Baby Rudin 3rd Ed

November 25, 2013

Chapter 1

1.1

- (+): Take $r = \frac{a}{b}$ so $r + x = \frac{a}{b} + x = \frac{y}{z} \implies x = \frac{y}{z} \frac{a}{b} = \frac{by az}{bz}$ and x must be rational (*): Take $r = \frac{a}{b}$ so $rx = \frac{xa}{b} = \frac{y}{z} \implies x = \frac{by}{az}$ and x must be rational

1.2

Notice this problem reduces to proving the irrationality of $\sqrt{3}$ Take a, b to be coprime integers, $b \neq 0 \implies \frac{a^2}{b^2} = 3 \implies a^2 = 3b^2$ a, b must be odd, since they would not be coprime otherwise. Now take a = 2i + 1; b = 2n + 1; $i \neq n \implies (2i + 1)^2 = 3(2n + 1)^2 \implies 4i^2 + 4i + 1 = 12n^2 + 12n + 3 \implies 2(i^2 + i) = 2(3n^2 + 3n) + 1$ Since the i terms describe an even integer, and the n terms describe an odd integer, it is impossible to choose i, n such that $a^2 = 3b^2$

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