315	1.706	2.056	2.479	2.779	3.435	3.707
27	0.000	0.684	0.855	1.057	1.314	1.703	2.052	2.473	2.771	3.421	3.690
28	0.000	0.683	0.855	1.056	1.313	1.701	2.048	2.467	2.763	3.408	3.674
29	0.000	0.683	0.854	1.055	1.311	1.699	2.045	2.462	2.756	3.396	3.659
30	0.000	0.683	0.854	1.055	1.310	1.697	2.042	2.457	2.750	3.385	3.646
40	0.000	0.681	0.851	1.050	1.303	1.684	2.021	2.423	2.704	3.307	3.551
60	0.000	0.679	0.848	1.045	1.296	1.671	2.000	2.390	2.660	3.232	3.460
80	0.000	0.678	0.846	1.043	1.292	1.664	1.990	2.374	2.639	3.195	3.416
100	0.000	0.677	0.845	1.042	1.290	1.660	1.984	2.364	2.626	3.174	3.390
1000	0.000	0.675	0.842	1.037	1.282	1.646	1.962	2.330	2.581	3.098	3.300
z	0.000	0.674	0.842	1.036	1.282	1.645	1.960	2.326	2.576	3.090	3.291
	0%	50%	60%	70%	80%	90%	95%	98%	99%	99.8%	99.9%
	Confidence Level										