

GAMES 204



Computational Imaging

Lecture 04: Cameras



Qilin Sun (孙启霖)

香港中文大学（深圳）

点昀技术（Point Spread Technology）



Todays Topic

- Introduction
- Imaging Optics
- Aperture
- Depth of Field
- Field of View
- Tips for Photography
- Diffraction Limit
- Sensors
- Noise Introduction
- Exposure
- Dynamic Range

Slide credits

Many of these slides were adapted from:

Wolfgang Heidrich(KAUST)

Ren Ng(Uc Bakery)

Kris Kitani, Ioannis Gkioulekas (15-463, 15-663, 15-862).

Fredo Durand (MIT).

Marc Levoy, Gordon Wetzstein (Stanford).

CS559-Computer Graphics

Introduction



Introduction

nautilus eye
[wikipedia](#)



Introduction

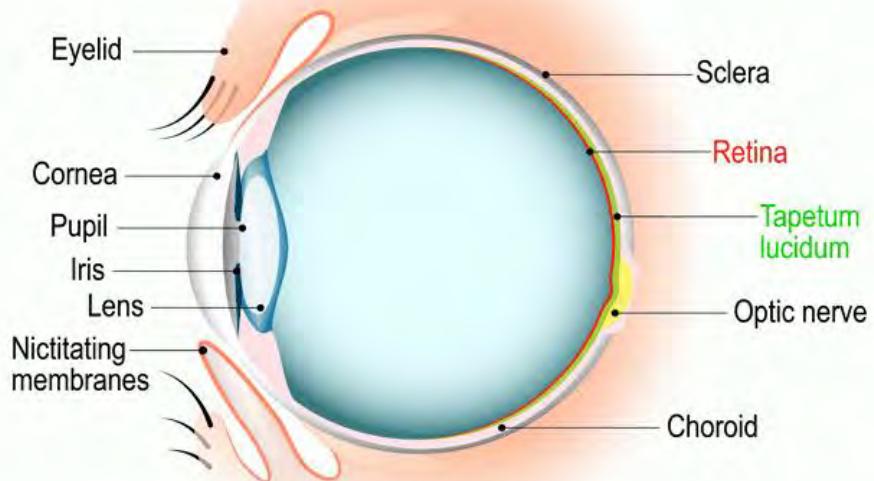


<https://www.dailypaws.com/cats-kittens/behavior/common-cat-behaviors/why-do-cats-eyes-glow-in-the-dark>



Why Do Cats' Eyes Glow in the Dark?

Cat eye anatomy



The dark blue, teal, and gold tapetum lucidum from the eye of a cow



香港中文大學(深圳)
The Chinese University of Hong Kong, Shenzhen



Compound Eye



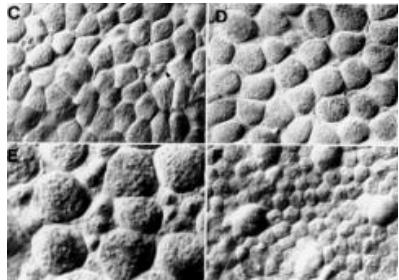
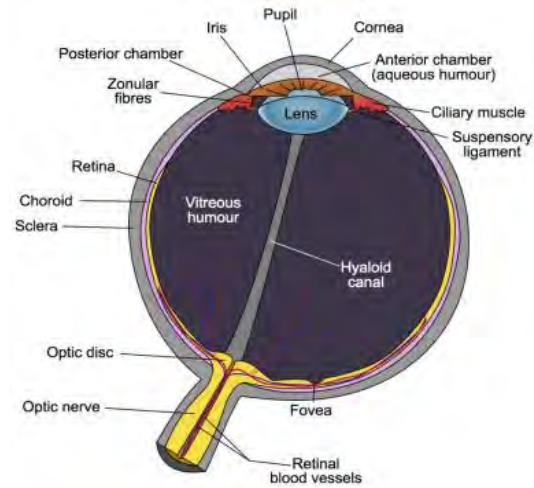
National Geographic



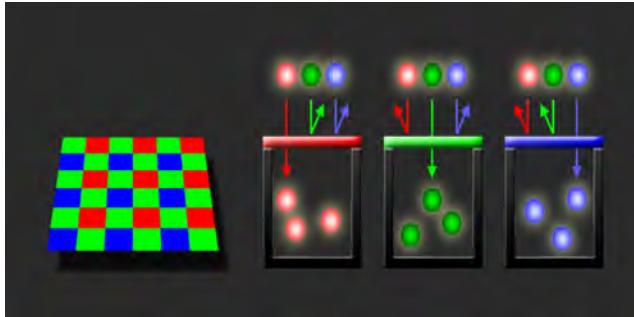
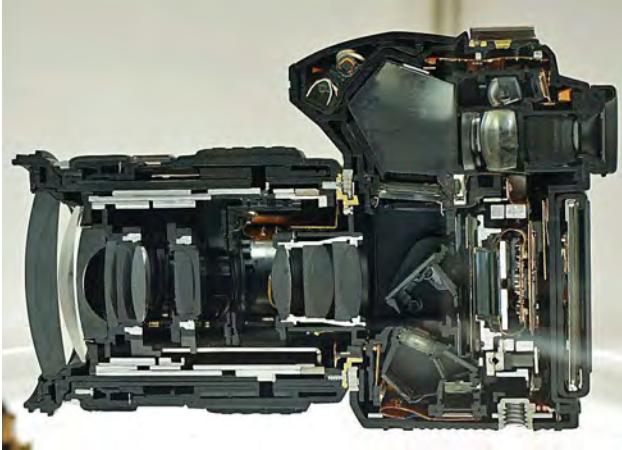
Human Visual System

- **Visual acuity: 20/20 is ~1 arc min**
- **Field of view: ~190° monocular, ~120° binocular, ~135° vertical**
- **Temporal resolution: ~60 Hz (depends on contrast, luminance)**
- **Dynamic range: instantaneous 6.5 f-stops, adapt to 46.5 f-stops**
- **Color: everything in the CIE xy diagram; distances are linear in CIE Lab**
- **Depth cues in 3D displays: vergence, focus, conflicts, (dis)comfort**
- **Accommodation range: ~8cm to ∞ , degrades with age**

Eye vs Camera



[Williams 91]



RocketStock

Imaging Optics



Camera Optics: Lens

- Focus light
- Magnify objects



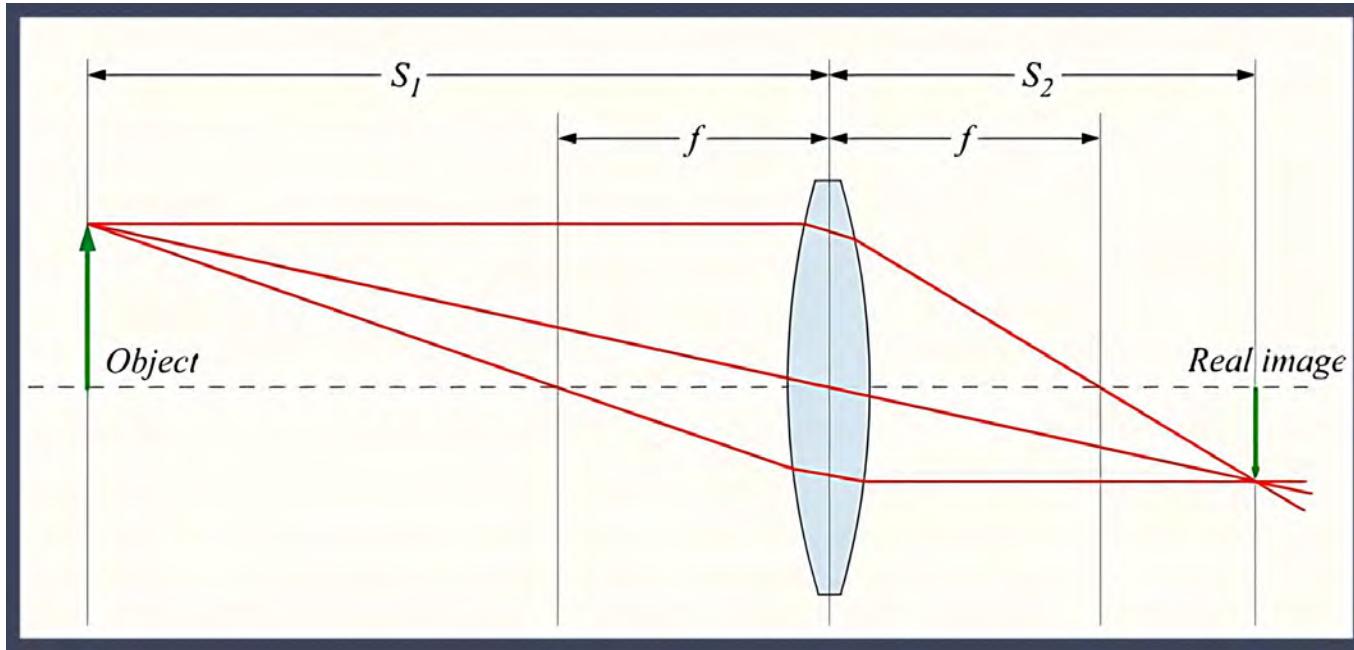
Nimrud lens - 2700 years old



Camera Optics: Lens

lensmaker's equation: $\frac{1}{f} = \frac{1}{S_1} + \frac{1}{S_2}$

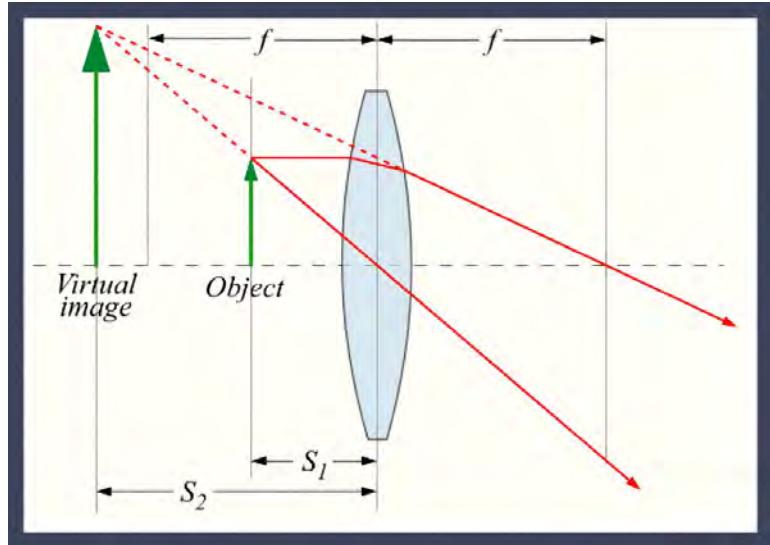
magnification: $M = -\frac{S_2}{S_1} = \frac{f}{f - S_1}$



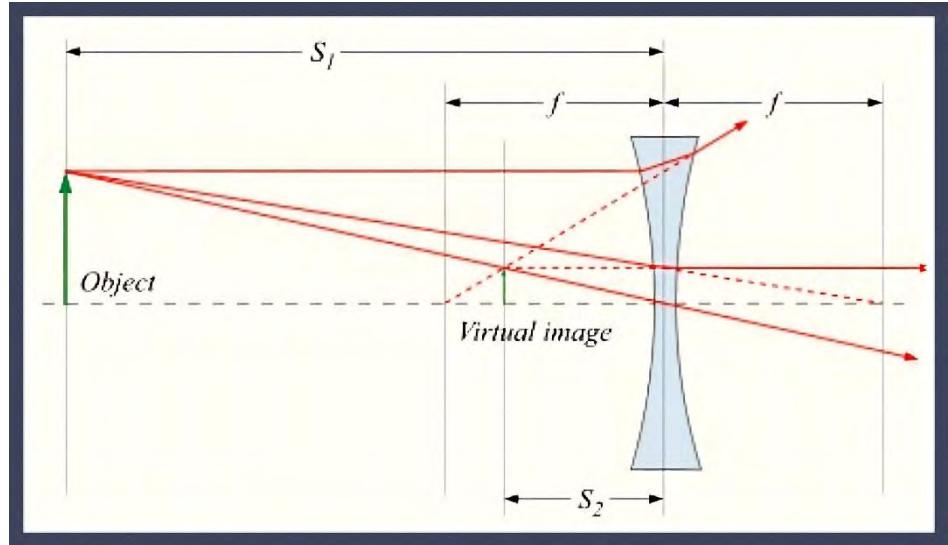


Camera Optics: Lens

$S_1 < f$: magnifying glass

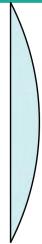


magnification

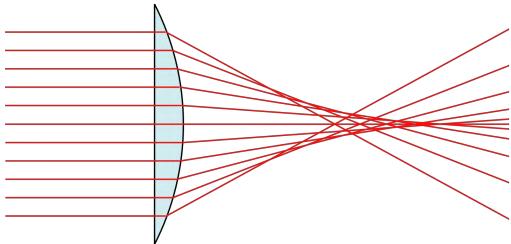




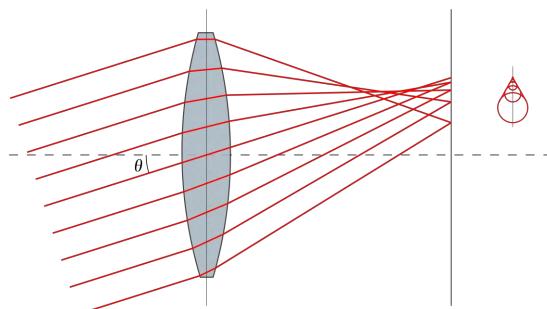
Camera Optics: Lens Aberrations



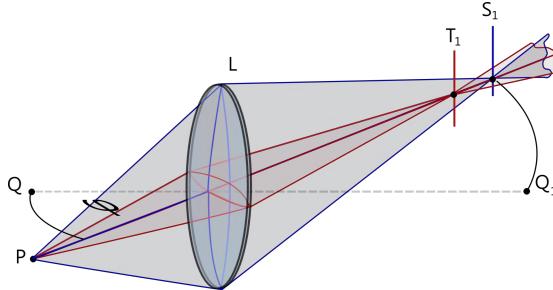
Ideal



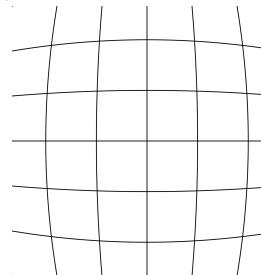
Spherical Abberation



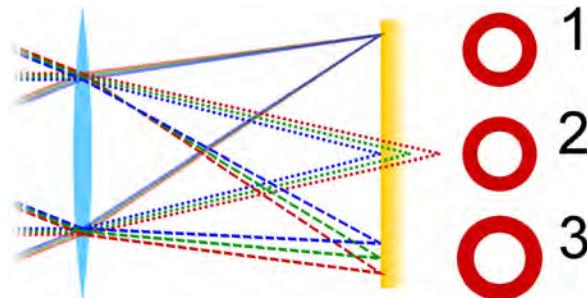
Coma



Astigmatism



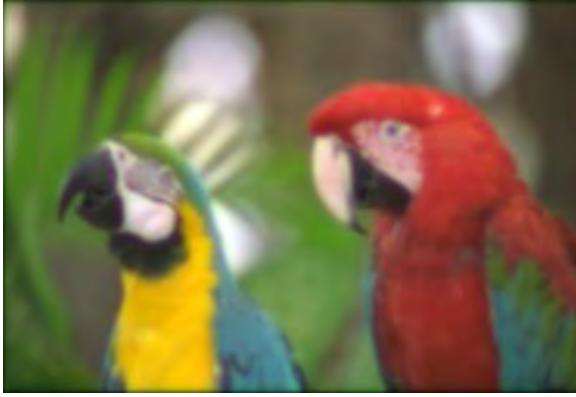
Distortion



Chromatic Abberation



Camera Optics: Lens Aberrations



Sharp Image



Blurred Image due to optical aberrations





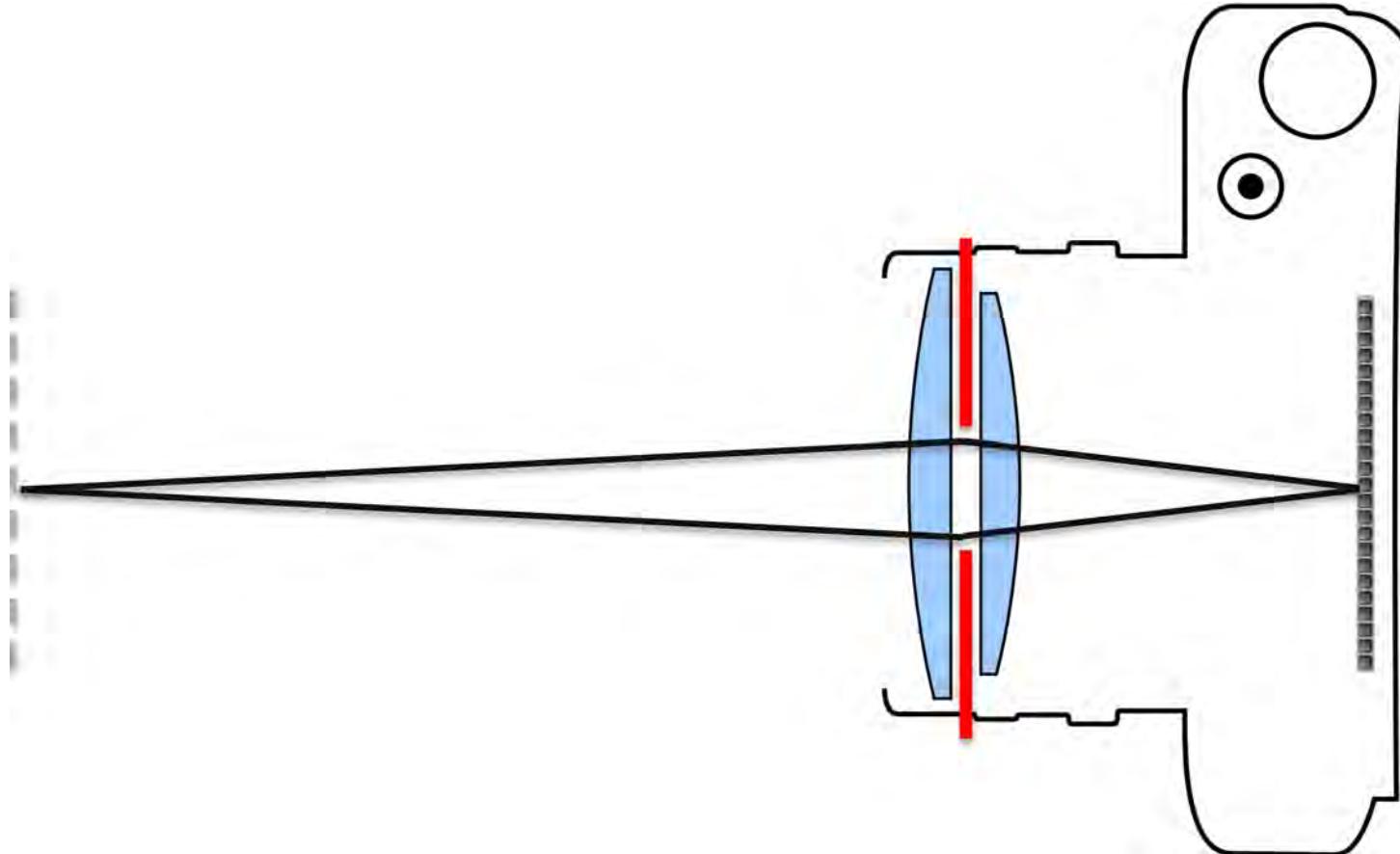
香港中文大學(深圳)
The Chinese University of Hong Kong, Shenzhen



Aperture

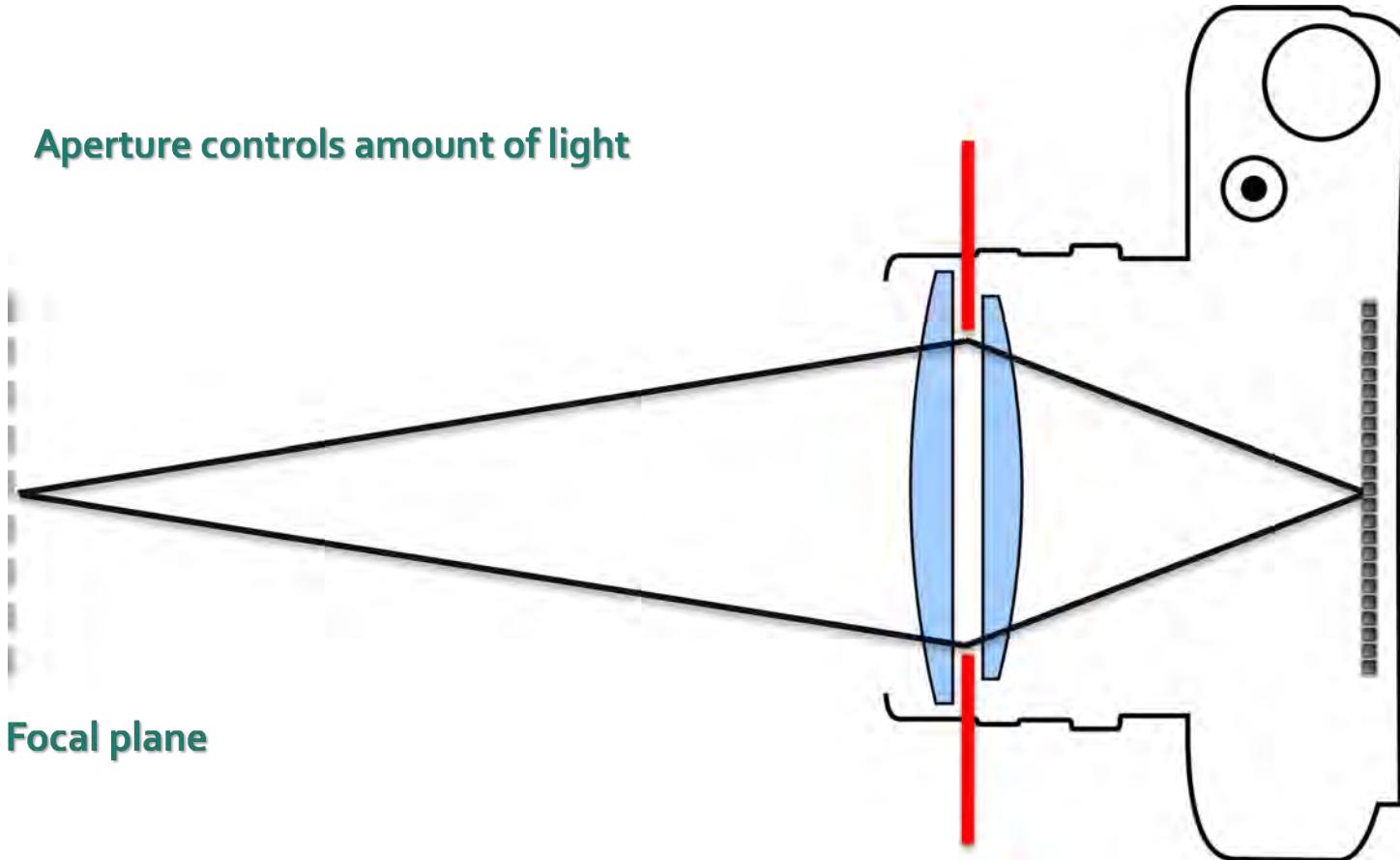


Camera Aperture



Camera Aperture

Aperture controls amount of light

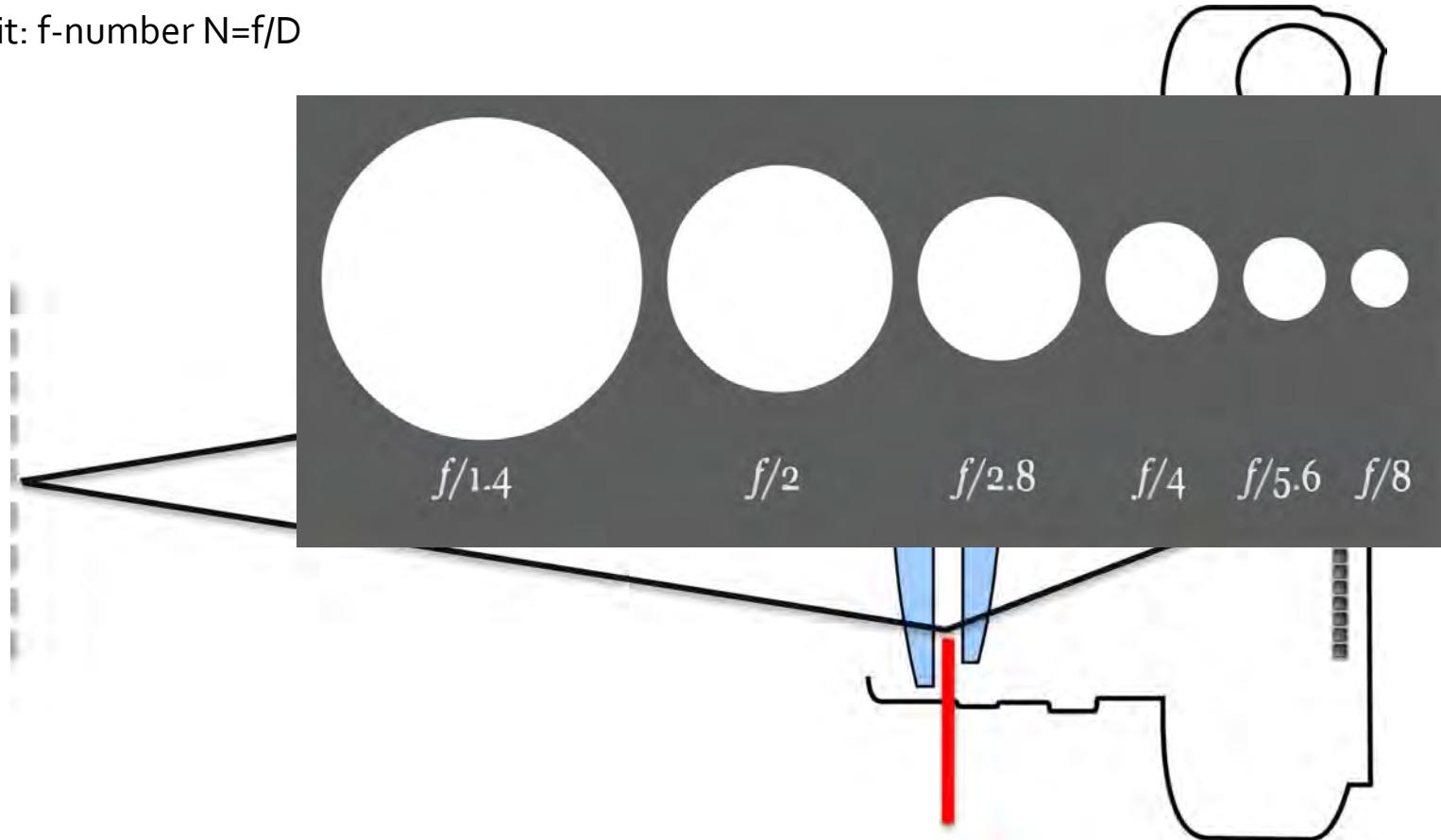


Focal plane



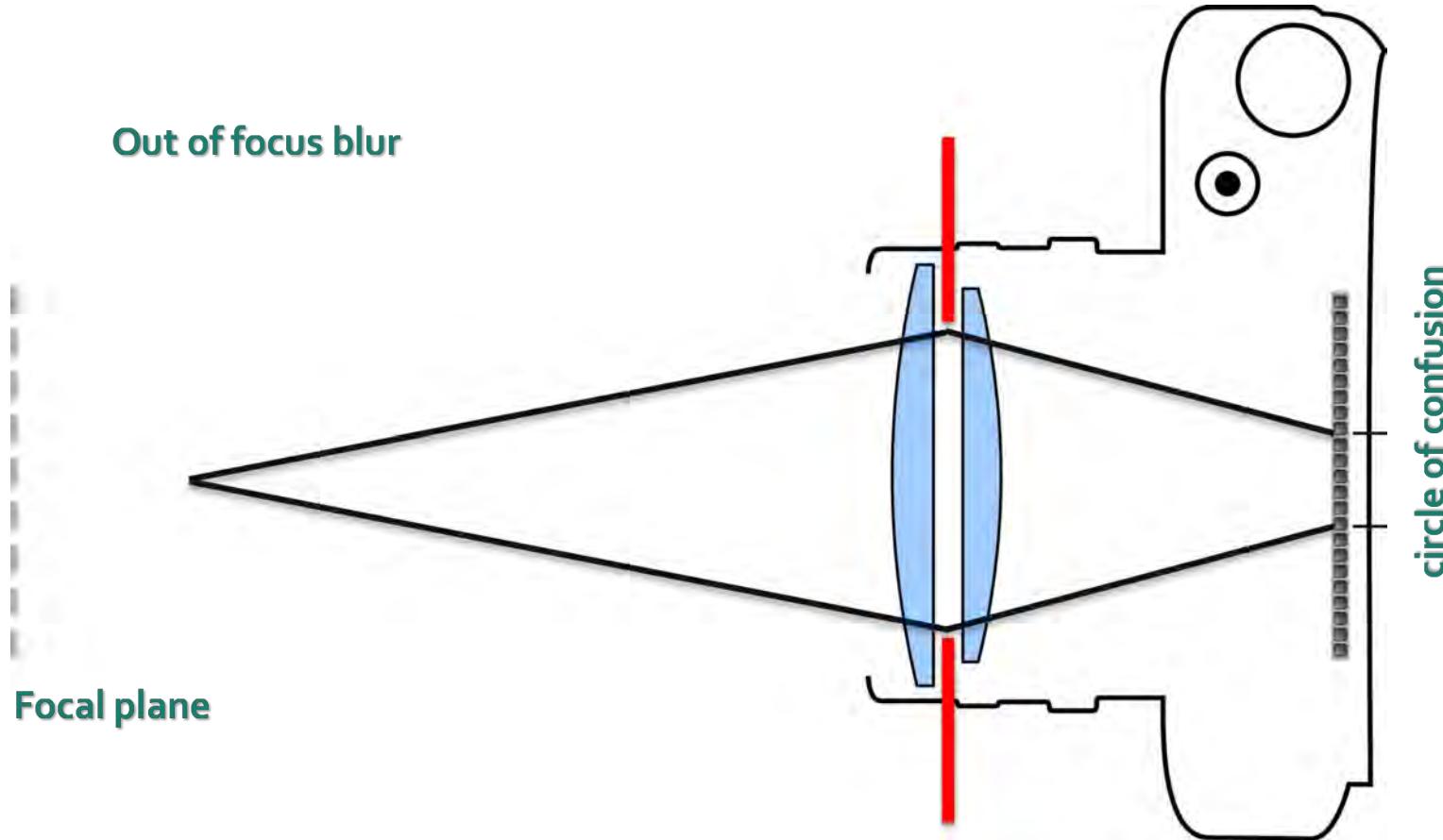
Camera Aperture

Unit: f-number $N=f/D$



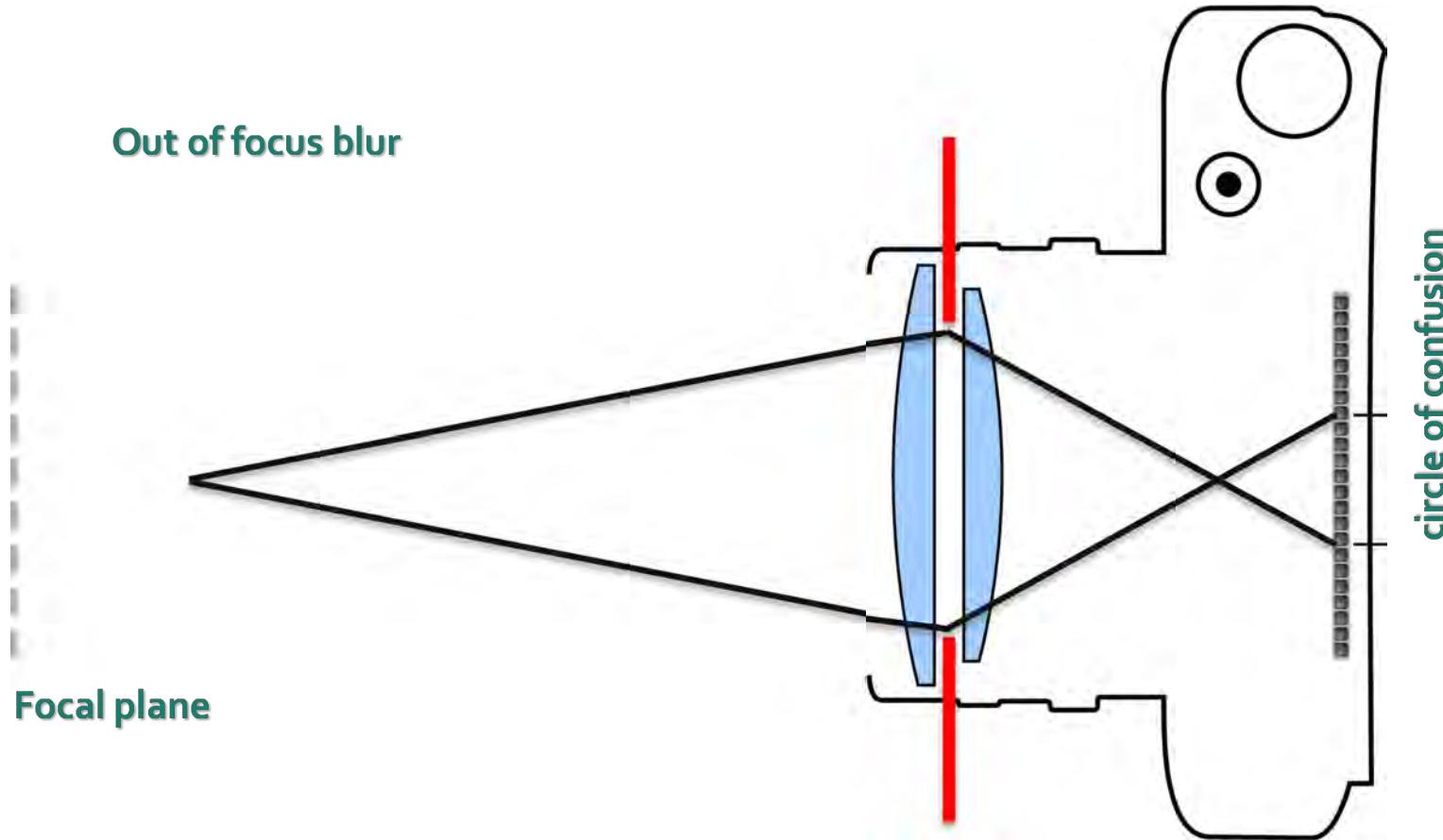


Camera Aperture



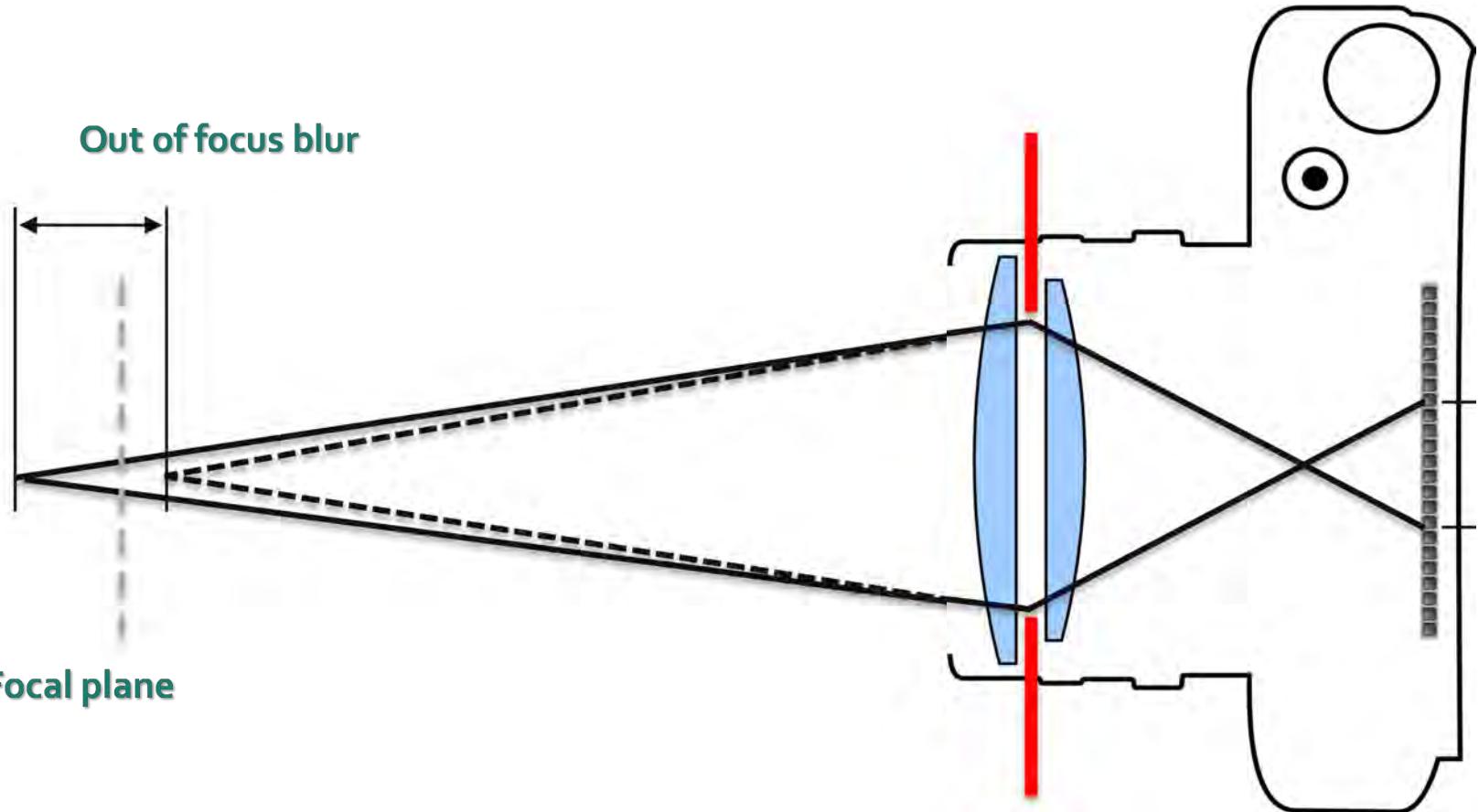


Camera Aperture





Camera Depth of Field



Focal plane



香港中文大學(深圳)
The Chinese University of Hong Kong, Shenzhen



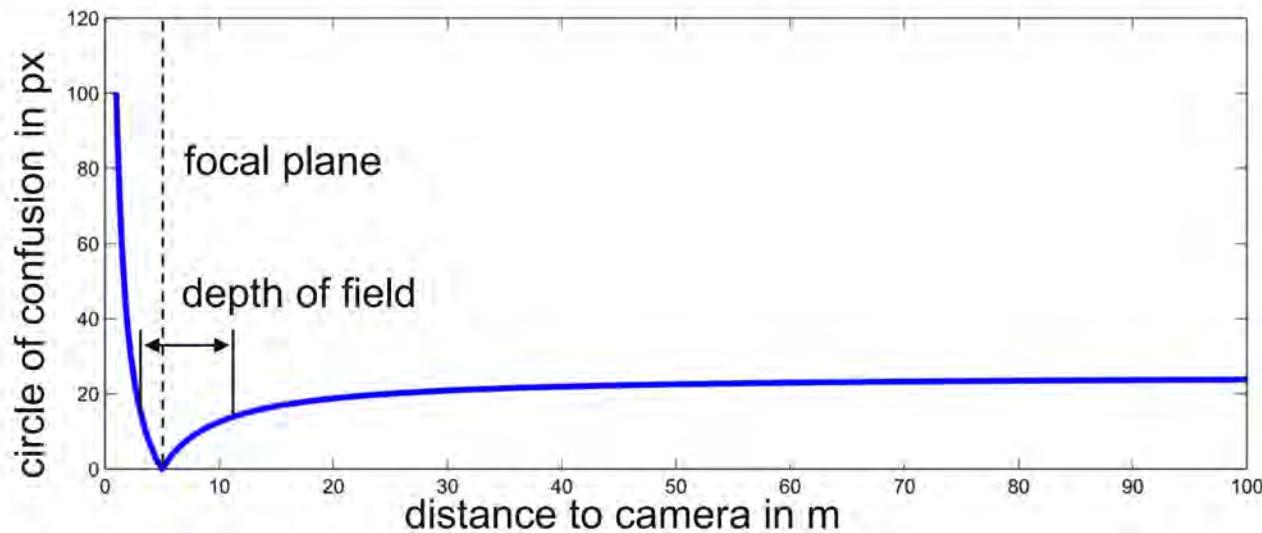
Depth of Field



Camera Depth of Field

$$c = MD \frac{|S - S_1|}{S}$$

Canon 5D Mark III: f=50mm, f/2.8 (N=2.8),
focused at 5m, pixel size=7.5um

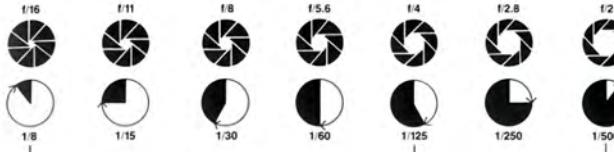


Camera Depth of Field





Camera Depth of Field



London, Photography

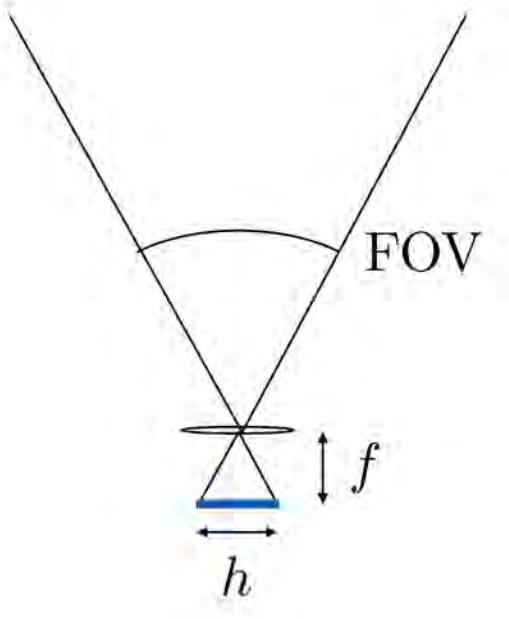
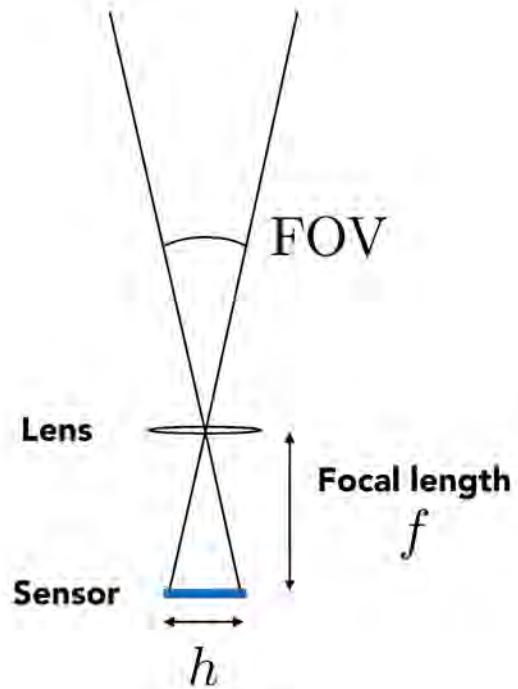


香港中文大學(深圳)
The Chinese University of Hong Kong, Shenzhen



Field of View

Camera Field of View (FOV)

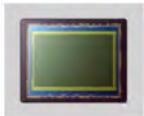
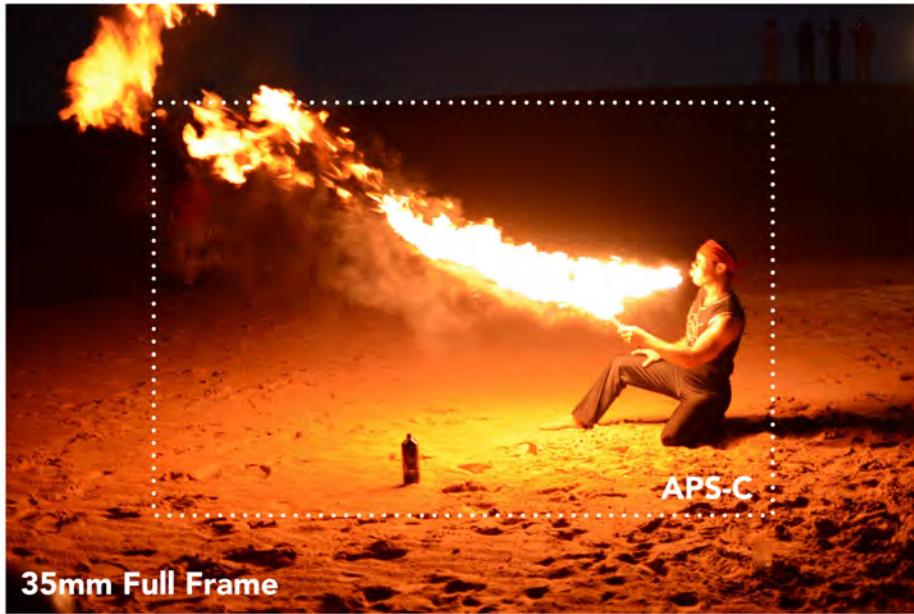


$$\text{FOV} = 2 \arctan \left(\frac{h}{2f} \right)$$

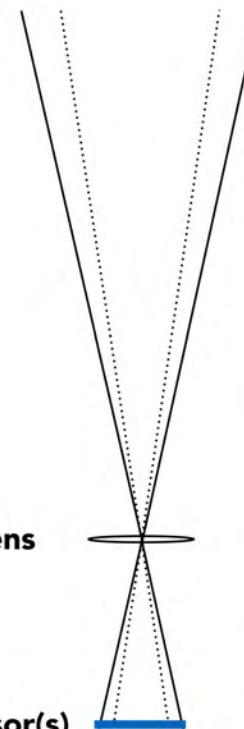
For a fixed sensor size, decreasing the focal length
increases the field of view.



Camera Field of View (FOV)

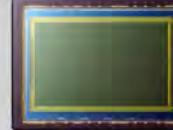


Object





Camera Field of View (FOV)

Sensor Name	Medium Format	Full Frame	APS-H	APS-C	4/3	1"	1/1.63"	1/2.3"	1/3.2"
Sensor Size	53.7 x 40.2mm	36 x 23.9mm	27.9x18.6mm	23.6x15.8mm	17.3x13mm	13.2x8.8mm	8.38x5.59mm	6.16x4.62mm	4.54x3.42mm
Sensor Area	21.59 cm ²	8.6 cm ²	5.19 cm ²	3.73 cm ²	2.25 cm ²	1.16 cm ²	0.47 cm ²	0.28 cm ²	0.15 cm ²
Crop Factor	0.64	1.0	1.29	1.52	2.0	2.7	4.3	5.62	7.61
Image									
Example									

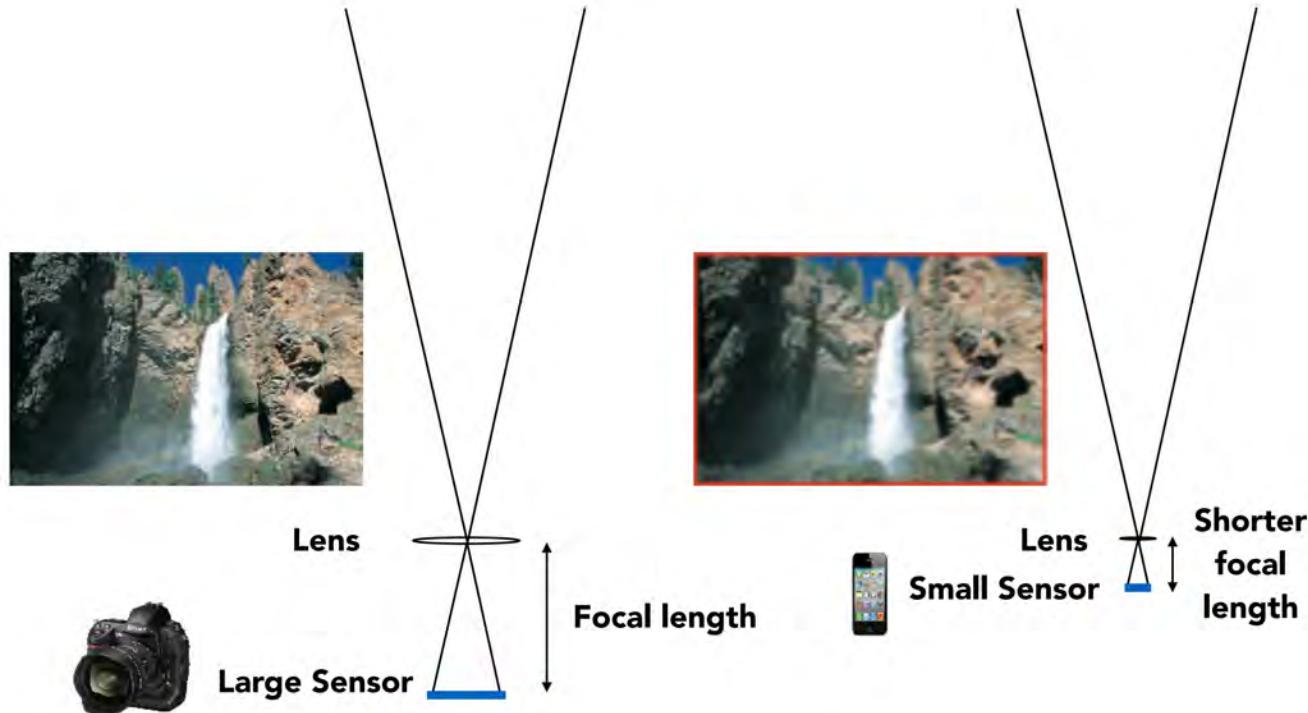


Credit: lensvid.com



Camera Field of View (FOV)

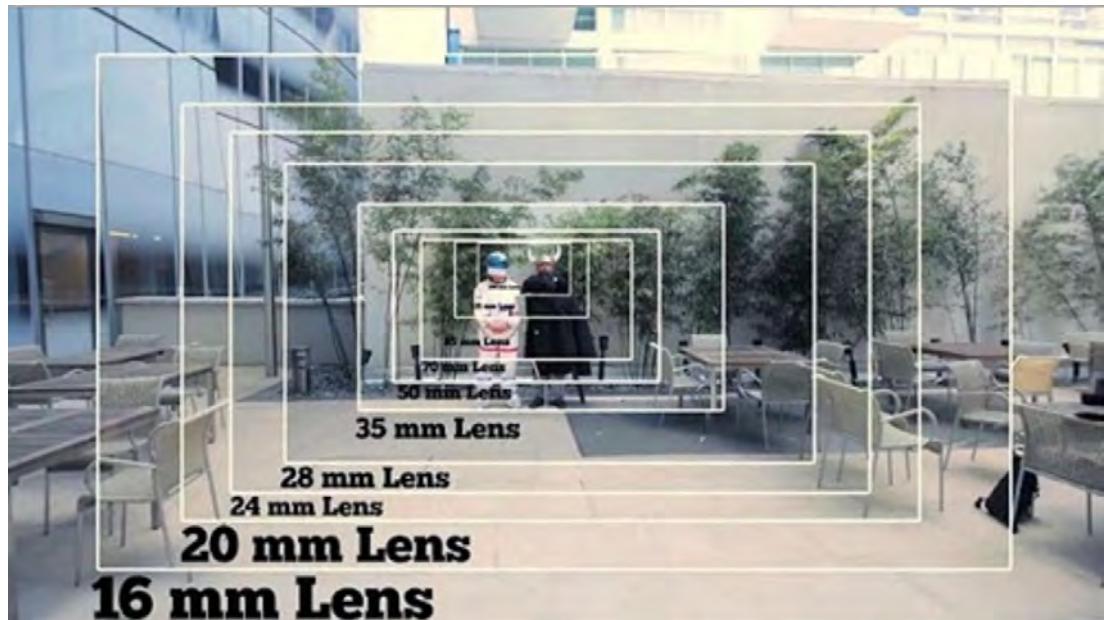
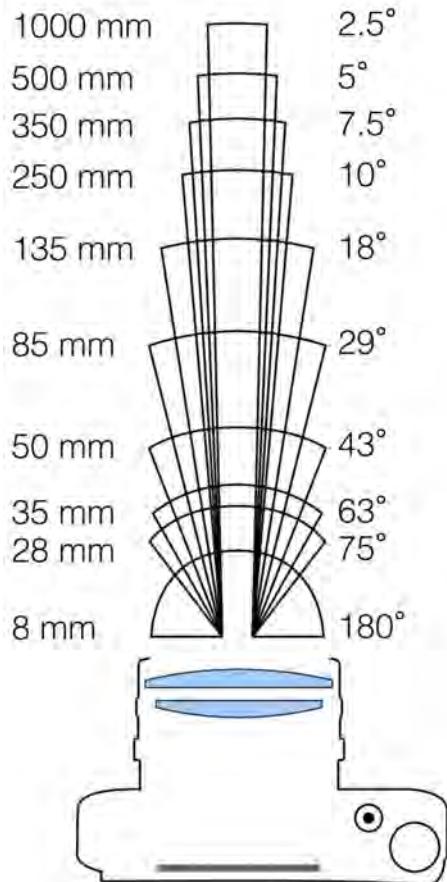
Mobile Phone: Maintain FOV on Smaller Sensor?



To maintain FOV, decrease focal length of lens
in proportion to width/height of sensor

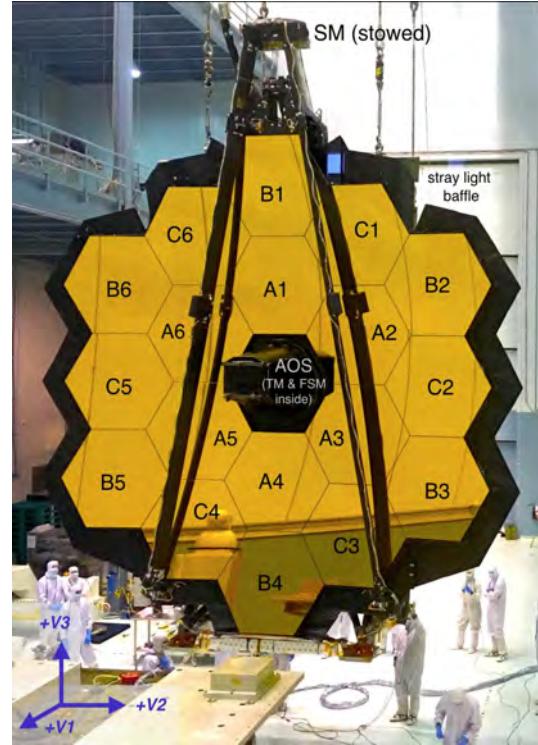
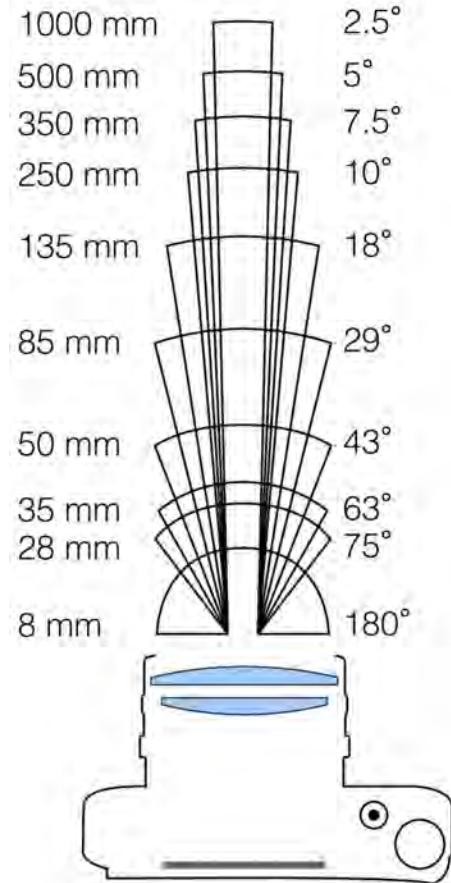


Camera Field of View (FOV)



Andrew McWilliams

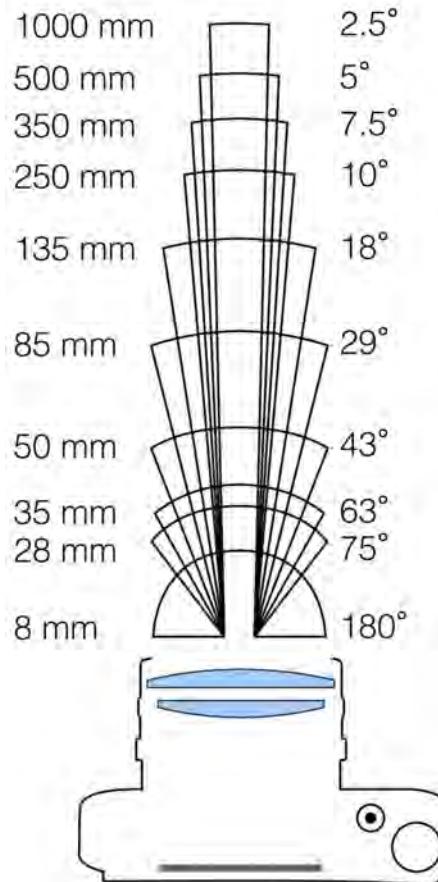
Camera Field of View (FOV)



**James Webb– What's the focal length?
A: 131.4m**



Camera Field of View (FOV)



- For historical reasons, usually refer to angular FOV by focal length of a lens used on a 35mm-format film (36 x 24mm)
- Examples of focal lengths on 35mm format:
 - 17mm is wide angle 104°
 - 50mm is a “normal” lens 47°
 - 200mm is telephoto lens 12°
- Note: When we say current cell phones have approximately 28mm “equivalent” focal length, this uses the above convention. The physical focal length is often 5-6 times shorter, because the sensor is correspondingly smaller



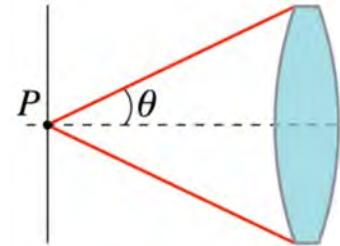
Diffraction Limit

Ernst Abbe 1873:

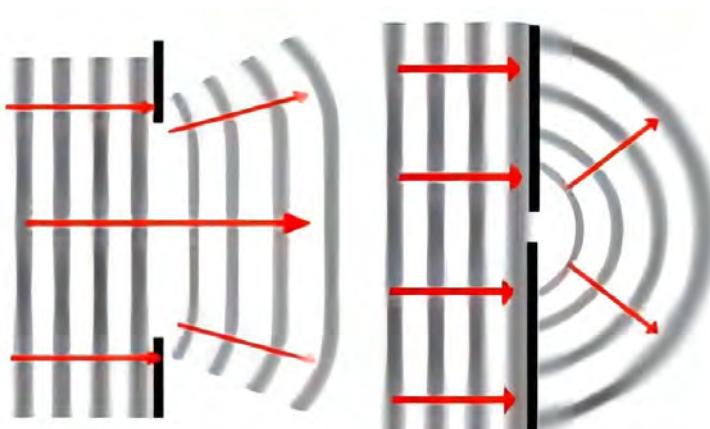
$$d = \frac{\lambda}{2n \sin \theta} = \frac{\lambda}{2NA} \approx \frac{\lambda}{f\text{-number}}$$

spot radius (image space)

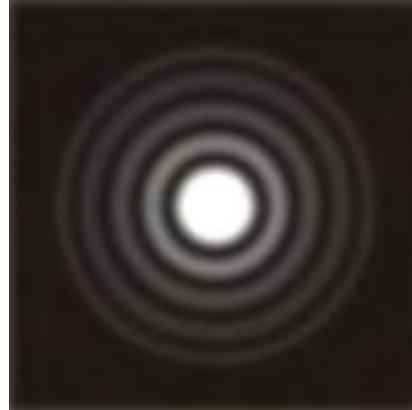
numerical aperture



Diffraction



Airy pattern

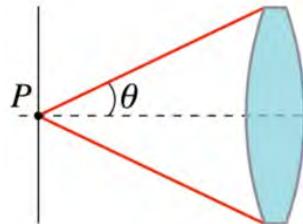


Diffraction Limit

Ernst Abbe 1873: $d = \frac{\lambda}{2n \sin \theta} = \frac{\lambda}{2NA} \approx \lambda N$

↑
numerical aperture

↓
f-number



- Microscope objectives today: NA 1.4-1.6 à $d=\lambda/2.8$
 - Small f-number (large NA) = high resolution but shallow depth of field
 - inherent tradeoff between “3D” information and 2D resolution
 - space-bandwidth product (uncertainty principle)

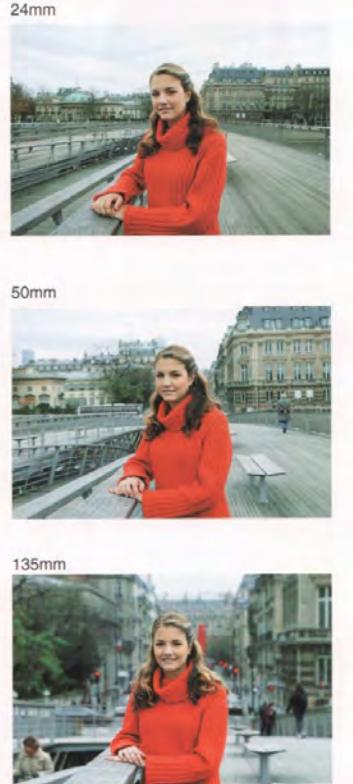
Tips for Photography



Tips: Photographer's Mindset



From Canon EF Lens Work III



In this sequence,
distance from subject increases
with focal length to maintain
image size of human subject.

Notice the dramatic change in
background perspective.

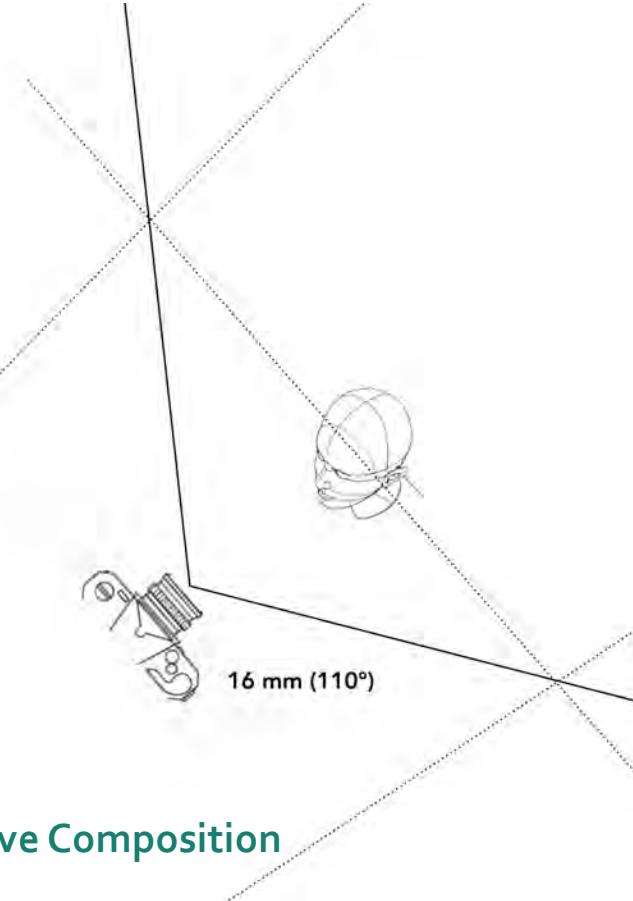
Perspective Composition – Camera Position / Focal Length



Tips: Photographer's Mindset



Up close and zoomed wide
with short focal length

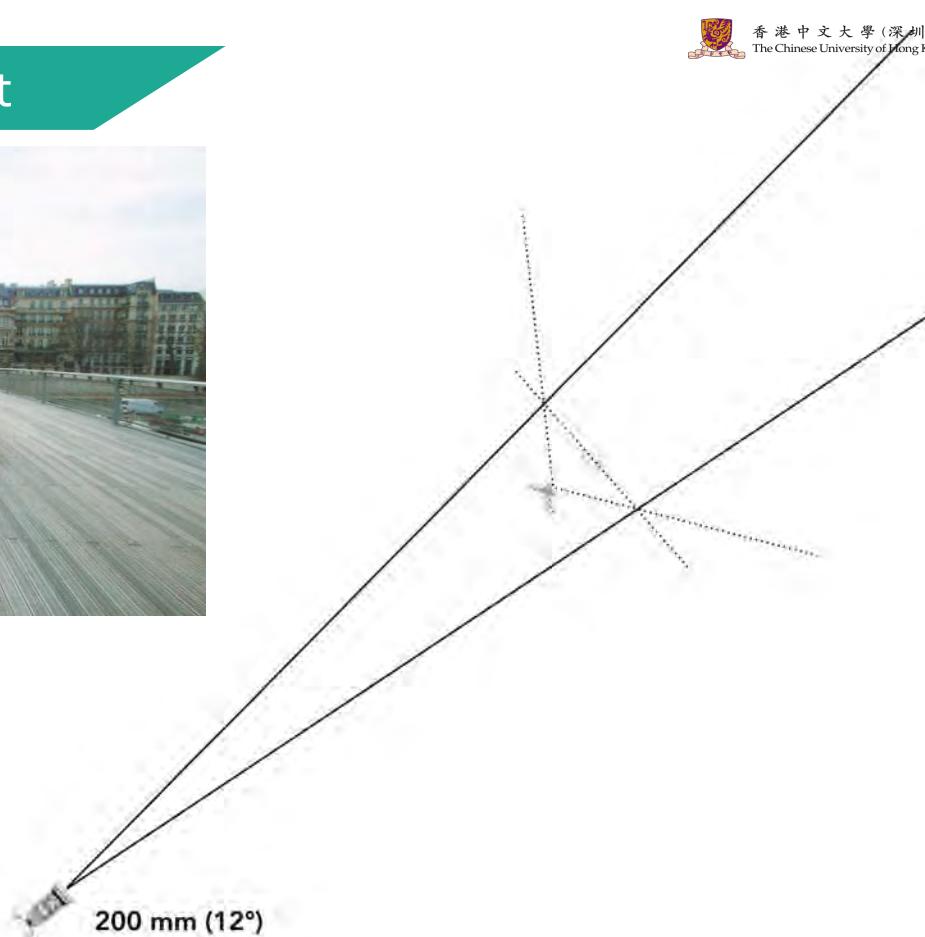




Tips: Photographer's Mindset



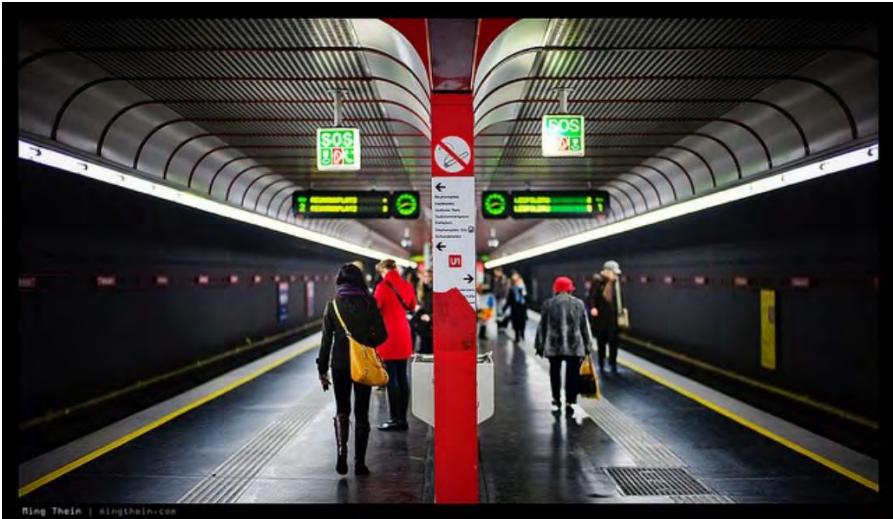
Walk back and zoom in
with long focal length



Perspective Composition



Tips: Photographer's Mindset



“Choose your perspective before you choose your lens.”
— Ming Thein, mingthein.com

Perspective Composition



Tips: Improve Your Own Photography

Tip 1: Make sure you have a strong subject

- Make it prominent, e.g. 1/3 of your image

Tip 2: Choose a good perspective relationship (relative size) between your subject and background (or foreground)

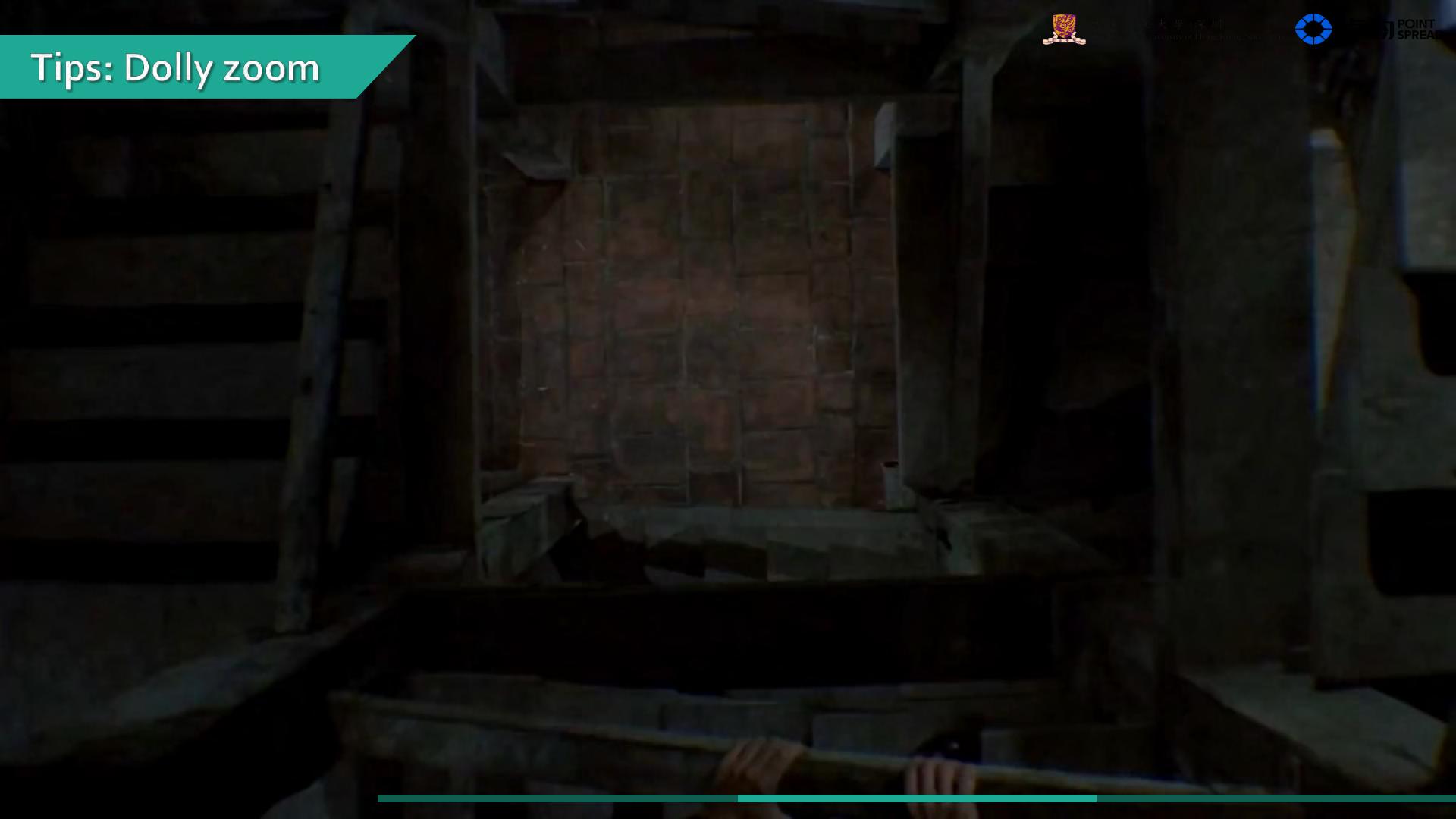
- Complement, don't compete with the subject

Tip 3: Change the zoom and camera distance to your subject

- Implement: actively zoom, and move your camera in/out
- Even works with your smartphone!



Tips: Dolly zoom





香港中文大學(深圳)
The Chinese University of Hong Kong, Shenzhen



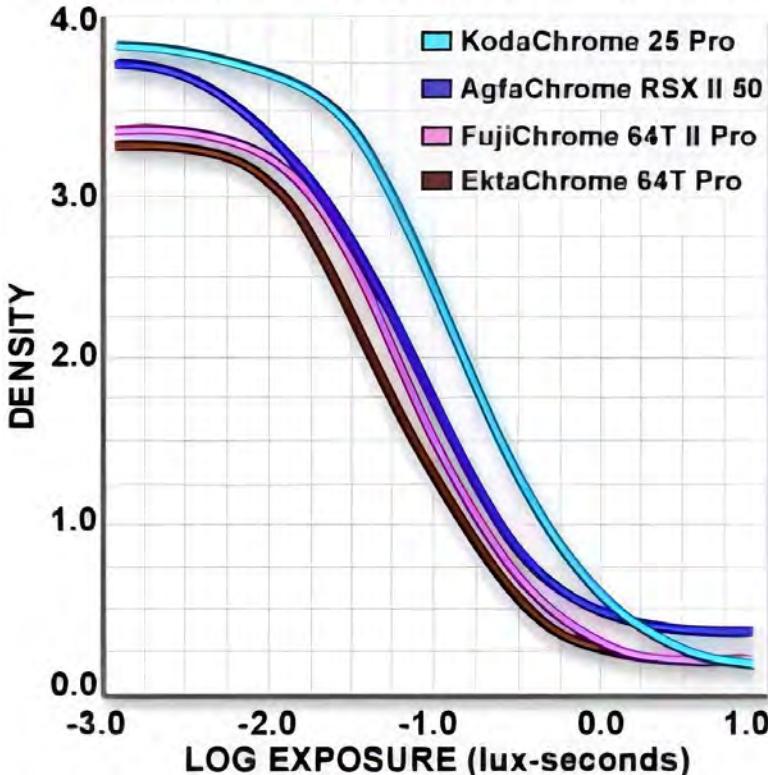
Sensors



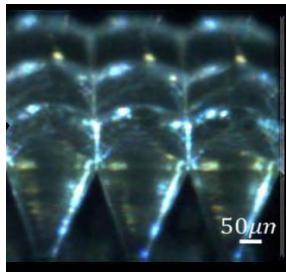
Analog Film

- Highly non-linear response:
 - Here shown for slide film
- Terminology:
 - Transmittance T: portion of light transmitted (0...1)
 - Density: $\log(1/T)$
 - Contrast: ratio between max. and min. discernible intensity
- Example:
 - Transmittance 0.001
 - Density: 3
- Contrast of film:
 - 1,000:1 or more

Characteristic Curves for Popular Color Transparency Films



Sensors: What's a Pixel?



3D Micro Lens
Point Spread Technology

Anatomy of the Active Pixel Sensor Photodiode

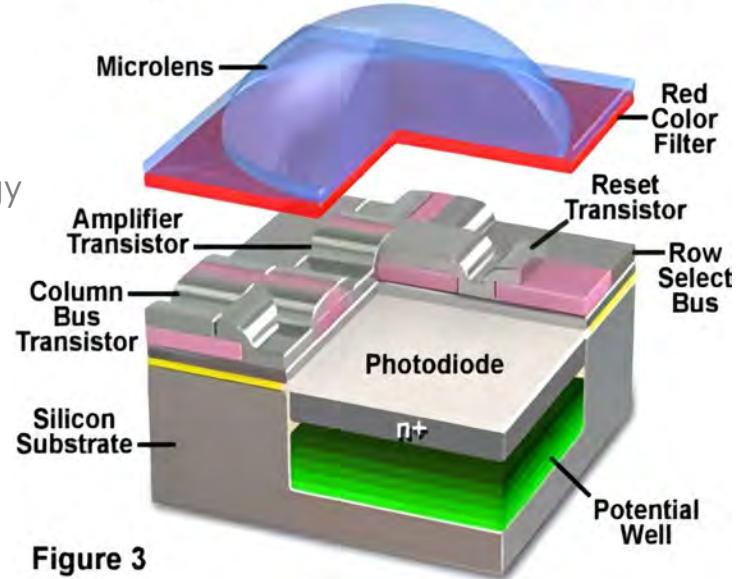
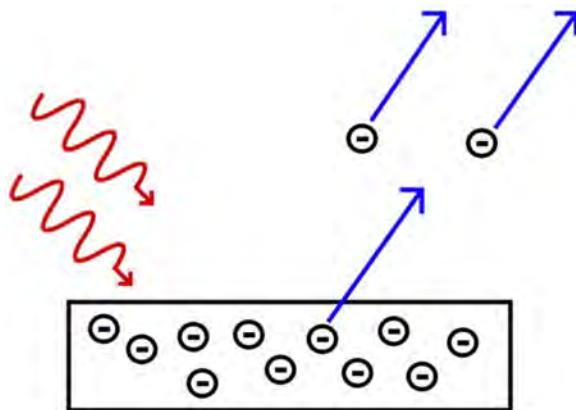


Figure 3

www.olympus-lifescience.com

Photon to electron converter
photoelectric effect!



$$QE = \frac{\text{\# electrons}}{\text{\# photons}}$$

wikipedia



Photosite response

The photosite response is mostly linear

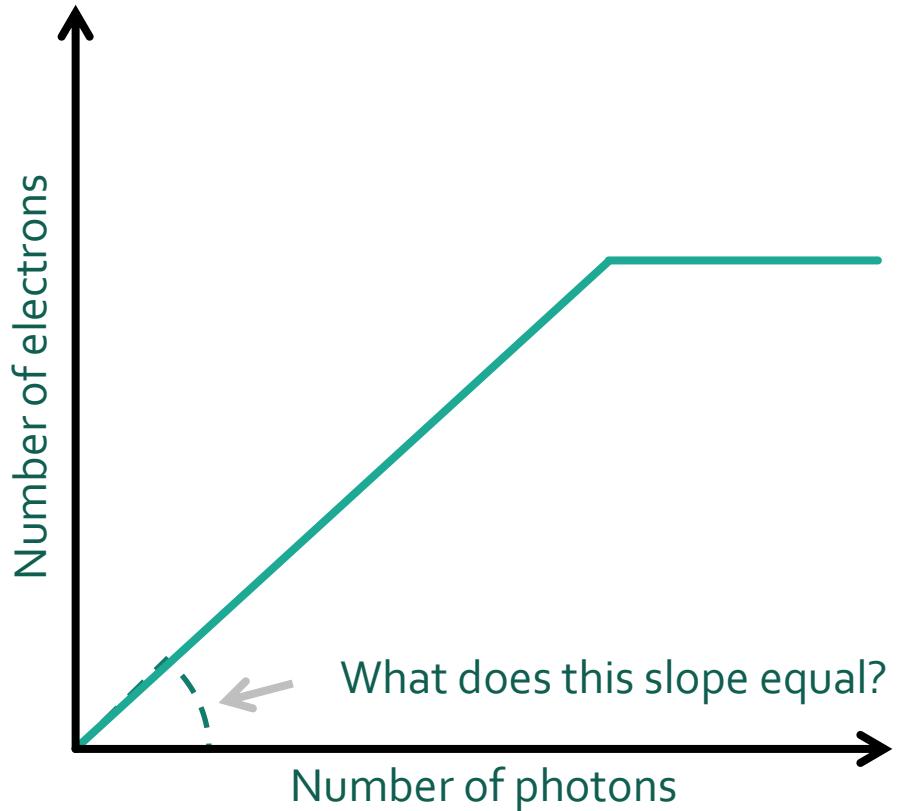
- non-linear when potential well is saturated (over-exposure)
- non-linear near zero (due to noise)

We will see how to deal with these issues in a later lecture (HDR imaging).

under-exposure
(non-linearity due to sensor noise)



over-exposure
(non-linearity due to sensor saturation)

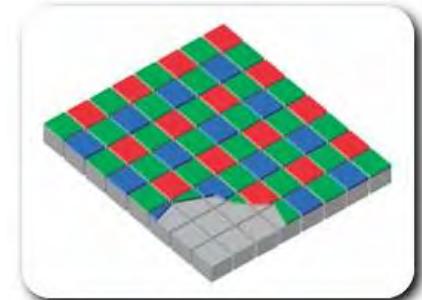




Color Filter Arrays

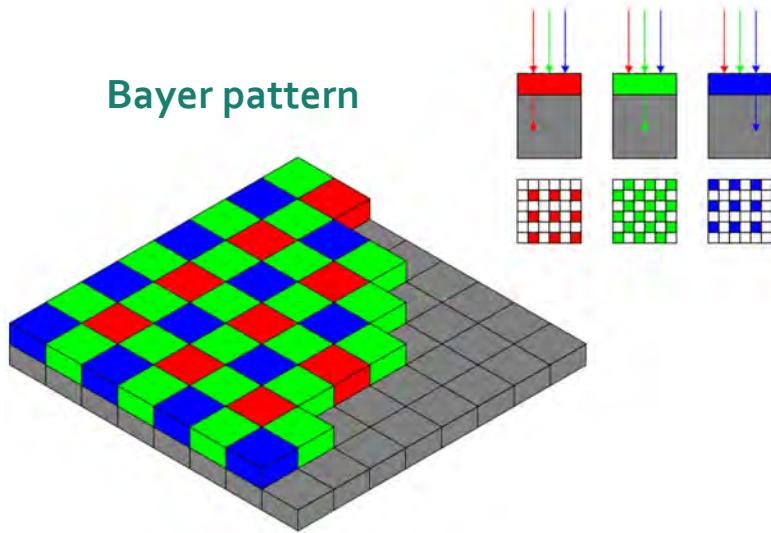
Approach

- Pixels are covered by color filters
 - Twice as many green pixels as red or blue ones
 - Interpreted as “intensity”
 - Missing color values are interpolated for every pixel
 - More in later lecture
 - Note: camera specs report the total number of pixels in a sensor
 - I.e., a image recorded by a 1-chip camera only consists of $\frac{1}{3}$ measured values, $\frac{2}{3}$ are interpolated

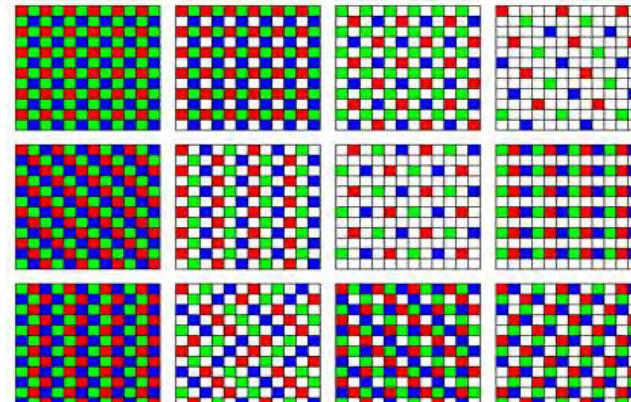
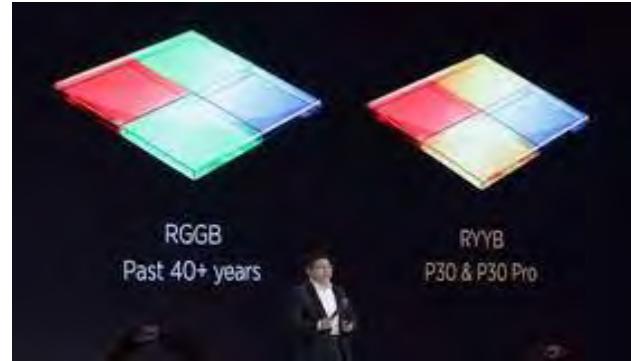




Color Filter Arrays



Any combination possible tradeoffs?





Sensors

Common Semiconductor sensors used in cameras:

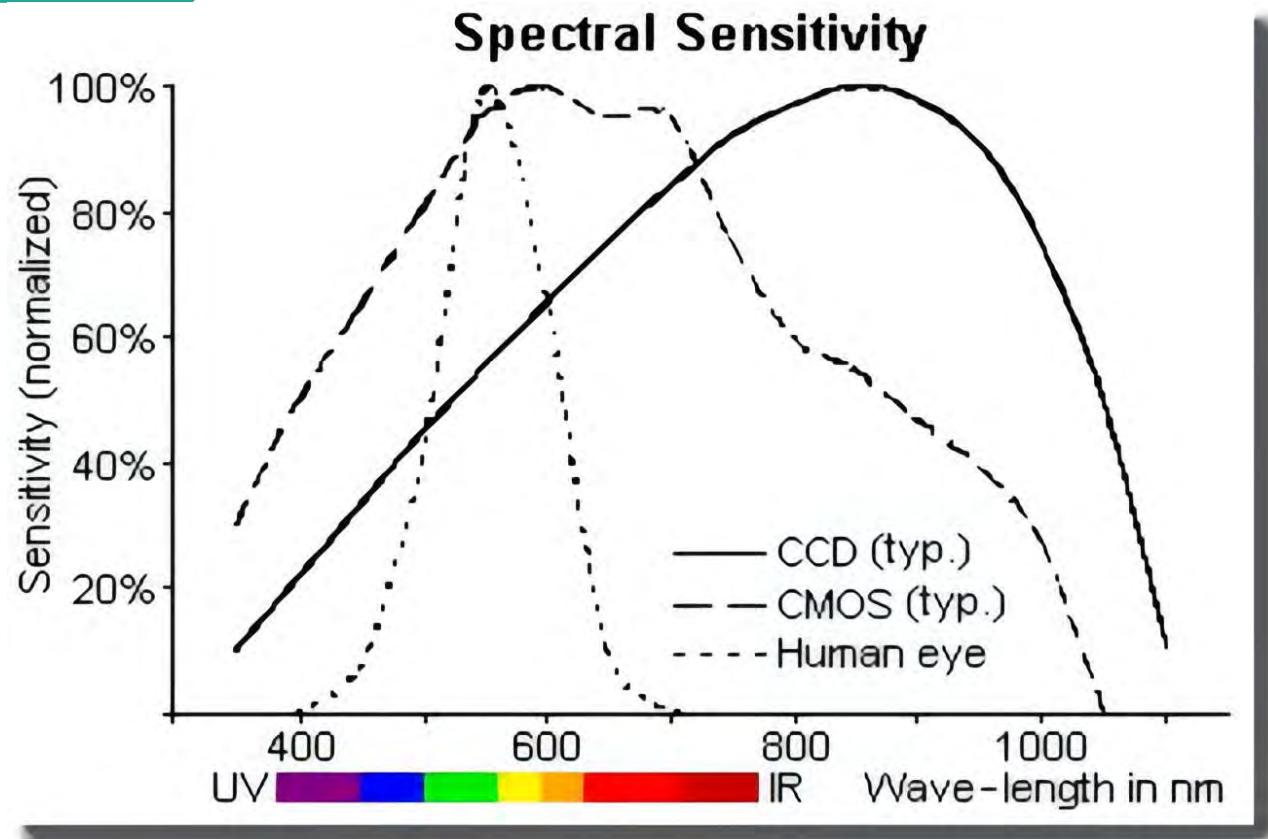
- Charge Coupled Devices (CCD)
- Complementary Metal-Oxide-Semiconductor (CMOS)
- Foveon

Others

- Charge Injection Devices (CID)
- Photomultipliers
- Cathode Ray Tubes (CRT)
- Single Photon Avalanche Diode Array(SPAD)
- Quanta Image Sensor (QIS)
- Two-bucket Sensor
- Photonic Mixer Device (PMD)
- ...



Spectral Sensitivity



CCD: High Sensivity for infrared

Noise Introduction



Photons to RAW Image

photon
noise

sensor defects =
fixed pattern noise

additive noise

quantization
“noise”

photons



RAW image



Sensor Noise

- **Noise is (usually) bad!**

- **Many sources of noise: heat, electronics, amplifier gain, photon to electron conversion, pixel defects, read, ...**

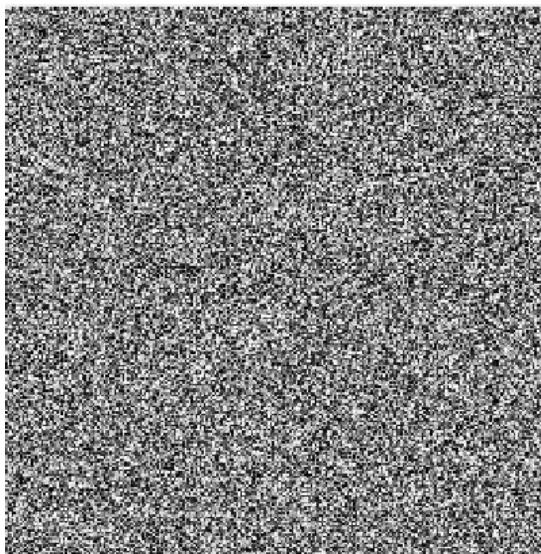
- **Different noise follows different statistical distributions, two crucial ones:**
 - **Gaussian**
 - **Poisson**

Gaussian Noise

- Thermal, read, amplifier
- Additive, signal-independent!



+



=





Photon or Shot Noise

➤ Signal dependent

➤ Poisson distribution:

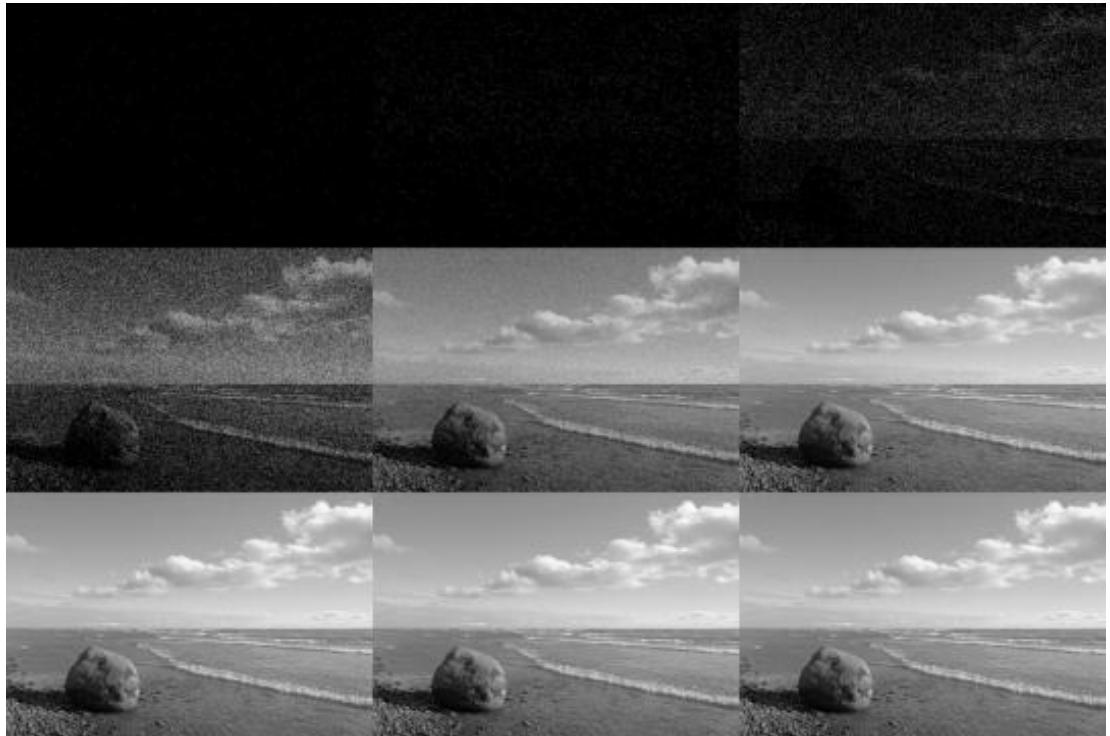
$$f(k; \lambda) = \frac{\lambda^k e^{-\lambda}}{k!}$$

$$\sigma = \sqrt{\lambda}$$

N photons: $\sigma = \sqrt{N}$

2N photons: $\sigma = \sqrt{2}\sqrt{N}$

nonlinear!



wikipedia



Signal-to-Noise Ratio (SNR)

$$SNR = \frac{\text{mean pixel value}}{\text{standard deviation of pixel value}} = \frac{\mu}{\sigma}$$

————— signal
————— noise

$$= \frac{PQ_e t}{\sqrt{PQ_e t + Dt + N_r^2}}$$

P = incident photon flux (photons/pixel/sec)

Q_e = quantum efficiency

t = exposure time (sec)

D = dark current (electrons/pixel/sec), including hot pixels

N_r = read noise (rms electrons/pixel), including fixed pattern noise



Scientific Sensors

- e.g., Andor iXon Ultra 897: cooled to -100°C
- Scientific CMOS & CCD
- Reduce pretty much all noise, except for photon noise





香港中文大學(深圳)
The Chinese University of Hong Kong, Shenzhen



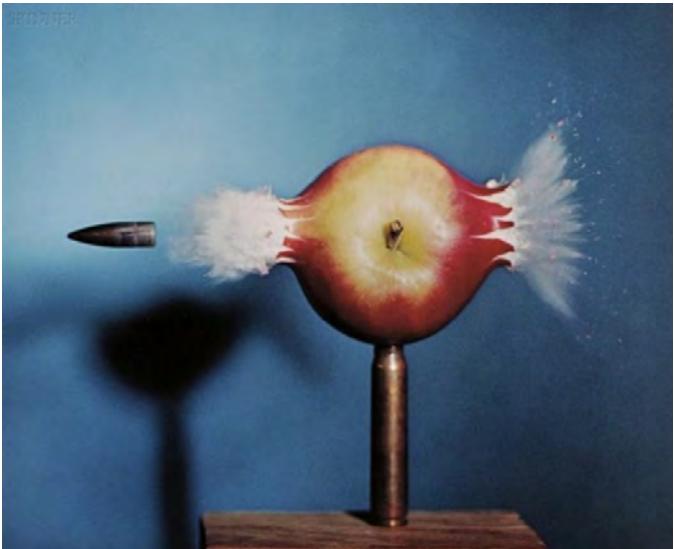
Exposure



Exposure

High-Speed Photography

- Short exposure
- Bright strobe illumination
- Gun synced to camera



Harold Edgerton

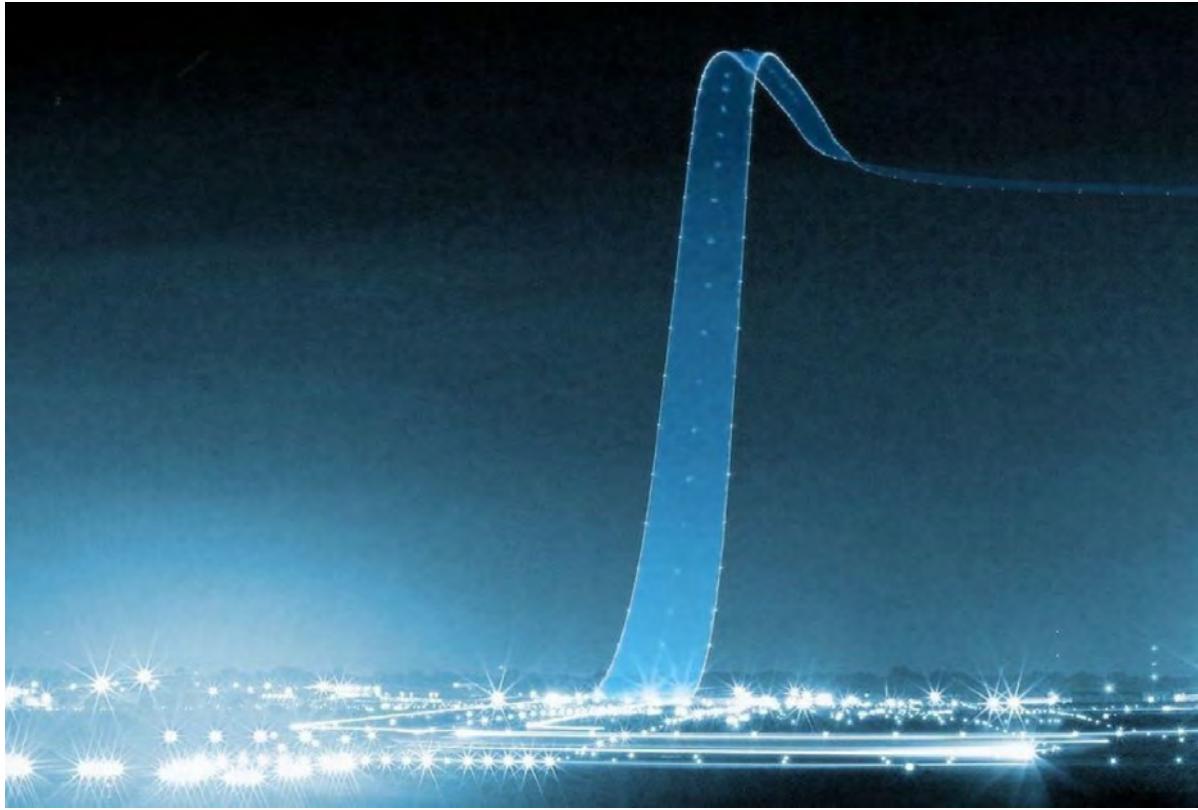


Mark Watson



Exposure

Long-Exposure Photography

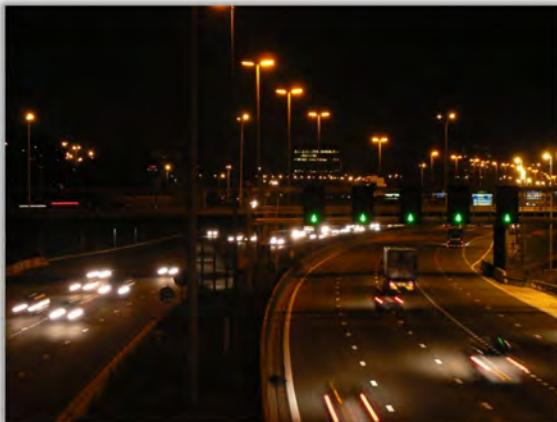


<https://www.demilked.com/best-long-exposure-photos/>



Exposure (shutter speed)

- $Q = T \times E$
- Exposure = time x irradiance (e.g. 1/250, 1/60, 1, 15, bulb)
- Exposure time (T)
 - Controlled by shutter
- Irradiance (E)
 - Power of light falling on a unit area of sensor
 - Controlled by lens aperture and focal length



1/4 sec, f/3.3



2 sec, f/6.3,

wikipedia

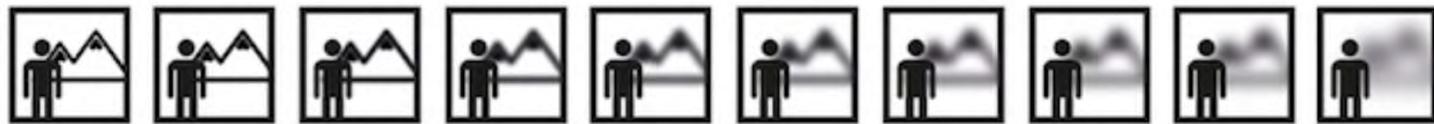
Exposure Levels (1 “Stop” = 2x Exposure)

Exposure bracketing with ± 1 stop exposure





Exposure Controls: Aperture, Shutter, Gain (ISO)



F32 F22 F16 F11 F8 F5,6 F4 F2,8 F2 F1,4



1/1000 1/500 1/250 1/125 1/60 1/30 1/15 1/8 1/4 1/2



ISO 50 ISO 100 ISO 200 ISO 400 ISO 800 ISO 1600 ISO 3200 ISO 6400 ISO 12800 ISO 25600



Definition: F-Number of a Lens

➤ F-Number

$$f/\# = N = f/D$$

where f is the focal length, and D is the diameter of the entrance pupil

- Common F-stops on real lenses: 1.4, 2, 2.8, 4.0, 5.6, 8, 11, 16, 22, 32
- 1 stop doubles exposure
- Notation: an f-stop of, e.g. 2 is sometimes written $f/2$, or $F:2$



Exposure Controls: Aperture, Shutter, Gain (ISO)

Aperture size:

- Change the f-stop by opening / closing the aperture (if camera has iris control)

Shutter speed:

- Change the duration the sensor pixels integrate light

ISO gain:

- Change the amplification (analog and/or digital) between sensor values and digital image values



Constant Exposure: F-Stop vs Shutter Speed

Example: these pairs of aperture and shutter speed give equivalent exposure

F-Stop	1.4	2.0	2.8	4.0	5.6	8.0	11.0	16.0	22.0	32.0
Shutter	1/500	1/250	1/125	1/60	1/30	1/15	1/8	1/4	1/2	1

If the exposure is too bright/dark, may need to adjust f-stop and/or shutter up/down.

ISO (Gain, “film speed”)

Third variable for exposure



Image sensor: trade sensitivity for noise

- Multiply signal before analog-to-digital conversion
- Linear effect (ISO 200 needs half the light as ISO 100)



ISO Gain vs Noise in Canon T2i

Sensor
sensitivity
-
Analog gain
applied before
ADC!

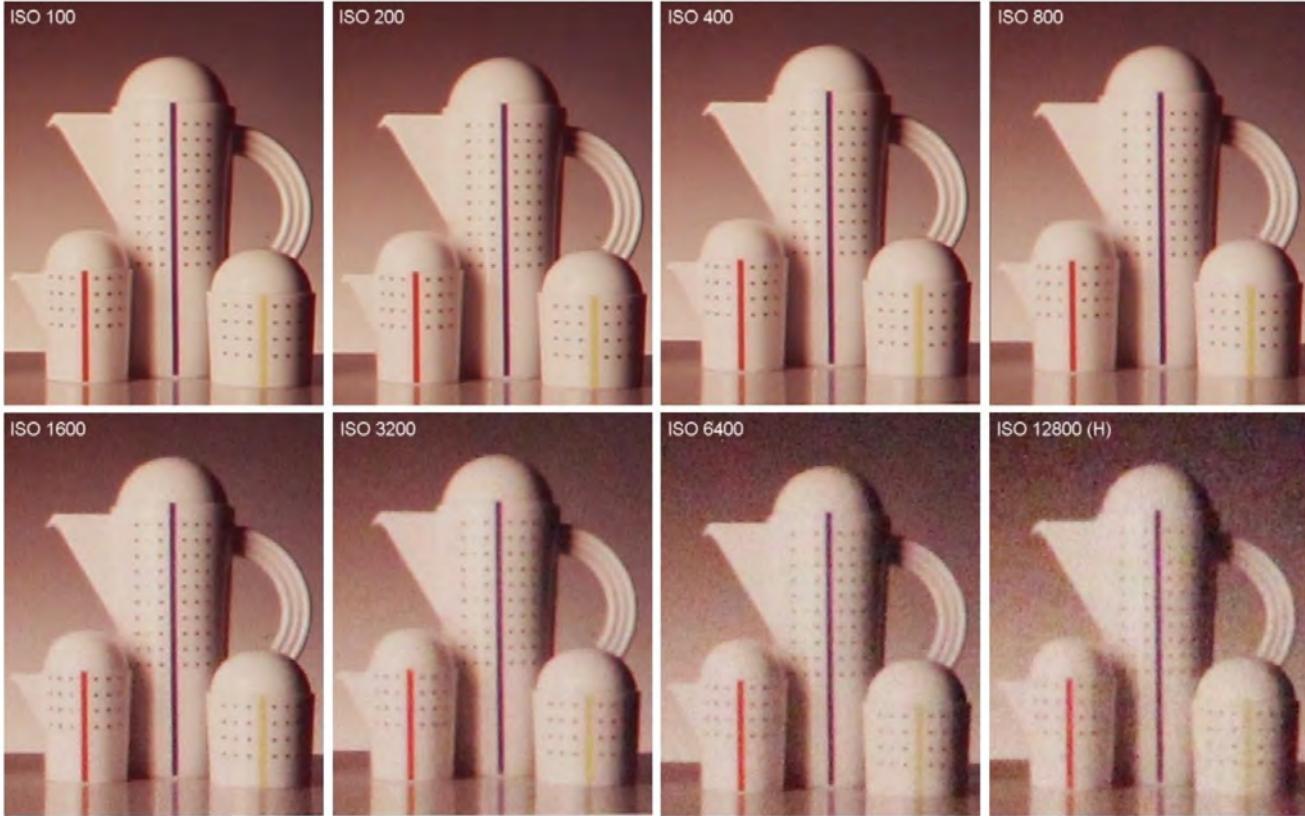


Image becomes very grainy because noise is amplified.

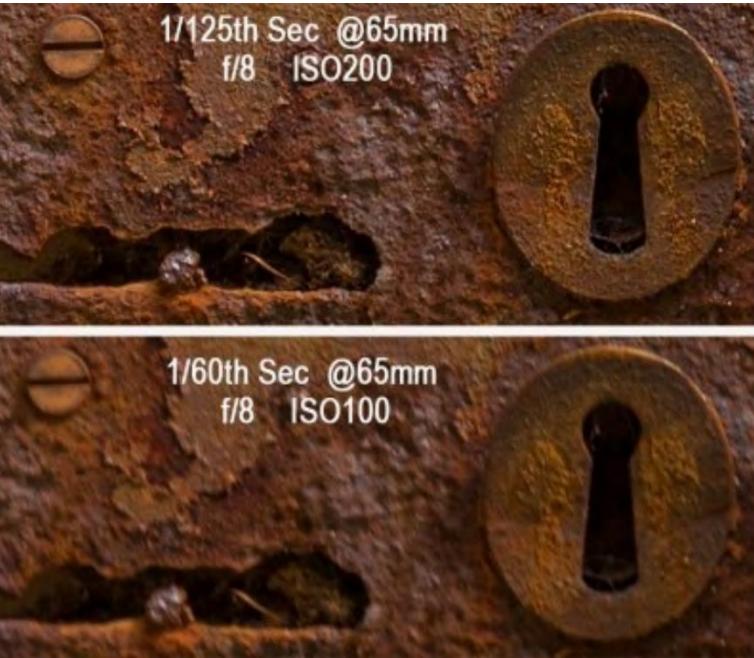


Shutters: Physical

Nikon D3s

Main Side Effect of Shutter Speed

Motion blur: handshake, subject movement
Doubling shutter time doubles motion blur



Gavin Hoey

<http://www.gavtrain.com/?p=3960>



Main Side Effect of Shutter Speed

Motion blur: handshake, subject movement
Doubling shutter time doubles motion blur

Slow shutter speed



Fast shutter speed



London

Electronic Shutter

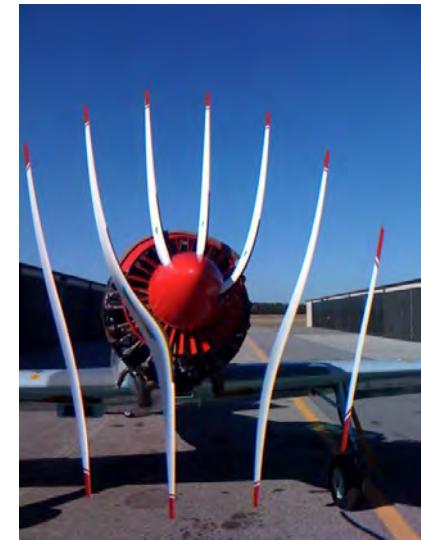
- Pixel is electronically reset to start exposure
- Fills with photoelectrons as light falls on sensor
- Reading out pixel electronically “ends” exposure
- Problem: most sensors read out pixels sequentially, takes time (e.g. 1/30 sec) to read entire sensor
 - If reset all pixels at the same time, last pixel read out will have longer exposure
 - So, usually stagger reset of pixels to ensure uniform exposure time
 - Problem: rolling shutter artifact



Electronic Rolling Shutter



Credit: David Adler, B&H Photo Video
<https://www.bhphotovideo.com/explora/video/tips-and-solutions/rolling-shutter-versus-global-shutter>



Credit: Soren Ragsdale
<https://flic.kr/p/5S6rKw>



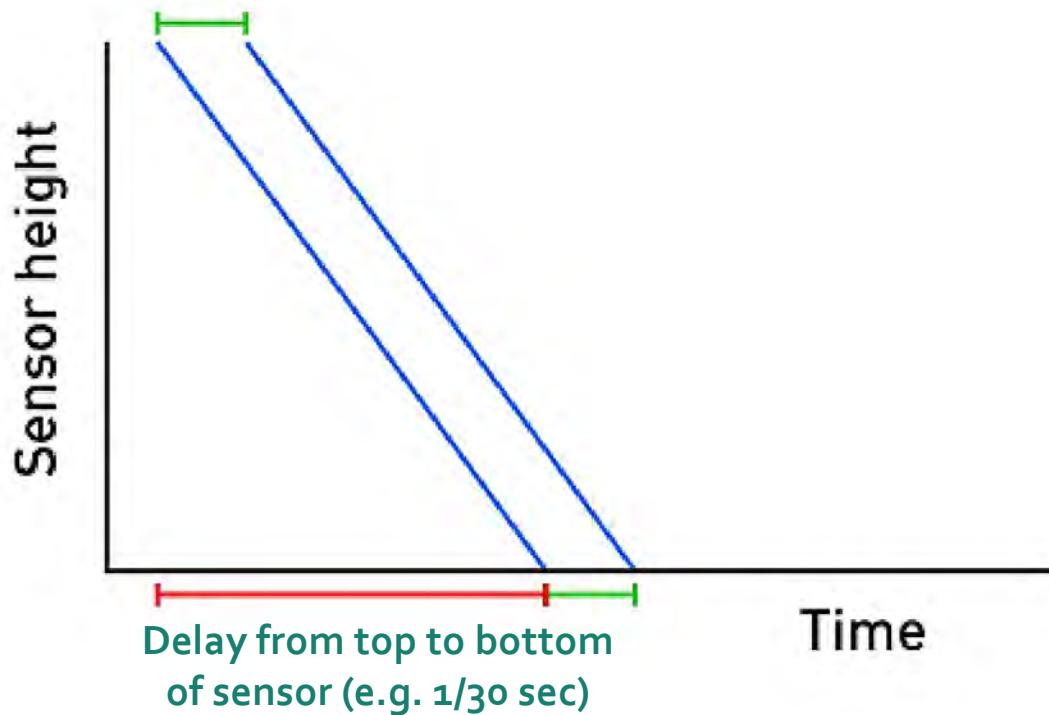
Electronic Rolling Shutter



The Slow Mo Guys, <https://youtu.be/CmjeCchGRQo>



Electronic Rolling Shutter



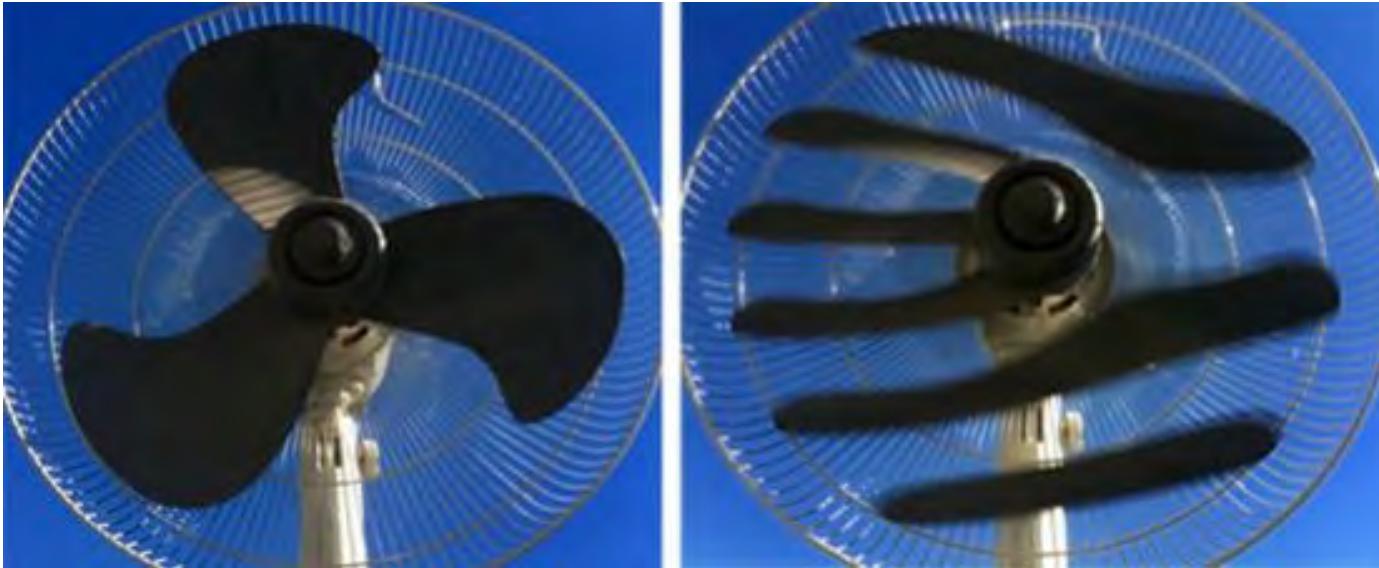


Focal Plane Shutter (Fast Exposures)

Nikon D3s



Global Shutter vs. Rolling Shutter

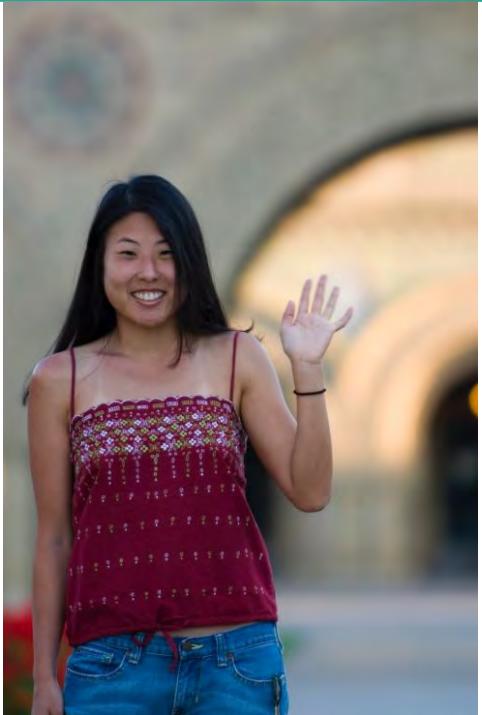


All sensor pixels exposed at
same time

Row-by-row readout of image
➤ shorter exposure times per pixel
➤ motion artifacts



Exposure Tradeoffs: Depth of Field vs Motion Blur



$f/4$
 $1/125$ sec



$f/11$
 $1/15$ sec



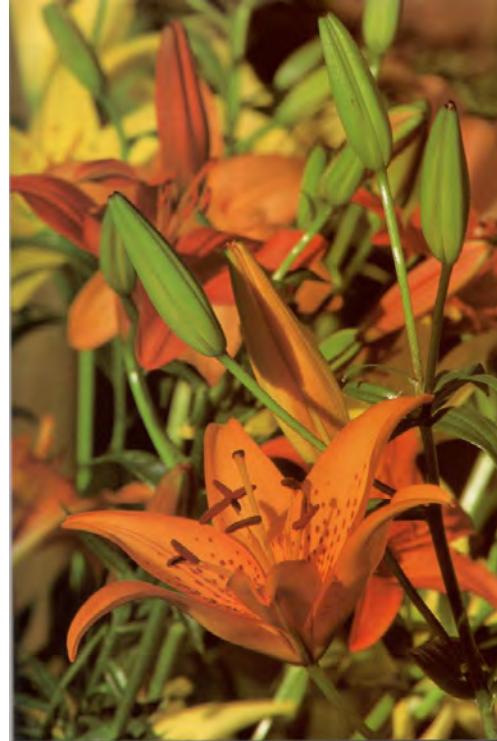
$f/32$
 $1/2$ sec

Photographers must trade off depth of field
and motion blur for moving subjects



Exposure Tradeoffs: Depth of Field vs Motion Blur

Shallow Depth of Field Can Create a Stronger Image

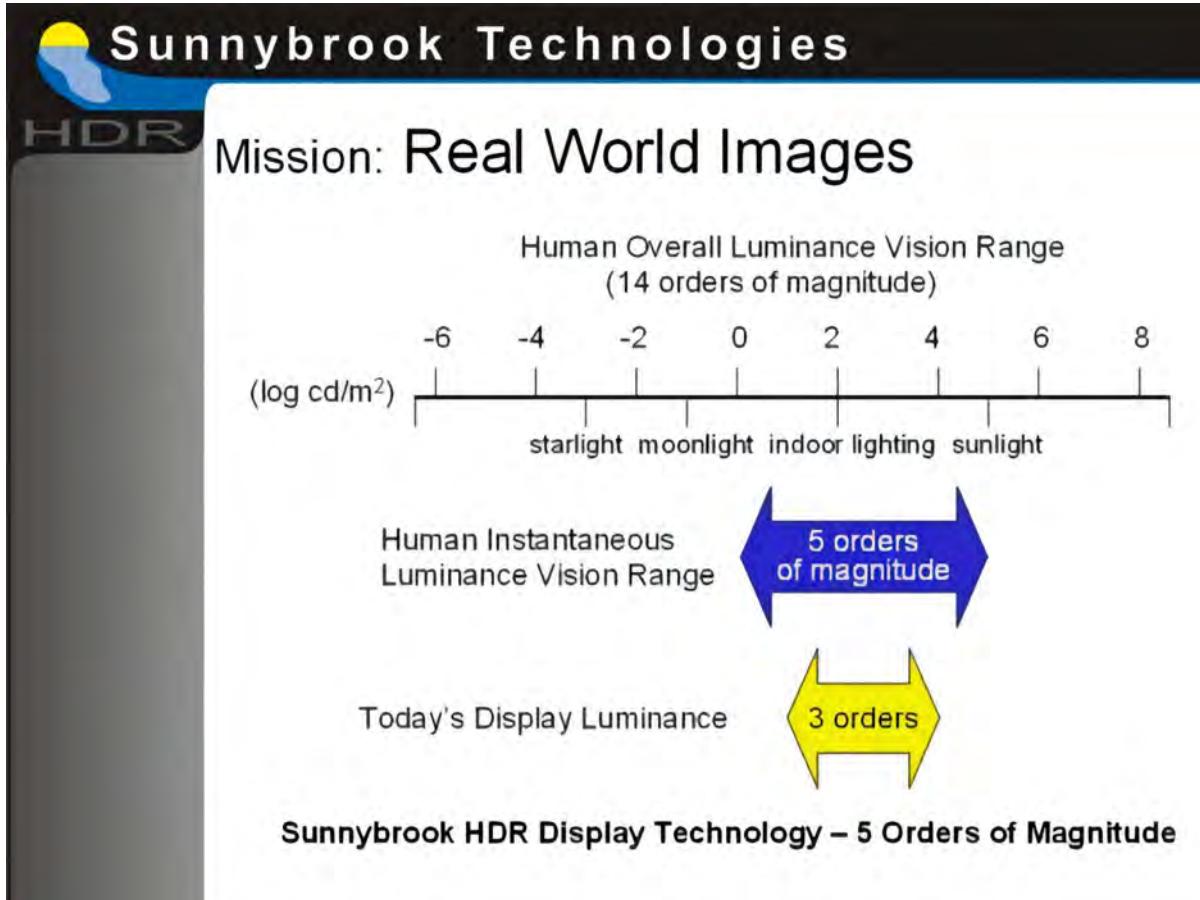


From Peterson, Understanding Exposure
zoommm, f/4, 1/1000 (left) and f/11, 1/125 (right)

Dynamic Range

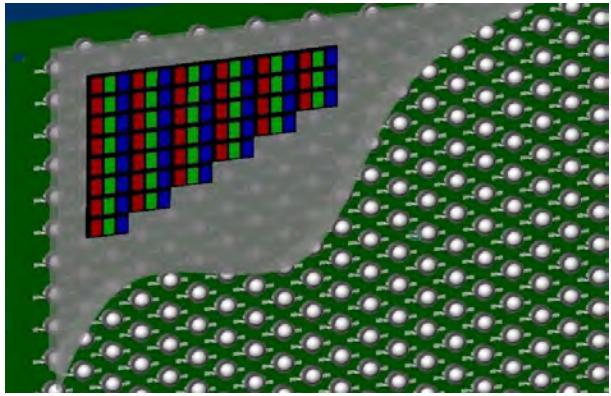


Dynamic Range





High Dynamic Range Displays



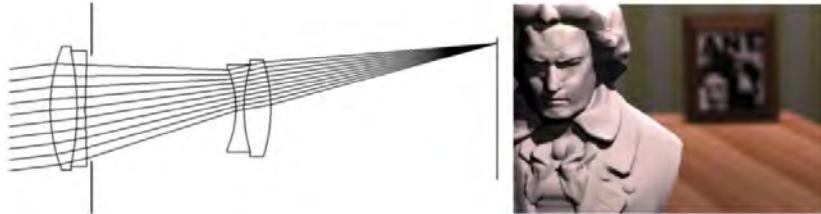
- Low Resolution LED Array
 - About 1000-2000 LEDs
- Conventional LCD
- Diffusion Optics

Wolfgang Heidrich [BrightSite Technology]

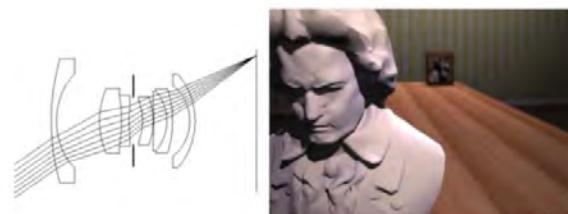
Ray Tracing Real Lens



Ray Tracing Through Real Lens Designs



200 mm telephoto



35 mm wide-angle



50 mm telephoto



16 mm fisheye

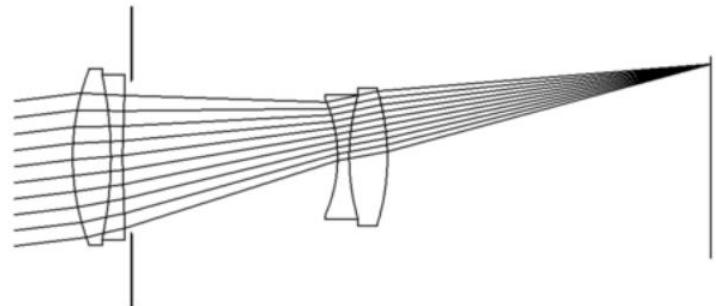
From Kolb, Mitchell and Hanrahan (1995)



Ray Tracing Through Real Lens Designs



200 mm telephoto



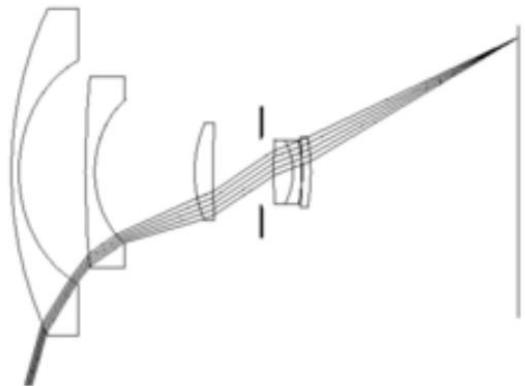
Notice shallow depth of field (out of focus background)



Ray Tracing Through Real Lens Designs



16 mm fisheye



Notice distortion in the corners (straight lines become curved)



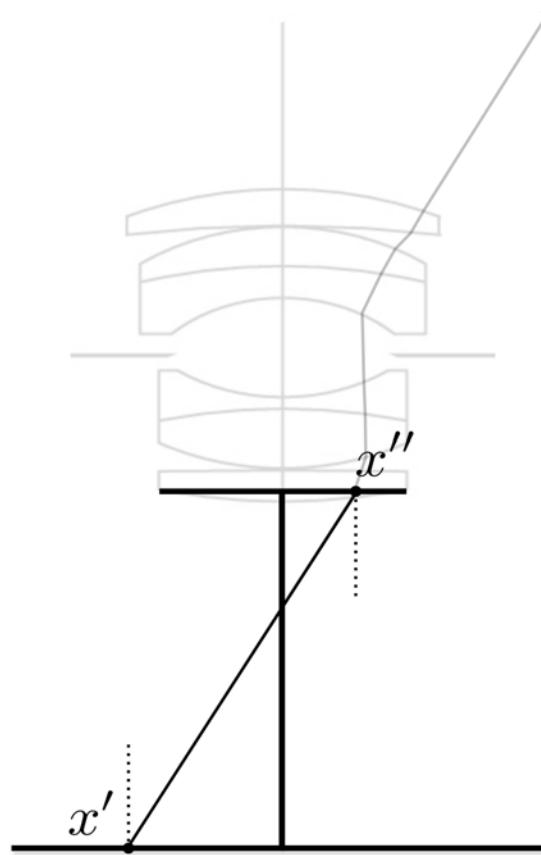
Ray Tracing Real Lens Designs

Monte Carlo approach

- At every sensor pixel, compute integral of rays incident on pixel area arriving from all paths through the lens

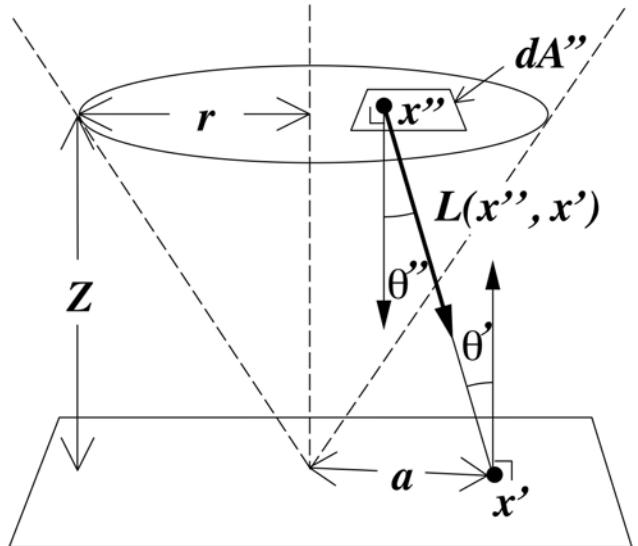
Algorithm (for a pixel)

- Choose N random positions in pixel
- For each position x' , choose a random position o the back element of the lens x''
- Trace a ray through from x' to x'' , trace refractions through lens elements until it misses the next element (kill ray) or exits the lens (path trace through the scene)
- Weight each ray according to radiometric calculation on next slide to estimate irradiance $E(x')$





Radiometry for Tracing Lens Designs



Back element of lens

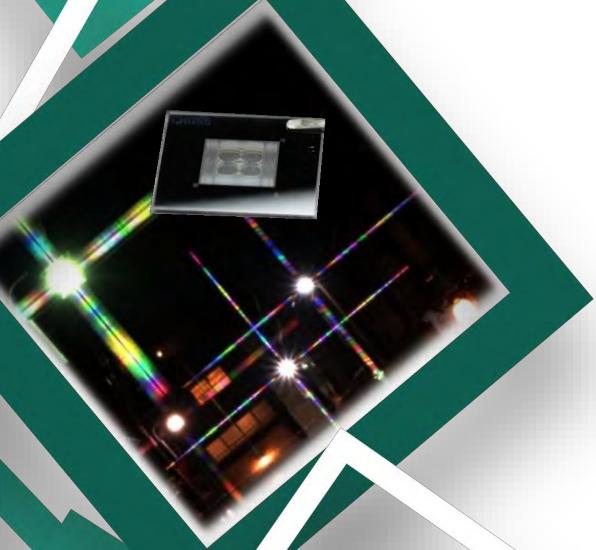
Sensor Plane

$$\begin{aligned} E(x') &= \int_{x'' \in D} L(x'' \rightarrow x') \frac{\cos \theta' \cos \theta''}{||x'' - x'||^2} dA'' \\ &= \frac{1}{Z^2} \int_{x'' \in D} L(x'' \rightarrow x') \cos^4 \theta dA'' \end{aligned}$$



Todays Topic

- Introduction
- Imaging Optics
- Aperture
- Depth of Field
- Field of View
- Tips for Photography
- Diffraction Limit
- Sensors
- Exposure
- Ray Tracing Thin Lens
- Ray Tracing Real Lens
- Noise



GAMES 204



Thank You!



Qilin Sun (孙启霖)

香港中文大学（深圳）

点昀技术 (Point Spread Technology)