

CS161 WEEK2 DISCUSSION 1C

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Contributed by Yewen W' and Shirley C's previous course materials

Agenda

SEARCH PROBLEM FORMULATION

DFS & BFS

Search Problem

5 KEY ELEMENTS

Initial state

State space

Actions

Successor function $F(\text{cur_state}, \text{action}) = \text{next_state}$

Goal test

Search Problem

EXAMPLE: EIGHT QUEENS

Initial State: Empty board
($0 \rightarrow 8$)
↓

State Space: All arrangements of 8 queens

Actions: Put a queen on the board

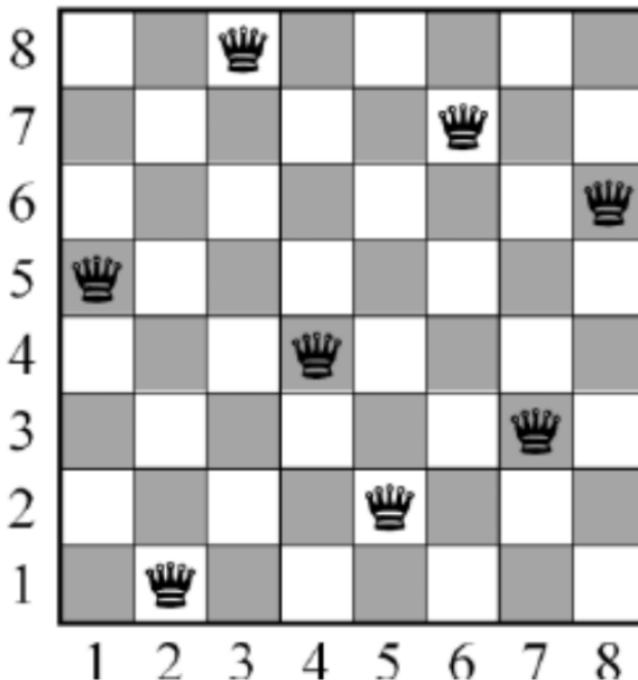
Successor function: The arrangement after putting

Goal test: whether current the new queen arrangement meets the conditions

Number of cases in total:

$$\underline{64 \times 63 \dots \times 57}$$

Action: Put a queen on a new row
 $8 \times 7 \times 6 \times \dots \times 1$



Search Problem

PRACTICE

Drive from CA to DC

Initial state: CA

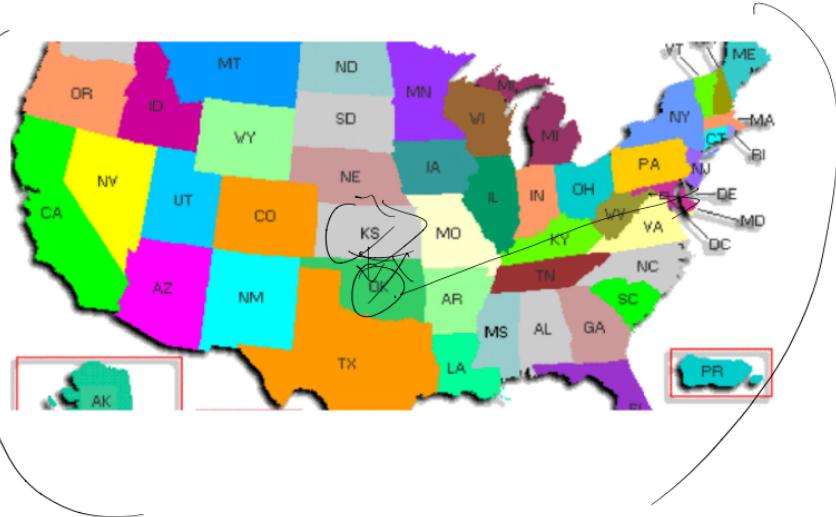
Actions: Move to a neighboring state
(four-state, drive)

Successor function:

Goal test: DC ?

cost/purpose = # state

= gasoline



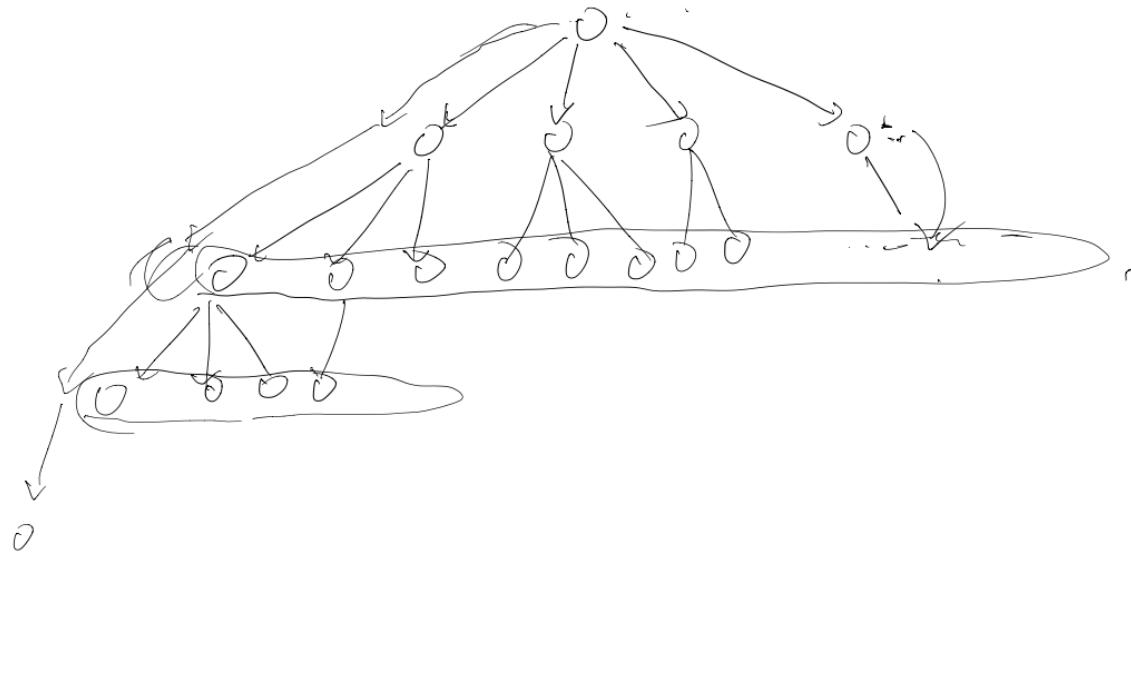
Search Problem

INFORMED VS UNINFORMED

Whether we have information on our goal state that helps our decision making

We know the dist from cur state to DC.

DFS & BFS



DFS & BFS

4 EVALUATORS

REFRESH YOUR MEMORY

	BFS	DFS	Limited DFS
Complete	Y	N	N
Optimal	Y	N	N
Time complexity	$O(b^d)$	$O(b^m)$	$O(b^l)$
Space complexity	$O(b^d)$	$O(b^m)$	$O(b^l)$

cost is uniform
if no infinite loops

limited depth = l

branching factor : b
depth : d
max-depth : m

Practice

ROTTING ORANGES

You are given an $m \times n$ grid where each cell can have one of three values:

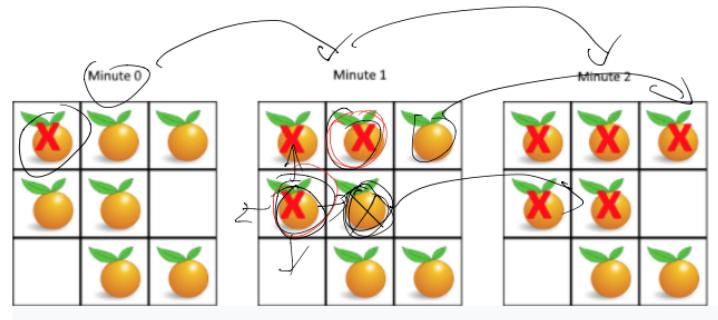
0 representing an empty cell,

1 representing a fresh orange, or

2 representing a rotten orange.

Every minute, any fresh orange that is **4-directionally adjacent** to a rotten orange becomes rotten.

Return *the minimum number of minutes that must elapse until no cell has a fresh orange*. If this is impossible, return -1.



Practice

- BFS or DFS?
- Divide the whole programs into parts

What functions do we need?

- Initial state
 - Get the loc of rotten oranges
 - Expand
 - Check
- Repeat until no further expansion

① Get all rotten oranges (state)

② Know the neighbors, expand (action)

③ How many total oranges (test)

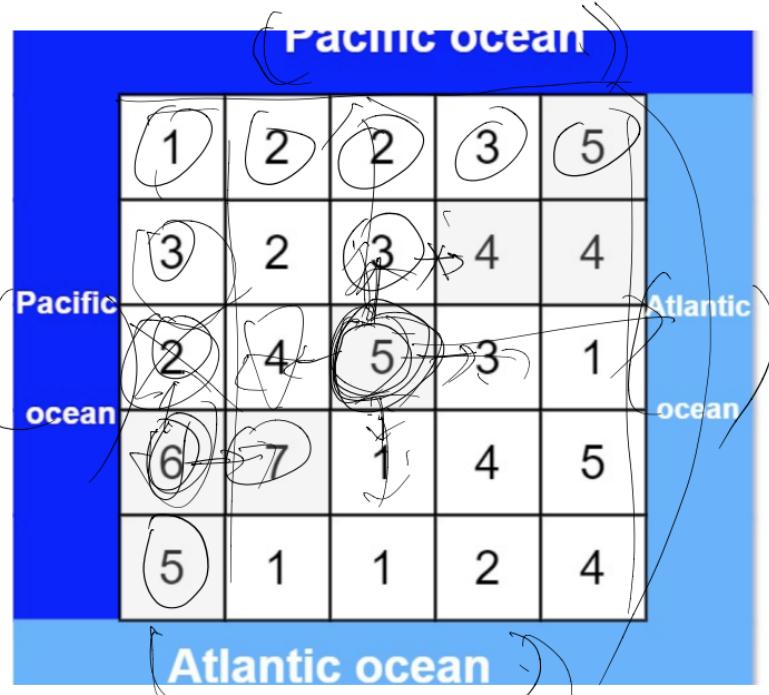
Practice

PACIFIC ATLANTIC WATER FLOW

You are given an $[m \times n]$ integer matrix heights representing the height of each unit cell in a continent. The **Pacific ocean** touches the continent's left and top edges, and the **Atlantic ocean** touches the continent's right and bottom edges.

Water can only flow in four directions: up, down, left, and right. Water flows from a cell to an adjacent one with an equal or lower height.

Return a *list of grid coordinates where water can flow to both the Pacific and Atlantic oceans.*



Practice

PACIFIC ATLANTIC WATER FLOW

start at a loc x_i, y_i

explore its neighbors

if moveable, then (x_n, y_n)
test

- ① keep tracking of test
- ② keep tracking of visited pts

Start from a loc near Pacific

Search 4 directions

If it can be a source of water, update cur loc

Do it again for Atlantic

Intersection

Homework1

- TREE-CONTAINS
 - Recursively check whether $(\text{car lst}) = x$
- TREE-MIN
 - Recursion again
 - If only has 1 element, return that element
 - Otherwise return the minimum of $\text{TREE-MIN}((\text{car lst}))$ and $\text{TREE-MIN}((\text{cdr lst}))$
 - But it is an ordered tree!
 - So we only need to look at the most left
 - $(\text{car} (\text{car} (\text{car} \dots)))$ until single atom

Homework1

- TREE-ORDER
 - Recursion.
 - If only 1 element, returns it
 - If 3 element, concatenate 3 parts.
 - [element2 (TREE-ORDER element1) (TREE-ORDER element3)]
 - Be clear of the argument format

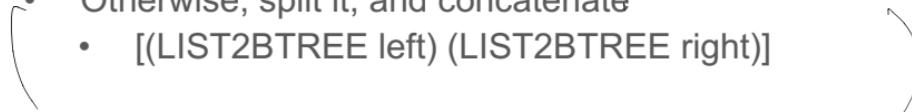
- SUB-LIST
 - Recursion
 - if LEN=0: nil
 - if START=0, and LEN!=0: (cons (car lst) (SUB-LIST lst START (- LEN 1)))
 - Otherwise: (SUB-LIST (cdr lst) (- START 1) LEN)

Homework1

- SPLIT
 - Super easy if you know the length. *use sub-list*
- BTREE-HEIGHT
 - Recursion
 - If only one atom: return 0
 - Otherwise: return $1 + \max(\text{left height}, \text{right height})$

Homework1

- LIST2BTREE
 - If only one element, return it
 - Otherwise, split it, and concatenate
 - [(LIST2BTREE left) (LIST2BTREE right)]



Q&A
