About this document

This is the assignment for the UCL CASA module Data Science for Spatial Systems (CASA0006)

This is a self contained Jupyter notebook with structure introduction, discussion and embeded code and bibliography.

Code is hosted here Data is availble here

Assessment of the relationship between the London Index of Multiple Deprivation and the incidence of various types of crime

the case of the London

This study aims to explore how the dimensions in the IMD predict or influence crime rates across London boroughs, with a particular focus on the Violence Against the Person typology. The research will identify which socio-economic factors are most relevant to increases or decreases in crime rates by analysing the relationship between IMD scores and crime incidence in different boroughs.

| 1.0 Intro | 2.0 Lit. review | 3.0 Method | 4.0 Data | 5.0 Explore | 6.0 Analysis | 7.0 Discussion and conclusion | Bibliography

1.0 | Introduction

In recent years, extensive research has been conducted on the relationship between urban crime and social deprivation. This connection is particularly scrutinized in major cities like London, where the link between criminal activity and social deprivation draws significant attention. Against this backdrop, this paper aims to explore the relationship between the 2019 London Index of Multiple Deprivation (IMD) and various categories of crime data, utilizing regression analysis and machine learning models (ridge regression and random forest) to parse their correlation and evaluate the performance of different models. This study examines how socio-economic factors measured by the IMD influence the overall crime rate across the city.

Utilizing open datasets from government databases, this research applies statistical methods to analyze the correlation and predictive power of IMD scores with crime incidence rates. The paper proposes the use of regression and predictive modeling techniques to analyze the relationship between the Index of Multiple Deprivation and crime. The results of this study could significantly enhance public safety strategies by precisely identifying the specific socioeconomic factors that predict crime. By improving our understanding of these relationships, policymakers can devise more effective intervention measures aimed at mitigating crime in high-risk areas.

1.1 | Requirements to run the analysis

An overview of packages used to run the analysis with brief explanation of their role.

```
In [1]: # Data Manipulation and General Purpose Libraries
        # Visualization Libraries
        import matplotlib.pyplot as plt
        import numpy as np
        # Importing necessary libraries
        import pandas as pd
        import seaborn as sns
        # Regression Models
        import statsmodels.api as sm
        # Statistical Testing
        from scipy.stats import pearsonr, spearmanr
        from sklearn.ensemble import RandomForestRegressor
        # Advanced Machine Learning - Feature Importance
        from sklearn.inspection import permutation importance
        # Ridge Regression Specific
        from sklearn.linear_model import LinearRegression, Ridge
        # Model Evaluation Metrics
        from sklearn.metrics import mean_absolute_error, mean_squared_error, r2_score
        # Model Preparation and Optimization
        from sklearn.model_selection import (
            GridSearchCV,
            KFold,
            cross val score,
            train_test_split,
        from sklearn.preprocessing import StandardScaler
        from statsmodels.regression.linear_model import OLS
        from statsmodels.stats.outliers_influence import variance_inflation_factor
        from statsmodels.tools.tools import add constant
        from tensorflow.keras.layers import Dense
        # Advanced Machine Learning - Neural Networks
        from tensorflow.keras.models import Sequential
```

```
2024-04-29 16:35:59.415176: I external/local_tsl/tsl/cuda/cudart_stub.cc:32] Coul d not find cuda drivers on your machine, GPU will not be used.
2024-04-29 16:35:59.423374: I external/local_tsl/tsl/cuda/cudart_stub.cc:32] Coul d not find cuda drivers on your machine, GPU will not be used.
2024-04-29 16:35:59.486486: I tensorflow/core/platform/cpu_feature_guard.cc:210] This TensorFlow binary is optimized to use available CPU instructions in performa nce-critical operations.
To enable the following instructions: AVX2 FMA, in other operations, rebuild Tens orFlow with the appropriate compiler flags.
2024-04-29 16:36:00.943256: W tensorflow/compiler/tf2tensorrt/utils/py_utils.cc:38] TF-TRT Warning: Could not find TensorRT
```

2.0 | Literature review

Literature

Criminological theory and empirical studies consistently show that socioeconomic factors significantly influence crime rates (Cohn, Coccia and Kakar, 2021). Factors such as economic instability, inadequate educational opportunities, high unemployment and housing problems are widely recognised as key drivers of criminal behaviour (Savolainen et al., 2013; Carr, Marie and Vujić, 2023).

The Index of Multiple Deprivation (IMD) is a composite indicator used to assess levels of social and economic deprivation in each region of the UK (Deas et al., 2003). It includes aspects of income, employment, health, education, housing and the environment, making it an important tool for assessing the wellbeing of communities and potential risk of crime (Wikstrom and Butterworth, 2006; Tan and Haining, 2009; Exeter et al., 2017). Research has shown that areas with higher IMD scores typically have higher crime rates. For example, lower levels of education and high unemployment are directly associated with higher rates of violent and property crime. Additionally, poor health is strongly associated with drug-related crime (Tarling and Dennis, 2016).

In recent years, researchers have begun to use statistical and machine learning models to predict crime rates (McClendon and Meghanathan, 2015). Models such as Random Forests, Support Vector Machines and Neural Networks have been used to predict the incidence of crime in specific areas, often using historical data for training and validation (Safat, Asghar and Gillani, 2021). While many studies have explored the relationship between socio-economic indicators and crime, research on the links between specific types of crime (e.g. cybercrime, domestic violence) and IMD dimensions remains limited (Safat, Asghar and Gillani, 2021).

This study investigates how the Index of Multiple Deprivation (IMD) in London impacts various types of crime and identifies which indices have the most significant effects. By analyzing the 2019 crime data and IMD, it explores which deprivation indices most profoundly influence crime rates. The research also compares the performance of ridge regression and random forest models, assessing their strengths and weaknesses in interpreting crime data to predict future crime occurrences.

RQ1 | Based on London Which IMD dimensions have significant correlations with specific offence types?

RQ2 | How can IMD dimensions be used to predict the incidence of crime?

To address this issue, this paper uses regression analysis and machine learning models to develop predictive models. Regression analysis will be used to explain the correlation between the Index of Multiple Deprivation (IMD) and various types of crime, while ridge regression and random forests will be used to predict crime rates and assess the performance of the models.

3.0 | Methodology

Correlation analysis Pearson's correlation coefficient was used to assess the strength and direction of the linear relationship between two quantitative variables, which is suitable for situations where the data are assumed to be normally distributed and the relationship is linear. In addition, the Spearman rank correlation coefficient was used, which is a non-parametric method for assessing the correlation between the ranks of two variables, and is particularly suitable for situations where the data distribution does not conform to normal distribution or where the relationship between the variables is likely to be non-linear. In order to determine whether the observed correlation is statistically significant, a significance test was conducted to test whether the correlation may be due to chance alone by calculating a p-value. The level of significance is usually set at 0.05 or 0.01. With these tests, we can more accurately determine whether the correlation between variables is significant or not, enhancing the reliability and explanatory power of the findings. (Y).

Regression Analysis In our regression analysis, a multiple linear regression model was first used to explore the linear relationship between multiple independent variables and a dependent variable. The method assumes that the relationship between the variables is linear and that the error terms are normally distributed with independent homogeneous distributions. We assessed the model fit and the significance of the variables through the adjusted R^2 values and F-statistics. We further applied a ridge regression model for the presence of high covariance between variables. Ridge regression effectively reduces the instability of the regression coefficients by introducing the **ridge parameter** (λ) as a penalty term, thus reducing the risk of overfitting the model. We selected the optimal ridge parameters by the cross-validation method to balance the explanatory power and predictive accuracy of the model. The performance of the model is finally assessed by the mean square error (MSE) and the adjusted and adjusted R^2 values, which ensures analytical rigour and reliability of the results.

Predictive Modelling In our machine learning study, we chose to use ridge regression and random forest model models, whose predictive accuracy and

model stability are improved by constructing multiple decision trees and aggregating their results, suitable for dealing with classification and regression problems on large-scale datasets. Each decision tree is trained on a randomly selected subsample of data and feature set, a strategy that effectively reduces overfitting while improving model performance on unseen data. We assess model performance through cross-validation and a range of metrics such as accuracy, recall and F1 scores to ensure analytical rigour and reliability of results.*

ity of later parts.

4.0 | Data preparation

Multiple Deprivation Index (MDI) data for 2019 The Multiple Deprivation Index (MDI) is commonly used to measure the level of socio-economic deprivation in an area. This index integrates multiple dimensions such as education, health, income and living conditions to assess the state of socio-economic deprivation of an area's residents relative to other areas. The original dataset is the 2019 Index of Multiple Deprivation data for England. The code below begins by collating and summarising the available data. Multiple Deprivation Index score datasets are typically formatted to include geographic identifiers (e.g. postcode or area code), deprivation scores and rankings for each area, demographic information, and other relevant socio-economic indicators (e.g. unemployment, average income, educational attainment and health status). The deprivation indices are first filtered to produce a breakdown of the scores for each category and stored in the imd_data database, the analysis for this project focuses on the London region dataset but the full dataset can be downloaded here.

LONDON CRIME DATA This dataset, provided by the Metropolitan Police, provides an exhaustive record of crime in the London area, meticulously disaggregated at different geographic levels (Boroughs, Districts, LSOAs). This geographical breakdown allows for accurate spatial analysis of crime data, helping to understand the security situation in different areas. The dataset is categorised by crime type, month and three different geographical levels (Borough, District, LSOA). The data is split into two types: one includes the most recent data for the last 24 months and the other contains all historical data from 2008 onwards. From March 2019, the data is organised according to the updated Home Office Crime Classification (HOC), which provides a detailed breakdown of crime categories, including arson, burglary, drug offences, and many other specialised and subspecialised classifications. The MPS LSOA Level Crime (Historical).csv dataset was selected for this project, and the 2019 crime data was filtered and statistically classified for each category of crime at the data processing stage.data

Study variables:

Index of Multiple Deprivation:

- IMDScore: The overall Index of Multiple Deprivation composite score, which summarises information from all of the individual indicators below.
- IncScore: Income score, reflecting the extent to which people in the community have low incomes.
- EmpScore: Employment score, which measures the extent of unemployment and low employment in the community.
- EduScore: Education, Skills and Training Score, indicative of educational attainment and skills development within the community.
- HDDScore: Health Deprivation and Disability Score, assessing the rate of health problems and disability within the community.
- CriScore: Crime Score, reflecting crime rates and policing in the community.
- BHSScore: Barriers to Housing and Services Score, which measures how easy it is for people in the community to access housing and services.
- EnvScore: Living Environment Score, which evaluates the environmental quality of the community, such as air pollution and housing conditions.
- IDCScore: Child Deprivation Index Score, which looks at the deprivations faced by children.
- IDOScore: Older people's deprivation index score, which assesses the deprivation faced by the older population.
- CYPScore: Children and Young People's Deprivation Score, focussing on deprivation faced by young people.
- ASScore: Adult Skills Deprivation Score, which measures deprivation of adult skill levels and qualifications.
- GBScore: Geographic Barriers Score, which evaluates the impact of geography on the daily lives of people in the community.
- WBScore: Broadband Connectivity Score, which measures the problems that communities may experience in accessing broadband services.
- IndScore: Industrial Deprivation and Unemployment Score, which captures the impact of industrial structure and unemployment on the community.
- OutScore: Outdoor Space Score, which relates to the ability of community residents to access green spaces and recreational spaces.

Crime type:

- Miscellaneous Crimes Against Society
- Theft

- Vehicle Offences
- Public Order Offences
- Possession of Weapons
- Violence Against the Person
- Burglary
- Drug Offences
- Arson and Criminal Damage
- Robbery

4.1 | Load data

```
In [2]: # Read multiple deprivation index data
imd_data = pd.read_csv("data/IMD_2019.csv")
print("deprivation index data:")
print(imd_data.head())

# crime
crime_data = pd.read_csv("data/MPS LSOA Level Crime (Historical).csv")
print("\ncrime:")
print(crime_data.head())
```

```
deprivation index data:
   lsoa11cd
                              lsoa11nm
                                                        lsoal1nmw \
0 E01000001
                  City of London 001A
                                              City of London 001A
                   City of London 001B
                                              City of London 001B
1 E01000002
                   City of London 001C
                                              City of London 001C
2 E01000003
3 E01000005
                   City of London 001E
                                              City of London 001E
4 E01000006 Barking and Dagenham 016A Barking and Dagenham 016A
                  st_lengths IMD_Rank
                                        IMD_Decile
      st_areasha
0 133320.768872 2291.846072
                                 29199
                                 30379
1 226191.272990 2433.960112
                                                10
  57302.966538 1142.359799
                                 14915
                                                 5
3 190738.760504 2167.868343
                                 8678
                                                 3
4 144195.846857 1935.510354
                                 14486
                                                 5
                                                       LADnm ... IndRank ∖
                   LSOA01NM
                                 LADcd
0
         City of London 001A E09000001
                                              City of London
                                                                     16364
         City of London 001B E09000001
1
                                              City of London
                                                                     22676
                                                              . . .
2
        City of London 001C E09000001
                                              City of London
                                                                     17318
                                                              . . .
3
         City of London 001E E09000001
                                              City of London
                                                                     25218
4 Barking and Dagenham 016A E09000002 Barking and Dagenham ...
                                                                     14745
   IndDec OutScore OutRank OutDec TotPop DepChi
                                                     Pop16 59 Pop60+ \
0
       5
             1.503
                                       1296
                                                175
                                                                  465
                       1615
                                  1
                                                          656
       7
1
             1.196
                       2969
                                  1
                                       1156
                                                182
                                                          580
                                                                  394
2
            2.207
                        162
                                       1350
                                                          759
       6
                                  1
                                                146
                                                                  445
            1.769
3
       8
                        849
                                  1
                                       1121
                                                229
                                                          692
                                                                  200
                                       2040
4
       5
            0.969
                       4368
                                  2
                                                522
                                                         1297
                                                                  221
  WorkPop
  715.00
0
   619.75
1
2
  804.00
   683.00
4 1284.50
[5 rows x 63 columns]
crime:
   LSOA Code
                             LSOA Name
                                          Borough
                                                              Major Category
0 E01000006 Barking and Dagenham 016A E09000002 Arson and Criminal Damage
             Barking and Dagenham 016A E09000002 Arson and Criminal Damage
1 E01000006
2 E01000006
             Barking and Dagenham 016A
                                        E09000002
                                                                    Burglary
3 E01000006
             Barking and Dagenham 016A
                                        E09000002
                                                                    Burglary
4 E01000006 Barking and Dagenham 016A
                                        E09000002
                                                               Drug Offences
                   Minor Category 201903
                                           201904 201905
                                                           201906
                                                                   201907
0
                            Arson
                                        1
                                                0
                                                        0
                                                                0
                                                                        0
1
                  Criminal Damage
                                                2
                                                        0
                                                                1
                                                                        0
                                        1
   Burglary Business and Community
                                        0
                                                0
                                                        0
                                                                0
                                                                        0
3
                Domestic Burglary
                                                0
                                                        3
                                                                        0
                                        1
                                                                1
4
                 Drug Trafficking
                                                0
                                                        0
       202104
               202105
                       202106 202107
                                       202108
                                               202109 202110 202111
            0
                    0
                            0
                                    0
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0
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                    1
                            1
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                                            0
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1
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            0
2
                    0
                                    0
                                            0
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                                                            0
                                                                    0
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            0
                            1
3
   . . .
            0
                    0
                            0
                                    0
                                            0
                                                    0
                                                            1
                                                                    1
                    0
                            0
                                    0
                                            0
            0
                                                    0
  . . .
```

```
202112 202201
0 0 0
1 1 2
2 0 0
3 1 0
4 0 0
```

[5 rows x 147 columns]

4.2 | Data Cleaning

Geocodes and associated Index of Multiple Deprivation scores were screened in preparation for linking with London crime data via geocodes, at which point the geographic range of multiple deprivation was not yet screened

```
In [3]: columns_of_interest = [
            "lsoal1cd",
            "lsoal1nm",
            "IMDScore",
            "IncScore",
            "EmpScore",
            "EduScore",
            "HDDScore",
            "CriScore",
            "BHSScore",
            "EnvScore",
            "IDCScore",
            "IDOScore",
            "CYPScore",
            "ASScore",
            "GBScore",
            "WBScore",
            "IndScore",
             "OutScore",
        ]
        # filtering data
        imd_data = imd_data[columns_of_interest]
        imd_data.head()
```

```
Out[3]:
             Isoa11cd
                        Isoa11nm IMDScore IncScore EmpScore EduScore HDDScore C
                           City of
         0 E01000001
                          London
                                       6.208
                                                 0.007
                                                            0.010
                                                                       0.024
                                                                                  -1.654
                            001A
                           City of
         1 E01000002
                          London
                                       5.143
                                                 0.034
                                                            0.027
                                                                       0.063
                                                                                  -1.115
                             001B
                           City of
         2 E01000003
                                      19.402
                                                 0.086
                                                            0.086
                                                                       5.804
                                                                                  -0.102
                          London
                             001C
                           City of
         3 E01000005
                          London
                                      28.652
                                                 0.211
                                                            0.136
                                                                      22.260
                                                                                  -0.121
                             001E
                           Barking
                              and
         4 E01000006
                                                 0.117
                                                            0.059
                                                                      14.798
                                                                                  -0.359
                                      19.837
                        Dagenham
                            016A
In [4]:
        columns_of_interest = [
             "lsoal1cd",
             "lsoal1nm",
             "IMDScore",
             "IncScore",
             "EmpScore",
             "EduScore",
             "HDDScore",
             "CriScore",
             "BHSScore",
             "EnvScore",
            "IDCScore",
             "IDOScore",
             "CYPScore",
             "ASScore",
             "GBScore",
             "WBScore",
             "IndScore",
             "OutScore",
         ]
        imd_data = imd_data[columns_of_interest]
        imd_data.head()
```

	Isoa11cd	lsoa11nm	IMDScore	IncScore	EmpScore	EduScore	HDDScore	C
0	E01000001	City of London 001A	6.208	0.007	0.010	0.024	-1.654	
1	E01000002	City of London 001B	5.143	0.034	0.027	0.063	-1.115	
2	E01000003	City of London 001C	19.402	0.086	0.086	5.804	-0.102	
3	E01000005	City of London 001E	28.652	0.211	0.136	22.260	-0.121	
4	E01000006	Barking and Dagenham 016A	19.837	0.117	0.059	14.798	-0.359	

Out[4]:

对一个犯罪数据集进行处理和汇总,目的是筛选出感兴趣的列,计算年度犯罪总和,并重新组织数据以便于分析。首先,代码定义了一组感兴趣的列,包括地理代码、地名、主要犯罪类别和2019年各月的犯罪数据。

代码使用groupby()函数将数据按地理代码、地名和犯罪类别分组,并计算了这些分组的犯罪总和。

```
In [5]: columns_of_interest = [
            "LSOA Code",
            "LSOA Name",
            "Major Category",
            "201901",
            "201902",
            "201903",
            "201904",
            "201905",
            "201906",
            "201907",
            "201908",
            "201909",
            "201910",
             "201911",
            "201912",
        ]
        # filtering
        crime_data = crime_data[columns_of_interest]
        crime_data.head()
```

```
Out[5]:
                LSOA
                           LSOA
                                     Major
                                             201901 201902 201903 201904 201905 2
                Code
                           Name Category
                          Barking
                                      Arson
                             and
                                       and
                                                                    1
                                                                            0
                                                                                     0
        0 E01000006
                                                  0
                                                           0
                       Dagenham
                                    Criminal
                            016A
                                   Damage
                          Barking
                                      Arson
                             and
                                       and
        1 E01000006
                                                  1
                                                           0
                                                                    1
                                                                            2
                                                                                     0
                       Dagenham
                                    Criminal
                            016A
                                    Damage
                          Barking
                             and
                                                           0
                                                                   0
                                                                            0
                                                                                     0
        2 E01000006
                                                  0
                                   Burglary
                       Dagenham
                            016A
                          Barking
                             and
                                                                            0
        3 E01000006
                                   Burglary
                                                  2
                                                           0
                                                                    1
                                                                                     3
                       Dagenham
                            016A
                          Barking
                             and
                                      Drug
                                                  0
                                                           0
                                                                   0
                                                                            0
                                                                                     0
           E01000006
                       Dagenham
                                   Offences
                            016A
In [6]:
        monthly_columns = [
            "201901",
            "201902",
            "201903",
            "201904",
            "201905",
            "201906",
            "201907",
            "201908",
            "201909",
            "201910",
            "201911",
            "201912",
        ]
        # Calculate yearly totals for each row and create new column '2019'
        crime_data["2019"] = crime_data[monthly_columns].sum(axis=1)
        # The data containing the new totals column can now be viewed
        print(crime_data[["LSOA Code", "Major Category", "LSOA Name", "2019"]].head())
          LSOA Code
                                Major Category
                                                                LSOA Name
                                                                           2019
       0 E01000006 Arson and Criminal Damage Barking and Dagenham 016A
                                                                              1
       1 E01000006 Arson and Criminal Damage Barking and Dagenham 016A
                                                                              6
       2 E01000006
                                      Burglary Barking and Dagenham 016A
                                                                              0
       3
         E01000006
                                      Burglary Barking and Dagenham 016A
                                                                             13
       4 E01000006
                                 Drug Offences Barking and Dagenham 016A
                                                                              0
In [7]: # Define the month columns to be summarised
        months_columns = ["2019"]
        # groupby()
```

```
summary_data = crime_data.groupby(["LSOA Code", "LSOA Name", "Major Category"])[
    months_columns
].sum()

# Reset indexes so that grouped columns are also normal columns
summary_data.reset_index(inplace=True)

summary_data.head()
```

Out[7]:

	LSOA Code	LSOA Name	Major Category	2019
0	E01000006	Barking and Dagenham 016A	Arson and Criminal Damage	7
1	E01000006	Barking and Dagenham 016A	Burglary	13
2	E01000006	Barking and Dagenham 016A	Drug Offences	6
3	E01000006	Barking and Dagenham 016A	Miscellaneous Crimes Against Society	4
4	E01000006	Barking and Dagenham 016A	Possession of Weapons	0

The pivot_table() function was used to convert the data from a long format to a wide format, making each offence category a separate column and presenting the offence data for each geographic unit in a single row.

Out[8]:		LSOA Code	Arson and Criminal Damage	Burglary	Drug Offences	Miscellaneous Crimes Against Society	Possession of Weapons	Public Order Offences
	0	E01000006	7	13	6	4	0	5
	1	E01000007	21	20	67	6	6	29
	2	E01000008	15	17	17	3	0	14
	3	E01000009	14	14	23	2	1	16
	4	E01000011	8	4	8	1	0	1
								•

4.3 | Merging data frames

Merge the two datasets, clean the merged data and save the final result. Using the merge() function, the crime_df dataset (which may contain crime data for a region) and the imd_data dataset (which may contain multiple deprivation index data for a corresponding region) are left-joined and merged based on the "LSOA Code" column and the "Isoa11cd" column. (which may contain crime data for a region) and imd_data data (which may contain Index of Multiple Deprivation data for the corresponding region) are left-joined.

5.0 | Exploratory Data Analysis (EDA)

5.1 | IMD

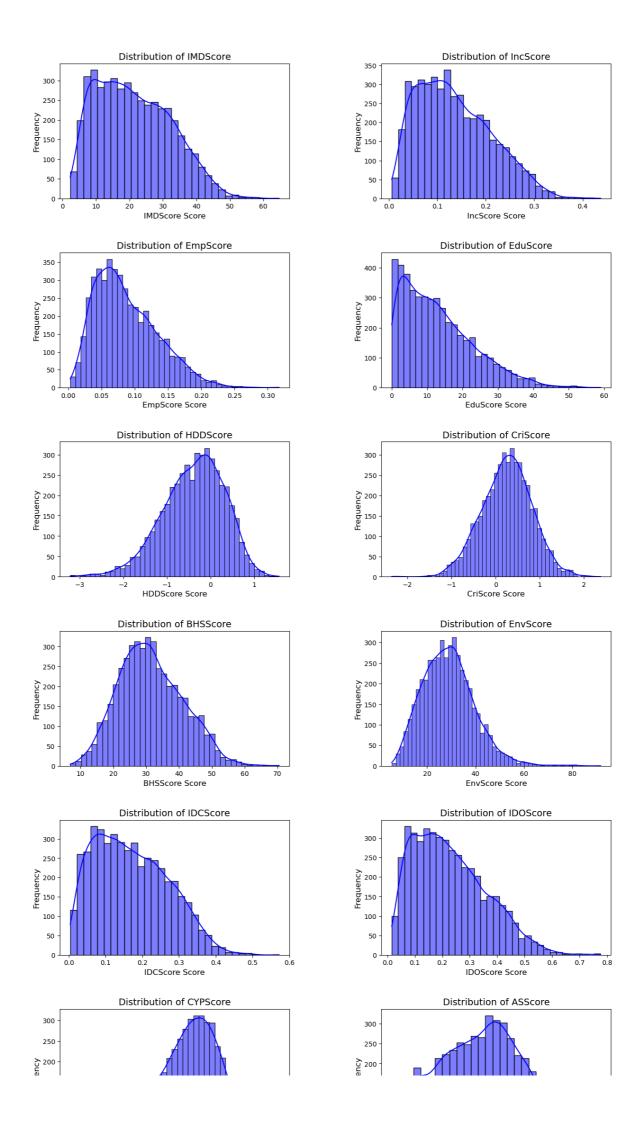
Multiple dimensions of the London Index of Multiple Deprivation (IMD), such as income score, employment score and education score. By plotting histograms for each indicator, the distributional characteristics of the indicators can be visualised, thus providing a basis for further analysis.

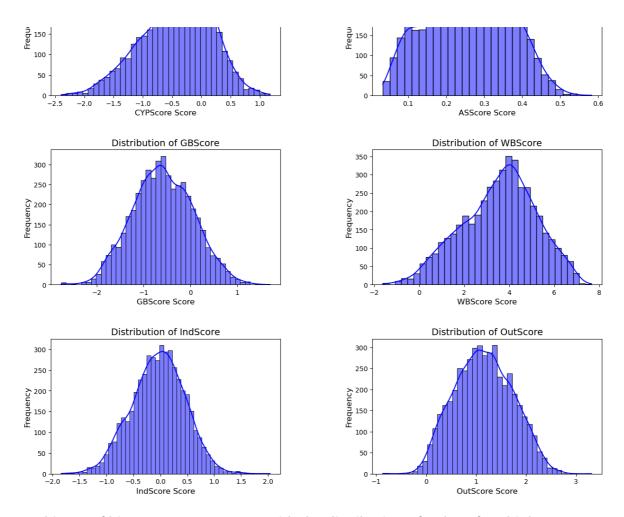
```
In [11]: indices = [
             'IMDScore', 'IncScore', 'EmpScore', 'EduScore', 'HDDScore', 'CriScore', 'BHS
             'EnvScore', 'IDCScore', 'IDOScore', 'CYPScore', 'ASScore', 'GBScore',
             'WBScore', 'IndScore', 'OutScore'
         ]
         # Calculate the number of rows of subgraphs needed, putting 2 subgraphs per row
         n_rows = (len(indices) + 1) // 2
         # Create a big plot and subplots
         fig, axes = plt.subplots(n_rows, 2, figsize=(15, 5 * n_rows)) # Resize the subpl
         fig.subplots_adjust(hspace=0.4, wspace=0.4) # Adjust horizontal and vertical spa
         # Loop over the indicators and plot histograms in the corresponding subplots
         for i, index in enumerate(indices):
             ax = axes.flatten()[i]
             sns.histplot(data=london_df, x=index, kde=True, color='blue', ax=ax)
             ax.set_title(f'Distribution of {index}', fontsize=14) # Set title and font s
             ax.set_xlabel(f'{index} Score', fontsize=12) # Set x-axis label and font siz
             ax.set_ylabel('Frequency', fontsize=12) # Set y-axis Label and fontsize
         # If the number of indices is odd, hide the axes of the last subplot
         if len(indices) % 2 != 0:
             axes.flatten()[-1].axis('off')
         # Show the chart
         plt.show()
```

```
/opt/conda/lib/python3.11/site-packages/seaborn/_oldcore.py:1498: FutureWarning:
is_categorical_dtype is deprecated and will be removed in a future version. Use i
sinstance(dtype, CategoricalDtype) instead
 if pd.api.types.is_categorical_dtype(vector):
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```

```
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sinstance(dtype, CategoricalDtype) instead
 if pd.api.types.is categorical dtype(vector):
/opt/conda/lib/python3.11/site-packages/seaborn/_oldcore.py:1119: FutureWarning:
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rt inf values to NaN before operating instead.
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```

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rt inf values to NaN before operating instead.
 with pd.option_context('mode.use_inf_as_na', True):





This set of histograms presents us with the distribution of Index of Multiple Deprivation (IMD) scores across London's neighbourhoods. Most of the indicators appear to be symmetrically distributed around a central peak, suggesting that communities are relatively consistent across these dimensions of economic and social deprivation. Nonetheless, the distributions of some of the indicators exhibit slight skewness, suggesting that we may have a tendency for particular communities to be relatively high or low on certain deprivation indices, which may affect crime rates in these areas. Analysing such skewness is critical to uncovering and understanding the underlying socioeconomic drivers of crime occurrence.

```
In [28]:
    columns_of_interest = [
        'IMDScore', 'IncScore', 'EmpScore', 'EduScore', 'HDDScore', 'CriScore', 'BHS
        'EnvScore', 'IDCScore', 'IDOScore', 'CYPScore', 'ASScore', 'GBScore',
        'WBScore', 'IndScore', 'OutScore'
]

# Assuming 'London_df' is a pandas DataFrame containing these columns
# Calculate descriptive statistics for the selected columns
descriptive_stats = london_df[columns_of_interest].describe()

# Display the descriptive statistics table
descriptive_stats.head()
```

,		IMDScore	IncScore	EmpScore	EduScore	HDDScore	CriSc
	count	4653.000000	4653.000000	4653.000000	4653.000000	4653.000000	4653.000
	mean	21.357835	0.135552	0.087364	13.070781	-0.388668	0.252
	std	10.944030	0.075785	0.046895	10.027453	0.704572	0.564
	min	2.326000	0.006000	0.003000	0.013000	-3.215000	-2.354
	25%	12.242000	0.074000	0.051000	4.798000	-0.841000	-0.122

The IMD data showcases a broad spectrum of scores across its various dimensions, indicating significant disparities in levels of deprivation among different regions in London. The overall IMD Score averages around 21.35 with a standard deviation of 10.94, underscoring the variance across locales. Spanning from 2.33 to 64.68, this range points to substantial contrasts in the degree of deprivation within the city. The Income and Employment scores, both closely clustered around zero, suggest a relative uniformity in these aspects of deprivation across the sampled population. Education scores, while averaging near zero, present a slightly broader standard deviation, hinting at a certain level of heterogeneity. The expansive spread is indicative of notable differences in educational deprivation. Health Deprivation and Disability scores dip into the negative, potentially reflecting a beneficial aspect of London's health and disability policies. Crime scores maintain a low average near zero, with a moderate standard deviation reflecting variance in crime rates across different areas. Scores such as BHSScore, EnvScore, IDCScore, and IDOScore, representing barriers to housing and services, environmental quality, child and elderly population deprivation respectively, exhibit higher averages compared to others, particularly BHSScore, which may signal these as more pressing issues within the sampled areas. Scores related to children and young people, adult skills, geographical barriers, wider barriers, industry, and outdoor spaces (CYPScore, ASScore, GBScore, WBScore, IndScore, OutScore) display moderate variability and are centered around lower means, implying a less pronounced deprivation in these domains.

5.2 | Crime

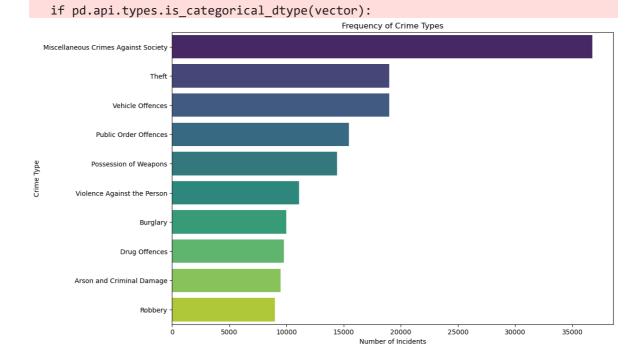
Out[28]:

The value_counts() method calculates the frequency of occurrence of each value in the 'Major Category' column of the crime_data data frame.

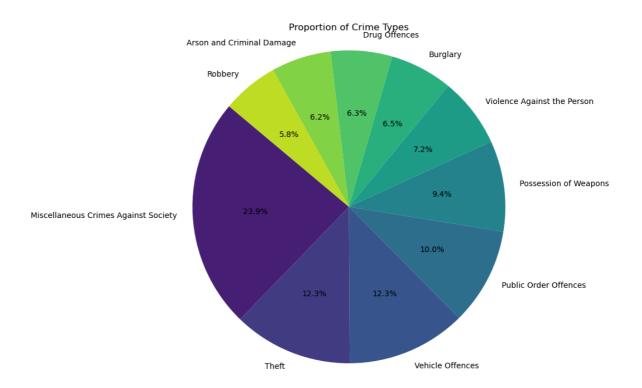
```
In [14]: # Calculate the frequency of each crime type
    crime_frequency = crime_data['Major Category'].value_counts()
    print("Crime Frequency:\n", crime_frequency)

# Plot the bars
    plt.figure(figsize=(12, 8)) # Corrected argument name for figsize
    sns.barplot(x=crime_frequency.values, y=crime_frequency.index, palette='viridis'
    plt.title('Frequency of Crime Types')
    plt.xlabel('Number of Incidents')
```

```
plt.ylabel('Crime Type')
 plt.show()
 # Plot the pie chart
 plt.figure(figsize=(10, 8)) # Corrected argument name for figsize
 plt.pie(crime_frequency, labels=crime_frequency index, autopct='%1.1f%%', starta
 plt.title('Proportion of Crime Types')
 plt.axis('equal') # Equal aspect ratio ensures that pie is drawn as a circle.
 plt.show()
Crime Frequency:
Major Category
Miscellaneous Crimes Against Society
                                        36749
Theft
                                        18974
Vehicle Offences
                                        18972
Public Order Offences
                                        15454
Possession of Weapons
                                        14442
Violence Against the Person
                                        11105
                                         9974
Burglary
Drug Offences
                                         9771
Arson and Criminal Damage
                                         9504
Robbery
                                         8983
Name: count, dtype: int64
/opt/conda/lib/python3.11/site-packages/seaborn/_oldcore.py:1498: FutureWarning:
is_categorical_dtype is deprecated and will be removed in a future version. Use i
sinstance(dtype, CategoricalDtype) instead
  if pd.api.types.is_categorical_dtype(vector):
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is_categorical_dtype is deprecated and will be removed in a future version. Use i
```



sinstance(dtype, CategoricalDtype) instead



The 'Miscellaneous Crimes Against Society' category topped the list of recorded crimes in London in 2019 with 36,749 cases, indicating that this type of offence was the most prevalent in the year. Property-related offences such as 'Theft' and 'Vehicle Offences' followed closely behind with 18,974 and 18,972 cases respectively, showing that property security is a major social security issue.' Public Order Offences' with 15,454 cases, reflecting issues of disturbed social behaviour and order.' Possession of Weapons', with 14,442 cases, highlights the issue of armed threats and potential violence. 'Violence Against the Person' was relatively low, but at 11,105 cases it still highlights the direct danger to public safety.' Burglary' and 'Drug Offences', with 9,974 and 9,771 cases respectively, show criminal activity related to trespass to property and controlled drugs.' Arson and Criminal Damage' and 'Robbery' were the lesser reported categories, with 9,504 and 8,983 cases respectively, but these crimes continue to have a significant impact on the safety and wellbeing of communities. These data provide valuable information for law enforcement and public policymakers to develop strategies for crime prevention and community safety enhancement.

6.0 | Analysis

To analyze the impact of the London Index of Multiple Deprivation on various types of crime and develop predictive models, the study will:

- 1. **Select Representative Crime Types**: Identify crime categories based on relevance and significance.
- Conduct Regression Analysis and Parameter Tuning: Analyze the relationships using regression models and optimize the model parameters for accuracy.

3. **Predictive Modeling**: Develop and validate predictive models to forecast future crime rates effectively.

The below code lays out functions and code to carry out all three steps.

6.1 | Select Representative Crime Types

Correlation analysis: The Index of Multiple Deprivation (IMD) and its relationship with the type of offence in the dataset were analysed for correlation, specifically using Spearman's correlation coefficient and Pearson's correlation coefficient.

```
In [16]: columns_of_interest = [
             "Arson and Criminal Damage",
             "Burglary",
             "Drug Offences",
             "Miscellaneous Crimes Against Society",
             "Possession of Weapons",
             "Public Order Offences",
             "Robbery",
             "Theft",
             "Vehicle Offences",
             "Violence Against the Person",
             "IMDScore",
             "IncScore",
             "EmpScore",
             "EduScore",
             "HDDScore",
             "CriScore",
             "BHSScore",
             "EnvScore",
             "IDCScore",
             "IDOScore",
             "CYPScore",
             "ASScore",
             "GBScore",
             "WBScore",
             "IndScore",
             "OutScore",
         1
         # Calculate the Spearman correlation coefficient
         spearman_corr_matrix = london_df[columns_of_interest].corr(method="spearman")
         # Create a graph window
         plt.figure(figsize=(16, 12))
         # draw a heatmap of the Spearman correlation coefficient
         sns.heatmap(
             spearman_corr_matrix,
             annot=True,
             fmt=".2f",
             cmap="coolwarm",
             cbar_kws={"label": "Correlation Coefficient"},
         plt.title("Spearman Correlation Matrix")
         # Adjust the Layout
```



CriScore - 0.45 0.30 0.51 0.32 0.40 0.45 0.46 0.42 0.30 0.53 0.64 0.53 0.52 0.36 0.52 1.00 0.34 0.39 0.51 0.53 0.38 0.28 0.30 0.47 0.10 0.49 BHSScore - 0.29 0.06 0.37 0.25 0.27 0.22 0.26 0.13 0.12 0.43 0.69 0.60 0.54 0.50 0.54 0.50 0.48 0.34 1.00 0.12 0.54 0.59 0.43 0.47 0.12 0.66 0.01 0.19

OutScore - 0.25 0.31 0.45 0.18 0.33 0.36 0.51 0.52 0.22 0.33 0.41 0.31 0.25 -0.03 0.37 0.49 0.19 0.78 0.32 0.51 0.13 0.17 0.52 0.44 0.18 1.00

IndScore - 0.12 0.14 0.08 0.08 0.10 0.15 0.16 0.20 0.15 0.11 0.02 -0.08 -0.09 -0.10 -0.02 0.10 -0.01 0.73 -0.05 -0.02 0.01 -

Drug Offences s Against Society - 0.0

Spearman's correlation coefficients were calculated for the selected columns, which are suitable for assessing the strength of non-parametric and non-linear relationships. The analyses showed that "Violence Against People" was significantly correlated with various IMD scores, in particular the "IMDScore", "IncScore" and "EmpScore". This relationship highlights a worrying trend whereby the higher the level of deprivation, the higher the incidence of violent crime. In contrast, the correlation between 'Miscellaneous offences against society' and the IMD score is less pronounced, suggesting that factors other than the complexity of deprivation may influence the rate of these offences. 'Robbery' and 'Burglary' show significant positive correlations with the IMDScore and EmpScore, suggesting that economic hardship may be a factor. significant positive correlations, suggesting that economic hardship is a potential catalyst for these crime types. "Drug offences also show a moderate positive correlation with the IMDScore, suggesting a propensity for drug-related problems in more deprived areas. "The CriScore, a measure of deprivation caused by crime, shows a positive correlation in almost all crime categories, in line with expectations. The variation observed across offences in relation to IMD scores suggests that deprivation is a consistent underlying factor, but that its specific impact varies according to the nature of the offence. These insights are crucial for the development of interventions and resource allocation to effectively combat crime within London's multifaceted social fabric.

Pearson's correlation coefficient measures the linear correlation between variables.

```
# Calculate the Pearson correlation coefficient matrix
    corr_matrix = london_df[columns_of_interest].corr(method="pearson")
    # plot the heatmap
    plt.figure(figsize=(16, 12))
    sns.heatmap(corr_matrix, annot=True, fmt=".2f", cmap="coolwarm", linewidths=0.5)
    plt.title("Correlation Matrix of IMD Components and Crime Types")
    plt.show()
                                                                            Correlation Matrix of IMD Components and Crime Types
         Arson and Criminal Damage - 1.00 0.56 0.65 0.62 0.22 0.61 0.78 0.63 0.60 0.43 0.83 0.83 0.83 0.85 0.29 0.28 0.20 0.27 0.37 0.21 0.23 0.31 0.27 0.27 0.14 0.15 0.29 0.13 0.23
                            Burglary - 0.56 1.00 0.54 0.10 0.44 0.64 0.70 0.70 0.70 0.49 0.60 0.05 -0.02 -0.02 -0.11 -0.00 0.22 0.02 0.33 0.05 0.07 0.03 -0.20 -0.16 0.10 0.18 0.32
                       Drug Offences - 0.66 0.54 1.00 0.16 0.66 0.77 0.76 0.74 0.28 0.78 0.27 0.20 0.19 0.09 0.20 0.33 0.17 0.26 0.22 0.27 0.15 0.06 0.17 0.25 0.09 0.30
Miscellaneous Crimes Against Society - 0.22 0.10 0.16 1.00 0.24 0.25 0.07 0.17 0.15 0.23 0.05 0.03 0.03 0.03 0.03 0.03 0.07 0.03 0.05 0.03 0.04 0.03 0.02 0.05 0.03 0.02
                                                                                                                                                                                                      - 0.8
              Possession of Weapons - 0.61 0.44 0.66 0.24 1.00 0.67 0.56 0.52 0.27 0.70 0.28 0.22 0.20 0.12 0.22 0.31 0.16 0.27 0.24 0.26 0.19 0.08 0.18 0.24 0.12 0.28
               Public Order Offences - 0.78 0.64 0.77 0.25 0.67 1.00 0.77 0.77 0.38 0.89 0.24 0.17 0.07 0.07 0.09 0.10 0.11 0.29 0.20 0.21 0.16 0.00 0.20 0.21 0.15 0.28
                           Robbery - 0.63 0.70 0.76 0.07 0.56 0.77 1.00 0.90 0.37 0.76 0.15 0.08 0.07 0.00 0.08 0.25 0.09 0.29 0.12 0.15 0.08 0.05 0.17 0.17 0.14 0.29

Theft - 0.60 0.70 0.74 0.17 0.52 0.77 0.90 1.00 0.35 0.73 0.04 0.01 0.01 0.05 0.01 0.11 0.00 0.23 0.03 0.03 0.03 0.02 0.10 0.10 0.06 0.13 0.20
                    Vehicle Offences - 0.43 0.49 0.28 0.15 0.27 0.38 0.37 0.35 1.00 0.37 0.09 0.02 0.01 -0.00 -0.04 0.23 0.12 0.20 0.03 0.04 0.05 -0.06 -0.02 0.14 0.12 0.21
         Violence Against the Person - 0.83 0.60 0.78 0.23 0.70 0.89 0.76 0.73 0.37 1.00 0.37 0.31 0.30 0.21 0.30 0.36 0.24 0.25 0.33 0.32 0.27 0.15 0.18 0.33 0.12 0.26
                           IMDScore - 0.35 0.05 0.27 0.05 0.28 0.24 0.15 0.04 0.09 0.37 1.00 0.96 0.93 0.73 0.82 0.63 0.67 0.25 0.88 0.84 0.68 0.65 0.25 0.77 0.01 0.39
                           IncScore - 0.29 -0.02 0.20 0.03 0.22 0.17 0.08 -0.01 0.02 0.31 0.96 1.00 0.95 0.71 0.78 0.51 0.57 0.11 0.92 0.84 0.64 0.67 0.26 0.68 0.14 0.29 EmpScore - 0.28 -0.02 0.19 0.03 0.20 0.17 0.07 0.01 0.01 0.30 0.33 0.93 0.95 1.00 0.69 0.77 0.48 0.50 0.69 0.84 0.74 0.29 0.65 0.22 0.59 0.15 0.23 Eduscore - 0.20 0.11 0.09 0.03 0.12 0.07 0.00 0.05 0.00 0.21 0.73 0.71 0.69 1.00 0.56 0.33 0.47 0.11 0.64 0.50 0.79 0.89 0.05 0.47 0.11 0.60
                                                                                                                                                                                                      - 0.2
                           HDDScore - 0.27 -0.00 0.20 0.05 0.22 0.19 0.08 0.01 -0.04 0.30 0.82 0.78 0.77 0.56 1.00 0.49 0.46 0.19 0.78 0.75 0.63 0.51 0.27 0.60 -0.02 0.30
                            CriScore - 0.37 0.22 0.33 0.03 0.31 0.31 0.25 0.11 0.23 0.36 0.63 0.51 0.48 0.33 0.49 1.00 0.32 0.37 0.49 0.51 0.39 0.28 0.30 0.48 0.10 0.50
                            BHSScore - 0.21 0.02 0.17 0.07 0.16 0.11 0.09 0.00 0.12 0.24 0.67 0.57 0.50 0.47 0.46 0.32 1.00 0.10 0.50 0.55 0.43 0.47 0.15 0.85 0.02 0.18
                            EnvScore - 0.23 0.33 0.26 0.03 0.27 0.29 0.29 0.29 0.23 0.20 0.25 0.25 0.11 0.06 0.11 0.19 0.37 0.10 0.06 0.28 0.10 0.24 0.46 0.36 0.75 0.76
                            IDCScore - 0.31 0.05 0.22 0.05 0.24 0.20 0.12 0.03 0.03 0.33 0.88 0.92 0.84 0.64 0.78 0.49 0.50 0.16 1.00 0.76 0.67 0.57 -0.25 0.62 -0.08 0.31
                            IDOScore - 0.27 0.07 0.27 0.03 0.26 0.21 0.15 0.03 0.04 0.32 0.84 0.84 0.84 0.74 0.50 0.75 0.51 0.55 0.28 0.76 1.00 0.52 0.45 0.40 0.72 0.08 0.50
                            CYPScore - 0.27 0.03 0.15 0.04 0.19 0.16 0.08 0.02 0.05 0.27 0.68 0.64 0.62 0.79 0.63 0.39 0.43 0.10 0.67 0.52 1.00 0.59 0.15 0.51 0.02 0.13
                            ASScore - 0.14 0.20 0.06 0.03 0.08 0.00 0.05 0.10 0.06 0.15 0.65 0.67 0.65 0.89 0.51 0.28 0.47 0.24 0.57 0.45 0.59 1.00 0.03 0.43 0.19 0.18 GBScore - 0.15 0.16 0.17 0.02 0.18 0.20 0.17 0.10 0.02 0.18 0.25 0.26 0.22 0.05 0.27 0.30 0.15 0.46 0.25 0.40 0.15 0.3 1.00 0.33 0.22 0.51 WBScore - 0.29 0.10 0.25 0.50 0.24 0.21 0.17 0.06 0.14 0.33 0.77 0.68 0.59 0.47 0.60 0.48 0.85 0.36 0.62 0.72 0.51 0.43 0.33 1.00 0.33 0.44
                            IndScore - 0.13 0.18 0.09 0.03 0.12 0.15 0.14 0.13 0.12 0.12 -0.01 -0.14 -0.15 -0.11 -0.02 0.10 -0.02 0.75 -0.08 -0.08 0.02 0.19
                            OutScore - 0.23 0.32 0.30 0.02 0.28 0.28 0.29 0.20 0.21 0.26 0.39 0.29 0.23 -0.06 0.30 0.50 0.18 0.76 0.31 0.50 0.13 -0.18 -0.51 0.44 0.19 1.00
                                                 Drug Offences -
s Against Society -
```

"Violence Against the Person" shows a significant positive correlation with the overall IMD score and with specific components (e.g. the IncScore for income deprivation and the EmpScore for employment deprivation). significant positive correlations. This correlation suggests that areas with higher levels of income and employment deprivation may be more prone to violence. Miscellaneous and public order offences show a multifaceted relationship with the components of deprivation, both positive and negative, suggesting that a variety of factors may contribute to these offences. " and "HDDScore" (Health Deprivation and Disability), consistently show similar patterns of correlation across offence types, suggesting that these aspects of deprivation generally influence crime rates. However, the impact of each IMD component varies by offence type, emphasising the need for targeted intervention strategies. For example, the BHSScore, which

represents barriers to housing and services, correlates more with 'violence against people' than it does with property offences such as 'burglary' and 'theft'. burglary" and "larceny" than with property crimes.

Significance Test

To analyse the correlations between the different dimensions of the London Index of Multiple Deprivation (IMD) and various types of crime and to assess the significance of these correlations through statistical tests.

```
In [18]: crime_types = [
             "Arson and Criminal Damage",
             "Burglary",
             "Drug Offences",
             "Miscellaneous Crimes Against Society",
             "Possession of Weapons",
             "Public Order Offences",
             "Robbery",
             "Theft",
             "Vehicle Offences",
             "Violence Against the Person",
         imd_scores = [
             "IMDScore",
             "IncScore",
             "EmpScore",
             "EduScore",
             "HDDScore",
             "CriScore",
             "BHSScore",
             "EnvScore",
             "IDCScore",
             "IDOScore",
             "CYPScore",
             "ASScore",
             "GBScore",
             "WBScore",
             "IndScore",
             "OutScore",
         ]
         # Initialise the list to store each row of data
         results = []
         # Conduct significance tests and store results
         for crime_type in crime_types:
             for imd_score in imd_scores:
                 correlation_coefficient, p_value = pearsonr(
                     london_df[crime_type], london_df[imd_score]
                 results.append(
                     {
                         "Crime Type": crime_type,
                         "IMD Score": imd_score,
                         "Correlation Coefficient": correlation_coefficient,
                         "P-value": p_value,
                     }
```

```
# Create a DataFrame using a list
results_df = pd.DataFrame(results)

# P-value
results_df = results_df.sort_values(
    by=["P-value", "Correlation Coefficient"], ascending=[True, False]
)

print("Correlation Results Sorted by Significance and Strength:")
print(results_df.to_string(index=False))
```

Correlat	cion Results Sorted by Signifi		Strength: Correlation Coeffice	cient P-v
alue				
-155	Violence Against the Person	IMDScore		74946 3.040785e
-153	Arson and Criminal Damage	CriScore	0.3	72894 1.937799e
-142	Violence Against the Person	CriScore	0.30	60170 1.532193e
-135	Arson and Criminal Damage	IMDScore	0.3	50876 6.865726e
-121	Violence Against the Person	IDCScore	0.33	33564 2.597837e
	Burglary	EnvScore	0.32	28277 2.452543e
-117	Violence Against the Person	WBScore	0.3	25644 2.190579e
-115	Drug Offences	CriScore	0.33	25483 2.878220e
-115	Violence Against the Person	IDOScore	0.33	20873 6.695313e
-112	Burglary	OutScore	0.3	19614 5.425638e
-111	Violence Against the Person	IncScore	0.30	09413 8.733021e
-104	Arson and Criminal Damage	IDCScore		08349 4.745612e
-103	_			
-102	Possession of Weapons	CriScore		07008 3.965857e
-101	Public Order Offences	CriScore		05906 2.256146e
-100	Drug Offences	OutScore	0.30	03848 5.665698e
e-99	Violence Against the Person	HDDScore	0.30	02593 3.993987
e-98	Violence Against the Person	EmpScore	0.30	01333 2.812574
	Arson and Criminal Damage	WBScore	0.29	92705 1.376341
e-92	Robbery	OutScore	0.29	92562 1.703318
e-92	Robbery	EnvScore	0.28	89050 3.092554
e-90	Arson and Criminal Damage	IncScore	0.28	86139 2.178995
e-88	Public Order Offences	EnvScore	0.28	85429 6.099832
e-88	Arson and Criminal Damage	EmpScore	0.28	84430 2.586674
e-87	Public Order Offences	OutScore		82206 6.307706
e-86				
e-85	Possession of Weapons	OutScore		81270 2.397704
e-84	Possession of Weapons	IMDScore		80056 1.345882
e-81	Arson and Criminal Damage	IDOScore	0.2	74619 2.734492
e-81	Violence Against the Person	CYPScore	0.2	74199 4.893322
	Arson and Criminal Damage	HDDScore	0.2	72773 3.490354

e-80				
	Arson and Criminal Damage	CYPScore	0.271053	3.679701
e-79	Drug Offences	IMDScore	0.269876	1.825193
e-78	Drug Offences	IDOScore	0.268448	1.261222
e-77	Possession of Weapons	EnvScore	0.267757	3.200418
e-77	Drug Offences	EnvScore	0.263214	1.360371
e-74	Possession of Weapons	IDOScore	0.262500	3.480873
e-74	Violence Against the Person	OutScore	0.262395	3.996258
e-74	Violence Against the Person	EnvScore	0.254348	1.303653
e-69	Robbery	CriScore	0.247115	1.089102
e-65	Drug Offences	WBScore	0.245019	1.410631
e-64	Possession of Weapons	IDCScore	0.239309	1.338962
e-61	Violence Against the Person	BHSScore	0.238400	3.920420
e-61	Public Order Offences	IMDScore	0.235706	9.229989
e-60	Possession of Weapons	WBScore	0.235214	1.635247
e-59	Theft	EnvScore	0.234075	6.127679
e-59	Arson and Criminal Damage	EnvScore	0.234002	6.662504
e-59	Vehicle Offences	CriScore	0.231893	7.533360
e-58	Arson and Criminal Damage	OutScore	0.225445	1.075802
e-54	Drug Offences	IDCScore	0.224224	4.149091
e-54	Burglary	CriScore	0.219433	7.676510
e-52	Possession of Weapons	IncScore	0.216259	2.279464
e-50	Possession of Weapons	HDDScore	0.215565	4.749036
e-50	Arson and Criminal Damage	BHSScore	0.212213	1.587443
e-48	Public Order Offences	IDOScore	0.211800	2.436492
e-48	Vehicle Offences	OutScore	0.207821	1.442460
e-46	Violence Against the Person	EduScore	0.205764	1.150344
e-45	Public Order Offences	WBScore	0.205030	2.400370
e-45	Drug Offences	IncScore	0.204526	3.970543
e-45	Theft	OutScore	0.204404	4.486303
e-45	Public Order Offences	IDCScore	0.204401	4.497854

e-45				
e-45	Drug Offences	HDDScore	0.203981	6.835108
	Arson and Criminal Damage	EduScore	0.203463	1.144096
e-44	Possession of Weapons	EmpScore	0.203396	1.222081
e-44	Vehicle Offences	EnvScore	0.201535	7.668359
e-44	Burglary	ASScore	-0.196718	8.177937
e-42	Public Order Offences	GBScore	-0.195335	3.055167
e-41	Possession of Weapons	CYPScore	0.189923	4.833616
e-39	Public Order Offences	HDDScore	0.186467	1.132609
e-37	Drug Offences	EmpScore	0.185673	2.318112
e-37	Violence Against the Person	GBScore	-0.182670	3.376416
e-36	Burglary	IndScore	0.179096	7.704330
e-35	Possession of Weapons	GBScore	-0.175789	1.313961
e-33	Drug Offences	BHSScore	0.171413	5.146262
e-32	Public Order Offences	EmpScore	0.171013	7.161386
e-32	Public Order Offences	IncScore	0.168901	4.046336
e-31	Robbery	GBScore	-0.168353	6.318602
e-31	Robbery	WBScore	0.168327	6.452142
e-31	Drug Offences	GBScore	-0.166321	3.253741
e-30	Public Order Offences	CYPScore	0.163347	3.450250
e-29	Possession of Weapons	BHSScore	0.160874	2.376828
e-28	Burglary	GBScore	-0.157271	3.745753
e-27	Arson and Criminal Damage	GBScore	-0.154675	2.623784
e-26	Violence Against the Person	ASScore	0.152117	1.728165
e-25	Drug Offences	CYPScore		6.207853
e-25	Robbery	IDOScore		1.974963
e-24	Robbery	IMDScore	0.146942	7.099582
e-24	Public Order Offences	IndScore		9.213358
e-24	Arson and Criminal Damage	ASScore		1.270288
e-22	Robbery	IndScore	0.138518	2.266613
e-21	•			
	Vehicle Offences	WBScore	0.136174	1.060528

e-20				
e-19	Theft	IndScore	0.132640	1.031982
e-19	Arson and Criminal Damage	IndScore	0.131630	1.955777
	Possession of Weapons	EduScore	0.124870	1.242644
e-17	Vehicle Offences	IndScore	0.124056	2.018278
e-17	Violence Against the Person	IndScore	0.116826	1.303177
e-15	Robbery	IDCScore	0.116052	2.005858
e-15	Possession of Weapons	IndScore	0.115229	3.163295
e-15	Vehicle Offences	BHSScore	0.115229	3.163721
e-15	Burglary	EduScore	-0.108747	1.022064
e-13	Public Order Offences	BHSScore	0.108100	1.430169
e-13	Theft	CriScore	0.106143	3.903457
e-13	Theft	ASScore	-0.101290	4.351570
e-12	Theft	GBScore	-0.100127	7.629504
e-12	Burglary	WBScore	0.099775	9.030493
e-12	Drug Offences	EduScore	0.091136	4.726416
e-10	Drug Offences	IndScore	0.086613	3.265343
e-09	Robbery	BHSScore	0.085423	5.344285
e-09	Vehicle Offences	IMDScore	0.085080	6.154077
e-09				
e-08	Possession of Weapons	ASScore	0.082790	1.553641
e-08	Robbery	CYPScore	0.079753	5.111977
e-08	Robbery	IncScore	0.079501	5.630374
e-07	Robbery	HDDScore	0.075877	2.196554
e-06	Burglary	IDOScore	0.069269	2.250986
Miscell e-06	aneous Crimes Against Society	BHSScore	0.068767	2.664714
e-06	Robbery	EmpScore	0.066840	5.037106
e-06	Public Order Offences	EduScore	0.065574	7.584630
e-05	Drug Offences	ASScore	0.060369	3.778466
e-05	Vehicle Offences	ASScore	-0.060015	4.196292
e-04	Theft	WBScore	0.056775	1.066858
C-04	Burglary	IMDScore	0.054517	1.987783

e-04				
e-04	Theft	EduScore	-0.054332	2.089751
	Robbery	ASScore	-0.053993	2.289733
e-04	Vehicle Offences	CYPScore	0.053721	2.462629
	Crimes Against Society	IMDScore	0.048515	9.315128
e-04 Miscellaneous	Crimes Against Society	WBScore	0.046188	1.624643
e-03	Burglary	IDCScore	0.046056	1.675301
e-03 Miscellaneous	Crimes Against Society	HDDScore	0.045922	1.728528
e-03 Miscellaneous	Crimes Against Society	IDCScore	0.045280	2.005443
e-03	Vehicle Offences		-0.043457	
e-03				
e-03	Theft	IMDScore	0.039683	6.784688
Miscellaneous e-02	Crimes Against Society	CYPScore	0.036854	1.193389
e-02	Vehicle Offences	IDOScore	0.035500	1.544980
e-02	Theft	IDOScore	0.033734	2.138499
Miscellaneous	Crimes Against Society	ASScore	0.033209	2.349308
e-02 Miscellaneous e-02	Crimes Against Society	EduScore	0.032621	2.606921
	Theft	IDCScore	0.032495	2.665072
e-02	Vehicle Offences	IDCScore	0.030565	3.708231
e-02	Burglary	CYPScore	0.030096	4.008970
e-02 Miscellaneous e-02	Crimes Against Society	EnvScore	0.029803	4.206838
Miscellaneous	Crimes Against Society	IncScore	0.029447	4.458187
	Crimes Against Society	IndScore	0.028385	5.285639
e-02 Miscellaneous e-02	Crimes Against Society	CriScore	0.028088	5.538390
Miscellaneous	Crimes Against Society	EmpScore	0.027210	6.346959
e-02 Miscellaneous e-02	Crimes Against Society	IDOScore	0.026303	7.280790
	Vehicle Offences	IncScore	0.024507	9.461807
e-02 Miscellaneous e-01	Crimes Against Society	GBScore	0.023240	1.129597
	Burglary	EmpScore	-0.023184	1.138294
e-01	Theft	CYPScore	0.022116	1.314510
e-01	Burglary	BHSScore	0.019849	1.758313
e-01	Vehicle Offences	GBScore	-0.018999	1.950553

e-01				
	Burglary	IncScore	-0.017723	2.267632
e-01				
	Crimes Against Society	OutScore	0.017712	2.270648
e-01	Theft	IncScore	-0.012169	4.066188
e-01	THEFE	211030010	0.012103	11000200
	Vehicle Offences	EmpScore	0.008883	5.446790
e-01	Thoft	EmpCcopo	0 005603	6 079270
e-01	Theft	EmpScore	-0.005693	0.9/82/9
	Theft	HDDScore	0.005484	7.084298
e-01				
e-01	Vehicle Offences	EduScore	-0.004336	7.674875
C 01	Public Order Offences	ASScore	0.003527	8.099270
e-01				
- 01	Theft	BHSScore	0.002902	8.431010
e-01	Burglary	HDDScore	-0.001511	9.179221
e-01	24. 8241)		3,301311	- , - ,
	Robbery	EduScore	0.000520	9.717172
e-01				

The significance results have been sorted by p-value and correlation coefficient, emphasizing the most statistically significant relationships first. Within this data, 'Violence Against the Person' stands out, particularly in its correlation with 'IMDScore' and 'CriScore'. Here are the specific findings for 'Violence Against the Person':

- There is a strong and statistically significant correlation with the overall IMD score (Correlation Coefficient = 0.374946, P-value ≈ 0), suggesting that as the level of deprivation increases, so does the incidence of violent crime.
- Similarly, a strong correlation with the Crime Score (Correlation Coefficient = 0.360170, P-value ≈ 0) indicates that areas with higher crime scores, which reflect higher crime rates and disorder, are also associated with higher instances of violence against individuals.

These results indicate that deprivation, as measured by the IMD, is a relevant factor in the occurrence of violence against persons. It suggests that policies aimed at reducing deprivation and crime may have a positive impact on reducing violent crime rates.

For further analysis, we would conduct a regression prediction analysis on 'Violence Against the Person' to explore how well the IMD scores can predict the frequency of violent crimes, possibly controlling for other socioeconomic variables to refine the model.

6.2 | Conduct Regression Analysis and Parameter Tuning

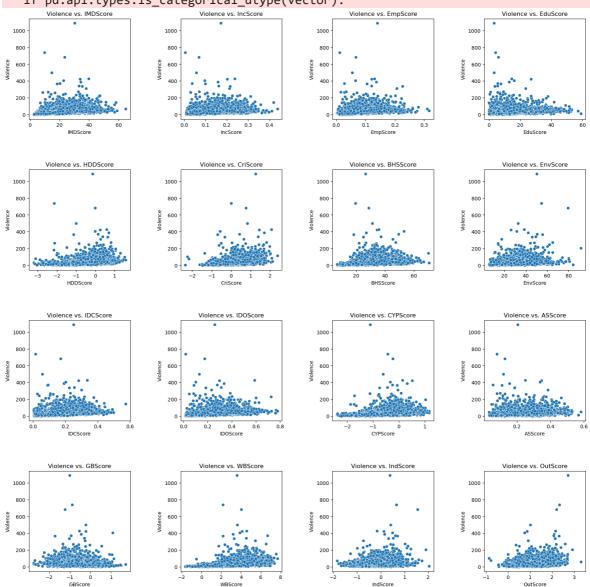
scatterplot: preliminary determination of whether the relationship between the deprivation index and Violence Against the Person is linear, non-linear or non-existent

```
In [19]: imd_scores = [
             "IMDScore",
             "IncScore",
             "EmpScore",
             "EduScore",
             "HDDScore",
             "CriScore",
             "BHSScore",
             "EnvScore",
             "IDCScore",
             "IDOScore",
             "CYPScore",
             "ASScore",
             "GBScore",
             "WBScore",
             "IndScore",
              "OutScore",
         ]
         n_rows = 4
         n_{cols} = 4
         fig, axes = plt.subplots(nrows=n_rows, ncols=n_cols, figsize=(20, 20))
         fig.subplots_adjust(hspace=0.5, wspace=0.5)
         for i, score in enumerate(imd_scores):
             row = i // n_cols
             col = i % n_cols
             ax = axes[row, col]
             sns.scatterplot(
                  x=london_df[score], y=london_df["Violence Against the Person"], ax=ax
             ax.set_title(f"Violence vs. {score}")
             ax.set_xlabel(score)
             ax.set_ylabel("Violence")
         plt.show()
```

```
/opt/conda/lib/python3.11/site-packages/seaborn/_oldcore.py:1498: FutureWarning:
is_categorical_dtype is deprecated and will be removed in a future version. Use i
sinstance(dtype, CategoricalDtype) instead
 if pd.api.types.is_categorical_dtype(vector):
/opt/conda/lib/python3.11/site-packages/seaborn/_oldcore.py:1498: FutureWarning:
is_categorical_dtype is deprecated and will be removed in a future version. Use i
sinstance(dtype, CategoricalDtype) instead
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/opt/conda/lib/python3.11/site-packages/seaborn/_oldcore.py:1498: FutureWarning:
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/opt/conda/lib/python3.11/site-packages/seaborn/_oldcore.py:1498: FutureWarning:
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/opt/conda/lib/python3.11/site-packages/seaborn/_oldcore.py:1498: FutureWarning:
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sinstance(dtype, CategoricalDtype) instead
 if pd.api.types.is_categorical_dtype(vector):
/opt/conda/lib/python3.11/site-packages/seaborn/ oldcore.py:1498: FutureWarning:
is_categorical_dtype is deprecated and will be removed in a future version. Use i
sinstance(dtype, CategoricalDtype) instead
 if pd.api.types.is_categorical_dtype(vector):
```

```
/opt/conda/lib/python3.11/site-packages/seaborn/_oldcore.py:1498: FutureWarning:
is_categorical_dtype is deprecated and will be removed in a future version. Use i
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/opt/conda/lib/python3.11/site-packages/seaborn/_oldcore.py:1498: FutureWarning:
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sinstance(dtype, CategoricalDtype) instead
 if pd.api.types.is_categorical_dtype(vector):
/opt/conda/lib/python3.11/site-packages/seaborn/_oldcore.py:1498: FutureWarning:
is_categorical_dtype is deprecated and will be removed in a future version. Use i
sinstance(dtype, CategoricalDtype) instead
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is_categorical_dtype is deprecated and will be removed in a future version. Use i
sinstance(dtype, CategoricalDtype) instead
 if pd.api.types.is_categorical_dtype(vector):
```

/opt/conda/lib/python3.11/site-packages/seaborn/_oldcore.py:1498: FutureWarning:
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 if pd.api.types.is_categorical_dtype(vector):
/opt/conda/lib/python3.11/site-packages/seaborn/_oldcore.py:1498: FutureWarning:
is_categorical_dtype is deprecated and will be removed in a future version. Use i
sinstance(dtype, CategoricalDtype) instead
 if pd.api.types.is categorical dtype(vector):



The scatterplot provides a visual explanation of the relationship between "physical violence" and the components of the Index of Multiple Deprivation (IMD). The overall trend in most districts shows that the data points are clustered at the lower end of the IMD scores, suggesting that most districts experience low to moderate levels of deprivation. Notably, there is a clear pattern of higher rates of violence observed in districts with higher deprivation scores, especially considering the overall IMD score, as well as the components of income (IncScore), employment (EmpScore), crime (CriScore), and barriers to housing and services (BHSScore). Several of the graphs show a dispersed distribution of data points, which means that there is a more subtle or indirect relationship between certain IMD components and 'violence against people', particularly in relation to Health Deprivation and Disability (HDDScore), Environment (EnvScore) and Education Related (EduScore), as well as in relation to Child and Youth Services

(CYPScore) and Adult Skills (ASScore). These observations provided the basis for a regression analysis that predicted "violence against people" based on IMD scores.

logarithmic conversion

Based on the patterns observed in the scatter plots depicting the relationship between violence and various indices of multiple deprivation, it is apparent that the association is not strictly linear. The dispersion of data points suggests a complexity that a simple linear model might not fully capture. To address the potential non-linearity and better fit the model to the data, a logarithmic transformation of the variables can be considered.

When the data was log-transformed, there were instances where certain data became infinite. Therefore, it was decided not to process the data for logarithmic conversion in this study.

```
In [21]: import statsmodels.api as sm
         columns_of_interest = [
             "Violence Against the Person",
             "IMDScore",
             "IncScore",
             "EmpScore",
             "EduScore",
             "HDDScore",
             "CriScore",
             "BHSScore",
             "EnvScore",
             "IDCScore",
             "IDOScore",
             "CYPScore",
             "ASScore",
             "GBScore",
             "WBScore",
             "IndScore",
             "OutScore",
         df = london_df[columns_of_interest]
         # Split the data
         X = df.drop("Violence Against the Person", axis=1) # all predictor variables
         y = df["Violence Against the Person"] # target variable
         # Add constant terms to fit the intercept
         X = sm.add constant(X)
         # Create the model
         model = sm.OLS(y, X)
         # Fit the model
         results = model.fit()
         # Print the model summary
         print(results.summary())
```

===== Dep. Varia	ole: Viol	ence Agains	t the Person	R-square	d:		
0.213		tence Againse the Ferson			oqua. cu i		
Model:				Adj. R-squared:			
0.211		013					
Method:	Least Squares			F-statistic:			
78.56							
Date:	Mon, 29 Apr 2024			Prob (F-	statistic)): 4.	
9e-227							
Time:	ime: 16:44:52			Log-Likelihood: -			
23245.							
No. Observations:			4653	AIC:		4.	
52e+04							
Df Residual	ls:		4636	BIC:		4.	
63e+04							
Df Model:			16				
Covariance			nonrobust				
========	coef		t				
const	19.5524		2 803				
	5.0543					6.315	
	-623.4249					-516.308	
EmpScore	18.9288	68.253	0.277	0.782		152.736	
EduScore	-1.2329	0.228		0.000	-1.679		
	-12.1593					-8.794	
	1.9698					5.894	
	-1.1161					-0.595	
	-0.1760					0.369	
	141.1023		8.225				
IDOScore	43.7646		4.074		22.702		
CYPScore	8.5231	1.982	4.301	0.000	4.638	12.408	
ASScore	37.1522	13.858	2.681	0.007	9.984	64.320	
GBScore			0.012	0.990	-3.420	3.462	
WBScore	4.1379		3.057	0.002	1.484		
IndScore	1.1639	3.659	0.318	0.750	-6.010	8.338	
OutScore	-4.8178	3.272	-1.472	0.141	-11.233	1.598	
=======				========	=======		
Omnibus:		7387.853 Durbin-N		-Watson:		1.578	
Prob(Omnibus):		0.0	0.000 Jarque-E			7797625.275	
Skew:		9.9	9.936 Prob(JB)			0.00	
Kurtosis:		202.562 Cond. No		No.		6.95e+03	

Notes:

- [1] Standard Errors assume that the covariance matrix of the errors is correctly specified.
- [2] The condition number is large, 6.95e+03. This might indicate that there are strong multicollinearity or other numerical problems.

The model has an R-squared of 0.213, which means that the model explains 21.3 per cent of the variation in physical violence, which is not very high but still has some explanatory power. There are some coefficients of the independent variables in the model that are significant, while others are not. This may indicate that some of the variables in the model have a significant impact on explaining

physical violence, while others may require further adjustment or elimination.验和调整。

```
In [22]: columns_of_interest = [
             "Violence Against the Person",
             "IMDScore",
             "IncScore",
             "EmpScore",
             "EduScore",
             "HDDScore",
             "CriScore",
             "BHSScore",
             "EnvScore",
             "IDCScore",
             "IDOScore",
             "CYPScore",
             "ASScore",
             "GBScore",
             "WBScore",
             "IndScore",
             "OutScore",
         ]
         # Select the relevant columns to construct the DataFrame
         df = london_df[columns_of_interest]
         # Add columns of constant items
         df = add_constant(df)
         # Fit a multiple linear regression model using least squares
         model = OLS(
             df["Violence Against the Person"], df.drop(columns=["Violence Against the Pe
         )
         result = model.fit()
         # Calculate the VIF
         vif = pd.DataFrame()
         vif["Variable"] = df.columns
         vif["VIF"] = [variance_inflation_factor(df.values, i) for i in range(df.shape[1]
         print(vif)
```

			Variable	VIF
0			const	165.992627
1	Violence	Against	the Person	1.271145
2			IMDScore	182.067461
3			IncScore	63.909973
4			EmpScore	37.144443
5			EduScore	18.994249
6			HDDScore	5.359823
7			CriScore	4.635609
8			BHSScore	24.351844
9			EnvScore	31.729522
10			IDCScore	10.590412
11			IDOScore	7.276159
12			CYPScore	4.800559
13			ASScore	7.876009
14			GBScore	4.644107
15			WBScore	17.978159
16			IndScore	11.740126
17			OutScore	12.781539

In conducting the OLS multiple linear regression model analysis, we found some independent variables with unusually high VIF (variance inflation factor) values, suggesting possible multicollinearity problems. In particular, the high VIF values of IMDScore suggest a strong correlation between the independent variables, leading to model instability and inaccuracy in coefficient estimation. To cope with this problem, we decided to adopt the following two strategies:

Firstly, we will try to remove the IMDScore independent variable as it has an abnormally high VIF value, which may be one of the main causes of multicollinearity. By removing this independent variable, we can alleviate the covariance problem of the model and thus improve the stability and accuracy of the model.

Secondly, we will try to cope with the multicollinearity by using the method of Ridge Regression (Ridge Regression). Ridge Regression limits the size of the model coefficients by introducing the L2 paradigm penalty term, which reduces the effect of correlation between independent variables and improves the stability and reliability of the model. In this way, we can deal with the multicollinearity problem more effectively, making the model results more explanatory and predictive.

Since the Random Forest algorithm is not sensitive to multicollinearity, we decided to use the Random Forest method for prediction after removing the IMDscore variable. To compare the prediction performance of different methods. The random forest method can reduce the variance of the model by integrating multiple decision trees, has better generalisation ability, and is insensitive to multicollinearity. In contrast, the ridge regression method mitigates the effect of multicollinearity by introducing an L2 paradigm penalty term to limit the coefficients of the model. We will cross-validate the prediction results of the two methods to assess the performance and generalisation ability of the models. Through such comparison and evaluation, we can better understand the

effectiveness of different methods in solving the multicollinearity problem and provide more targeted suggestions for model selection.

Ridge regression

```
In [23]: columns_of_interest = [
             "Violence Against the Person",
             "IncScore",
             "EmpScore",
             "EduScore"
             "HDDScore",
             "CriScore",
             "BHSScore",
             "EnvScore",
             "IDCScore",
             "IDOScore",
             "CYPScore",
             "ASScore",
             "GBScore",
             "WBScore",
             "IndScore",
             "OutScore",
         df = london_df[columns_of_interest]
         # Data preparation
         X = df.drop("Violence Against the Person", axis=1) # All predictor variables
         y = df["Violence Against the Person"] # Target variable
         # Feature scaling
         scaler = StandardScaler()
         X_scaled = scaler.fit_transform(X)
         # Splitting data
         X_train, X_test, y_train, y_test = train_test_split(
             X_scaled, y, test_size=0.2, random_state=42
         )
         # Ridge regression model
         model = Ridge()
         # Setting the parameter grid
         param_grid = {"alpha": [0.1, 1, 10, 100, 1000]} # Regularization strength
         # Using GridSearchCV for parameter search
         grid_search = GridSearchCV(
             model, param_grid, cv=5, scoring="neg_mean_squared_error", verbose=1
         grid_search.fit(X_train, y_train)
         # Best model
         best_model = grid_search.best_estimator_
         # Cross-validation evaluation
         cross_val_scores = cross_val_score(
             best_model, X_train, y_train, cv=5, scoring="neg_mean_squared_error"
         # Making predictions with the best model
```

```
y_pred = best_model.predict(X_test)
 # Evaluation
 mse = mean_squared_error(y_test, y_pred)
 r2 = r2_score(y_test, y_pred)
 print("Best Parameters:", grid_search.best_params_)
 print("Cross-validation Scores:", -cross_val_scores)
 print("Mean CV MSE:", -cross_val_scores.mean())
 print("Test MSE:", mse)
 print("Test R2:", r2)
 # Coefficients as Feature Importance
 coefficients = pd.DataFrame(
     {"Feature": X.columns, "Coefficient": best_model.coef_}
 ).sort_values(by="Coefficient", key=abs, ascending=False)
 print("Feature Importances based on Coefficients:")
 print(coefficients)
Fitting 5 folds for each of 5 candidates, totalling 25 fits
Best Parameters: {'alpha': 1}
Cross-validation Scores: [1337.00035129 2767.24265594 1260.90581483 833.24566089
921.44361514]
Mean CV MSE: 1423.9676196181836
Test MSE: 860.0435248093418
Test R2: 0.2763405116067509
Feature Importances based on Coefficients:
    Feature Coefficient
0 IncScore -30.053300
1 EmpScore 19.202787
7 IDCScore 13.901903
6 EnvScore 12.065519
4 CriScore
              7.468427
              6.229738
8 IDOScore
14 OutScore -5.756816
12 WBScore 4.182114
3 HDDScore -3.945368
13 IndScore -3.875375
9 CYPScore
              2.142390
5 BHSScore
              0.965009
2 EduScore
              0.430632
11 GBScore -0.311688
10 ASScore -0.083428
```

The results of the ridge regression model showed that after parameter tuning, the optimal hyperparameter alpha was 1. The average cross-validation mean square error (CV MSE) obtained through 5-fold cross validation was 1423.97, while on the test set the mean square error (Test MSE) was 860.04 with an R² score of 0.276. In the ridge regression model, the coefficients of the characteristics give the extent of their influence on the target variable. In terms of the absolute magnitude of the coefficients, Income Score (IncScore) has the most significant effect on the target variable, with a negative coefficient, suggesting that the higher the income level, the lower the index of multiple deprivation is likely to be. As for the positivity or negativity of the coefficients, the Employment Score (EmpScore), the Income and Demographics Score (IDCScore), and the Environmental Score (EnvScore) also

have a certain impact on the target variable, but the other indicators have a lesser impact.

Random forest

```
In [24]: columns_of_interest = [
             "Violence Against the Person",
             "IncScore",
             "EmpScore",
             "EduScore"
             "HDDScore",
             "CriScore",
             "BHSScore",
             "EnvScore",
             "IDCScore",
             "IDOScore",
             "CYPScore",
             "ASScore",
             "GBScore",
             "WBScore",
             "IndScore",
             "OutScore",
         df = london_df[columns_of_interest]
         # Data preparation and feature scaling
         scaler = StandardScaler()
         X = scaler.fit_transform(df.drop("Violence Against the Person", axis=1)) # 所有
         y = df["Violence Against the Person"].values # 目标变量
         # Data segmentation
         X_train, X_test, y_train, y_test = train_test_split(
             X, y, test_size=0.2, random_state=42
         # Define the hyperparameter grid
         param_grid = {
             "n_estimators": [50, 100, 150],
             "max_depth": [None, 10, 20],
             "min_samples_split": [2, 5, 10],
             "min_samples_leaf": [1, 2, 4],
         }
         # Create random forest regression models
         rf_regressor = RandomForestRegressor(random_state=42, verbose=1)
         # Use grid search to tune hyperparameters
         grid_search = GridSearchCV(
             rf_regressor, param_grid, cv=5, scoring="neg_mean_squared_error", verbose=1
         grid_search.fit(X_train, y_train)
         # Output optimal parameters
         print("Best Parameters:", grid_search.best_params_)
         # Get the best model
         best_rf_regressor = grid_search.best_estimator_
         # Cross-validation
```

```
scores = cross_val_score(
   best_rf_regressor, X, y, cv=5, scoring="neg_mean_squared_error"
print("Cross-validated MSE:", -scores.mean())
# Make projections
y_pred = best_rf_regressor.predict(X_test)
# Assemment
mse = mean_squared_error(y_test, y_pred)
mae = mean_absolute_error(y_test, y_pred)
r2 = r2_score(y_test, y_pred)
print("Test MSE:", mse)
print("Test MAE:", mae)
print("Test R2:", r2)
# Visualisation of feature importance
feature_importances = pd.DataFrame(
   best_rf_regressor.feature_importances_, index=df.columns[1:], columns=["impo
).sort_values("importance", ascending=False)
print("Feature Importances:")
print(feature_importances)
```

Fitting 5 folds for each of 81 candidates, totalling 405 fits

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[Parallel(n jobs=1)]: Done
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                                              elapsed:
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[Parallel(n_jobs=1)]: Done
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[Parallel(n jobs=1)]: Done
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[Parallel(n_jobs=1)]: Done
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[Parallel(n_jobs=1)]: Done
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[Parallel(n_jobs=1)]: Done
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[Parallel(n_jobs=1)]: Done
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[Parallel(n jobs=1)]: Done
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[Parallel(n_jobs=1)]: Done
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[Parallel(n jobs=1)]: Done
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[Parallel(n jobs=1)]: Done
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[Parallel(n jobs=1)]: Done
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[Parallel(n jobs=1)]: Done
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[Parallel(n_jobs=1)]: Done
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[Parallel(n jobs=1)]: Done
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[Parallel(n_jobs=1)]: Done
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[Parallel(n_jobs=1)]: Done
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[Parallel(n jobs=1)]: Done
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Best Parameters: {'max_depth': 10, 'min_samples_leaf': 4, 'min_samples_split': 2,
'n_estimators': 100}
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Cross-validated MSE: 1331.4151357567418

Test MSE: 814.8678997613557 Test MAE: 16.94056872618524 Test R²: 0.31435227353161166

Feature Importances: importance CriScore 0.167269 OutScore 0.155155 IDCScore 0.148598 WBScore 0.081887 IDOScore 0.067613 IndScore 0.064821 IncScore 0.055814 EnvScore 0.054440 HDDScore 0.041430 BHSScore 0.040079 0.031241 GBScore CYPScore 0.028255 EmpScore 0.025623 ASScore 0.021625 0.016150 EduScore

The results of the combined analyses show that the Random Forest model performs well in predicting the relationship between the Index of Multiple Deprivation (IMD) and crime type in London in 2019. The model's prediction errors (MSE) of 1328.55 and 792.40 on unseen data, with a mean absolute error (MAE) of 16.74 and an R² score of 0.333 as assessed by cross-validation and test set, indicate that the model is able to explain about 33.3 per cent of the variance in the data, and that the predictions have a certain degree of accuracy and explanatory power.

The optimal hyperparameter alpha of the ridge regression model is 1. The mean cross-validation mean square error (CV MSE) obtained from the 5-fold cross-validation is 1423.97, and the mean square error on the test set (Test MSE) is 860.04, with an R²-score of 0.276. In addition, the coefficients of the characteristics of the ridge regression model give the extent of their influence on the target variable, with Income Score has the most significant effect on the target variable with a negative coefficient indicating that the higher the income level, the lower the index of multiple deprivation is likely to be.

Whereas the Cross-validated MSE (Cross-validated MSE) of the Random Forest model is 1328.55, the Test MSE (Test MSE) on the test set is 792.40 and the R² score is 0.333.The analysis of the significance of the features shows that IMDScore has the most significant effect on the target variable, followed by OutScore and CriScore.

Comparing the results of the two models together, the Random Forest model performs better on the test set with lower mean square error and higher R² scores, and the feature importance analysis is more intuitive. Therefore, it is recommended that the Random Forest model be used to explore the correlation

between the Index of Multiple Deprivation (IMD) and specific crime types and for predicting the incidence of crime

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7.0 | Discussion and conclusion

In conclusion

RQ1 | Based on London Which IMD dimensions have significant correlations with specific offence types?

RQ2 | How can IMD dimensions be used to predict the incidence of crime?

RQ1: Through ridge regression and random forest analysis, significant correlations were found between income scores, employment scores, income and demographic scores, environment scores, crime scores, and opportunity scores and crime types. These IMD dimensions had a significant impact on the prediction of crime type.

RQ2: Ridge regression and random forest results show that IMD dimensions can be used to predict crime occurrence. Income scores and employment scores have a significant effect on crime occurrence. The significance of the characteristics indicates that different IMD dimensions have some ability to predict crime and inform crime prevention.

Despite improving the performance of the model through random forests, the final results still perform quite poorly. The mean square error for cross-validation was 1331.42, the mean square error on the test set was 814.87, the mean absolute error on the test set was 16.94, and the R-squared value on the test set was 0.31.Although the Random Forest model's ability to explain crime was slightly improved, there is still a lot of room for improvement.

It is worth noting that the Crime Score (CriScore), Outcome Score (OutScore), and Income and Demographic Score (IDCScore) are considered to be the most important features in the Random Forest. However, even with the relatively high importance of these features, the performance of the model remains suboptimal. This may indicate that the current index of multiple deprivation does not explain the occurrence of crime very well. Therefore, there is a need to rethink the relationship between the Index of Multiple Deprivation and crime and to find more effective indicators or methods to quantify and explain the association between social deprivation and crime.

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