

Computational Imaging

Lecture 22 Temporal Encoding V - Time Encoded Photography



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点昀技术（Point Spread Technology）



Today's Topic

- Dealing with Motion Blur: Coded Exposure
- Optimized Codes for PSF Estimation and Invertibility
- Dealing with Motion Blur: Parabolic Sweep

Dealing with Motion Blur: Coded Exposure



Motion Blur





Motion Blur



blurry image of
moving object

$$= \text{motion blur kernel} *$$



sharp image of
static object

What does the motion blur kernel depend on?

- Motion velocity determines direction of kernel.
- Shutter speed determines width of kernel.

Can we use deconvolution to remove motion blur?



Challenges of Motion Deblurring

- Blur kernel is not invertible.



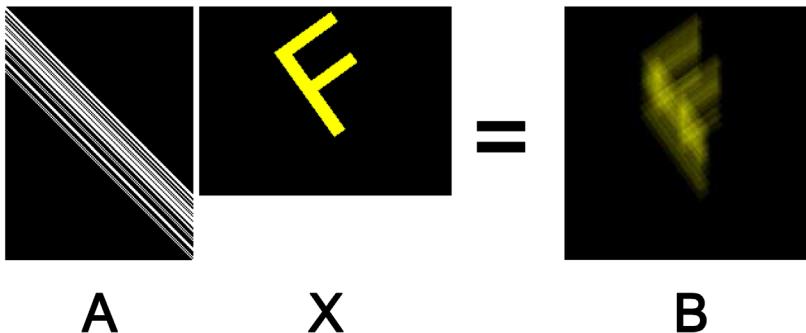
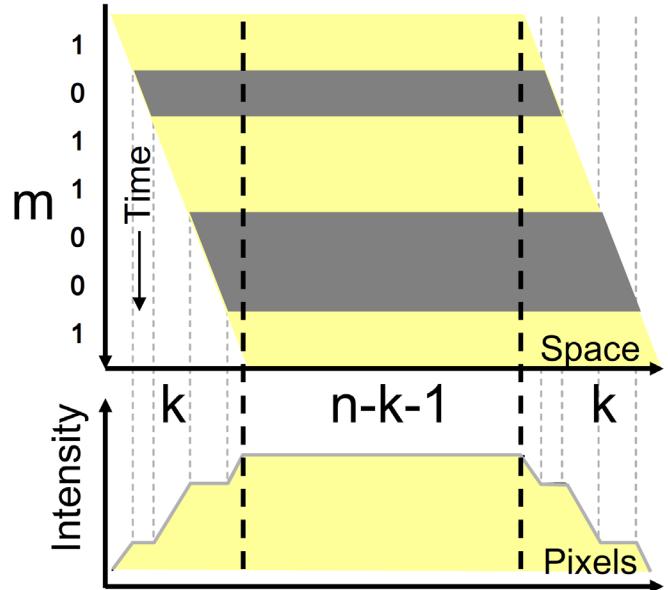
How would you deal with this?

- Blur kernel is unknown.
- Blur kernel is different for different objects.





The 1-D Motion Blur Process



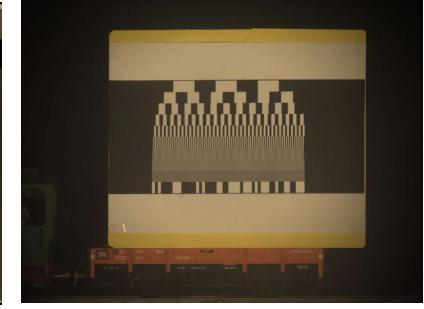
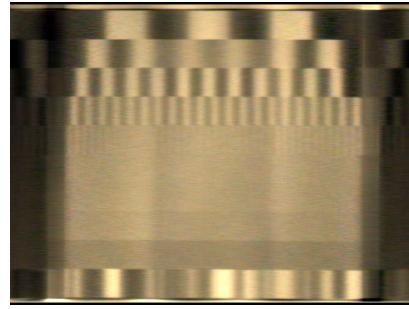
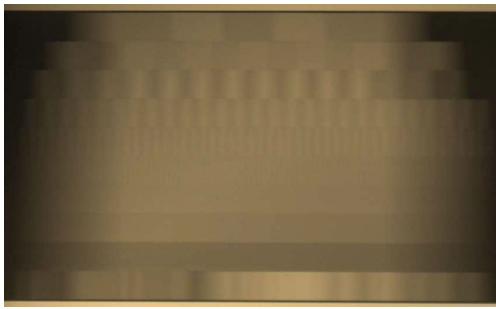
A time-to-space projection for a moving object of size n , with blur of k pixels



Sample The Motion with More Spatial Frequencies

Code exposure (i.e., shutter speed) to make motion blur kernel better conditioned.

Traditional Exposure



Coded Exposure

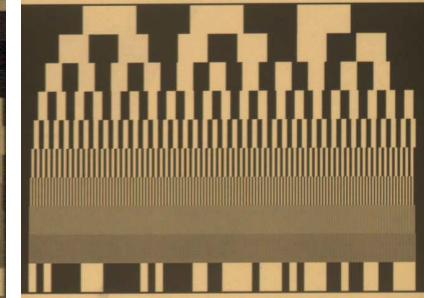
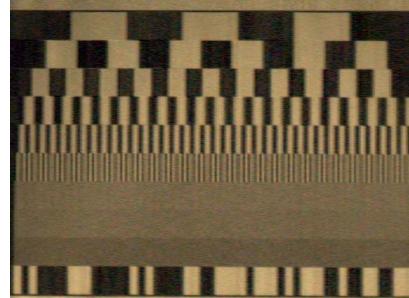
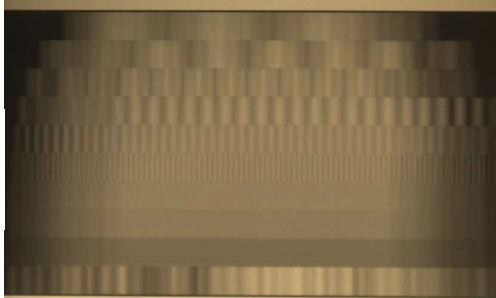
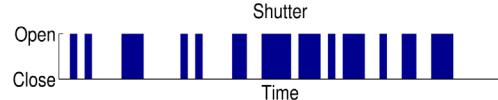


Photo of Test Setup

Blurred Photo

Deblurred Image

Photo of Test Target



Coded Exposure a.k.a. Flutter Shutter

Code exposure (i.e., shutter speed) to make motion blur kernel better conditioned.

traditional
camera



blurry image of
moving object

=



*



sharp image of
static object

flutter-shutter
camera



blurry image of
moving object

=

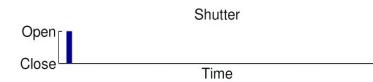


*

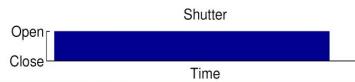


sharp image of
static object

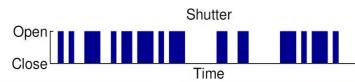
Goal: Select a More Invertible Temporal Code



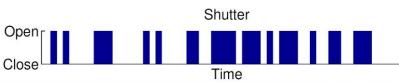
(a) Short Exposure Photo



(b) Traditional, 200ms



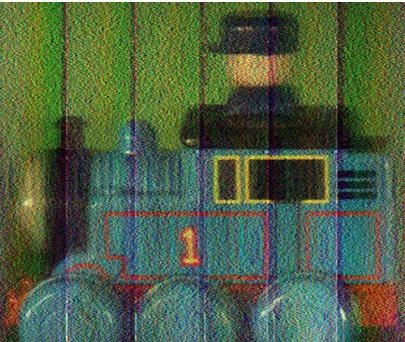
(c) MURA Code, 200ms



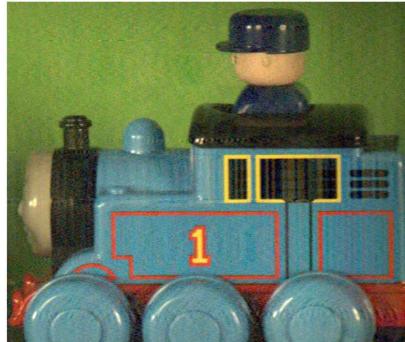
(d) Our Code, 200ms



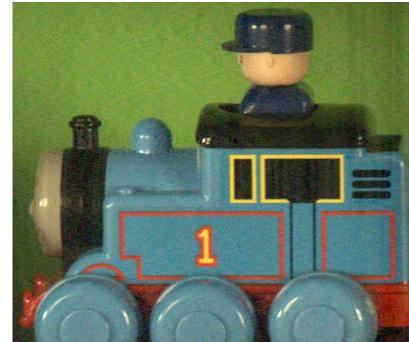
(e) Log intensity of (a)



(f) Deblurred Image



(g) Deblurred Image



(h) Deblurred Image



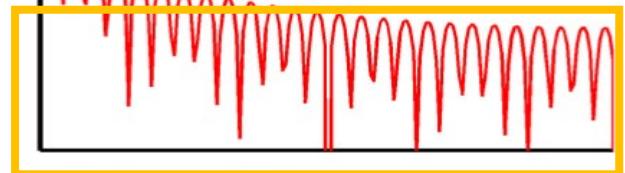
Coded Exposure a.k.a. Flutter Shutter

motion blur kernel
in time domain

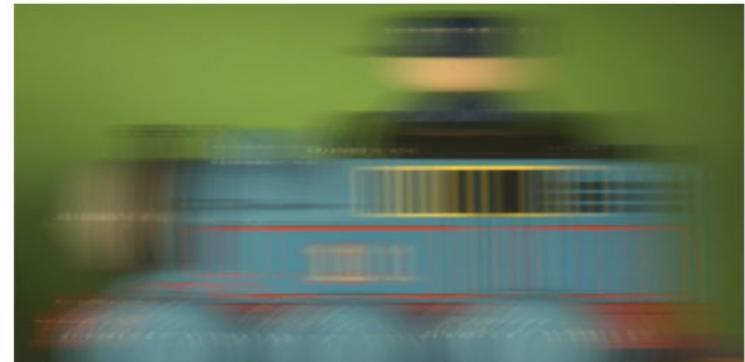
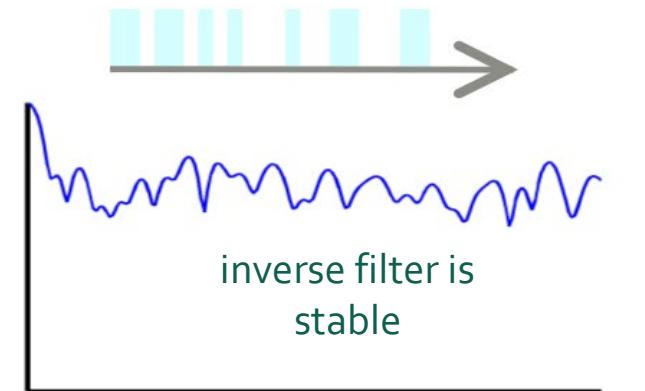


zeros make inverse filter
unstable

motion blur kernel
in Fourier domain

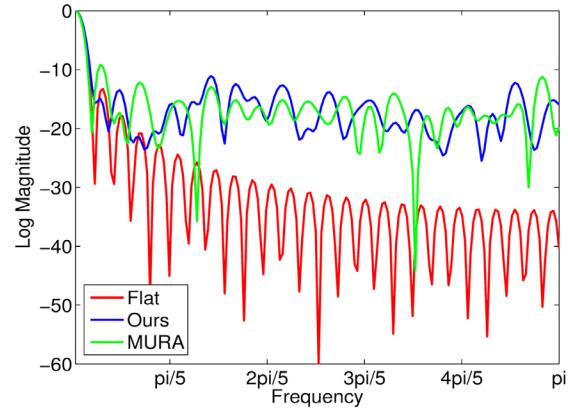


Why is flutter
shutter
better?

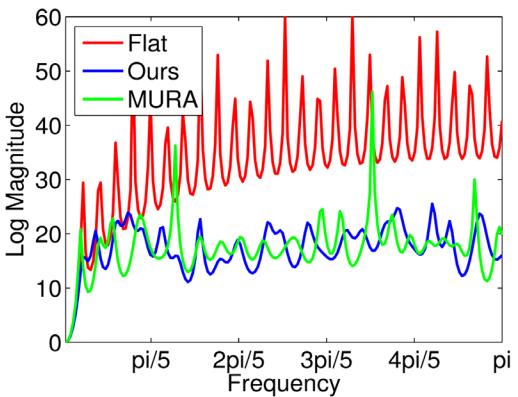




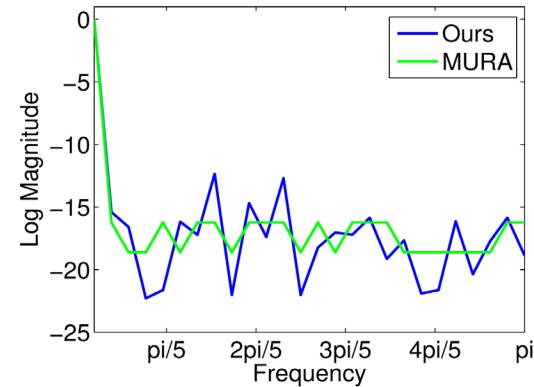
Frequency, Covariance and Matrix Conditionality Analysis



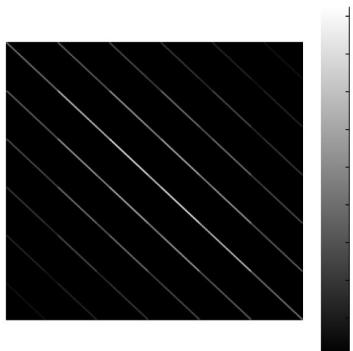
Linear Convolution Filter DFT



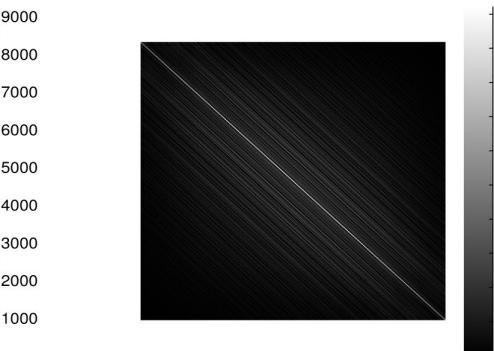
Decoding Filter DFT



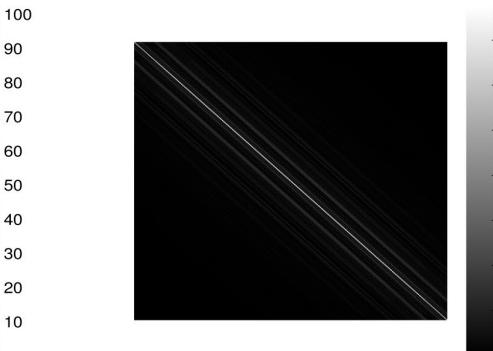
Circular Convolution Filter DFT



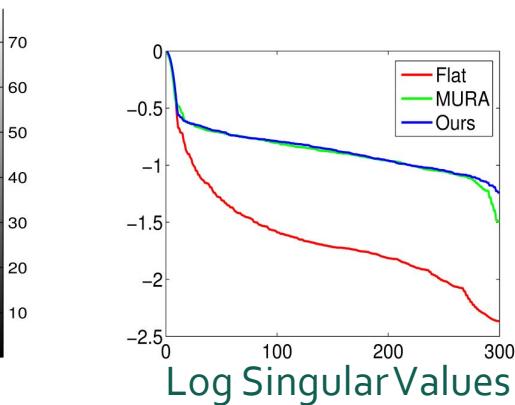
Covariance:Box



Covariance:MURA



Covariance:Optimal



Log Singular Values



The Near Optimal Temporal Code

- Implementing a **randomized linear search** and considered approximately 3×10^6 candidate codes.

```
1010000111000001010000110011110111010111001001100111
```



Motion Decoding

- Motion Model

$$AX = B + \eta$$

- Use a least-square estimation to solve for the deblurred image \hat{X}

$$\hat{X} = A^+ B$$



Background Estimation

An opaque object moving in front of a stationary (non-blurred) but non-zero-valued background.

Not sufficient to know the moving object's PSF to deblur the image.

- In the case of a non-zero background, the blurred image is given by

$$B = AX + A_g X_g$$

where X is the moving foreground object, X_g is the static background.
 A_g is a diagonal matrix whose elements attenuate the static background.

$$A_g = I - \text{diag}(A * I_{(n+k-1) \times 1})$$



Different Types of Backgrounds



Continuity with the unblurred part of the face



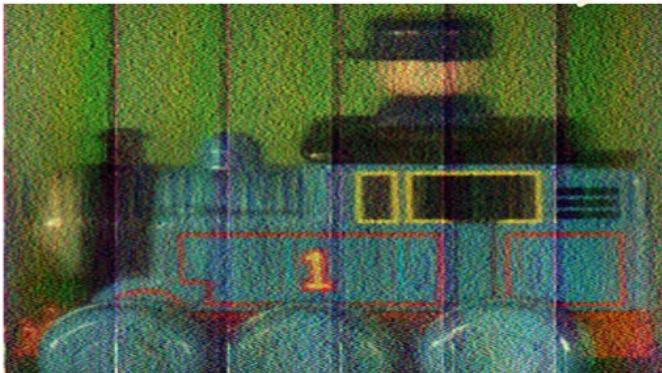
With a striped background aligned with motion lines

Paper smears across the face

Motion Deblurring Comparison

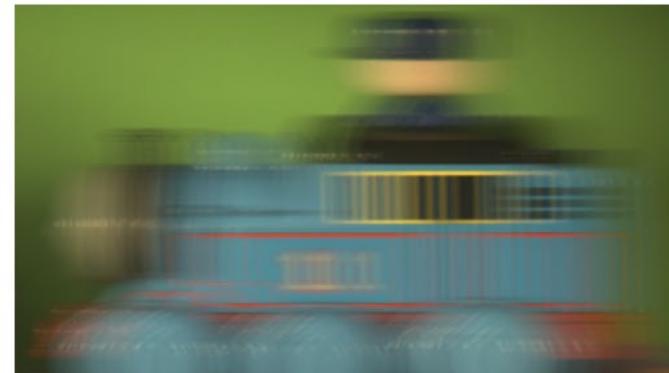
deconvolved
output

conventional photography

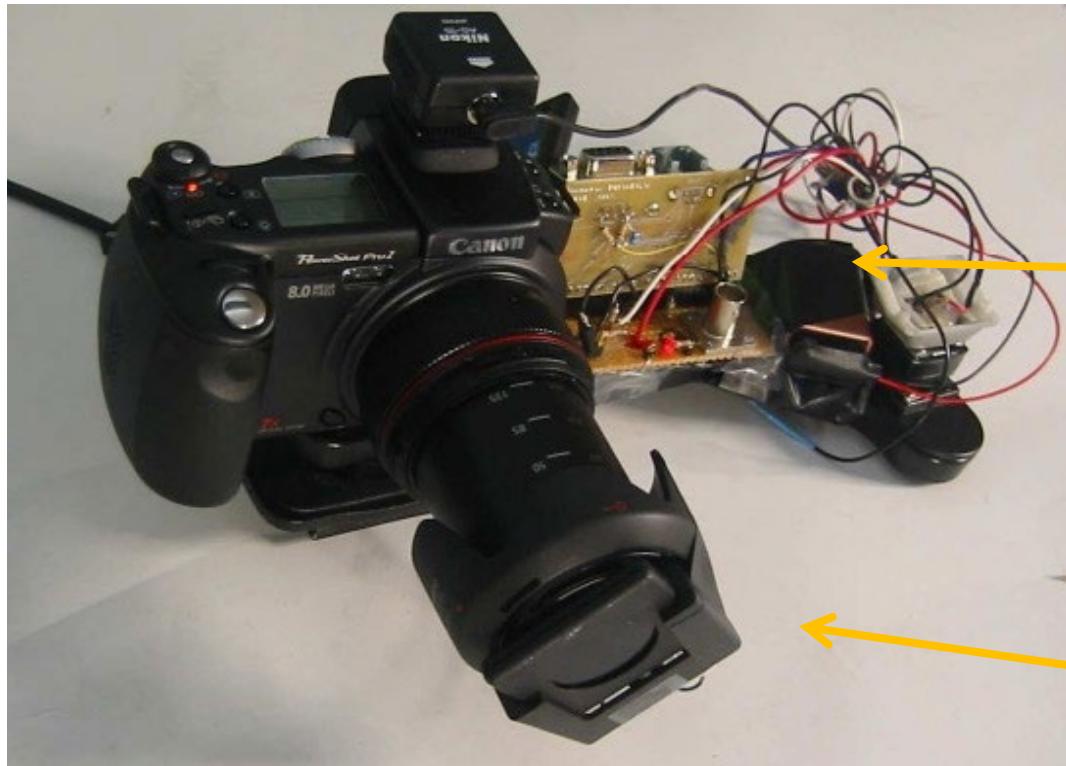


blurry
input

flutter-shutter photography



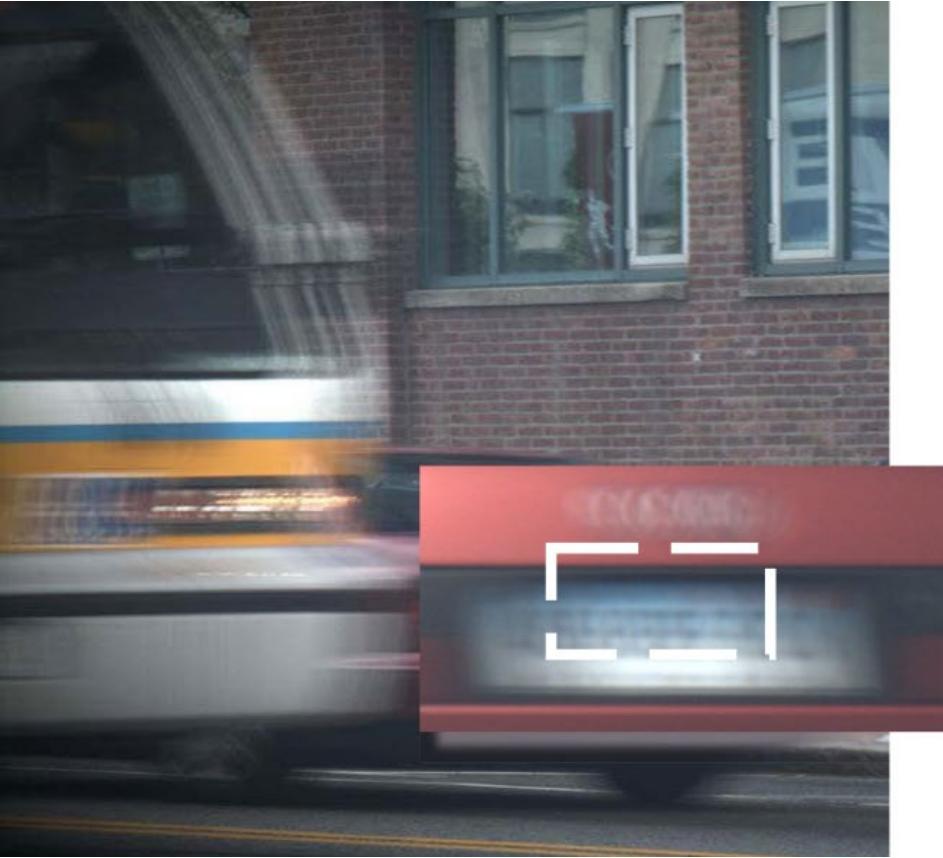
How Would You Implement Coded Exposure?



electronics for external
shutter control

very fast external
shutter

Results



[Raskar et al. 2006]



License Plate Retrieval



Results



[Raskar et al. 2006]



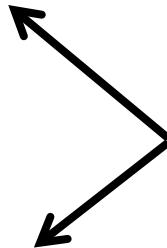
License Plate Retrieval



Challenges of Motion Deblurring

- Blur kernel is not invertible.

- Blur kernel is unknown.



How would you deal
with these two?

- Blur kernel is different for different objects.



Coded Exposure Deblurring: Optimized Codes for PSF Estimation and Invertibility



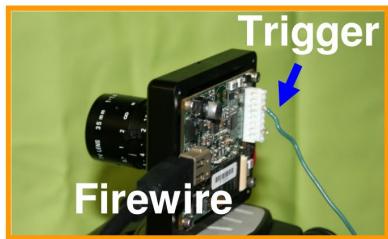
Optimized Codes



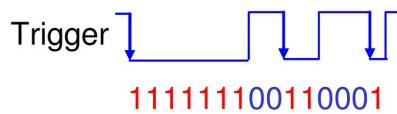
Captured frame



Cropped input frame



Coded exposure camera



Deblurring result

Using a carefully designed code, one can achieve both PSF estimation and invertibility for motion deblurring via coded exposure camera.



Blur Estimation Using Alpha Matting

The captured blurred image I is given by the sum of blurred foreground object and partial background

$$I = s * h + (1 - M * h)b$$

$$s(x, y)$$

image of the object

$$h(x, y)$$

the motion PSF

$$M(x, y)$$

binary indicator function

$$b(x, y)$$

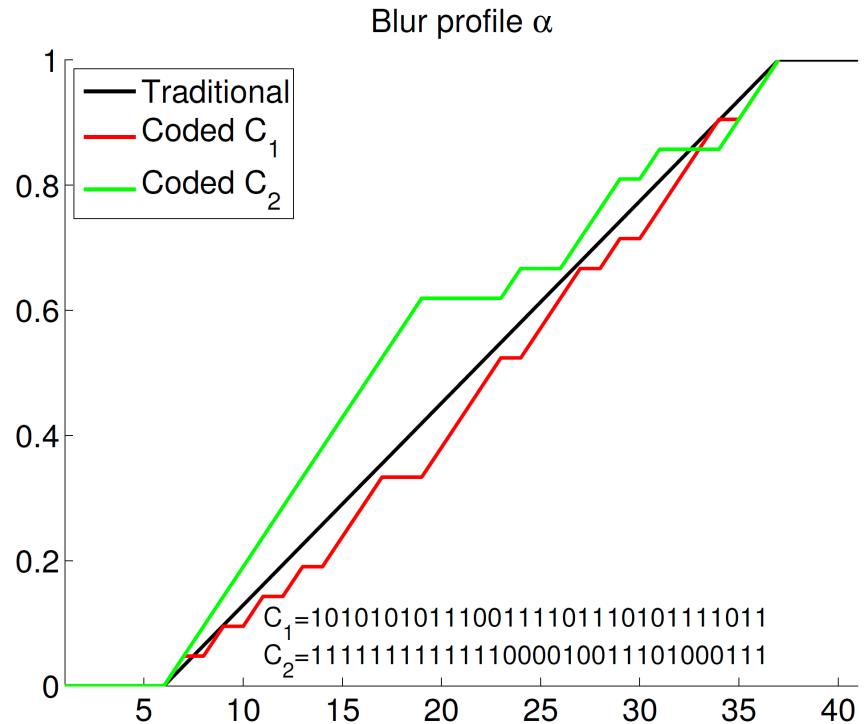
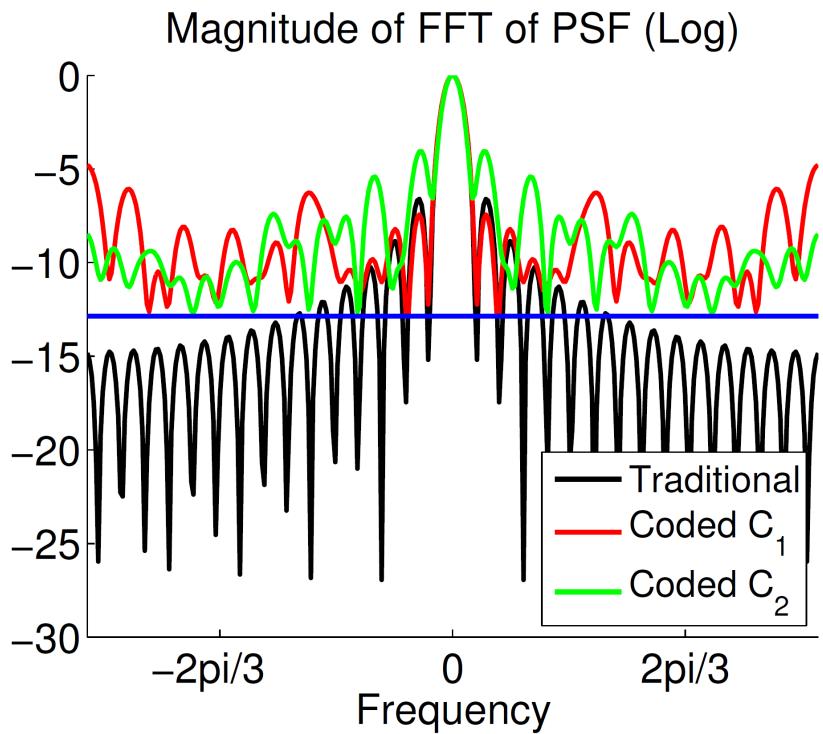
background

The matting equation:

$$I = F + (1 - \alpha)B$$

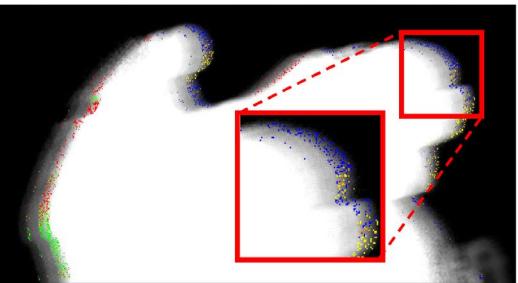
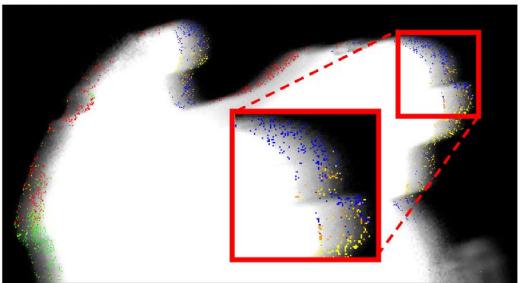
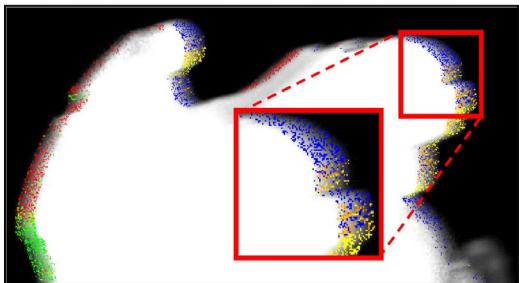
$$B = b, \quad \alpha = M * h, \quad F = (s * h) / (M * h)$$

Two Different Codes



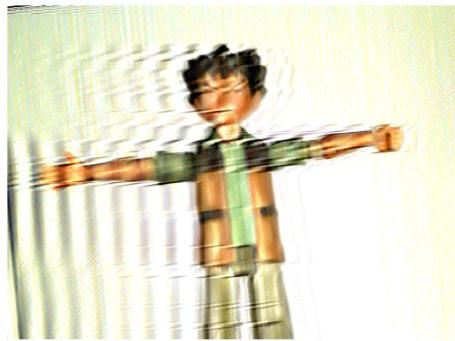


Implementation





Implementation



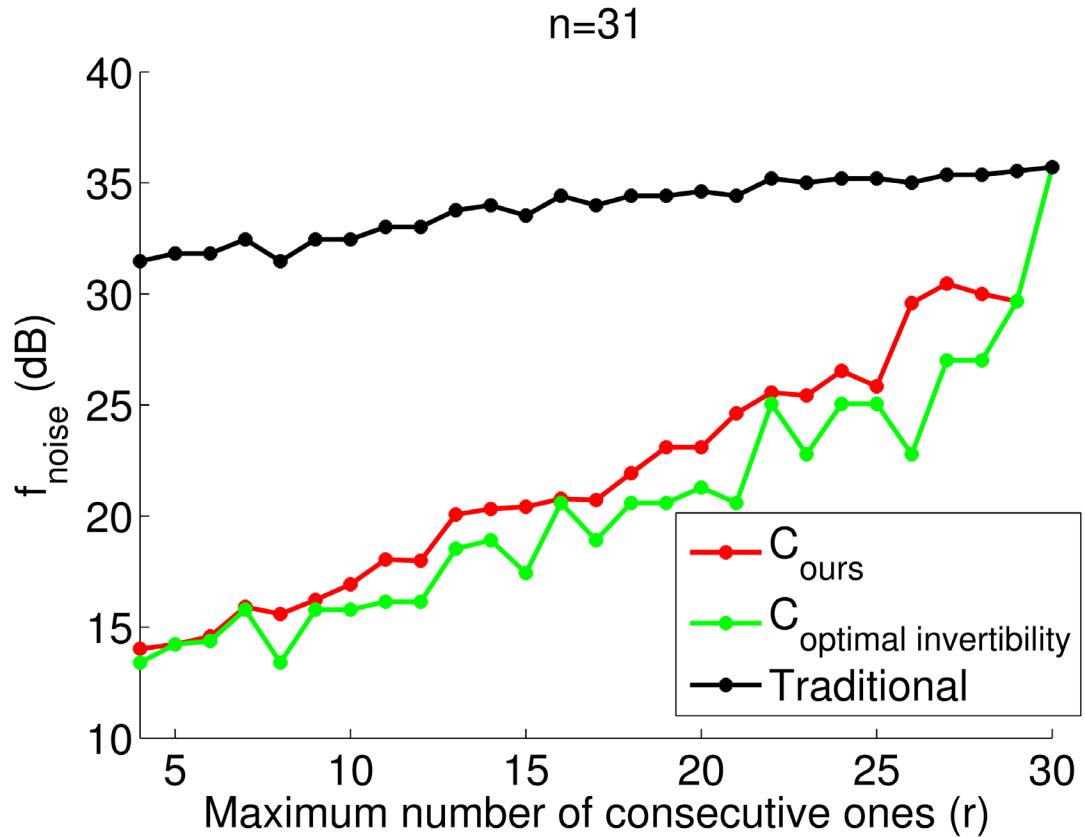
Traditional

Coded C₁

Coded C₂

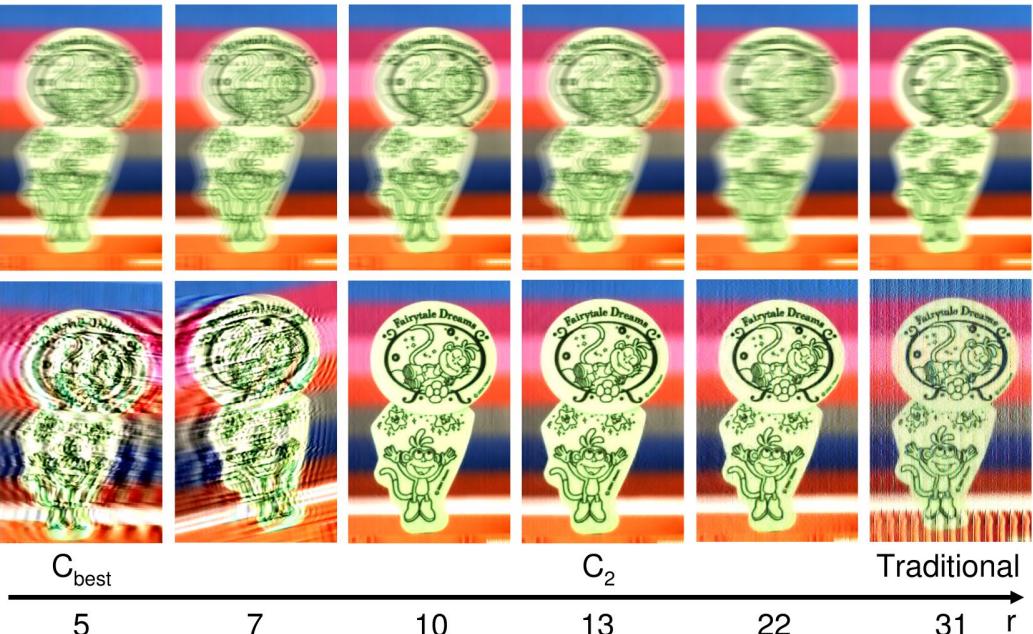
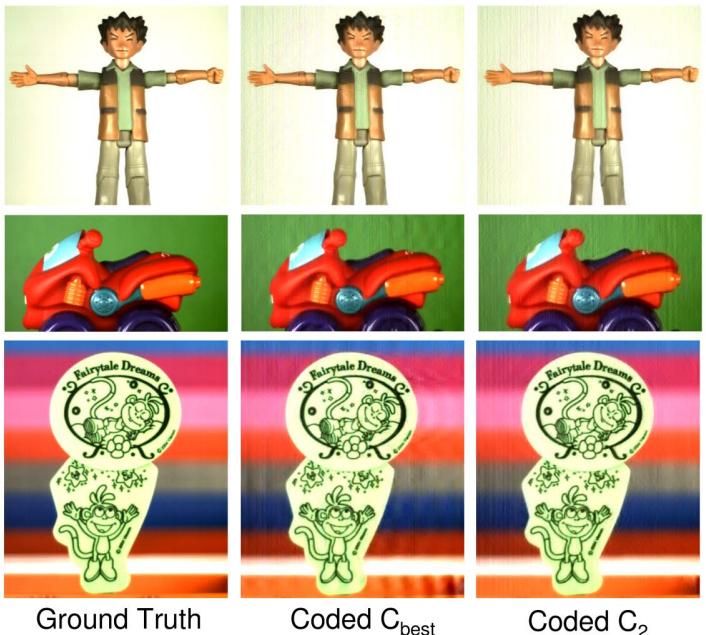


Fast Binary Code Search





Best Codes



Dealing With Motion Blur: Parabolic Sweep

Motion-invariant Photography

Introduce extra motion so that:

- Everything is blurry; and
- The blur kernel is *motion invariant* (same for all objects).

How would you achieve this?

Motion-invariant Photography



Blurred motion captured
by a static camera.



Blurred motion captured
with a specially designed
motion that causes both the
static and dynamic regions to
blur **identically**.

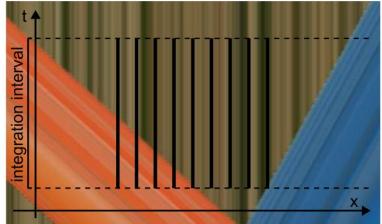


Deconvoluted Image of the
entire image with a single
known PSF.



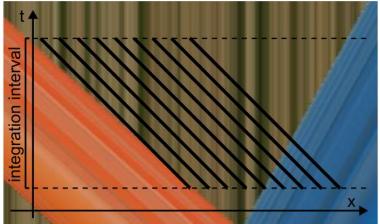
From Integration Curves to PSF

Static Camera



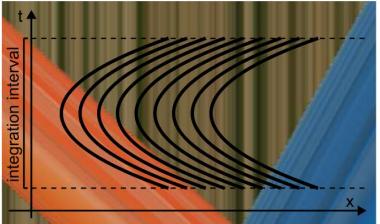
(a)

Linear Translation



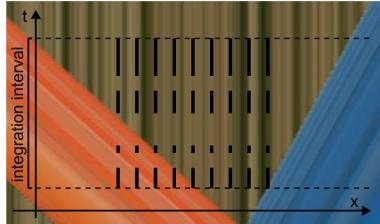
(b)

Parabolic Translation

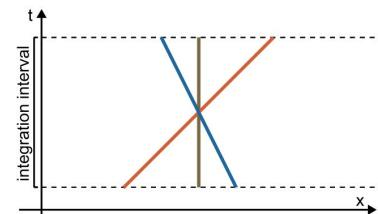


(c)

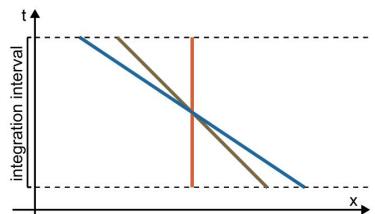
Flutter Shutter



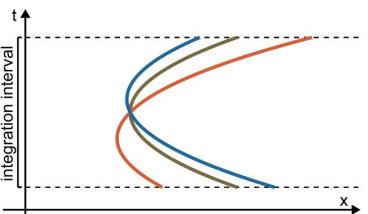
(d)



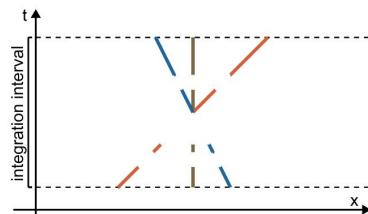
(e)



(f)

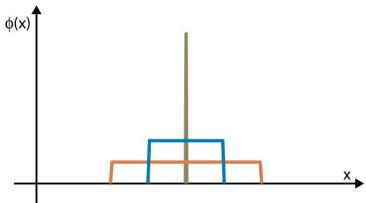


(g)

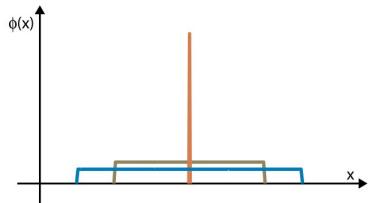


(h)

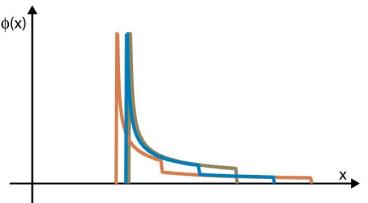
PSF



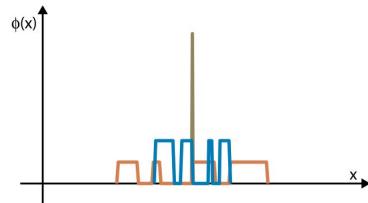
(i)



(j)



(k)

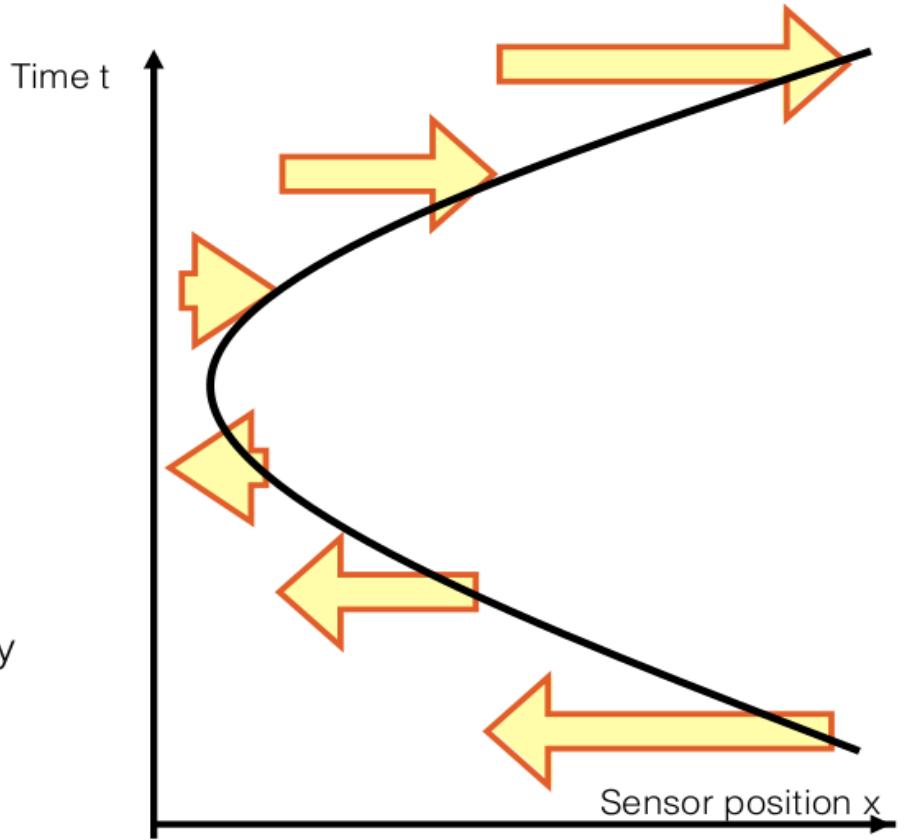


(l)

Parabolic Sweep

Sensor position $x(t)=a t^2$

- start by moving very fast to the right
- continuously slow down until stop
- continuously accelerate to the left
- Intuition:
 - for any velocity, there is one instant where we track perfectly
 - all velocities captured same amount of time

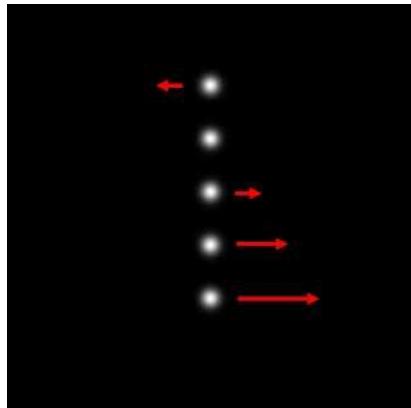




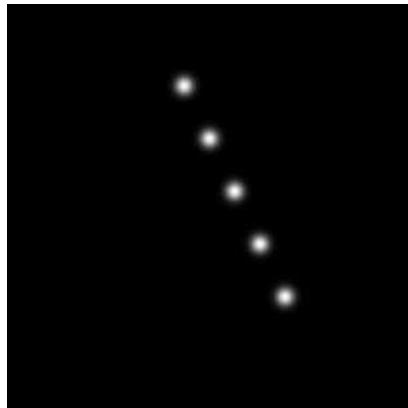
Goal: Create a Velocity Invariant PSF

- We note that a sheared parabola is also a parabola with the same scale, only the center is shifting

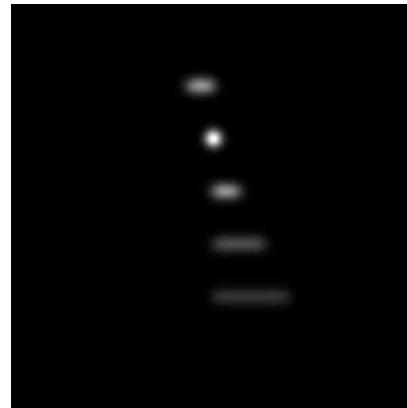
$$f_s(t) = f(t) - st = a_0 \left(t - \frac{s}{2a_0} \right)^2 - \frac{s^2}{4a_0}$$



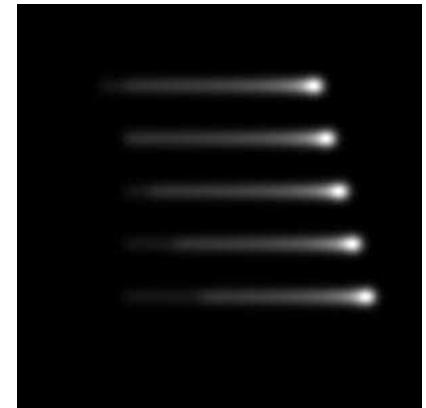
Time 1



Time 2



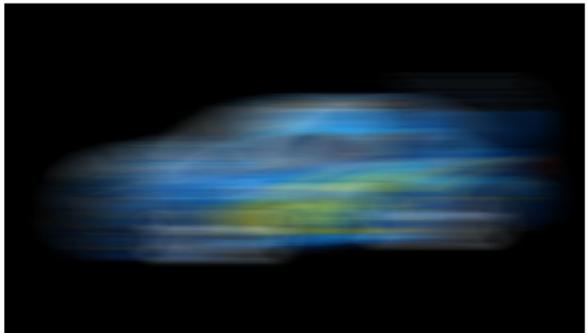
Static camera



Parabolic camera



Synthetic visualization of PSF information loss



Static

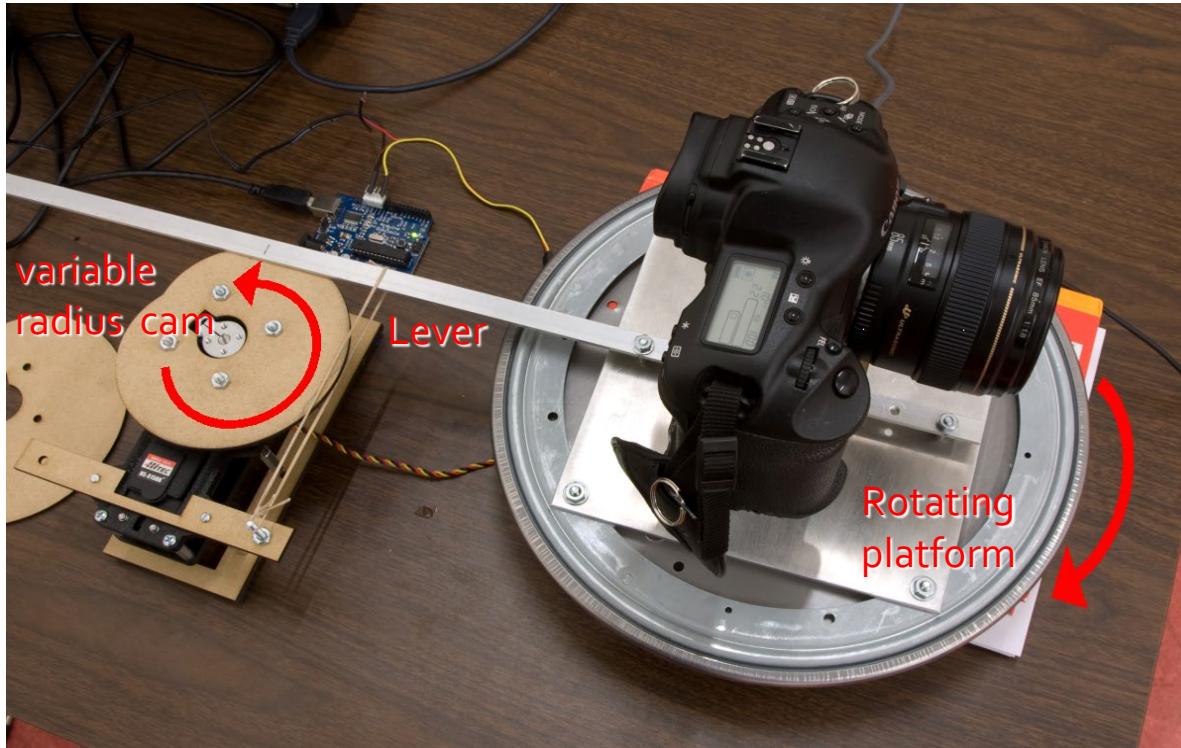
Parabola

Flutter Shutter



Prototype Camera Setup

Approximate small translation by small rotation





Results



static camera input – unknown and
variable blur



parabolic input –
blur is invariant to velocity



Results



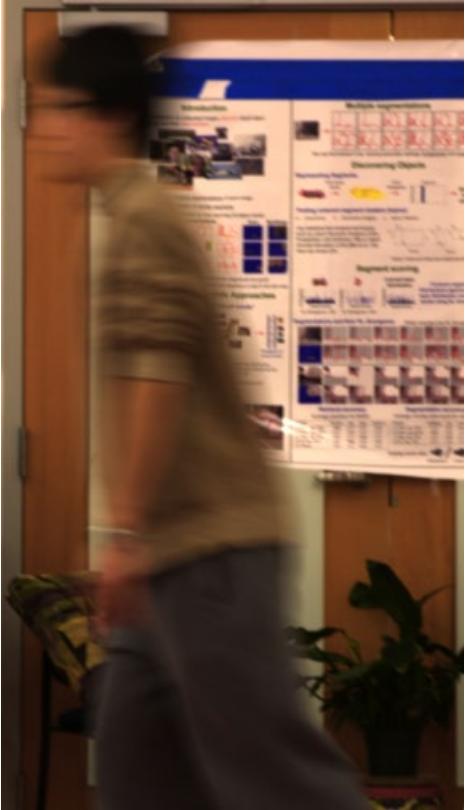
static camera input – unknown and
variable blur



parabolic input –
blur is invariant to velocity



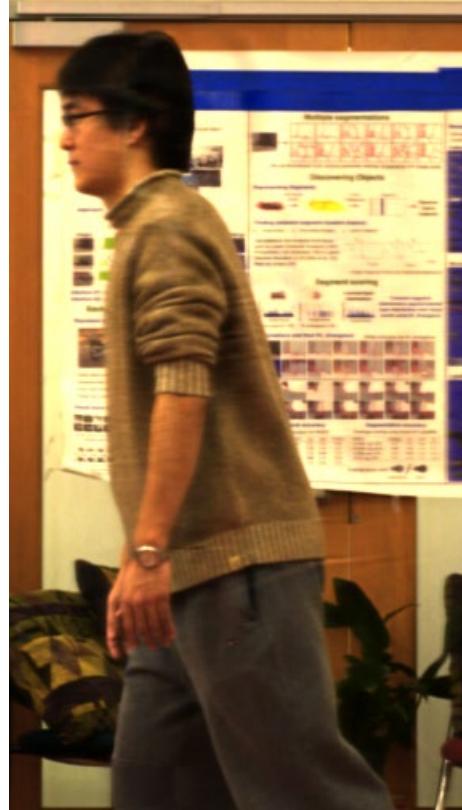
Results



static camera input



parabolic camera input

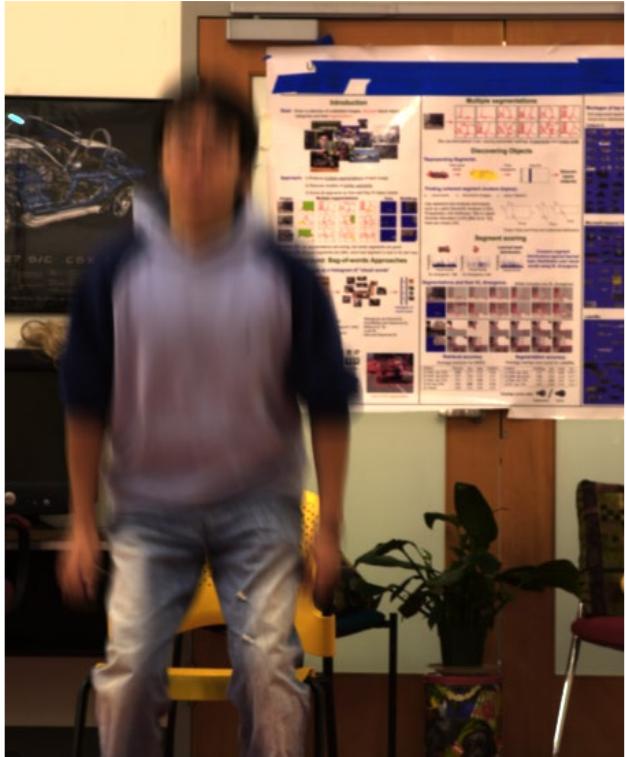


deconvolution output

Results



香港中文大學(深圳)
The Chinese University of Hong Kong, Shenzhen



static camera input



output after deconvolution
Why does it fail in this case?



Experiments



Static camera input



Deblurring results by [Levin 2006]



Box filter fitted manually to moving layer
and applied to deblur the entire image



Spatially uniform deconvolution of
image from parabolic integration





Today's Topic

- Dealing with Motion Blur: Coded Exposure
- Optimized Codes for PSF Estimation and Invertibility
- Dealing with Motion Blur: Parabolic Sweep



Thank You!



Qilin Sun (孙启霖)

香港中文大学（深圳）
点昀技术（Point Spread Technology）