

Y	E	$12C_5$	$12C_5^2$	$15C_2$	$20C_3$
A	1	1	1	1	1
$\Rightarrow T_1$	3				
$T_2$	3				
H	4				
$\Rightarrow \textcircled{5}$	5				

$$1^2 + 3^2 + 3^2 + 4^2 + 5^2 = \overset{10}{1+9} + \overset{25}{9+16+25} = 60$$

↓ ↓

$$SO(3) \quad l = 0, 1, 2, 3, \dots, \infty$$

$$\rightarrow l \leq m \leq l \quad v = 1, 3, 5, 7, \dots$$

$$v = 2l + 1$$

$$C(\varphi) \quad T_l(\varphi) = \begin{pmatrix} e^{il\varphi} & & & 0 \\ & e^{i(l-1)\varphi} & & \\ & & \ddots & \\ 0 & & & e^{-il\varphi} \end{pmatrix}$$

$$\chi_l(\varphi) = \sum_{m=-l}^l e^{im\varphi} =$$

$$= \frac{e^{i(l+1)\varphi} - e^{-il\varphi}}{e^{i\varphi} - 1} \cdot \frac{e^{-i\varphi/2}}{e^{-i\varphi/2}} =$$

$$= \frac{e^{i(l+1/2)\varphi} - e^{-i(l+1/2)\varphi}}{e^{i\varphi/2} - e^{-i\varphi/2}} = \frac{\sin\left(\frac{2l+1}{2}\varphi\right)}{\sin\varphi/2}$$

$$\chi_0(\varphi) = 1$$



$$T_3(\phi) = \begin{pmatrix} e^{i3\phi} & & & \\ & e^{i2\phi} & & \\ & & e^{i\phi} & \\ & & & 1 \\ & & & & e^{-i\phi} \\ & & & & & e^{-i2\phi} \\ & & & & & & e^{-i3\phi} \end{pmatrix}$$

4

