CR<sub>3</sub> ( r(iR<sub>1</sub>,iR<sub>2</sub>), f(i<sub>1</sub>, i<sub>2</sub>), F ), iR<sub>1</sub> = i<sub>1</sub> 
$$\wedge$$
 iR<sub>2</sub> = i<sub>2</sub>, f' =inv17(i<sub>2</sub>) have CR<sub>3</sub> ...proof ( cut\_tac a1 a2 b1, simp, rule\_tac x =inv17(i<sub>2</sub>) in exl, auto ) qed ...}

CR<sub>3</sub> ( r(iR<sub>1</sub>,iR<sub>2</sub>), f(i<sub>1</sub>, i<sub>2</sub>), F ), iR<sub>1</sub> = i<sub>1</sub>  $\wedge$   $\wedge$   $^2$ <sub>j=1</sub> iR<sub>2</sub>  $\neq$  i<sub>j</sub>  $\wedge$  have CR<sub>3</sub> ...proof ( cut\_tac a1 a2 b1, simp, rule\_tac x =inv17(i<sub>2</sub>) in exl, auto ) qed ...}

CR<sub>2</sub> ( r(iR<sub>1</sub>,iR<sub>2</sub>), f(i<sub>1</sub>, i<sub>2</sub>), F ),  $\wedge$   $^2$ <sub>j=1</sub> iR<sub>1</sub> $\neq$  i<sub>j</sub>  $\wedge$   $\wedge$   $^2$ <sub>j=1</sub> iR<sub>2</sub> $\neq$  i<sub>j</sub> moreover{ assume b1 : iR<sub>1</sub> = i<sub>1</sub>  $\wedge$   $\wedge$   $^2$ <sub>j=1</sub> iR<sub>2</sub> $\neq$  i<sub>j</sub> have CR<sub>3</sub> ...proof ( cut\_tac a1 a2 b1, simp, rule\_tac x =inv17(i<sub>2</sub>) in exl, auto ) qed ...}

CR<sub>2</sub> ( r(iR<sub>1</sub>,iR<sub>2</sub>), f(i<sub>1</sub>, i<sub>2</sub>), F ),  $\wedge$   $\wedge$   $\wedge$   $\wedge$  i=1 iR<sub>1</sub> $\neq$  i<sub>j</sub>  $\wedge$   $\wedge$   $\wedge$  i=1 iR<sub>2</sub> $\neq$  i<sub>j</sub> moreover{ assume b1 :  $\wedge$   $\wedge$  i=1 iR<sub>1</sub> $\neq$  i<sub>j</sub>  $\wedge$   $\wedge$  i=1 iR<sub>2</sub> $\neq$  i<sub>j</sub> moreover{ assume b1 :  $\wedge$  i=1 iR<sub>1</sub> $\neq$  i<sub>j</sub>  $\wedge$   $\wedge$  i=1 iR<sub>2</sub> $\neq$  i<sub>j</sub>

have CR<sub>2</sub> ...proof (cut tac a1 a2 b1, auto) ged ...}